

Analyzing Machupo virus-receptor binding by molecular dynamics simulations

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1 Introduction

2 The computational prediction of mutational effects on protein–protein interactions remains a chal-
3 lenging problem. Several methods are available to perform an energy difference calculation from an
4 experimentally determined co-crystal structure. For example, end point methods can be performed
5 rapidly, with relatively low computational cost (Gront et al. 2011; Kortemme et al. 2004). How-
6 ever, such methods can suffer from various simplifying assumptions. For example, they generally
7 use an implicit solvent approximation and assume the end state difference with minimal structural
8 rearrangement is sufficient to discriminate energetic differences (Gront et al. 2011; Kortemme et al.
9 2004). Alternative approaches have been developed using machine learning, training coefficients
10 in a weighted equation containing geometric and energetic parameters (Vreven et al. 2011, 2012;
11 Bajaj et al. 2011; Hwang et al. 2010). Unfortunately, such machine-learning approaches often suf-
12 fer in novel applications, for which available training sets are small or non-existent. As such, these
13 methods are poorly suited for most host-virus protein–protein systems. By contrast, first principles
14 methods can forgo training, but currently available methods such as free energy perturbation (FEP)
15 and thermodynamic integration (TI) rely on a transitional model (where one state may be wild-type
16 and the other may be a mutant) to make rigorous free energy calculations (Gilson et al. 1997; Lu
17 et al. 2004; Chodera et al. 2011; Gumbart et al. 2013a). While these may be considered two of the
18 gold standard techniques for calculating affinity differences, there are a huge number of theoreti-
19 cal and technical complexities that must all be properly managed to ensure a converged solution
20 (Gumbart et al. 2013b). Such considerations quickly come to dominate the protocol, and the nec-
21 essary book keeping introduces the possibility of human error (Gumbart et al. 2013b). Moreover,
22 as the two ending states look ever more dissimilar the chances of convergence fall rapidly. To en-
23 sure convergence, these techniques are typically limited to small differences (such as point mutant
24 comparisons) with a few, very impressive exceptions (Wang et al. 2006; Gumbart et al. 2013a,b).
25 For most investigators, larger differences quickly become intractable as the number of intermedi-
26 ate steps required to compute a converged solution grows or the complexity of adding restraining
27 potentials and computing approximations expands (Wang et al. 2006; Gumbart et al. 2013a,b).

28 Here we propose that much of these complexities can be avoided if all we are interested in is a
29 relative comparison of the effects of different mutations on protein-protein interactions, rather than

measuring an absolute or relative binding affinity with experimentally realistic units. We impart a pulling force within an all-atom molecular dynamics simulation on one member of the complex while the other is held in place. Then, we measure the force required for dissociation (Lu and Schulten 1999; Isralewitz et al. 2001b,a; Park and Schulten 2004; Gumbart et al. 2012; Miño et al. 2013). Although such biasing techniques are commonly used in protein-ligand binding problems, they are less commonly applied to protein–protein interactions, and almost never to mutational analysis in a protein–protein system. This is largely the result of free energy convergence difficulties and computational limitations (Cuendet and Michelin 2008; Cuendet and Zoete 2011). Using a proxy for relative binding affinity rather than caluclating absolute affinities can solve these problems. Here, as proxies, we use the maximum applied force required for separation and the area under the force-versus-distance curve (AUC). For comparison, we also calculate relative free energy differences using the traditional dual topology FEP paradigm, and we show that the two approaches yield congruent results.

We used SMD and FEP to interrogate the interaction between machupo virus (MACV) spike glycoprotein (GP1) and the human transferrin receptor (hTfR1) (Abraham et al. 2010; Charrel and de Lamballerie 2003). Machupo virus is an ambisense RNA virus of the arenavirus family (Charrel and de Lamballerie 2003). Worldwide, arenaviruses represent a significant source of emerging zoonotic diseases for the human population (Charrel and de Lamballerie 2003). Members of the arenavirus family include the Lassa fever virus endemic to West Africa, the lymphochoriomeningitis virus (LCMV) endemic to rodents in several areas of the United States, and the Guanarito, Junin, and Machupo viruses endemic to rodents in South America (Charrel and de Lamballerie 2003). The South American arenaviruses typically infect humans after rodent contamination and can cause a devastating hemorrhagic fever with high mortality (Charrel and de Lamballerie 2003).

The hTfR1 is the primary receptor used by MACV for binding its host cell prior to infection. The primary role of hTfR1 *in vivo* is to bind transferrin for cellular iron uptake. The hTfR1 protein contains three extracellular domains: two basilar domains and an apical domain. The two basilar domains serve most of the transferrin-binding function (Abraham et al. 2010; Radoshitsky et al. 2011). Viral entry is initiated by GP1 binding to the apical domain of hTfR1. Previous work has indicated that the GP1/hTfR1 binding interaction is the primary determinant of MACV host range variation (Choe et al. 2011; Radoshitsky et al. 2011). The co-crystal structure shows that the high

60 affinity interaction between GP1 and hTfR1 forces the normally flexible loop in the apical domain
61 of hTfR1 into a rigid β -pleated sheet domain. For GP1, several extended loops mediate binding to
62 hTfR1 (Abraham et al. 2010; Radoshitzky et al. 2011), and many of the interface interactions are
63 mediated by extensive hydrogen-bonding networks (Abraham et al. 2010) (Figure 1). Experimental
64 alanine-scanning and whole-cell infectivity assays have identified several sites in both GP1 and
65 hTfR1 that are probably critical for establishing infection (Choe et al. 2011; Radoshitzky et al.
66 2011).

67 We applied our computational method to wild type (WT) and mutant complexes, and found
68 that we could resolve relative differences in unbinding and predict significant affinity changes.
69 Importantly, the affinity changes predicted using only max force or AUC show a strong correlation
70 with rigorous relative free energy differences computed by FEP. At sites known to be important for
71 successful viral entry, we found that the biochemical cause of reduced infectivity may not be as
72 simple as the static structure suggests. For example, the static structure shows a hydrogen-bonding
73 network connected to site N348 in hTfR1. According to our simulations, this network may not
74 affect binding affinity directly. In addition, our study offers an all-atom steered molecular dynamic
75 approach to avoid some of the pitfalls of several existing methods used to evaluate mutations in
76 protein–protein interfaces.

77 2 Materials and Methods

78 2.1 System Modeling

79 For our experiments, we used the experimentally determined GP1/hTfR1 structure (PDB-ID: 3KAS)
80 (Abraham et al. 2010). The apical domain of hTfR1 interacts directly with GP1 while the other two
81 domains are closer to the cell membrane and have essentially no interaction with GP1. The bio-
82 physical independence of the apical domain allowed us to isolate it without significantly affecting
83 the GP1/hTfR1 interaction.

84 We used the protein visualization software PyMOL (Schrödinger 2010) to remove residues
85 121-190, 301-329, and 383-756 in the hTfR1. No residues were removed from the viral protein.
86 Figure 2 shows a model of the initial structure and that of the pared structure. Although GP1 has

87 several glycosylatable residues, we opted to use the de-glycosylated protein for this study. The
88 complexity of correctly parameterizing diverse sugar moieties is outside of the scope of this paper.
89 Furthermore, although it is known that GP1 is glycosylated, and some of those sugars contact
90 hTfR1, the sugars in the available PDB structure are not physiological for mammals (Abraham
91 et al. 2010). In total we removed 10 sugars from the crystal structure for this study.

92 After system reduction, the Visual Molecular Dynamics (VMD) (Humphrey et al. 1996) pack-
93 age along with its system of back-ends was used for all subsequent modeling. The Orient add-on
94 package allowed us to rotate the system axis such that the direction of steering was oriented di-
95 rectly down the z-axis. De-glycosylation simplified the system such that Autopsf could easily find
96 the chain terminations and patch them appropriately. The Solvate package was used to generate a
97 TIP3P water model with a 5 Ångstrom buffer (relative to the maximum dimensions of the proteins)
98 on all sides except down the positive z-axis where a 20 Ångstrom buffer was created. Finally, we
99 used the Autoionize package to place 150 millimolar NaCl and neutralize the total system charge.
100 In the end, each modeled system had approximately 28,000 atoms.

101 **2.2 Equilibration**

102 NAMD was used for all simulations in this study (Phillips et al. 2005). In addition to the modeled
103 system, for equilibration we generated a configuration file that fixed the α -carbon backbone. This
104 was accomplished by setting the B-factor column to 1 for the fixed atoms and to zero for all other
105 atoms. Further, we generated a configuration file with fixed α -carbon atoms at residues 41-92 (num-
106 bered linearly, in this case, starting at 1 for the first amino acid as was required for NAMD) in the
107 hTfR1. The second file was used to affix a harmonic restraint, thus preventing any unfolding due to
108 system reduction. More importantly, the harmonic restraint allowed the protein complex to equili-
109 brate while preventing any drift from its predefined position; the restraint did not constrain the struc-
110 ture of each protein, or the relative position or orientation of the two proteins to each other. Finally,
111 we calculated the system center and dimensions for use in molecular dynamics settings. The exact
112 NAMD configuration files are available on github (https://github.com/clauswilke/MACV_SMD).

113 We used the Charmm27 (Brooks et al. 1983) all-atom force field. The initial system temperature
114 was set to 310K. Several typical MD settings were used including switching and cutoff distances
115 (see provided configuration files). In addition, we used a 2 femtosecond time step with rigid bonds.

116 We used periodic boundary conditions with the particle mesh ewald (PME) method of computing
117 full system electrostatics outside of the explicit box. Furthermore, we used a group pressure cell,
118 flexible box, langevin barostat, and lavegin thermostat during equilibration. A harmonic restraint
119 (called harmonic constraint in VMD) was set as stated previously.

120 To start the simulation, the barostat was switched off and the system was minimized for 1000
121 steps. Next, the fixed backbone was released, and the system was minimized for an additional 1000
122 time steps. Subsequently, the system was released into all-atom molecular dynamics for 3000 steps.
123 Finally, the langevin barostat was turned on and the system was simulated for 2 ns (1,000,000 steps)
124 of chemical time. For each mutant, twenty independent equilibration replicates were run with an
125 identical protocol.

