Optimization-based computation of locomotion trajectories for Crowd Patches

Abstract

Abstract, abstract, abstract ...

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5 1 Introduction

Video Games are constantly displaying larger and livelier virtual environments due to increased computational power and advanced rendering techniques. For example, the recent Grand Theft Auto (GTA) game [Rockstar-Games 2004] takes place in Los Santos and its surroundings, a completely virtual city. In spite of the impres-10 sive quality and liveliness of the scene, Los Santos still remains 11 relatively sparsely populated with virtual people. The reason for 12 this phenomenon is the large computational cost required to get an ambient crowd in such large environments. To address this issue, 14 the technique of Crowd Patches has been recently introduced by 15 Yersin et al. [Yersin et al. 2009].

Crowd patches are precomputed elements (patches) of crowd animations. Patches are time-periodic so that they can be endlessly played in time. The boundary conditions of precomputed animations are accurately controlled to enable combining patches in space (i.e., characters can move from in-between patches) and compose large ambient crowds. This technique eases the process of designing performance efficient ambient crowds.

One problem with this technique however, is the computation of internal animation trajectories for patches that satisfy both, time-periodicity and boundary conditions amongst patches. Satisfying both of these constraints is difficult, since it is equivalent to computing collision-free trajectories that exactly pass through spatio-temporal waypoints (i.e., at some exact position in time) whilst at the same time solving possibly complex interactions between agents (collision-avoidance). In addition to that, trajectories should look as natural as possible.

In this paper we propose a new optimization-based method to com-33 pute these internal trajectories. Our method starts by initially as-34 signing linear space-time trajectories which are easy to compute 35 and satisfy both, periodicity and boundary conditions, but at the same time might introduce collisions between characters. Then, iteratively, we optimize the trajectories to handle collisions. We try to 38 keep the generated trajectories as close as possible to the initial lin-39 ear trajectories, to minimize the magnitude of collision-avoidance maneuvers. How do we define this? Do we measure it? Could we present this as the principle of least effort; i.e. the agents do as 42 little as possible to achieve their goals without doing any complex 43 movement...

To conclude, the main contribution of this work is an optimizationbased algorithm to compute high quality animation trajectories (2D global navigation trajectories) for individual crowd patches under constraints (expressed as a set of spatio-temporal boundary control points).

The remainder of this paper is organized as follows: Section 2 proposes a short overview on the state of the art. Section 3 details our technique to compute these internal trajectories. Then, in Section

4 some results, together with their performance and quality analysis are shown before a brief discussion and concluding remarks (Sections 5 and 6 respectively).

2 State of the Art

Most often, virtual environments are populated based on crowd simulation approaches [Thalmann and Raupp Muse 2013]. An ambient crowd is generated from a large set of moving characters, mainly walking ones. Recent efforts in crowd simulation have enabled dealing with great performances [Pettré et al. 2006; Treuille et al. 2006], high densities [Narain et al. 2009] or controllable crowds [Guy et al. 2009]. There has been a lot of effort to develop velocity-based approaches [Paris et al. 2007; van den Berg et al. 2007] which display much more smooth and realistic locomotion trajectories, especially thanks to anticipatory adaptation to avoid collisions between characters. Nevertheless, . . .

Most of the related work we present here is agent based, even though flow based approaches are relevant also.

Simulation-based techniques are ideal for creating an ambient crowd for large environments. Several problems are recurrent with such approaches: a) crowd simulation is computationally demanding, crowd size is severely limited for interactive applications on light computers; b) simulation is based on simplistic behaviours (e.g., walking, avoiding collisions, etc.) and therefore it is difficult to generate diverse and rich crowds based on classical approaches; c) crowd simulation is prone to animation artifacts or deadlock situations, it is impossible to guarantee animation quality.

Example-based approaches attempt to solve the limitations on animation quality. The key idea of this approaches is to indirectly define the crowd rules from existing crowd data (such as real people trajectories) [Lerner et al. 2007; Ju et al. 2010; Charalambous and Chrysanthou 2014]. Locally, trajectories are typically of good quality, because they reproduce real recorded ones. However, such approaches raise other difficulties: it is difficult to guarantee that the example database will cover all the required content and it can also be difficult to control behaviors and interactions displayed by characters if the database content is not carefully selected. Finally, those approaches are most of the times computationally demanding; even more so than traditional simulation based techniques.

