# Why mgc v is awesome

- **∠** chris.mainey@uhb.nhs.uk
- mainard.co.uk
- github.com/chrismainey
- **y** twitter.com/chrismainey

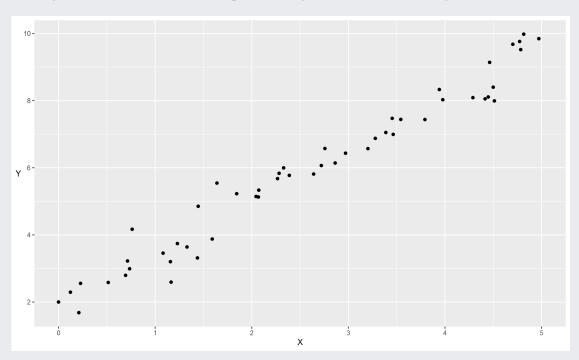


*Don't think about it too hard... ⊙* 

1/19

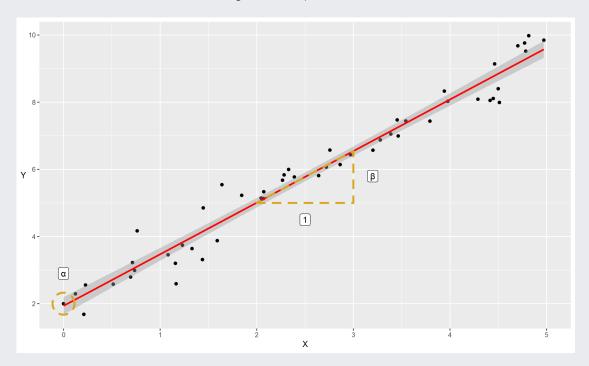
### Regression models on non-linear data