126 **2.3 Steered Molecular Dynamics**

127 We used the final state from each equilibrated system to restart another MD simulation. Our steer-
128 ing protocol is fundamentally similar to Cuendet and Michelin (2008) with slightly different pa-
129 rameter choices. Perhaps the one significant difference lies in our choosing to not use a thermostat
130 or barostat. We can make this choice because we are not trying to calculate the binding free en-
131 ergy by any physically rigorous approach (the Jarzynski inequality being one example). Following
132 equilibration, the final state of each simulation was used to generate a configuration file fixing the
133 α -carbon on residues 1, 58, 73-83, 96, 136, 137, 138, and 161 (again with linear numbering) in
134 the hTfR1. These residues were selected as they are far from the binding interface and sufficiently
135 distributed to prevent any orientational motion of the receptor relative to the viral spike protein.
136 The center of mass of the α -carbons of all residues (163-318 in linear numbering) in GP1 received
137 an applied force during the simulation. The NAMD convention does not actually apply a force to
138 all α -carbon atoms but rather uses the selection to compute an initial center of mass. Then, during
139 the steering run, the single center of mass point is pulled with the parameters described below.
140 We used the same force field parameters (exclude, cutoff, switching, etc.), the same integrator pa-
141 rameters (time step, rigidbonds on, all molecular being wrapped, etc.), and the same particle mesh
142 ewald parameters as in equilibration. Periodic boundary conditions were incorporated as part of
143 the system (as is the convention in NAMD restart) and PME was again used to approximate full
144 system electrostatics.

145 We ran test simulations at several force constants and visually inspected the results. A force
146 constant of 5 kcal/mol/Å² was chosen due to its relatively low signal-to-noise ratio. This constant
147 is slightly lower than the more common 7 kcal/mol/Å² found in several recent studies; that value is
148 commonly selected primarily because it is the force constant found in the SMD tutorial available
149 through the NAMD developers. Moreover, the force constant could very likely be set to a range of
150 nearby values with little loss in predictive power.

151 In SMD experiments the pulling velocity should be as low as possible for the available com-
152 putational time (Cuendet and Michelin 2008; Cuendet and Zoete 2011). We choose a velocity of
153 0.000001 Å/fs = 1 Å/ns, and direction down the positive *z*-axis. One could use faster pulling if
154 the computing time must be reduced, but slower than necessary pulling speeds are not typically
155 considered problematic.

156 SMD was run for 15 ns (7,500,000 time steps) of chemical time. For each simulation, we
157 randomly selected one of the equilibration runs for restart. We ran 50 replicate simulations per
158 mutant for a total of 550 SMD simulations. All GP1/hTfR1 complexes separated by greater than 4
159 Å and many separated to 10 or more.

160 To leave the final trajectory of a tractable size, only 1000 evenly spaced frames were retained
161 from each simulation, leaving a final trajectory size of 323 MB. See the supplemental movie for
162 a representative unbinding trajectory. Initial development of the SMD protocol was carried out
163 on the Lonestar cluster at the Texas Advanced Computing Center (TACC). All production SMD
164 simulations were performed on the Hrothgar cluster at Texas Tech University, using NAMD 2.9.
165 Each simulation was parallelized over 60 computational cores and utilized approximately 20 hours
166 of computing time. The total chemical time simulated for this project was nearly 10 μs, requiring
167 slightly over 1 million cpu-hours.

168 2.4 Free Energy Perturbation

169 Briefly, we used the traditional dual topology approach to FEP (Gao et al. 1989; Pearlman 1989).
170 This involves a thermodynamic cycle where a set of atoms are progressively decoupled from the
171 environment while another set of atoms are progressively coupled. To compute the relative free
172 energy difference requires knowing the free energy change when the transformation is carried out
173 for the bound complex and the individual protein. Then, one can compute the relative free energy

174 difference between a WT and mutant complex by taking the difference between the energy required
175 to decouple/couple the atoms in solution from the energy required to decouple/couple the atoms in
176 the bound complex (Gao et al. 1989; Pearlman 1989).

177 Again, the NAMD configuration file is made available via github (https://github.com/clauswilke/MACV_SMD)
178 We used a similar configuration to that in equilibration. One significant difference was to make a
179 cubic water box with a side length equal to the long axis of the complex plus a 10 Å buffer on either
180 side, and simply restrict center of mass motion with the NAMD setting. This was done to avoid
181 affecting the system energy while calculating free energy differences.

182 The transition protocol for bound and free protein systems were identical. They started with
183 1000 steps of minimization and 250,000 steps of equilibration in the starting state for the forward
184 and reverse directions. Phase transitions were carried out in steps of $\lambda=0.05$. Each transition
185 was carried out for 250,000 steps. The first 100,000 steps after phase transition were reserved for
186 equilibration and the final 150,000 steps were used for data collection.

187 The VMD mutator tool was used to generate the necessary topology file and the parseFEP tool
188 (Liu et al. 2012) in VMD was used for subsequent analysis. We used it to perform error analysis
189 and compute the Bennett acceptance ratio as the maximum likelihood free energy difference of the
190 two states under consideration. Though the larger transitions presented difficulty in a small number
191 of windows, forward and reverse hysteresis was generally in good agreement for all complexes.
192 The double mutants were performed by first doing the Y211A mutation followed by the other of
193 the two mutants. Then, the ΔG 's were simply added together to get the total energetic difference.

194 2.5 Post-processing

195 The python packages MDAnalysis (Michaud-Agrawal et al. 2011) and ProDy (Bakan et al. 2011)
196 were both used at various points in post-processing. The molecular trajectory (comprising the
197 atomic coordinates per time) was parsed to compute the center-of-mass for each of the two com-
198 plexes. The starting center-of-mass distance was set to zero and the distance was re-computed at
199 each time step relative to the starting distance.

200 The statistical package R was used for all further analysis and visualization. Each of the 50
201 independent trajectories per mutant produced a fairly noisy force curve. The force curves for each
202 mutant were smoothed over all replicates by using the smooth.spline() and predict() functions in R

203 with default settings. The two primary descriptive statistics we used were maximum interpolated
204 applied force and total area under the interpolated curve (AUC). We tested for significant differences
205 in maximum force or AUC by carrying out t tests for all pairwise combinations (each mutant com-
206 pared to each other mutant), using the pairwise.t.test() function in R. We adjusted p values to cor-
207 rect for multiple testing using the False-Discovery-Rate (FDR) method (Benjamini and Hochberg
208 1995). The ggplot (Wickham 2009) package was used to generate most of the figures.

209 Analysis scripts and final data (except MD trajectories) are available on the github repository
210 accompanying this publication (https://github.com/clauswilke/MACV_SMD).

211 3 Results

212 3.1 The GP1/hTfR1 system

213 The GP1/hTfR1 interface marks a particularly important and useful test system. There are sev-
214 eral sites on both the human and viral protein known to affect the infectivity phenotype of MACV.
215 Many of the important sites have been mapped by *in vitro* flow-cytometry based entry assays. The
216 GP1/hTfR1 interface appears not to be dominated by one particular type of interaction (electro-
217 statics, hydrogen-bonding, or van der Waals). In addition, much of the binding domain on hTfR1
218 is on a loop that is flexible prior to viral binding, but organizes to become a strand of a β -sheet
219 on binding. As a result, many other computational techniques (Gront et al. 2011; Kortemme et al.
220 2004) are only marginally useful. The complex nature of this interface represents a particularly
221 difficult challenge for traditional computational analysis.

222 In total, we tested 7 point mutants and 3 double mutants in addition to the WT complex (Table 1
223 and Figure 9). All of the mutations are within 5 Å of the protein–protein interface. Mutations in
224 hTfR1 at site 211 have proven capable of causing loss-of-entry according to *in vitro* flow-cytometry
225 infection assays or known host-range limitations (Radoshitsky et al. 2008; Choe et al. 2011; Ra-
226 doshitsky et al. 2011). Most likely, this effect is caused by the destruction of a critical hydrogen
227 bond to Ser113 or Ser111 in GP1. The lost hydrogen bond would lead to the subsequent loss of a
228 large hydrogen-bonding network seen in the crystal structure (Table 1) (Abraham et al. 2010). In a
229 manner similar to site 211, N348 appears to be important for binding by participating in a critical

hydrogen bonding network (Radoshitzky et al. 2008; Abraham et al. 2010) to GP1. In particular, N348Lys is reported in the literature to cause significantly reduced viral entry *in vivo* (Table 1) (Radoshitzky et al. 2008; Abraham et al. 2010). Finally, an alanine mutation at site 111 in GP1 (mutation vR111A) has also been shown to cause decreased entry (Table 1) (Radoshitzky et al. 2011). For notation purposes, the viral site is always referred to with a preceding ‘v’.

Despite the fact that viral binding occurs at the site of a flexible loop in the free hTfR structure, our data shows after binding the strand is extremely rigid. In the bound conformation, only two sites of the loop have root mean squared fluctuation (RMSF) values in the top half of all receptor sites during equilibration (Figure 3), and those are almost completely exposed to solvent. This is unsurprising considering the high degree of burial that occurs as a result of viral binding. Computing the root mean squared deviation (RMSD) of the entire structure over the trajectory shows that none of the mutations are so deleterious as to cause rapid unbinding. In fact, the RMSD over trajectory looks highly invariant across mutants (Figure 4). In the unbound state, calculated near the end of the SMD trajectory, all of the residues in the WT receptor interfacial strand are in the top half of RMSF over all receptor sites (Figure 5). Thus, if sufficient simulation time is not dedicated to allowing this unfolding process, standard free energy techniques may miss the energetic contributions that result from ordering the flexible loop in the hTfR apical domain.