To solve both performance as well as quality issues, crowd patches were introduced by Yersin et al. [Yersin et al. 2009]. The key idea is to generate an ambient moving crowd from a set of interconnected patches. Each patch is a kind of 3D animated texture element, which records the trajectories of several moving characters. Trajectories are periodic in time so that the crowd motion can be played endlessly. Trajectories boundary conditions at the geometrical limits of patches are controlled to be able to connect together two different patches with characters moving from one patch to another. Thus, a crowd animated from a set of patches have a seamless motion and patches' limits cannot be easily detected. The boundary conditions are all registered into patterns, which are sort of gates for patches with a set of spacetime input/output points. For a more detailed expanation please refer to [Yersin et al. 2009] for more details.

Nevertheless, using the crowd patches approach, it is important to work with a limited set of patterns to be able to connect various patches together. As a result, it is important to be able to compose

a patch by starting from a set of patterns, and then deducing internal trajectories of patches from the set of boundary conditions defined by the patterns. As a result, we need to compute trajectories for characters that pass through a given set of spatiotemporal waypoints; i.e., characters should reach specific points in space at specific points in time. This problem is difficult since generally speaking steering techniques for characters consider 2D spatial goals, but do not consider the time a character should take to reach its waypoint. Therefore, dedicated techniques are required.

Yersin et al. suggest using an adapted Social Forces technique to compute internal trajectories [Helbing et al. 2005]. The key idea is to connect input/output points together with linear trajectories and model characters as particles attracted by a goal moving along one of these linear trajectories, combined with repulsion forces to avoid collision between them and static obstacles. One problem with this approach is limited density level, as well as the level of quality of trajectories that suffer from the usual drawbacks of Helbing's generated trajectories, i.e., lack of anticipation, which results into non natural local avoidance maneuvers (see Figure XXXXXXXX).

Compared to previous techniques to compute internal trajectories, we suggest formulating the problem of computing internal trajectories as an optimization problem. First, we suggest optimizing the way input and output points are connected. Especially, since way-points are defined in space and time, we connect them trying to have some *good* walking speed (i.e., close to the average human walking speed). Indeed, characters moving too slow or too fast are visually evident artifacts. Secondly, after having connected waypoints with linear trajectories, we deform them to remove any collisions by employing an iterative approach. This approach aims in minimizing as much as possible the changes to the initial trajectories. We show improvements in the quality of results as compared to the original work by Yersin et al (see Figure XXXXXXXX - same as previous paragraph, could keep only one of the two references, this one).

142 3 Methodology

In this section we present the proposed methodology for generating trajectories for patches. We first give some definitions and notations (Section 3.1), followed by an overview of the method (Section 3.2), and trajectories initial generation, collision handling and smoothing out (Sections 3.3–3.5).

8 3.1 Definitions

Before presenting our approach on trajectory generation for Crowd Patches, we present some definitions and notations regarding Crowd Patches. Please refer to Figure 2 for a visual representation of the definitions and [Yersin et al. 2009] for a more detailed description.

A **patch** is a set $\{A, \pi, D, S\}$ where A is geometrical area with a convex polygonal shape, π the period of time of the animation and D and S are the sets of dynamic and static objects, respectively. These last two sets may be empty in case of an empty patch.

Static objects are simple obstacles whose geometry is fully contained inside the patch.

Dynamic objects are animated; i.e., they are moving in time according to a set of trajectories T.

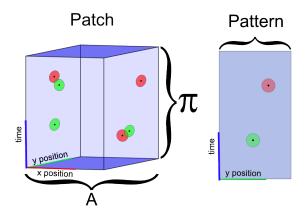


Figure 2: Patches and Patterns A patch is defined by the geometrical area A where a set of dynamic and static objects (D and S respectively) can move over a period of time π . Patterns define boundary conditions for the patches and act as portals connecting neighboring patches.

3.1.1 Trajectories

We define a **trajectory** inside a patch as a function $\tau(t)$ going from time to position, more specifically from a subset of $[0, \pi]$ to A:

$$\tau: [t_1, t_2] \to A, \quad 0 \le t_1 < t_2 \le \pi$$
 (1)

We represent a trajectory as a list of control points connected by segments:

- A control point is a point in space and time cp = {p_{cp}, t_{cp}}.
 All control points in a trajectory can either be boundary or movable ones. Boundary control points serve as entry and exit points to the patch and cannot be moved, added or deleted. Movable control points on the other hand can be moved, added, or removed from the trajectory as long as they do not violate the constraints of the patch; i.e., their positions must lie inside area A (p_{cp} ∈ A) and their time t_{cp} must be between t₁ and t₂.
- A segment is a straight line connecting two control points in a specific order. Since these are unidirectional lines in spacetime, it is important to remember that they are not allowed to go backwards in time.