• Regression is a method for predicting a variable, Y, using another, X



### Equation of a straight line (1)

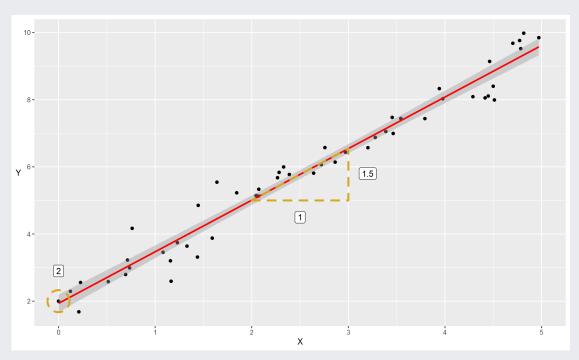
$$y = \alpha + \beta x + \epsilon$$



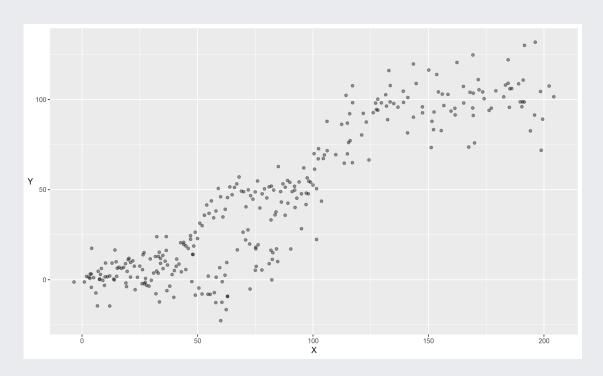
3 / 19

## Equation of a straight line (2)

$$y = 2 + 1.5x + \epsilon$$

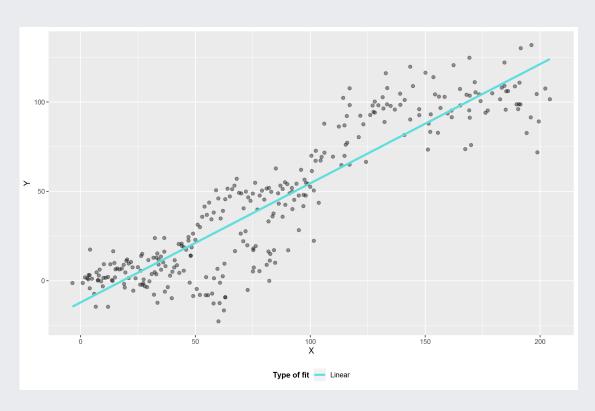


## What about nonlinear data? (1)

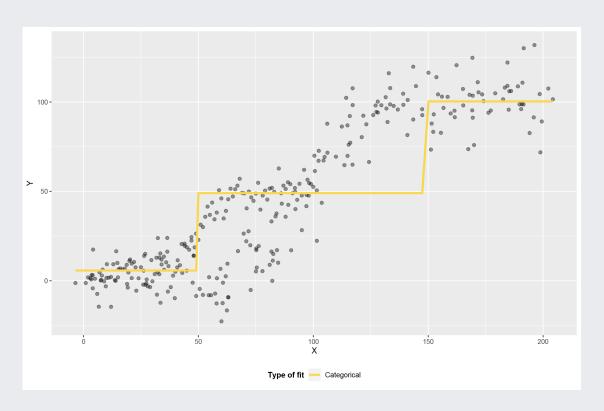


5 / 19

## What about nonlinear data? (2)

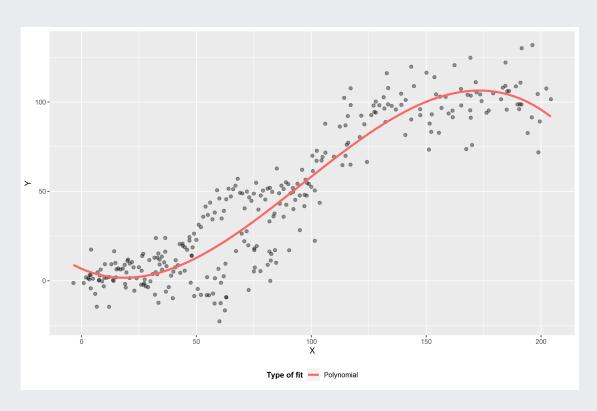


### What about nonlinear data? (3)

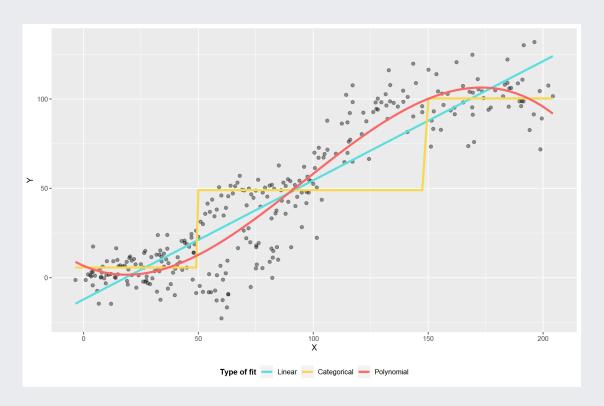


7 / 19

## What about nonlinear data? (4)



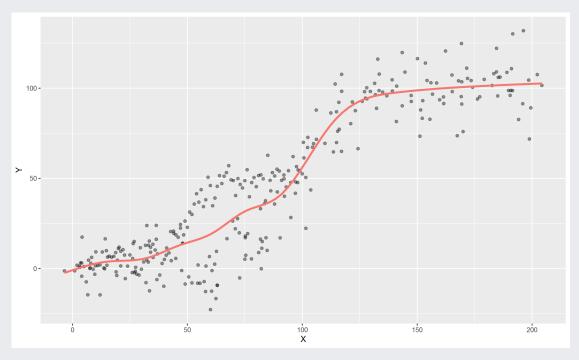
### What about nonlinear data? (5)



9 / 19

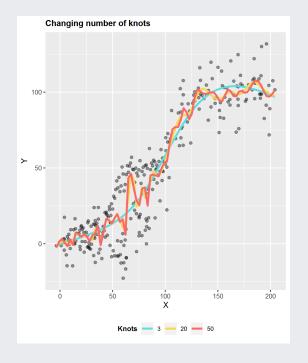
### **Splines**

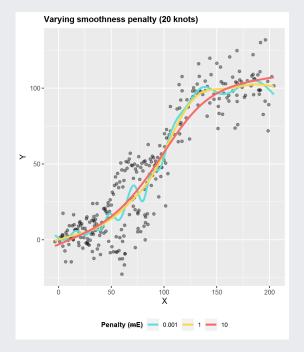
- Smooth, piece-wise polynomials, like a flexible strip for drawing curves.'Knot points' between each section



#### How smooth?

Can be controlled by number of knots (k), or by a penalty $\gamma$ .