3.2 Molecular dynamics simulations

We analyzed the GP1/hTfR1 system using two molecular dynamics techniques. First, by carrying out SMD using a known force constant and pulling with a constant velocity, we could calculate the applied force during protein–protein dissociation (Cuendet and Michielin 2008; Cuendet and Zoete 2011). A typical averaged force curve comparison can be seen in Figure 6, and individual images of all averaged force curves are available in the associated github repository, in folder figures/force_curves. As seen in Figure 6, the dissociation distance was relatively consistent among mutants. The supplementary movie visually illustrates the separation distance between peptide domains. The quantities maximum applied force and AUC were derived from the force-versus-distances curves. Their summary statistics are reported in Table 2. As we are more interested in the phenotypic impact of interface mutations we avoided many of the more physically rigorous, but technically complicated calculations that are possible with SMD (Isralewitz et al. 2001b,a).

259 Before systematically applying SMD to the GP1/hTfR1 interaction, we needed to ensure the
260 method was sufficiently sensitive to distinguish between relatively minor point mutations. While
261 SMD has been applied previously to measure the binding energy of high-affinity T-cell receptor
262 interactions (Cuendet and Michelin 2008; Cuendet and Zoete 2011), it is rarely used to parse small
263 energy differences in a protein–protein interaction energy landscape. For this initial sensitivity anal-
264 ysis, we tested alanine substitutions congruent with the traditional experimental and computational
265 approach.

266 We proceeded to compare our SMD results to that of the standard dual topology FEP approach
267 to calculate relative free energy differences. The correlation between the energetically rigorous
268 FEP and our statistical approach is high. For all 11 complexes tested, the correlation between max
269 force and FEP was $r = -0.795$ at $p = 0.0034$ (Figure 8), and the correlation between AUC and
270 FEP was $r = -0.593$ at $p = 0.055$. Because of the strong correlation, we refer exclusively to the
271 SMD results for the remainder of this work, focusing primarily on max force.

272 We found that relative to WT, one alanine mutation (Y211A) produced a very large and statis-
273 tically significant difference in the maximum applied force and AUC (Figure 6, Table 3), while the
274 other two did not (Table 3). When considering additional mutants (also discussed below), we found
275 that maximum applied force was generally sufficient to distinguish mutants (Tables 3 and 4), and
276 AUC was able to add a few more statistically significant differences (Table 5). In general, how-
277 ever, and consistent with the FEP results, maximum applied force seemed to be the more sensitive
278 statistic than AUC.

279 **3.3 Comparative analysis of the GP1/hTfR1 interface**

280 Considering the involvement of extended hydrogen-bonding networks in the GP1/hTfR1 interface,
281 it was not clear that individual alanine mutations, even those that should destroy such networks,
282 would significantly change the strength of interaction. One major advantage of first principles sim-
283 ulations is the ability to test mutations other than alanine without additional underlying assumptions
284 in the energy function. As shown in Table 1, we made additional mutations based on biochemical
285 intuition or available experimental data to chemically diverse amino acids including tryptophan,
286 lysine, aspartate, and threonine. Several mutations caused significant relative affinity changes. In
287 addition, to detect synergistic effects, we tested several double mutants where both mutations ap-

288 peared to cause similar changes in binding. Then, we compared the size of those differences to
289 single mutants (Figure 7 and 9).

290 Although Y211A appears to have a large impact on binding affinity, no single mutant can pro-
291 vide enough evidence to understand the biochemical difference in binding mechanism. Since ala-
292 nine is both smaller than tyrosine and also incapable of participating in hydrogen-bond interactions,
293 we tested further mutations to identify the critical biochemical difference responsible for change in
294 binding affinity. In particular, we substituted smaller side chains that, like tyrosine, were capable
295 of hydrogen bonding. We chose Y211D and Y211T, two mutations that have been discussed in the
296 context of selection pressure on hosts in rodent populations (Radoshitzky et al. 2008; Choe et al.
297 2011; Radoshitzky et al. 2011). Both mutations proved capable of causing a significant change
298 in binding affinity in our simulations, but the change appeared to be increased affinity (Figures 7
299 and 9, and Table 4).

300 We also simulated several point mutations at N348 in the hTfR1. As discussed above, the
301 alanine mutation at this site showed no significant difference in maximum applied force or AUC
302 from WT (Tables 4 and 5). In addition, neither the N348Lys nor the N348W mutation showed
303 a significant difference from WT. For both of these mutations, however, mean maximum applied
304 force and mean AUC was lower than for WT (See Table 2). On the other hand, there was a de-
305 tectable difference between N348A and N348Lys (Tables 4 and 5), with N348Lys being a weaker
306 binder. Moreover, N348W showed nearly identical results to N348Lys. The mutations to large
307 amino acids (N348W and N348Lys) produced nearly identical affinity changes, whereas the muta-
308 tions to amino acids not capable of hydrogen bonding (N348A and N348W) produced significantly
309 different affinity changes (Table 3). To check the consistency of our results, we hypothesized that
310 the combination of Y211A and N348W, being chemically disconnected in two different hydrogen-
311 bonding networks, would lead to a synergistic loss-of-binding. As expected, the double mutant
312 was the weakest binding mutant tested ($p < 10^{-6}$, Tables 4 and 5) in this study. Further, according
313 to maximum applied force (but not AUC), the combination of Y211A and N348W also showed
314 significantly weaker binding than Y211A by itself (Tables 4 and 5). We suspect that the effect
315 of N348W alone is near the limit of detection using our method. A larger number of replicates
316 would possibly have resolved affinity differences between N348W and WT or other mutants more
317 consistently.

318 Last, we further analyzed a single mutation in GP1, vR111A. As mentioned previously, in our
319 simulations this mutant showed no significant change in either maximum applied force or AUC
320 (Tables 4 and 5), even though both quantities were, on average, lower than in WT (Table 2). This
321 result was somewhat surprising, since Y211A, presumably disrupting the same hydrogen-bonding
322 network as vR111A, displayed a significant reduction in affinity. To probe the interaction between
323 position 111 in the GP1 and position 211 in the hTfR1 further, we also tested the double mutant
324 vR111A/Y211A. This double mutant showed affinity indistinguishable from WT and significantly
325 higher than Y211A alone (Table 3). This result shows that the two sites do indeed interact, and that
326 replacing the hydrogen-bonding network at these sites with a hydrophobic interaction could lead to
327 comparable binding affinity.

328 4 Discussion

329 We have applied a method utilizing steering forces in all-atom molecular dynamics simulations to
330 evaluate the effects of mutations at the GP1/hTfR1 interface. We modeled mutations at several sites
331 in the GP1/hTfR1 interface, and verified that our computational protocol was sensitive enough to
332 distinguish point mutants in hTfR1. Further, we identified two test statistics, maximum applied
333 force and AUC, that can be used as proxies for binding affinity. Both of these statistics correlate
334 well with FEP, but offer the simplicity of not requiring a large commitment to planning for the
335 theoretical issues inherent to free energy methods. We systematically tested several point mutations
336 to understand their contribution to the binding interaction. In the case of N348Lys, we have shown
337 that the static structure provides little insight into why this mutation causes loss-of-infectivity *in*
338 *vivo*. While N348 appears to be involved in a hydrogen-bonding network in the static structure,
339 change in binding at that site may actually be caused by size and charge restriction. We also found
340 that a negatively polar residue at site 211 in hTfR1 seem critical for a tight binding interaction.
341 Any non-polar mutation at Y211 in hTfR1 is likely to completely halt viral entry and dramatically
342 decrease the chances of MACV infection.

343 Traditionally SMD has been either applied to compute equilibrium free energies via a non-
344 equilibrium approximation (Park et al. 2003; Park and Schulten 2004; Giorgino and Fabritiis 2011),
345 used to estimate protein stability through unfolding (Lu and Schulten 1999), or used to calculate the

absolute free energy of small molecule ligand binding (Dixit and Chipot 2001). Likewise, others have used SMD to understand the process of binding and unbinding at a resolution unmatched by experiment (Cuendet and Zoete 2011; Giorgino and Fabritiis 2011). Here, we have shown that SMD can provide insight into the *relative* strength of protein–protein interactions. Via SMD, one can separate mutations whose likely effect is altered binding affinity with simple statistics like maximum force of separation. Thus, SMD may open avenues for subsequent experimental work in some situations where FEP may be prohibitively difficult.

Our findings rationalize several effects observed in both infectivity data and rodent populations (Radoshitzky et al. 2008; Choe et al. 2011). First, we found that some substitutions at positions 211 and 348 did affect the strength of receptor binding. However, the computational data suggest that the reason and nature of the effects at these two sites are very different. At position 211, mutations to non-polar residues cause a large change in binding. This is congruent with what is known from viral entry data (Radoshitzky et al. 2008; Choe et al. 2011). By contrast, mutations at position 348 need only be small to maintain WT binding. The ability to hydrogen bond appears to be insignificant. This can be inferred from the fact that Y211A paired with large (W) and positively charged (Lys) substitutions at position 348 results in a larger than expected synergistic difference. That is, the double mutant Y211A/N348W caused a much larger decrease in binding than we expected from either mutation individually. Third, the GP1 mutation vR111A causes a loss-of-infection during *in vitro* infectivity assays (Radoshitzky et al. 2011), yet it was indistinguishable from the WT complex in our simulations. Although Y211A was the most disruptive single mutant we tested, vR111A in the GP1 was able to restore mean maximum applied force to WT levels (Table 2), and to levels significantly higher than observed for Y211A alone.

We would like to emphasize here that we cannot expect perfect agreement between our simulations and the available experimental data, but the correspondence to a well established free energy method bolsters our conclusions. While we have shown that our method can distinguish individual point mutations, we do not know the limit of detection with our method. First, it is possible that some mutants display measurable phenotypic effects in experiments yet appear identical in simulation. More extensive sampling or refinement of the simulation protocol could help to differentiate such mutants (see also next paragraph). Second, the SMD method is fundamentally limited by the accuracy of our starting structure. Third, the available experimental data for the GP1/hTfR1 sys-

376 tem were generally obtained from entry assays or whole-cell binding assays rather than molecular
377 binding assays. A mutant may cause a phenotypic difference in infectivity without generating a
378 signal by our method. For example, entry could be lost in the experimental system because the
379 protein is grossly or partially misfolded. An additional analytical step with circular dichroism or an
380 analogous technique could clarify such large-scale folding differences. Further, since our simula-
381 tions start with a bound structure, any changes that may dramatically affect the rate of association
382 (different folds, trafficking issues, etc.) or relative orientation of the two proteins would be under-
383 estimated by our method.