There are two categories of dynamic objects: endogenous and exogenous agents. **Endogenous agents** remain inside A for the total period of time π . In order to achieve periodicity for the animation, they are associated with a trajectory $\tau:[0,\pi]\to A$, such that it respects the periodicity condition: the position at the start and at the end of the animation must be the same, i.e. $\tau(0) = \tau(\pi)$.

Exogenous agents on the other hand go outside A. They enter the patch at time $t_{initial}$ and position $\mathbf{p}_{initial}$, and they exit at time t_{final} and position \mathbf{p}_{final} . For each agent we associate a sequence of $n \geq 1$ trajectories $\{\tau_1, \tau_2, \ldots, \tau_n\}$. Sequences may have only one trajectory, but some agents require additional trajectories in order to satisfy speed and time constraints. The following conditions must be respected in each sequence of trajectories associated with an exogenous agent:

1. $\mathbf{p}_{initial}$ and \mathbf{p}_{final} must be points on the borders of A otherwise they cannot be exogenous agents.

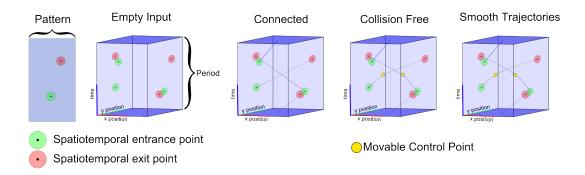


Figure 1: Overview Input and output points in a patch's patterns are initially connected and subsequently modified using the proposed optimization approach and smoothed out to be collision free.

2. If the sequence is composed by more than one trajectory, for each two contiguous trajectories, the following must be true to ensure continuity: $\tau_i(\pi) = \tau_{i+1}(0)$.

Note that the second condition implicitly implies that in sequences with multiple trajectories, each middle trajectory must be fully defined in the period of time $[0,\pi]$, while τ_1 must be defined in $[t_{initial},\pi]$ and τ_n must be defined in $[0,t_{final}]$.

3.1.2 Patterns

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A patch can be considered as a spatio-temporal right prism depending on the type of polygon used as its area (cube in the case of a squared area patch). A **pattern** can be defined as one lateral side of the prism (Figure 2). Specifically, it is a rectangle whose base is one of the edges of the polygonal area (we define $l \in \mathbb{R}^2$ as this two dimensional vector), and its height is equal to the period π . In addition to these, patterns also include the sets \mathbf{I} and \mathbf{O} of input and output boundary control points respectively. The input set contains the boundary control points where exogenous agents begin their trajectories; we call these *entry points*. Conversely the elements of output are called Exit Points; they establish the position in time and space that the exogenous agents finish their paths. Formally defined, a pattern $\mathbf{P}^{(i)}$ is:

$$\mathbf{P}^{(i)} = \{\mathbf{l}^{(i)}, \pi^{(i)}, \mathbf{I}^{(i)}, \mathbf{O}^{(i)}\}$$
 (2)

To populate virtual environments, patches are concatenated together. Thus, continuity between trajectories should be enforced for exogenous agents passing through two contiguous patches. This means that two adjacent patches must have a similar pattern on the side they share; i.e., the vector l and period π must be the same and the input and output sets must be exchanged. More formally, having two patterns \mathbf{P}_1 and \mathbf{P}_2 where $P^{(1)} = \{\mathbf{l}^{(1)}, \pi^{(1)}, \mathbf{I}^{(1)}, \mathbf{O}^{(1)}\}$ and $P^{(2)} = \{\mathbf{l}^{(2)}, \pi^{(2)}, \mathbf{I}^{(2)}, \mathbf{O}^{(2)}\}$, then, in order to satisfy C^0 continuity the following must apply:

$$l^{(1)} = l^{(2)}, \pi^{(1)} = \pi^{(2)}, \mathbf{I}^{(1)} = \mathbf{O}^{(2)}, \mathbf{I}^{(2)} = \mathbf{O}^{(1)}$$
 (3)

Under these conditions, P_1 is the mirror pattern of P_2 and vice versa. When these patches are animated, this will be observed as moving agents going from one patch to adjacent ones. If the area **A** of a patch is a square then 4 patterns are defined, one per side. 265

Patterns defined by a patch have the property that the sum of the cardinality of all the inputs is the same as the sum of the cardinality of all outputs; we call this the parity condition: $\sum(|inputs|) = \sum(|outputs|)$.

