

A Nowcasting Model for Time Series with Ragged-Edge Data

Model Run Date: March 14, 2021

charles@cmefi.com

CONTENTS 1

Contents

1	Mot	tivation	3
2	Met	thodology Overview	5
3	Esti	imation Process	7
	3.1	Data	7
	3.2	Time Periods	9
	3.3	Principal Components Analysis	9
	3.4	Factor VAR	12
	3.5	Dynamic Factor Models	14
	3.6	State-Space Setup	16
	3.7	Kalman Filtration	17
	3.8	Nowcast Step	19
4	Res	ults	22
$\mathbf{A}_{]}$	ppen	dices	25
\mathbf{A}	\mathbf{DF}	M Fitted Plots	25

LIST OF FIGURES 2

List of Tables

1	Correlation Between Major Leading Predictors
2	Imported Monthly Data - Leading Economic Variables
3	Imported Quarterly Data
4	Other Imported Monthly Data
5	Time Periods
6	Factor Selection Process
7	Factor VAR Coefficients
8	DFM Goodness of Fit
9	Estimated DFM Coefficients
10	DFM Goodness of Fit
11	Quarterly Data Covariates
12	DFM-AR(1) Forecasted GDP Subcomponents
13	Summable Quarterly Data Covariates
14	Nowcasts for GDP and Subcomponents (Annualized Percent Change)
15	Nowcasts for Other Quarterly Variables
16	Nowcasts for All Monthly Variables
List o	of Figures
1	Example of ragged-edge data
2	Overview of methodology (more detail in later sections)
3	Factor Selection
4	Factor VAR Residuals

1 MOTIVATION 3

1 Motivation

Nowcasting is the prediction of the present, the near future, and the near past. Nowcasting is important in economics because many important macroeconomic statistics are released with a lengthy delay. For example, the Bureau of Economic Analysis releases quarterly GDP data typically two months after the quarter has already ended - a significant delay for any companies or individuals who need the data for planning and forecast models.

This delay is particularly salient during times of high volatility. During the first few months of the COVID-19 pandemic in the United States, many companies attempted to use high-frequency indicators to attempt nowcasts of the state of the macroeconomy. For example, a major investment bank forecasted Q2 GDP growth of -3% on March 3rd; the estimate was revised down to -14% by March 21st, -25% by March 25th, and -40% by April 10th. Yet many such models were ad-hoc and only able to use a small number of predictive indicators, such as jobless claims or traffic data.

Nowcasting is about deciphering key information about the state of the economy before official data is released. Because of the fundamentally urgent nature of nowcasting, it is important that nowcast models exploit any latest, high-frequency data available. Nowcasts should be able to generate constantly rolling forecasts, updating these numbers in response to any new data releases.

For example, suppose the date is early March, and the variable we want to predict is Q1 GDP. The simplest way to predict Q1 GDP would be to use historical quarterly data from various economic variables. But this data would only go up to Q4 of last year, and would fail to capture the critically important predictive power that could be provided by monthly and daily data released throughout January and February. This lag in publication dates of different data series is known as the **ragged-edge** problem.

Suppose instead, we used monthly data as our predictors of Q1 GDP. Again, we will soon run in to a problem. As an example, imagine that we had imported 20 monthly data series. Suppose 5 of these series ended in December, 10 ended in January, and 5 ended in March.



Traditional modeling methods would require us to either throw out variables or throw out months - for example, we could truncate all our data series at January and lose out the information provided by the 5 February data points. Alternatively, we could completely remove the 15 variables with data releasing before March. Both methods result in a serious loss of useful data and are unappealing.

1 MOTIVATION 4

In this paper, we will develop and utilize a methodology that will allow us to use the information from all variables at any dates. This model will give an updated forecast in response to any new data releases. Additionally, the model can be generalized to nowcast any time series variable, not just GDP. The methodology for the model will be described in the next section.

2 Methodology Overview

Our goal will be to take monthly-frequency leading economic predictor variables — industrial production, consumer sentiment, vehicle sales, and so on — and use these to predict our quarterly variables. However, we will need a way to adjust for the ragged edges of the data.



Figure 2: Overview of methodology (more detail in later sections)

To do this, we will use a methodology that relies heavily on principal components. It is well known that most economic variables are highly correlated with one another (see, for example, Bernanke et al 2005).

term	VehicleSales	ConsumerSentiment	AdvSales	IndustrialProd	VIX	SP500
VehicleSales						
ConsumerSentiment	0.83					
AdvSales	0.24	0.11				
IndustrialProd	0.29	0.18	0.76			
VIX	-0.56	-0.48	-0.35	-0.41		
SP500	0.11	0.15	0.53	0.42	-0.64	
CFNAI	0.48	0.37	0.72	0.88	-0.64	0.54

Table 1: Correlation Between Major Leading Predictors

As a result, we can take a very high-dimensional dataset of indicator variables and extract a few time series, factors or principal components, using principal components analysis. These factors will be able to contain the majority of information within our larger, high-dimensional dataset.