384 There are a few additional challenges for investigating host-virus interactions via molecular
385 dynamics simulation. As with any atomistic simulation, there is going to be a fairly large noise-to-
386 signal ratio. To reduce noise, one could further customize each simulation, e.g. by determining the
387 optimal pulling speed. Furthermore, larger amounts of computational resources will have a direct
388 and powerful impact on the strength of any atomistic study (Jensen et al. 2012). Such resources
389 could come in the form of increased compute time, improved code, or customized hardware for
390 floating point operations (Shaw et al. 2011). With improved resources, we could investigate thou-
391 sands of individual permutations in the GP1/hTfR1 binding interface. In addition, with additional
392 compute time it would be possible to incorporate equilibrium sampling approaches (Buch et al.
393 2011) or use brute force equilibrium approaches (Giorgino et al. 2012) to improve resolution.

394 For future studies, although our approach offers the simplicity of not requiring prior knowledge
395 about a system of interest (other than a bound model), at this point SMD may not be the best approach
396 for many relative affinity calculations. To ensure one's results are independent of the dissociation
397 path one selects would require computing the work of separation for all likely paths. Such an
398 approach eventually requires using the Jarzynski inequality (Jarzynski 1997) to establish a lower
399 limit for binding energy and would quickly become computationally inefficient for evaluating a
400 large number of mutations in most systems. However, considering the strong correlation between
401 FEP and SMD in this system, it may not be important to ensure one's results are path independent
402 for relative affinity calculations, as long as the same path is used for all complexes.

403 More importantly, with no *a priori* knowledge of the appropriate number of equilibration sam-
404 ples, the best duration of equilibration, the appropriate number of pulling runs, or the best pulling
405 speed means the computational expense in our SMD protocol may not be commensurate with the

406 information provided. For example, another all atom approach that makes calculations via short
407 simulations of spatially restrained complexes has proven capable of generating relatively accurate
408 binding affinities with less compute time than is required from our steering strategy (Gumbart et al.
409 2013a,b). That being said, there is no reason to believe this SMD approach to mutagenic stud-
410 ies could not be optimized to reduce computational expense. Further analysis will be needed to
411 understand the lower limits of resources required for accurate predictions.

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418 References

- 419 **Abraham J, Corbett K, Farzan M, Choe H, Harrison S. 2010.** Structural basis for receptor
420 recognition by new world hemorrhagic fever arenaviruses. *Nat. Struct. Mol. Bio.* **17**:438–444.
- 421 **Bajaj C, Chowdhury R, Siddahanavalli V. 2011.** *F²Dock*: Fast fourier protein-protein docking.
422 *IEEE Transactions on Computational Biology and Bioinformatics* **8**:45–58.
- 423 **Bakan A, Meireles L, Bahar I. 2011.** ProDy: Protein dynamics inferred from theory and experi-
424 ments. *Bioinformatics* **27**:1575–1577.
- 425 **Benjamini Y, Hochberg Y. 1995.** Controlling the false discovery rate: a practical and powerful
426 approach to multiple testing. *J. Royal Stat. Soc., Series B* **57**:289–300.
- 427 **Brooks B, Bruccoleri R, Olafson B, States D, Swaminathan S, Karplus M. 1983.** CHARMM:
428 A program for macromolecular energy, minimization, and dynamics calculations. *J. Comput.*
429 *Chem.* **4**:187–217.

- 430 **Buch I, Sadiq S, Fabritiis GD.** 2011. Optimized potential of mean force calculations for standard
431 binding free energies. *J. Chem. Theory Comput.* **7**:1765–1772.
- 432 **Charrel RN, de Lamballerie X.** 2003. Arenaviruses other than Lassa virus. *Antiviral Res.* **57**:89–
433 100.
- 434 **Chodera J, Mobley D, Shirts M, Dixon R, Branson K, Pande V.** 2011. Alchemical free energy
435 methods for drug discovery: progress and challenges. *Current Opinion in Structural Biology*
436 **21**:150–160.
- 437 **Choe H, Jemielity S, Abraham J, Radoshitzky S, Farzan M.** 2011. Transferrin receptor 1 in the
438 zoonosis and pathogenesis of new world hemorrhagic fever arenaviruses. *Current Opinion in
439 Microbiology* **12**:467–482.
- 440 **Cuendet M, Michelin O.** 2008. Protein-protein interaction investigated by steered molecular
441 dynamics: The TCR-PMHC complex. *Biophysical J.* **95**:3575–3590.
- 442 **Cuendet M, Zoete V.** 2011. How T-cell receptors interact with peptide-MHCs: A multiple steered
443 molecular dynamics study. *Proteins* **79**:3007–3024.
- 444 **Dixit S, Chipot C.** 2001. Can absolute free energies of association be estimated from molecular
445 mechanical simulations? The biotin-streptavidin system revisited. *J. Phys. Chem. A* **105**:9795–
446 9799.
- 447 **Gao J, Kuczera K, Tidor B, Karplus M.** 1989. Hidden thermodynamics of mutant proteins: A
448 molecular dynamics analysis. *Science* **244**:1069–1072.
- 449 **Gilson MK, Given JA, Bush BL, McCammon JA.** 1997. The statistical-thermodynamic basis for
450 computation of binding affinities: A critical review. *Biophys. J* **72**:11047–1069.
- 451 **Giorgino T, Buch I, Fabritiis GD.** 2012. Visualizing the induced binding of SH2-phosphopeptide.
452 *J. Chem. Theory Comput.* **8**:1171–1175.
- 453 **Giorgino T, Fabritiis GD.** 2011. A high-throughput steered molecular dynamics study on the free
454 energy profile of ion permeation through Gramicidin A. *J. Chem. Theory Comput.* **7**:1943–1950.

- 455 **Gront D, Kulp DW, Vernon RM, Strauss CEM, Baker D.** 2011. Generalized fragment picking
456 in Rosetta: Design, protocols and applications. *PLoS ONE* **6**.
- 457 **Gumbart J, Roux B, Chipot C.** 2013a. Standard binding free energies from computer simulations:
458 What is the best strategy? *J. Chem. Theory Comput.* **9**:794–802.
- 459 **Gumbart J, Schreiner E, Wilson D, Beckmann R, Schulten K.** 2012. Mechanisms of SecM-
460 mediated stalling in the ribosome. *Biophys. J.* **203**:331–341.
- 461 **Gumbart JC, Roux B, Chipot C.** 2013b. Efficient determination of protein-protein standard
462 binding free energies from first principles. *J. Chem. Theory Comput.* **9**:3780–3798.
- 463 **Humphrey W, Dalke A, Schulten K.** 1996. VMD - Visual Molecular Dynamics. *J. Molec.*
464 *Graphics* **14**:33–38.
- 465 **Hwang H, Vreven T, Janin J, Weng Z.** 2010. Protein-protein docking benchmark version 4.0.
466 *Proteins* **78**:3111–3114.
- 467 **Isralewitz B, Baudry J, Gullingsruda J, Kosztinav D, Schulten K.** 2001a. Steered molecular
468 dynamics investigations of protein function. *J. Molec. Graphics* **19**:13–25.
- 469 **Isralewitz B, Gao M, Schulten K.** 2001b. Steered molecular dynamics and mechanical functions
470 of proteins. *Current Opinion in Structural Biology* **25**:225–230.
- 471 **Jarzynski C.** 1997. Equilibrium free-energy differences from nonequilibrium measurements: A
472 master-equation approach. *Physical Review E* **56**:5018–5035.
- 473 **Jensen M, Jogini V, Borhani D, Leffler A, Dror R, Shaw D.** 2012. Mechanism of voltage gating
474 in potassium channels. *Science* **336**:229–233.
- 475 **Kortemme T, Kim DE, Baker D.** 2004. Computational alanine scanning of protein-protein inter-
476 faces. *Sci. STKE* **2004**:12.
- 477 **Liu P, Dehez F, Cai W, Chipot C.** 2012. A toolkit for the analysis of free-energy perturbation
478 calculations. *J. Chem. Theor. Comput.* **8**:2606–2616.

- 479 **Lu H, Schulten K. 1999.** Steered molecular dynamics simulations of force-induced protein domain
480 unfolding. *Protein Struct. Funct. Genet.* **35**:453–463.
- 481 **Lu N, Kofke DA, Woolf TB. 2004.** Improving the efficiency and reliability of free energy pertur-
482 bation calculations using overlap sampling methods. *J. Comput. Chem.* **25**:28–39.
- 483 **Miño G, Baez M, Gutierrez G. 2013.** Effect of mutation at the interface of Trp-repressor dimeric
484 protein: a steered molecular dynamics simulation. *Eur. Biophys. J.* **42**:683–690.
- 485 **Michaud-Agrawal N, Denning E, Woolf T, Beckstein O. 2011.** MDAnalysis: A toolkit for the
486 analysis of molecular dynamics simulations. *J. Comput. Chem.* **32**:2319–2327.
- 487 **Park S, Khalili-Araghi F, Tajkhorshid E, Schulten K. 2003.** Free energy calculation from steered
488 molecular dynamics simulations using Jarzynski’s equality. *J. Chem. Phys.* **119**:3559–3567.
- 489 **Park S, Schulten K. 2004.** Calculating potentials of mean force from steered molecular dynamics
490 simulations. *J. Chem. Phys.* **120**:5946–5961.
- 491 **Pearlman DA. 1989.** A comparison of alternative approaches to free energy calculations. *J. Phys.*
492 *Chem.* **98**:1487–1493.
- 493 **Phillips J, Braun R, Wang W, Gumbart J, Tajkhorshid E, Villa E, Chipot C, Skeel R, Kale L,**
494 **Schulten K. 2005.** Scalable molecular dynamics with NAMD. *J. Comput. Chem.* **26**:1781–1802.
- 495 **Radoshitsky S, Kuhn J, Spiropoulou C, Albarino C, Nguyen D, Salazar-Bravo J, Dorfman
496 T, Lee A, Wang E, Ross S, Choe H, Farzan M. 2008.** Receptor determinants of zoonotic
497 transmission of new world hemorrhagic fever arenaviruses. *Proc. Natl. Acad. Sci.* **19**:2664–
498 2669.
- 499 **Radoshitsky S, Longobardi L, Kuhn J, Retterer C, Clester J, K Kota JC, Bavari S. 2011.**
500 Machupo virus glycoprotein determinants for human transferrin receptor 1 binding and cell entry.
501 *PLoS ONE* **6**.
- 502 **Schrödinger. 2010.** The PyMOL molecular graphics system, version 1.3r1. Schrödinger, LLC.