A patch defines a set of patterns, and conversely, a set of patterns satisfying the parity condition, having the same period, and whose vectors define a convex polygonal area, can be used to create a patch indirectly.

3.2 Overview

The objective is, given a set of patterns, we want to construct a patch. This process has three main steps:

- Make a matching between the elements in the Input and Output sets contained within a patch. In this step, we connect Entry to Exit Points based on a scoring function. This function tries to keep agents close to their prefered speed while at the same time avoiding connections to similar patterns, thus reducing unwanted u-turns. The input for this function is a set of patterns and the output is a set of piecewise linear trajectories connecting the entry and exit points.
- Create collision free trajectories for these pairings. We start with simple line trajectories and start bending them until they are collision free. Points lying at the borders, i.e. the Entry and Exit points, are hard restraints and can never be moved.
- Smoothing trajectories (if needed). Last, we use splines to minimize the hard turns. We make sure the new trajectories stay close to the original ones, lest we create new collisions.

Problem: is to compute internal trajectories that join all boundary conditions with conitnuous and believable motion trajectories.

2 steps: - step 1: connect waypoints INPUT first boudnary conditions are "alone" in patches \rightarrow associate/connect waypoints them OUTPUT: initial trajectories (piecewise linear trajs, possibly colliding, with "good" properties that we will define later on)

- step 2: optimize intial trajectories by moving control points to remove collisions INPUIT: initial trazjectories OUTPUT: colliision trajectories, still enforcing boundary conditions

- step 3 is smoothing

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Initialize all $m \in M$ and $w \in W$ to free;

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while \exists free man m who still has a woman w to propose to do

| w \leftarrow m's highest ranked woman to whom he has not yet proposed;
| if w is free then
| (m, w) become engaged;
| else
| some pair (m', w) already exists;
| if w prefers m to m' then
| (m, w) become engaged;
| m' becomes free;
| else
| (m', w) remain engaged;
| end
| end
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Algorithm 1: Stable Matching Algorithm

3.3 Connecting Boundary Control Points

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The first step to this algorithm is to match all the entry and exit points. To do this, we have to measure how good or bad a match is. Intuitively, there are some better matches than others, Judging by sight, trajectories passing near the center of the patch look better that the ones staying close to the borders. We can consider some other aspects too, like how close the speed needed for the agent to go from the Entry Point to the Exit Point is to comfort speed. We use a comfort speed u_{cft} of $1.33\ m/s$ which is the normal walking speed of humans in an unconstrained environment.

For a square patch, we prefer to match points with points on the opposite pattern. Then the points on the contiguous pattern and finally, the points that are in the same pattern. If there are multiple options on the same pattern we choose the point whose associated trajectory is closest to comfort speed.

To solve this matching problem, we make use of the Gale-Shapley algorithm [Gale and Shapley 1962] (see Algorithm 1), commonly referred to as the algorithm to solve the stable marriage problem. This algorithm assures that at the end, if we have Alice engaged to Bob and Carol engaged to Dave, it is not possible for Alice to prefer Dave and Dave to prefer Alice. We call that a stable matching.

This pseudocode demonstrates the Gale-Shapley algorithm in relation to two equal lists of men and women who are being matched for marriage. However the algorithm generalizes to any matchable objects, which in our case is entry and exit points.

All we need in order to use this algorithm is a to generate preferences for entry and exit points. We do this with the following steps:

- 1. Find the speed it would take to travel from an Entry Point to an Exit Point. Let assume (\mathbf{p}_1,t_1) is position and time of the Entry Point and (\mathbf{p}_2,t_2) the equivalent of the Exit point. Speed u is d/t where $d=|\mathbf{p}_1-\mathbf{p}_2|$ and $t=t_2-t_1$ in case $t_2>t_1$. Otherwise, $t=period+t_2-t_1$. More details on why we take this time will be given later when we create the initial set of trajectories.
- 2. Now, we assign each pair of points a number between 0 and $\pi/2$, where 0 represents maximum closeness to comfort speed with $arctan(|u_{cft} u|)$.
- 3. We add penalties for points being in the same patch, for those points, we add 4. For points lying in the contiguous pattern we also add a smaller penalty, 2.

4. We sort each list.

307 The steps above need editing

We will have a list similar to this for each entry and exit point, we call this list the proposal list (see Table 1).

Exit Points F and D lie in the same pattern as Entry Point A, so they receive a higher number. After this, we use the stable matching algorithm mentioned above.