11/19

#### **Generalized Additive Model**

- Regression models where we fit smoothers (like splines) from our data.
- Strictly additive, but smoothers can describe complex relationships.
- In our case:

$$y = \alpha + f(x) + \epsilon$$

Or more formally, an example GAM might be (Wood, 2017):

$$g(\mu i) = A_i heta + f_1(x_1) + f_2(x_{2i}) + f_3(x_{3i}, x_{4i}) + \dots$$

#### Where:

- $\mu i \equiv E(Y_i)$ , the expectation of Y
- $Yi \sim EF(\mu_i, \phi_i)$ , Yi is a response variable, distributed according to exponential family distribution with mean  $\mu_i$  and shape parameter  $\phi$ .
- $A_i$  is a row of the model matrix for any strictly parametric model components with  $\theta$  the corresponding parameter vector.
- $f_i$  are smooth functions of the covariates, xk, where k is each function basis.

#### What does that mean for me?

- Can build regression models with smoothers
- Suited to non-linear, or noisy data
- *Hastie (1985)* used knot every point, *Wood (2017)* uses reduced-rank version

#### mgcv: mixed gam computation vehicle

- Prof. Simon Wood's package, pretty much the standard
- Included in standard R distribution, used in ggplot2 geom\_smooth etc.

```
library(mgcv)
my_gam <- gam(Y ~ s(X, bs="cr"), data=dt)</pre>
```

- s() control smoothers
- bs="cr" telling it to use cubic regression spline ('basis')
- Default is 10 knots (k=10 argument), but you can alter this

13 / 19

#### **Model Output:**

```
summary(my_gam)
##
## Family: gaussian
## Link function: identity
## Formula:
## Y \sim s(X, bs = "cr")
##
## Parametric coefficients:
    Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 43.9659 0.8305 52.94 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Approximate significance of smooth terms:
## edf Ref.df F p-value
## s(X) 6.087 7.143 296.3 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-sq.(adj) = 0.876 Deviance explained = 87.9%
## GCV = 211.94 Scale est. = 206.93 n = 300
```

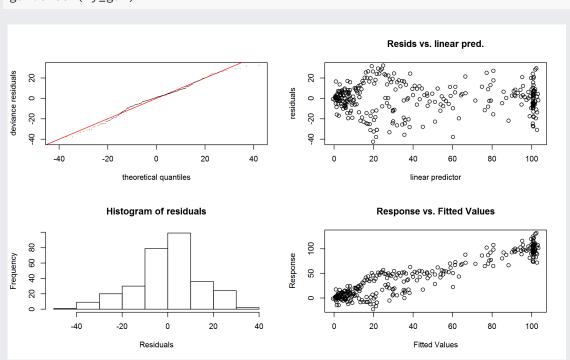
### Check your model:

```
##
## Method: GCV Optimizer: magic
## Smoothing parameter selection converged after 4 iterations.
## The RMS GCV score gradient at convergence was 1.107369e-05 .
## The Hessian was positive definite.
## Model rank = 10 / 10
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
## k' edf k-index p-value
## s(X) 9.00 6.09 1.1 0.97</pre>
```

15 / 19

### Check your model:

gam.check(my\_gam)



### Is it any better than linear model?

```
my_lm <- lm(Y ~ X, data=dt)
anova(my_lm, my_gam)

## Analysis of Variance Table
##
## Model 1: Y ~ X
## Model 2: Y ~ s(X, bs = "cr")
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 298.00 88154
## 2 292.91 60613 5.0873 27540 26.161 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1</pre>
```

#### Yes, yes it is!

17 / 19

### Summary

- Regression models are concerned with explaining one variable: y, with another: x
- This relationship is assumed to be linear
- If your data are not linear, or noisy, a smoother might be appropriate
- Splines are ideal smoothers, and are polynomials joined at 'knot' points
- GAMs are a framework for regressions using smoothers
- mgcv is a great package for GAMs with various smoothers available
- $\bullet\,$  mgcv estimates the required smoothing penalty for you
- gratia or mgcViz packages are good visualization tool for GAMs

### References and Further reading:

#### GitHub code:

https://github.com/chrismainey/Why\_mgcv\_is\_awesome

#### Simon Wood's comprehensive book:

• WOOD, S. N. 2017. Generalized Additive Models: An Introduction with R, Second Edition, Florida, USA, CRC Press.

#### Noam Ross free online GAM course:

https://noamross.github.io/gams-in-r-course/

- HARRELL, F. E., JR. 2001. Regression Modeling Strategies, New York, Springer-Verlag New York.
- HASTIE, T. & TIBSHIRANI, R. 1986. Generalized Additive Models. Statistical Science, 1, 297-310. 291
- HASTIE, T., TIBSHIRANI, R. & FRIEDMAN, J. 2009. The Elements of Statistical Learning: Data Mining, Inference, and Prediction, New York, NETHERLANDS, Springer.