- 503 Shaw D, Dror R, Salmon J, Grossman J, Mackenzie K, Bank J, Young C, Deneroff M, Batson
504 B, Bowers K, Chow E, Eastwood M, Ierardi D, Klepeis J, Kuskin J, Larson R, Lindorff-
505 Larsen K, Maragakis P, Moraes M, Piana S, Shan Y, Towles B. 2011. Millisecond-scale
506 molecular dynamics simulations on anton. *Proceedings of the Conference on High Performance*
507 *Computing, Networking, Storage and Analysis* SC09:39.
- 508 Vreven T, Hwang H, Pierce B, Weng Z. 2012. Prediction of protein-protein binding free energies.
509 *Protein Science* 21:396–404.
- 510 Vreven T, Hwang H, Weng Z. 2011. Integrating atom-based and residue-based scoring functions
511 for protein-protein docking. *Protein Science* 20:1576–1586.
- 512 Wang J, Deng Y, Roux B. 2006. Absolute binding free energy calculations using molecular dy-
513 namics simulations with restraining potentials. *Biophys. J.* 91:2798–2814.
- 514 Wickham H. 2009. *ggplot2: Elegant graphics for data analysis.* Springer New York. URL
515 <http://had.co.nz/ggplot2/book>.

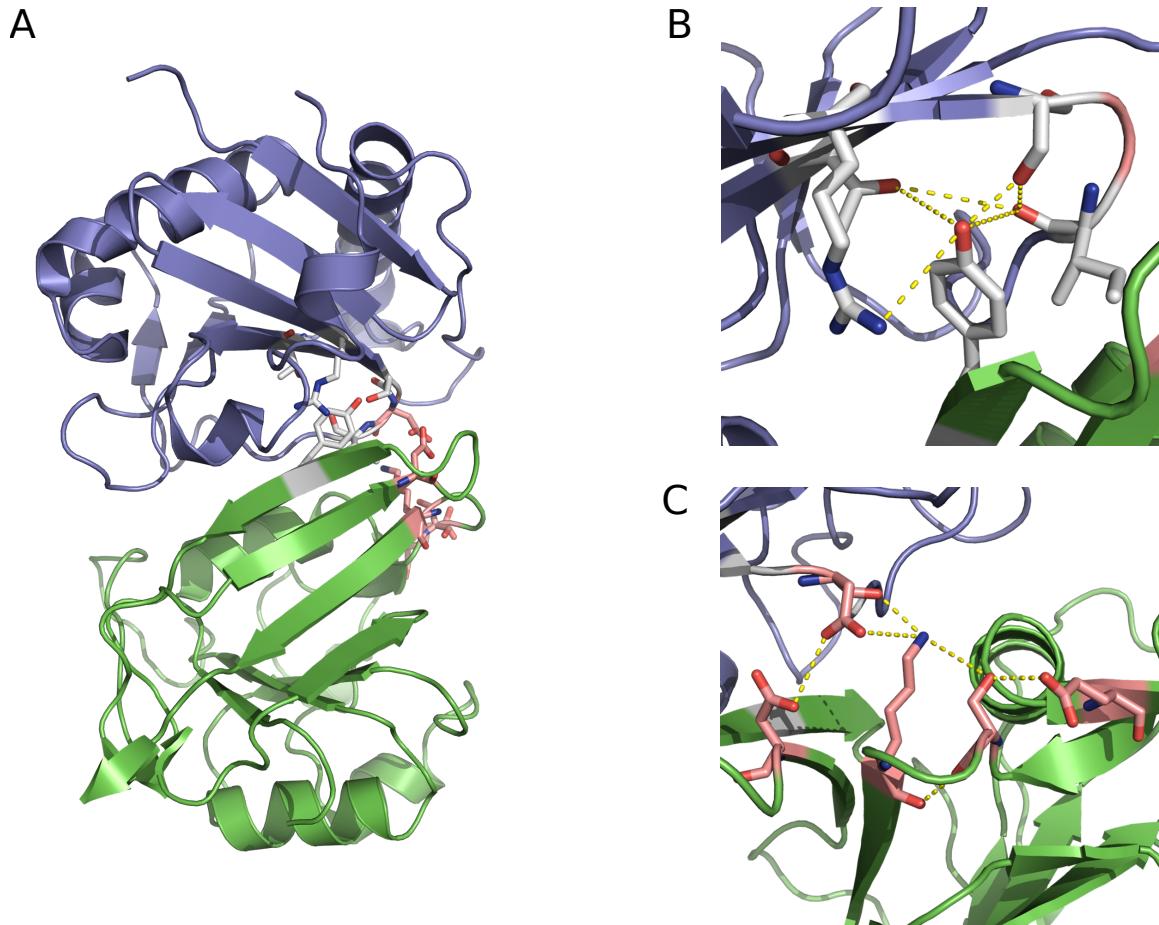


Figure 1: The two hydrogen bonding networks. GP1 is shown in blue and hTfR1 is shown in green. (A) The first network including Y211 and R111 is shown in white, and the second network containing N348 is shown in pink. (B) Near view of the first network with contacts in yellow. (C) Near view of the second network with contacts in yellow.

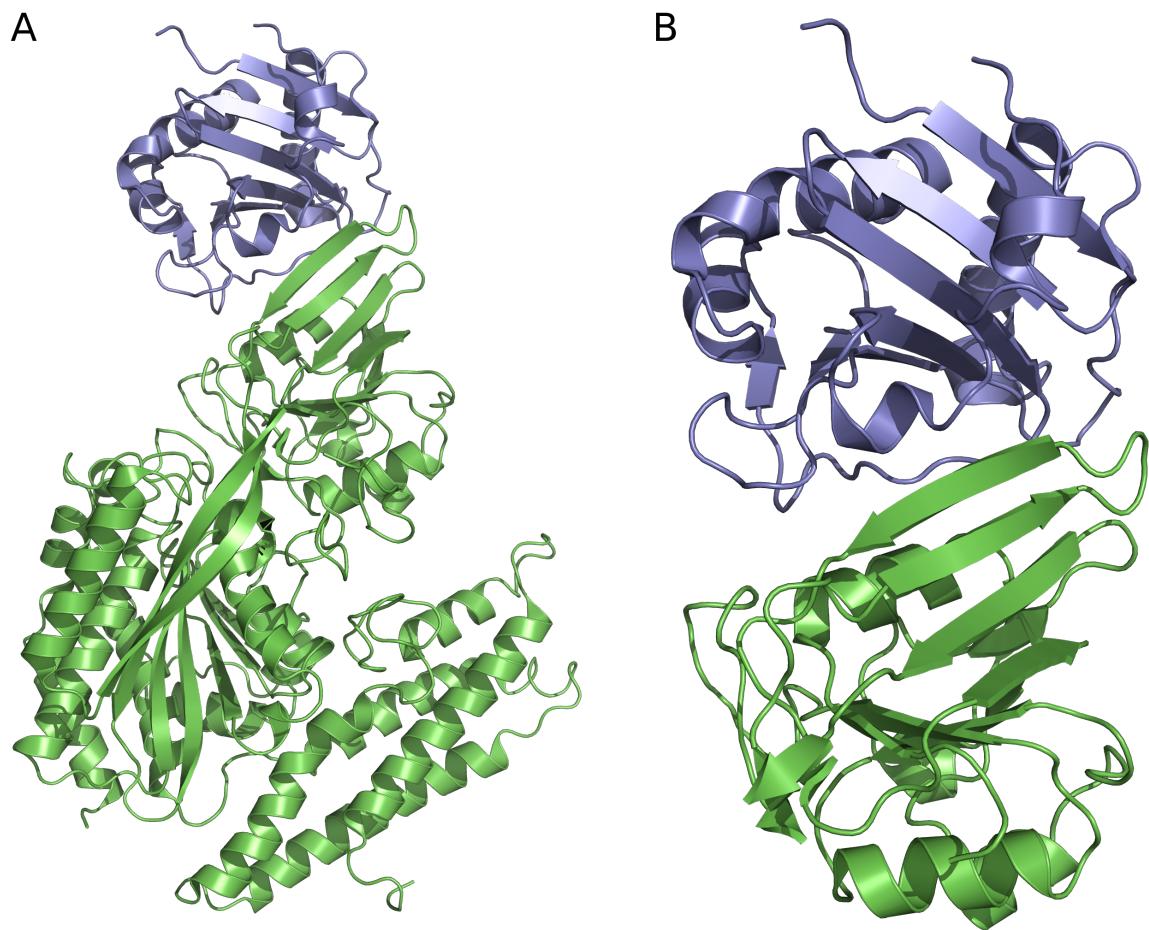


Figure 2: The GP1/hTfR1 complex. GP1 is shown in blue and hTfR1 is shown in green. (A) The full, de-glycosylated GP1/hTfR1 co-crystal structure. (B) The reduced structure used in SMD simulations.