Every two points that remained engaged at the end of the algorithm become a pair. The last step is to create the initial batch of trajectories. We start by trying to connect the points with a straight line. We do something special when a line tries to travel backwards in time, i.e. $t_2 < t_1$. For these cases we split the initial trajectory in two. One going from t_1 to period π , another one going from 0 to t_2 . The positions of these new control points are in the same straight line, taken in such a way that the speed is the same going from t_1 to π and from 0 to t_2 . We use the same method if the trajectory is moving at unrealistically fast speeds.

We make further adjustments in the initial trajectory in some special cases. For agents traveling only over the edge, we add a control point near the center of the patch. For agents moving slowly we add a control point with same position, but different time, thus making the agent do a full stop (as if pausing to look around), after a few moments it continues its journey with a better speed.

The output of this function is a set of trajectories. Collisions are probably still present in the trajectories at this point.

- INPUT OUTPUT objective

- when you connect two boundary conditions, you connect two spation temporal waypoints. This means that you determine this way where characters enter, where they exit patches and the speed between waypoints.

- we can define what is a oodconnection: avoid half turn, avoid extreme speeds.

- we define an objective function, we solve this using the stable marriage problem.

- reminder of 2009 paper - you explain the specific case of splitting trajectories.

- you provide pseudo algo for this,

- you define all the variables/parameters you use.

summarize what you get as an aoutput, and what is the next step.

3.4 Removing Collisions

Make sure for all the equation that the correct symbols are inserted: bold for vectors, normal fonts for scalars, etc.

Table 1: Proposal List

Rankings of preferred partners for Entry Point A

Preference	Exit Point	
0.34	В	
1.3	C	
2.3	A	
2.4	Е	
4.5	D	
4.6	F	

Table 2: Minimum Distances

	τ_0	$ au_1$	$ au_2$
τ_0	0	100	8.31
$ au_1$	100	0	0.14
$ au_2$	8.31	0.14	0

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389 390 We are given a set of trajectories within a patch consisting of both movable and boundary control points. What we expect in return is modified trajectories that have maintained their spatio-temporal entrance and exit points while removing all collisions throughout the entire period of the patch. Our objective is to use these patches in larger crowd simulations of people. We would like to create trajectories that could represent human motion. We focus on creating collision free motion since obvious collisions in simulations greatly reduces the realism of the animation.

Given two trajectories you can find the distance between them at any moment in time. The shortest distance between trajectories is the minimum of all these distances computed over the period of the patch. To compute the minimum distance between two trajectories we find the minimum distance between all the segments of the trajectories and take the minimum of the minimums as our final answer. When looking at two segments we find the intersection of the time intervals. If the intersection is not empty, we find the minimum distance. We call the start and end time of this intersection t_0 and t_1 respectively.

Each one of those segments represent a moving agent with an initial position \mathbf{p}_0 and \mathbf{p}_1 with velocities \mathbf{v}_0 and \mathbf{v}_1 moving in the time interval $[t_0, t_1]$.

We can then define the distance at a certain time between the two segments with the following equation.

$$d(t) = ||(\mathbf{p}_0 + \mathbf{v}_0 * t) - (\mathbf{p}_1 + \mathbf{v}_1 * t)|| \tag{4}$$

For simplicity we say $\mathbf{w} = \mathbf{p}_0 - \mathbf{p}_1$ and $\mathbf{d}\mathbf{v} = \mathbf{v}_0 - \mathbf{v}_1$, so then,

$$d(t) = ||\mathbf{w} + \mathbf{dv} * t|| \tag{5}$$

We are looking for the minimum so we solve for t when when the derivative equals zero.

$$t_c = (-\mathbf{w} \cdot \mathbf{d}\mathbf{v})/||\mathbf{d}\mathbf{v}||^2 \tag{6}$$

With t_c , the time at which the two line segments are closest we can easily calculate the position on each of those segments, and thus the distance between them. If the time is outside the bounds of the segment we check the endpoints of the line segment for collision.

We compute a minimum distance between each pair of trajectories. We store each value in a minimum distance matrix M. The position in the matrix corresponds to the trajectory ID. So the value at M(i,j) would be the minimum distance from trajectory τ_i to trajectory τ_j . It's good to note that this value will be the same as M(j,i). Furthermore M(i,i) will always be zero and distance for trajectories that don't intersect in time, we set them to a number bigger than the threshold for collisions, for example 100 for a threshold of 1 (see Table 2). These facts can be used to reduce computation while filling out the minimum distance matrix.

