

Let the line $y = mx + b$ intersect the parabola $y = kx^2$ at two points A and B. Let C be the point on the parabolic arc AB that is furthest from the line $y = mx + b$.

Find the ratio of the area of the region bounded by the parabola and the line, and the area of the triangle ABC.

♣ Please **Submit** your solution to

- Dr. Tirtha Timsina, ttimsina@gsu.edu or
- Dr. Christian Avart, cavart@gsu.edu

before the deadline: **Friday, November 30th, 7:00PM.**

♣ The WINNER will be awarded with a \$15 gift certificate and will be announced in the NEXT issue.

Problem of the last month: Given two sets A and B, the symmetric difference $A \Delta B$ is defined by the union of $A \setminus B$ and $B \setminus A$. For any $n \geq 2$, let A_1, A_2, \dots, A_n be n finite subsets of the integers. Show that $A_1 \Delta A_2 \Delta \dots \Delta A_n$ is the set consisting of the integers contained in exactly an odd number of the sets A_i , $1 \leq i \leq n$.

Solution: We prove it by induction. It is clearly true for $n=2$. Now if $N = A_1 \Delta A_2 \Delta \dots \Delta A_n \Delta A_{n+1}$ we can write $N = P \Delta A_{n+1}$. We then see that an element x belongs to N if it either belongs to P and not A_{n+1} or it belongs to A_{n+1} and not P . In either case, by the induction hypothesis we see that x belongs to N if and only if it belongs to an odd number of the A_i 's.

Winner: Joseph Moravitz