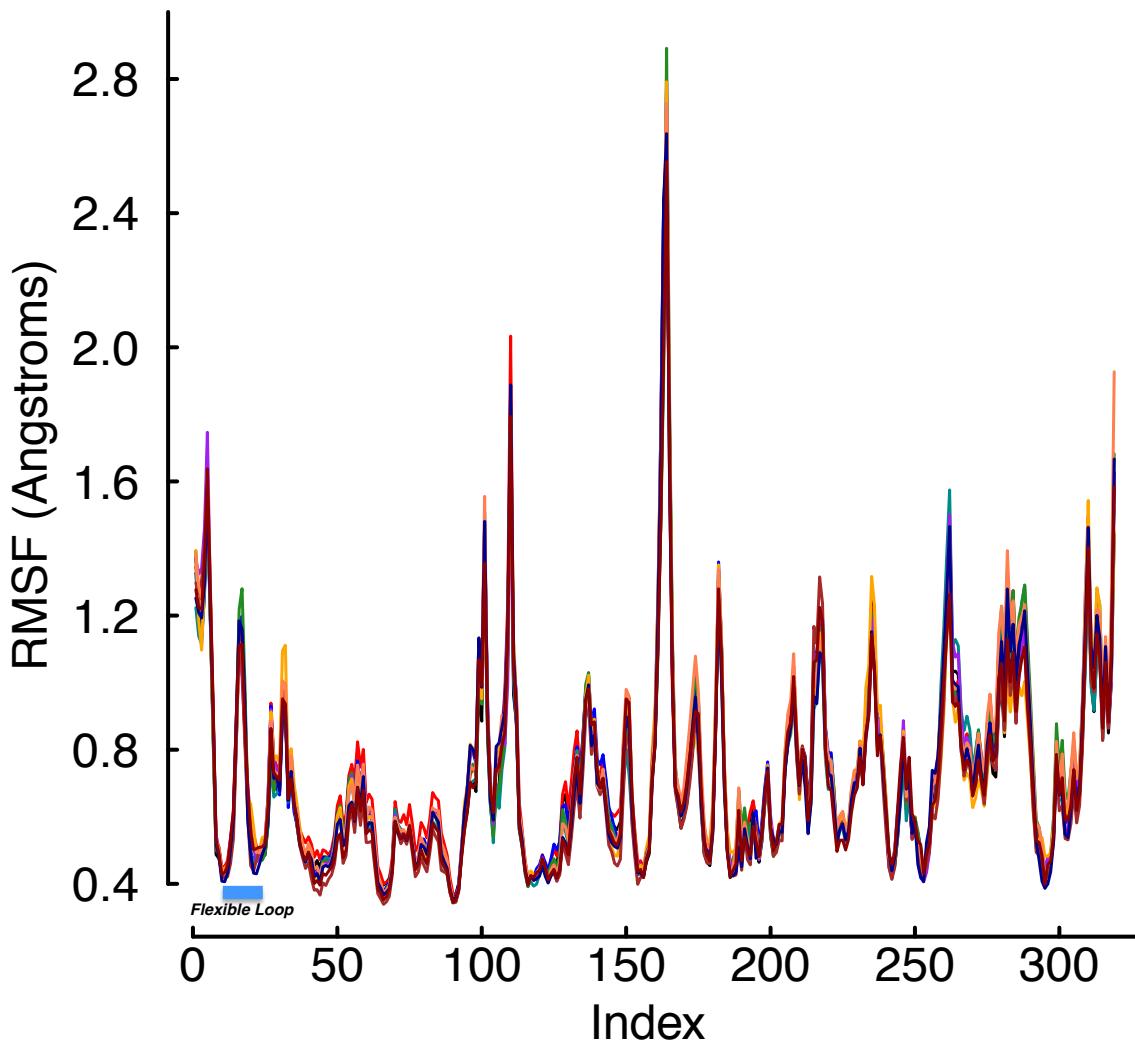


Figure 3: RMSF values during equilibration. The RMSF values for every site in the bound complex computed during the equilibration phase of the protocol. Each color represents the average over 20 trajectories of a single mutant. Indices 17–25 are the hTfR flexible loop. The plot shows the flexibility of each site is essentially independent of mutation, and two sites (indices 17 and 18) above 0.72 Å are a part of the flexible loop in the free receptor. However, these two residues are not actually found in the protein–protein interface, but rather are almost completely solvent exposed with the virus bound.

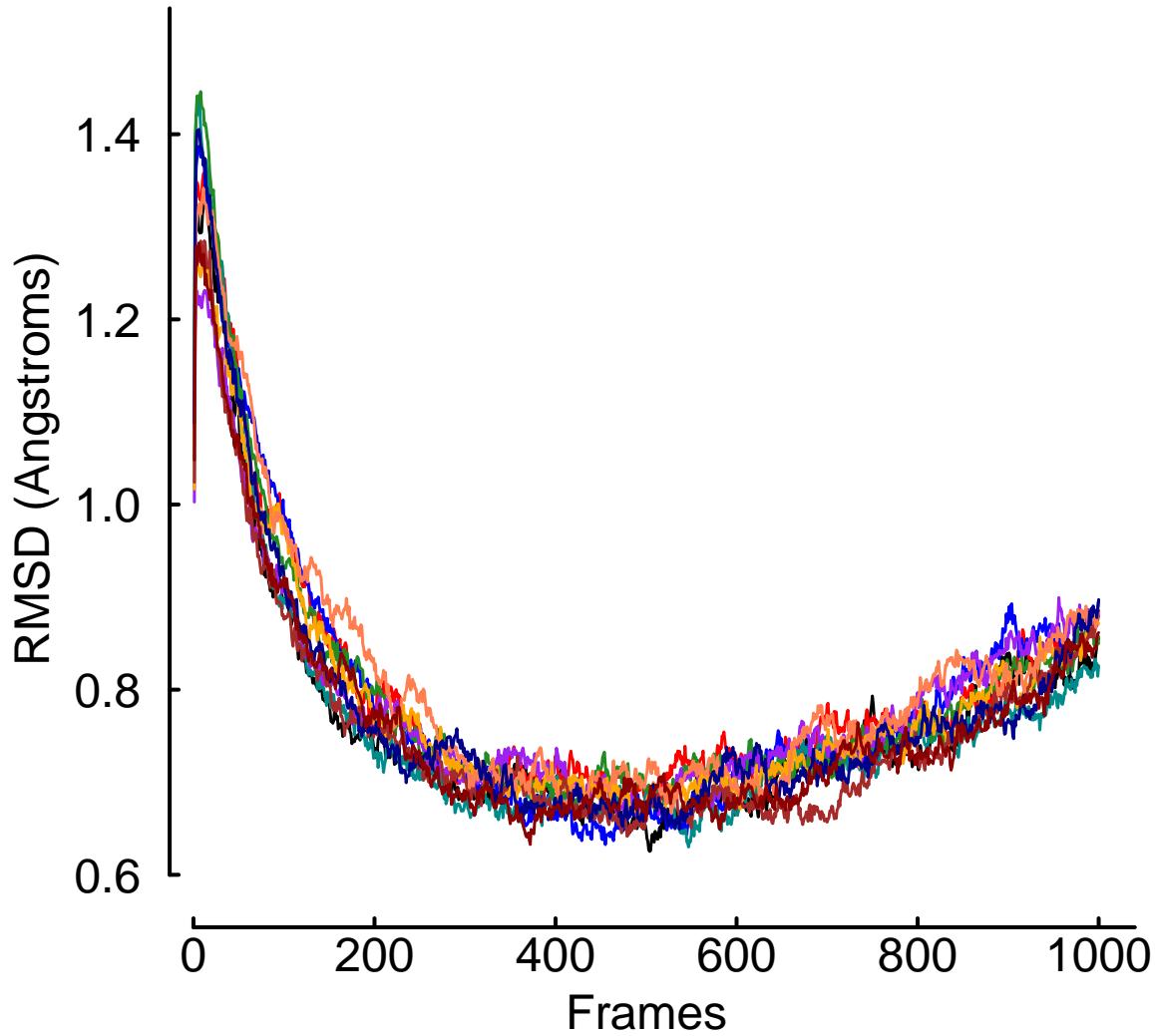


Figure 4: RMSD values during equilibration. The RMSD values over the time of the trajectory computed during the equilibration phase of the protocol. Each color represents the average over 20 trajectories of a single mutant. The plot shows none of the mutants causes immediate unbinding of the protein–protein complex. In addition, the universal upward trend near the end of the equilibration trajectories may indicate the crystal is more tightly packed than would normally occur in solution.