Do we have an image for this distance matrix? Actual image? Or a table? I can do that anyways, as soon as I figure out how to create a nxn table in latex 428

Compute minimum distance matrix M;

while there exists at least one entry in M below the threshold ${\bf do}$ Find indices i and j for which M(i,j) has the smallest value d; Create temporary control points ${\bf cp}_i$ and ${\bf cp}_j$ in τ_i and τ_j that are at distance d; Apply repulsion forces to ${\bf cp}_i$ and ${\bf cp}_j$; Update τ_i and τ_j ;

Update M; end

Algorithm 2: The control points generation algorithm

Our algorithm (see Algorithm 2) creates collision free trajectories by adding and modifying control points. We can guarantee this by looking at the minimum distance matrix. If every value in the matrix is above some threshold then we know that for the entire period of the patch no two agents come closer than that threshold. So if we make that threshold equal to the sum of the radii being compared, those agents will never touch.

Write the pseudo code in an algorithm format

We begin by computing the minimum distance matrix. Then while collisions still exist we find the smallest value in the minimum distance matrix. From that we find the corresponding trajectories and a point of closest approach for each trajectory \mathbf{p}_1 and \mathbf{p}_2 . We then find an updated position for each of these points.

To find the the updated position of a new point we add a correction force \mathbf{F}_c to its current position \mathbf{p}_1^{old} .

$$\mathbf{p}_1^{new} = \mathbf{p}_1^{old} + \mathbf{F}_{c_1} \tag{7}$$

Why P_1 and not just \mathbf{p} ? Clarify p_1 and p_2

assign symbols for all forces and position mentioned to make the equations more compact. . .

The correction force \mathbf{F}_c for each point is found based on: the radius of the two agents, r_1 and r_2 , which define a threshold $e=r_1+r_2$; a constant weight to help reduce speed artifacts and prevent agents from leaving the bounds the patch w_1 and w_2 , each of them depending on the values of speeds u_1 and u_2 ; and a small random noise rotation matrix R to help prevent infinite loops, the angle of rotation is chosen between -.5 and .5 radians.

$$\mathbf{F}_{c_1} = \widehat{R(\mathbf{p}_1 - \mathbf{p}_2)} * e * w_1 \tag{8}$$

Do we need the wide hat?

NOTE: In our implementation $r_1 = r_2$, making the threshold constant.

SHORTEN THE TEXT IN THE EQUATIONS!!

$$w_1 = \begin{cases} u_2/(u_1 + u_2) & \text{if the point won't go outside the patch.} \\ 0 & \text{otherwise} \end{cases}$$
 (9)

The calculations for \mathbf{p}_2 are symmetric. Once we have this new point for the trajectory we check to see if there is already a control point within a small time interval of the new point. If there is we move that control point to this new position in space and time. Otherwise we add a control point in the trajectory at this new position. Finally we update the minimum distance matrix. We do not need to recheck all the distances in the matrix, only the ones that interact with the trajectory we have modified.

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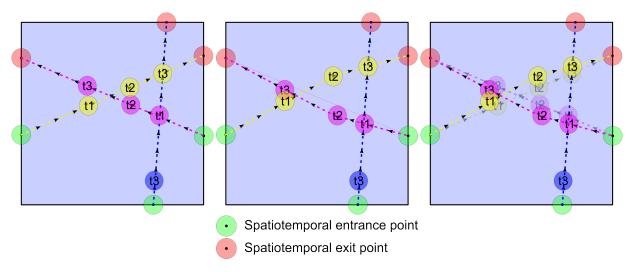


Figure 3: Collision removal

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We find that in many situations this algorithm converges quickly 464 and produces collision free trajectories. However there are still sit- 465 uations where it converges slowly or even gets stuck in an infinite 466 loop.

Smoothing 3.5

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Smoothing: We have obtained some collision free trajectories, but they may have a jerky trajectory, so we need a final the step to smooth them. We need to take special care of how we do this, we don want the trajectories to change in such a way that they make new collisions. A simple approach is to use cubic splines. Cubic splines connects every pair of points in a trajectory with a polynomial function of degree 3:

$$S(x) = a + bx + cx^{2} + dx^{3}$$
 (10)

In total, we will need to find the coefficients a, b, c, and d for every segment we have in our trajectory. Those coefficients are determined by continuity C^1 restrictions: 443

For every spline associated with a trajectory between control point $\mathbf{cp}_1 = (\mathbf{p}_1, t_1)$ and $\mathbf{cp}_2 = (\mathbf{p}_2, t_2)$, the spline must pass through 445 those same points, that is, $S(t_1) = (\mathbf{p}_1)$ and $S(t_2) = (\mathbf{p}_2)$.

For every two contiguous splines S_1 and S_2 , for the common point 447 they share p, the velocity must be equivalent, that is, $S'_1(\mathbf{p})$ 448

This restrictions can be accommodated in a such way that they form 450 a system of linear equations that can be solved using Cholesky de- 489 composition. 452

We can not apply directly this method using our current control 492 points. That results in trajectories that vary too much from the original, thus they may end up creating new collisions. To make the spline more similar to the original trajectory, we add new virtual control points sampled uniformly in the linear segments of the trajectories. We call these tacks. These tacks help fix the splines, because they will now pass through the control points and the tacks. Note that the more tacks we put, the closer the spline will fit to the original path.

After that, we compute the coefficients to create the splines and 500 resample along the spline to get new control points. The new trajectory will still be composed of line segments, but since they are smaller, and following closely the path of a cubic function, to the naked eye they will look like curves. The finer the sample, the more it will look like a smooth path.

For optimization purposes, the second sampling is not taken uniformly. The trajectories are relatively straight in the middle of the the segments and have higher curvature near control points. For that reason, we take more samples around inflexion points (old control points) than far from them. These samples become the new control points that define the trajectory.

There may be cases, even with a healthy number of tacks, that the splines still vary too much from the original trajectory. We define a threshold based on the same threshold of collision to know how far a way a point can be moved. For these cases where the new control point surpasses the threshold, we simply don add it to the set of new control points. There may be extreme cases (for example, due to too a bad sampling of the tacks at the beginning), where the spline has extreme curves that are very different from our initial trajectory. In those extreme cases most of the new control points would not be added and the new smooth trajectory would end up being very similar to the original one.

Having splines for trajectories is better than having simple straight lines, but we know humans don follow either of them when walking, so other methods can be tried to improve this initial approach.

Results

We found that our algorithm created trajectories that were free of collisions and produced smooth motion. In Figure 4 we have a diagram showing the patch in various steps of our algorithm. Next we show the final curved trajectories with various sized input. Lastly we show some performance tests.

the images are not lining up how I want them too. Devin, I took the liberty of modifying the figures below to show you how its typically done. Note the label for referencing the figures in the text. I don't really know how to control the position at which the figures appear, or where do we want them exactly.

The performance was measured on a computer with an Intel Xeon quad core 2.8 GHz processor and 8GB of RAM. We found trajectories for patches with randomly generated entry and exit points. The

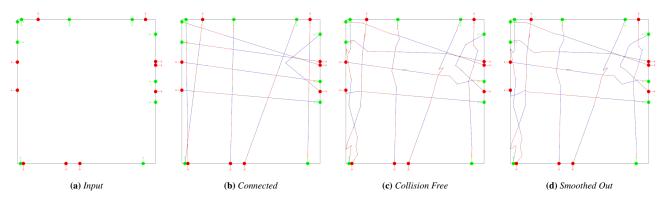


Figure 4: Various steps of our algorithm.

patches all had base square of size 16 by 16. The period was 10 seconds. There were 20 samples for each number of agents between 1 and 50 for a total of 1000 samples. 994 of these were collision free. The other 6 were stopped after they reached 2000 iterations. We recorded the number of iterations required for collision free trajectories as well as the computation time in seconds.

5 Discussion

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Convergence The convergence of this algorithm, depends mostly on the how many agents well want in the scene. As we can see, the bigger that number is, the slower it takes to create a patch and the most dangerous it becomes not reaching a solution.

When we have two boundary control points very near each other in space-time coordinates, the harder it will be for the trajectories to converge, since the only way to find a collision free trajectory would be moving those fixed boundary control points. For that, a better technique may be implemented, so when we just want a random initial batch of boundary control points, they are generated in such a way there is enough space between one another. 553

Spatial moving of waypoints only In this paper, we use mostly spatial corrections to the trajectories of the agents. For some scenarios, moving the point in space coordinates may not be the best way to go, it could provoke the control point to try to move outside of the patch boundaries or make a huge change in the agents speed.

Some collisions may be avoided just by changing the time in one of the two movable control points of a segment, thus making the agent move faster or slower without modifying the spatial trajectory. This would solve the problem of going out of the boundaries, but we have to be careful on how we change the time if we dont want to produce an unrealistic change in velocity. We also have to be careful that trajectories can never go backwards in time.

Obstacles We mentioned earlier a patch may have static agents, called obstacles. With this technique, how can obstacles be added?