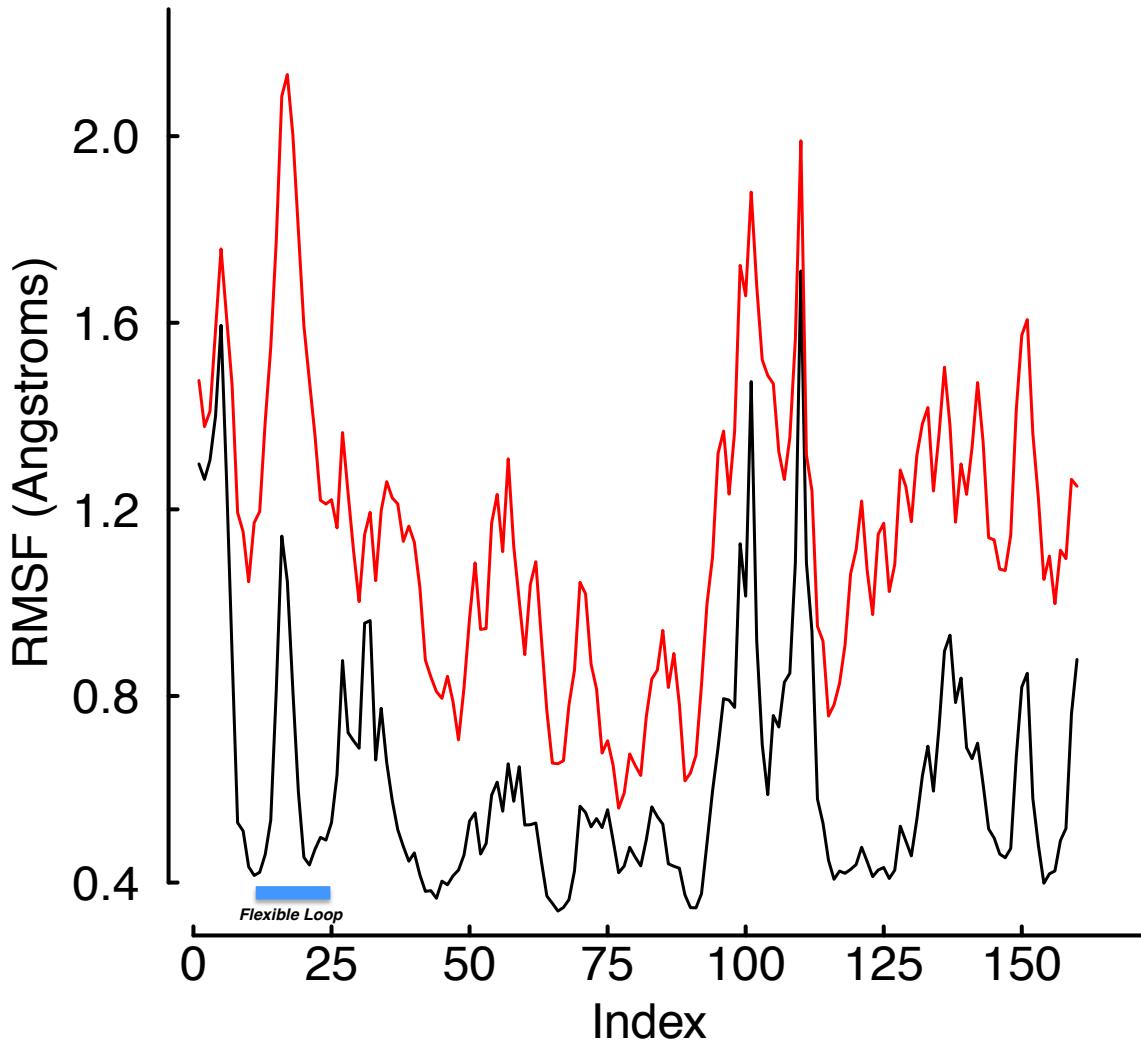


Figure 5: RMSF values of WT hTfR in equilibration and SMD. The RMSF values for every site in the WT receptor were computed during the equilibration phase and during final 50 frames of the SMD trajectories. The black line was computed over equilibration and the red line during SMD. The plot shows the solution mobility of the hTfR flexible loop increases more than the average during the unbinding process.

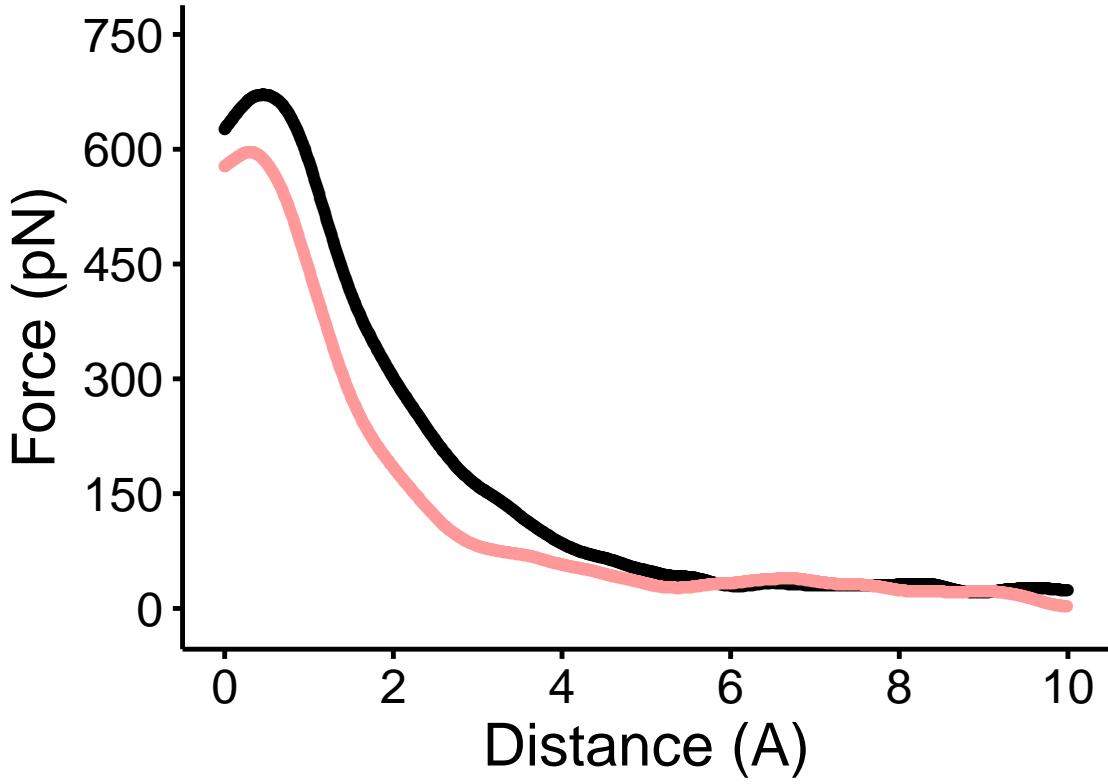


Figure 6: Force versus distance curve of WT and the Y211A mutant. The average force curve for 50 replicates of the WT complex is shown in black, and the average of 50 replicates of the Y211A mutant is shown in red. There is a large difference in both maximum applied force and AUC between the two complexes.

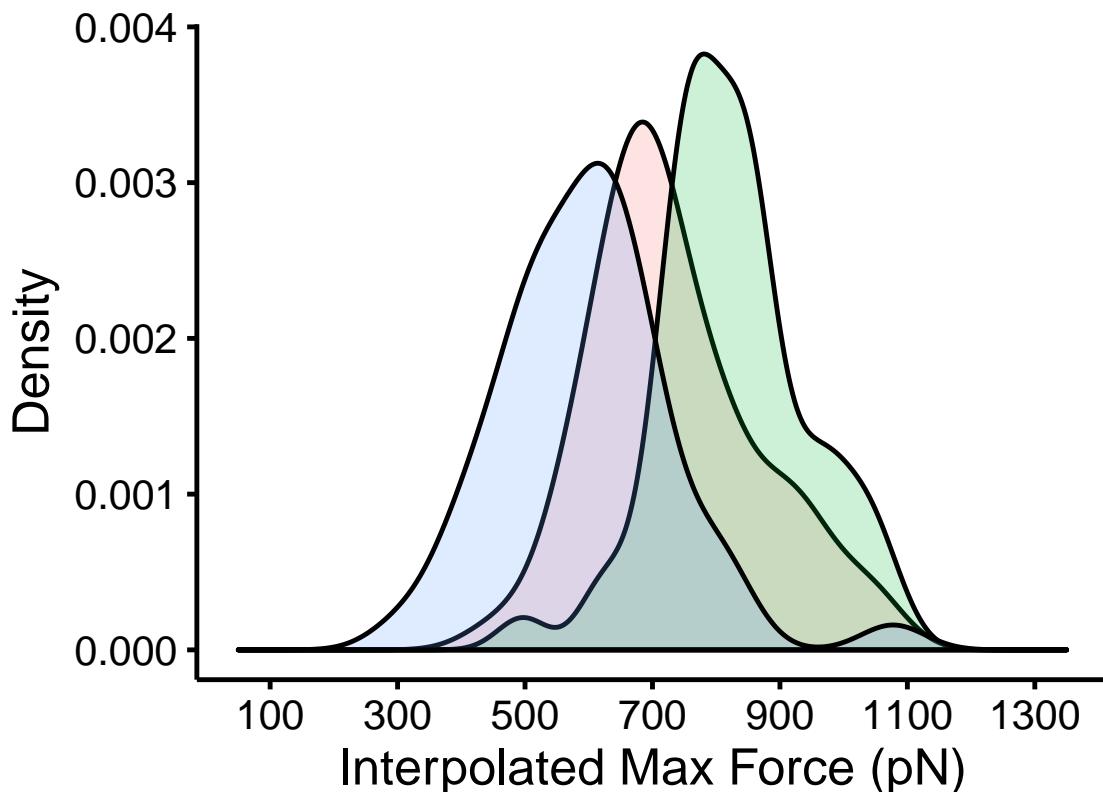


Figure 7: Distribution of interpolated maximum force for three different GP1/hTfR1 complexes. The WT GP1-hTfR1 complex in the middle is flanked by the tighter binding mutant Y211D on the right and the weaker binding double mutant N348W/Y211A on the left. The large non-overlapping areas indicate a large and statistically significant difference in these three complexes.