For a small number of obstacles, we can consider obstacles just like any other agent, and incorporate them into the algorithm with the extra condition that they can never be moved. The only problem, is that obstacles must be well placed. When two obstacles are close enough that the form a tunnel for one initial trajectory, the movable control point will start looping going from one obstacle to another, unable to find a collision free trajectory. A possible solution for this, may be grouping the obstacles that are close to one another and consider them as a bigger obstacle. This will quickly start occupying the area of the patch, so in general, the obstacles will need to be few.

6 Conclusions

We present a novel technique for computing trajectories for use in crowd patches. We can take an empty patch and generate trajectories within that can represent human motion. Our technique produces smooth collision free motion. This algorithm is slow to converge, especially with larger groups. Furthermore while our approach produces collision free trajectories it is lacking in other aspects of human motion. For one, agents can reach unrealistic speeds. Additionally agents can have abnormal motion that is not true to human behavior. In the future we plan to implement a more global approach that looks at more than just the closest agent and incorporates speed into the calculations. We hope that this will provide faster convergence in high density situations as will as fixing motion artifacts.

- reminder of contributions - comment on results and limitations - paths for future work.

Acknowledgements

Who do we love so much we want to worship them?

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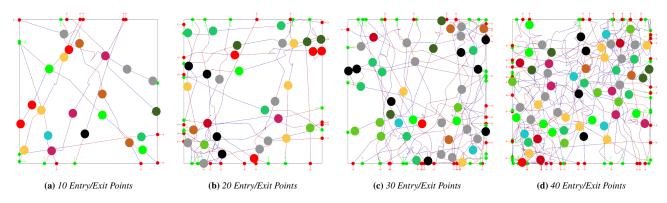


Figure 5: Various input to our algorithm.

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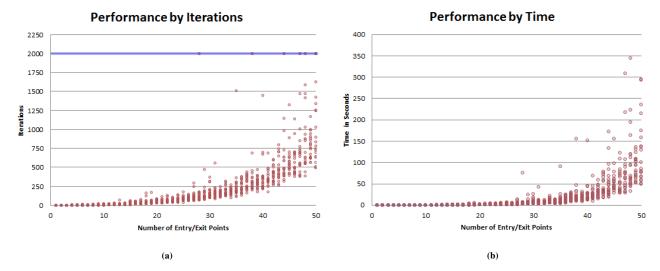


Figure 6: A dot on each graph represents a simulated patch. The patch had a specified number of entrance and exit points whose locations were randomly generated. Our algorithm was run until either the patch was collision free, or it reached 2000 iterations. (a) The the number of iterations was recorded in relation to number of Entry/Exit Points. The blue line at 2000 iterations shows where the simulation was stopped (6 out of 1000 patches were stopped here, and thus were not collision free). (b) The time to converge was measured in seconds. is this explanation more clear?

//each experiment needed to converge whereas the blue horizontal line indicates the maximum number of allowed iterations (6 out of 1000 inputs What do we mean by inputs? experiments or the total number of trajectories. Does this graph show how much time it took for a whole patch or for the trajectories with collisions? didn't converge after 2000 iterations). (b) The time to converge was measured in seconds. should I remove the titles on the images of the graphs, and instead put their title in the caption? No, you should leave them.. If you can edit the images, please remove the borders. I think it will look nicer. Also, this graphs confuse me a little bit. We should discuss them with Guillermo - I want to get a feeling of what exactly are we showing here

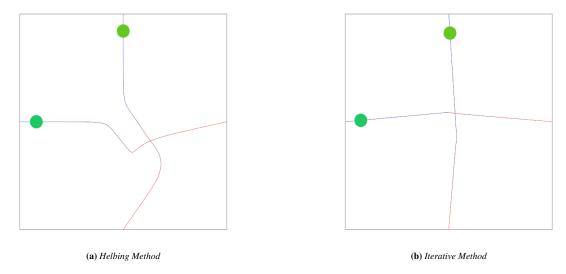


Figure 7: A comparison between both methods, shows the improvement in terms of anticipating a collision. Figure (a) shows little anticipation, it modifies its trajectory until it is about to collide, whereas (b) starts modifying its trajectory gradually from the beginning.

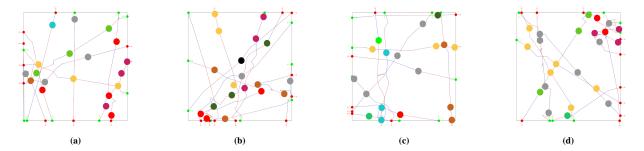


Figure 8: Several examples showing the final trajectories for 10 Entry/Exit Points