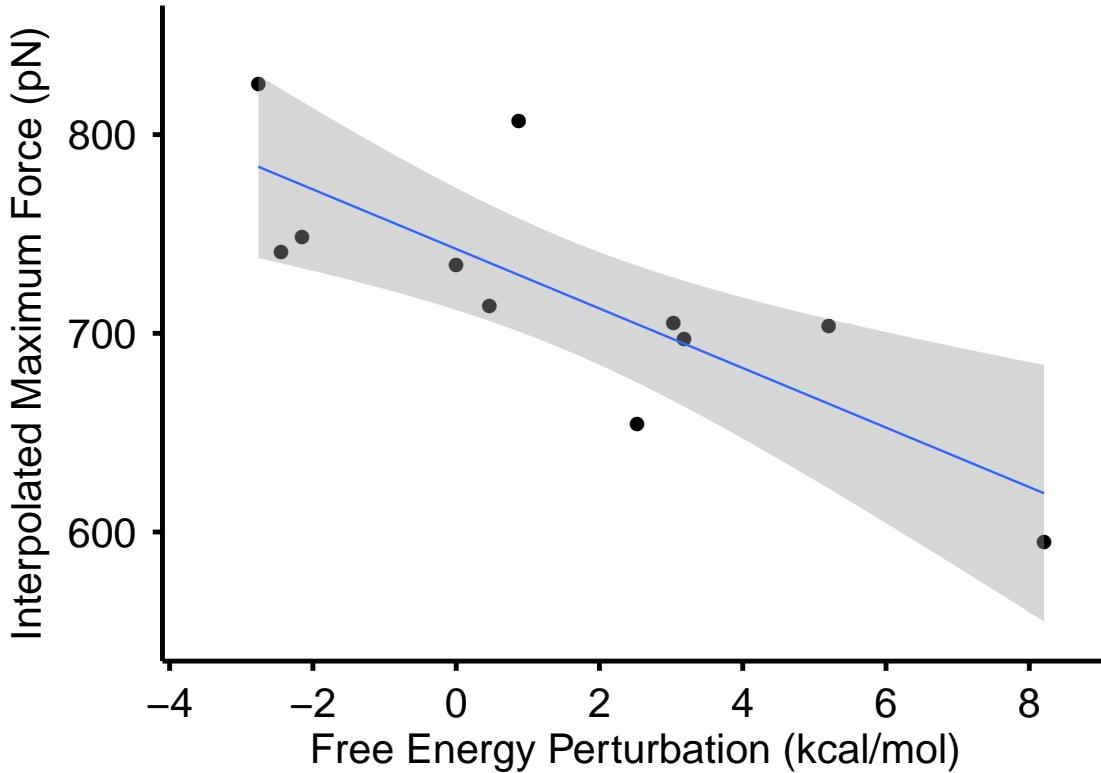


Figure 8: Max force versus free energy perturbation. Scatter plot of maximum force in SMD versus the relative free energy difference calculated by FEP for all 10 mutants tested plus the WT complex. The WT complex for FEP was simply set to 0.0. The correlation between the two is $r = -0.795$ with $p = 0.0034$.

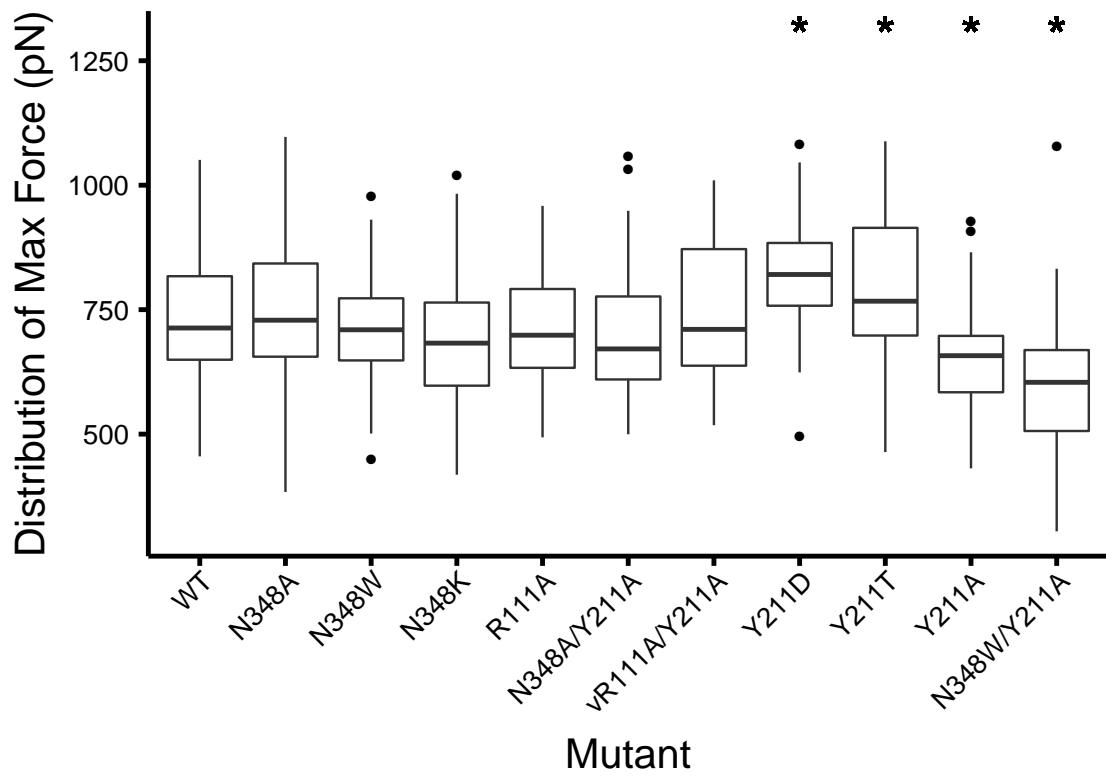


Figure 9: Distribution of interpolated maximum force for all bound complexes tested. Stars above the boxplots indicate a statistically significant difference in mean maximum force relative to the WT complex.

Table 1: Summary of prior information available for each mutation tested. Observed *in vivo* refers to mutations that have been observed in rodent populations. Phenotype *in vitro* refers to the observed phenotype in *in vitro* viral entry assays.

Mutation	Observed <i>in vivo</i>	Phenotype <i>in vitro</i>
WT	Yes	Normal Entry
N348A	No	-
N348K	Yes	Diminished Entry
N348W	No	-
vR111A	No	Diminished Entry
N348A/Y211A	No	-
vR111A/Y211A	No	-
Y211D	Yes	No Expression
Y211T	No	Diminished Entry
Y211A	No	No Expression
N348W/Y211A	No	-

Table 2: Summary statistics for each mutation tested. μ_{MAF} is the mean in piconewtons and σ_{MAF} is the standard deviation of maximum applied force over all simulations. μ_{AUC} is the mean and σ_{AUC} is the standard deviation of AUC over all simulations. ΔG is the free energy difference in kcal/mol calculated via FEP by the dual topology paradigm.

Mutation	μ_{MAF} (pN)	σ_{MAF}	μ_{AUC}	σ_{AUC}	ΔG (kcal/mol)
WT	734.4856	131.6513	145460.4	60232.26	0.000
N348A	748.5217	137.4864	133913.9	51078.64	-2.149
N348K	705.0707	108.5079	141084.4	54450.28	+3.184
N348W	697.3642	132.6436	136886.0	53796.44	+3.033
vR111A	713.8081	106.7374	136103.2	52070.85	+0.466
N348A/Y211A	703.7027	128.5866	113464.2	57451.62	+5.203
vR111A/Y211A	741.0642	131.6287	130070.6	47665.56	-2.440
Y211D	825.2586	115.4343	158878.7	63039.08	+2.760
Y211T	806.8593	136.5648	167110.7	78849.29	+0.875
Y211A	654.1138	108.5343	108090.0	43661.09	+2.526
N348W/Y211A	594.9044	134.8233	108984.2	45451.00	+8.206

Table 3: Pairwise differences (row variable minus column variable) in mean maximum applied force. Bolded values are statistically significant at $p < 0.05$.

	WT	N348A	N348W	N348K	vR111A	N348A/Y211A	vR111A/Y211A	Y211D	Y211T	Y211A
N348A	+14.036									
N348W	-29.414	-43.451								
N348K	-37.121	-51.157	-7.7060							
vR111A	-20.677	-34.713	+8.7370	+16.443						
N348A/Y211A	-30.782	-44.819	-1.3670	+6.3380	-10.105					
vR111A/Y211A	+6.5790	-7.4570	+35.993	+43.700	+27.256	+37.361				
Y211D	+90.772	+76.736	+120.19	+127.89	+111.45	+121.56	+84.194			
Y211T	+72.373	+58.337	+101.79	+109.50	+93.051	+103.16	+65.795	-18.399		
Y211A	-80.371	-94.407	-50.956	-43.250	-59.694	-49.588	-86.950	-171.14	-152.75	
N348W/Y211A	-139.58	-153.62	-110.17	+102.46	-118.903	-108.80	+146.16	+230.35	-211.95	-59.209

Table 4: Pairwise difference p -values for maximum applied force. Bolded values are statistically significant at $p < 0.05$.

	WT	N348A	N348W	N348K	vR111A	N348A/Y211A	vR111A/Y211A	Y211D	Y211T	Y211A
N348A	0.60									
N348W	0.31	0.077								
N348K	0.20	0.038	0.81							
vR111A	0.51	0.16	0.79	0.60						
N348A/Y211A	0.29	0.07	0.95	0.81	0.77					
vR111A/Y211A	0.82	0.79	0.21	0.13	0.35	0.20				
Y211D	0.00093	0.0012	1.4x10⁻⁵	5.0x10⁻⁶	5.6x10⁻⁵	1.2x10⁻⁵	0.0022			
Y211T	0.01	0.018	0.00022	8.7x10⁻⁵	0.0008	0.0002	0.021	0.56		
Y211A	0.0034	7.2x10⁻⁵	0.074	0.13	0.035	0.079	0.0016	4.2x10⁻¹⁰	4.2x10⁻⁸	
N348W/Y211A	3.9x10⁻⁷	1.1x10⁻¹⁰	6.5x10⁻⁵	0.00021	1.6x10⁻⁵	7.2x10⁻⁵	1.3x10⁻⁷	1.2x10⁻¹⁶	2.0x10⁻¹⁴	0.036

Table 5: Pairwise difference p -values for interpolated AUC. Bolded values are statistically significant at $p < 0.05$.

	WT	N348A	N348W	N348K	vR111A	N348A/Y211A	vR111A/Y211A	Y211D	Y211T	Y211A
N348A	0.33									
N348W	0.76	0.59								
N348K	0.59	0.80	0.76							
vR111A	0.55	0.85	0.76	0.94						
N348A/Y211A	0.017	0.07	0.031	0.076	0.08					
vR111A/Y211A	0.26	0.76	0.46	0.68	0.72	0.22				
Y211D	0.33	0.029	0.18	0.09	0.08	0.00046	0.029			
Y211T	0.09	0.0056	0.046	0.027	0.023	4.1x10⁻⁵	0.006	0.59		
Y211A	0.0056	0.027	0.016	0.029	0.031	0.75	0.09	8.2x10⁻⁵	8.5x10⁻⁶	
N348W/Y211A	0.006	0.029	0.017	0.032	0.034	0.76	0.1	9.4x10⁻⁵	8.5x10⁻⁶	0.94