Then we will use a time series model of the factor behavior — a vector autoregression, or VAR — to forecast the factors forward in time.

Finally, we will deal with the ragged edges of the data by casting our model dynamics in state-space form and using a Kalman filtration and smoothing process. This will, in essence, adjust our factor forecasts by whether or not the indicator variables used in the construction of the factors have been released. This procedure is a modified version of the two-step dynamic factor model utilized in Giannone et al (2008) and Doz et al (2011).

Finally, we will aggregate the smoothed and forecasted time series of factors up to a quarterly level. These now-quarterly forecasts of the factors can be used as covariates in an ARIMA model of the quarterly economic variables. The usage of factors as regressors of these economic variables is known as a *dynamic factor model* (DFM).

The next section will go over the data and estimation procedure in detail. While this model can be generalized to nowcasts of other economic variables, we will use the example of nowcasting GDP and components of GDP.

3 Estimation Process

The model is run every weekday; this documentation will use actual data and estimates from the most recent model run (2021-03-14) to illustrate the procedure. The final nowcasted output is located in the results section.

3.1 Data

We begin by importing monthly data of various leading indicators from the St. Louis Federal Reserve Database (FRED). We choose data of at least monthly frequency and with historical data available as of at least 2010. Data are transformed for stationarity as listed below; *dlog* refers to the natural log of the first difference, whereas *base* means that no transformation was necessary for the variable to be stationary.

Variable PCE Disposable Personal Income Case-Shiller Housing Price Index Housing Starts Houses Sold Houses Sold New Private Housing Permits Manufacturers New Orders: Durable Goods Capacity Utilization: Total Index dlog Total Construction Spending Effective Federal Funds Rate Treasury Yield 10Y base Treasury Yield 11Y base Unemployment Rate Unemployment Rate Hires: Total Nonfarm Hires: Total Nonfarm Weekly Economic Index S&P 500 VIX Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales KC Fed Labor Market Index Consumer Confidence (OECD) Industrial Production index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Dase Dase Chicago Fed Nativity Lydex Dase Chicago	77 • 11	Ct. t: D
Disposable Personal Income Case-Shiller Housing Price Index Housing Starts dlog Houses Sold New Private Housing Permits dlog Manufacturers New Orders: Durable Goods Capacity Utilization: Total Index dlog Effective Federal Funds Rate base Treasury Yield 10Y base Treasury Yield 10Y base Unemployment Rate dlog All Employees (Nonfarm) dlog Job Openings: Total Nonfarm base Weekly Economic Index base Weekly Economic Index base Weekly Economic Index base Outstanding Real Estate Loans dlog Outstanding Real Estate Loans dlog Outstanding Credit Card Balances dlog St. Louis Fed Financial Stress Index base U.S. Dollar Index base Average Weeks Unemployed base Retail & Food Sales KC Fed Labor Market Index base Consumer Confidence (OECD) Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey base Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey		
Case-Shiller Housing Price Index Housing Starts Houses Sold Houses Sold New Private Housing Permits Manufacturers New Orders: Durable Goods Capacity Utilization: Total Index dlog Total Construction Spending Effective Federal Funds Rate Treasury Yield 10Y base Treasury Yield 11Y base Unemployment Rate All Employees (Nonfarm) Job Openings: Total Nonfarm Hires: Total Nonfarm base Weekly Economic Index S&P 500 VIX Outstanding Real Estate Loans Outstanding Credit Card Balances U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Retail & Food Sales Industrial Production index Consumer Confidence (OECD) Indust Fed: Business Conditions Manufacturing Survey Dase Dallas Fed: Current General Business Activity Dase Philadelphia Fed: Future Capital Expenditures Survey Dase	-	
Housing Starts dlog Houses Sold New Private Housing Permits Manufacturers New Orders: Durable Goods Capacity Utilization: Total Index dlog Capacity Utilization: Total Index dlog Effective Federal Funds Rate Treasury Yield 10Y base Treasury Yield 11Y base Vehicle Sales Unemployment Rate All Employees (Nonfarm) dlog Hires: Total Nonfarm base Weekly Economic Index S&P 500 VIX Outstanding Real Estate Loans Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index Dase Dallas Fed: Current General Business Activity Dase Philadelphia Fed: Future Capital Expenditures Survey Dase Philadelphia Fed: Future Capital Expenditures Survey Dase	1	9
Houses Sold New Private Housing Permits Manufacturers New Orders: Durable Goods Capacity Utilization: Total Index dlog Total Construction Spending Effective Federal Funds Rate Treasury Yield 10Y base Treasury Yield 11Y base Unemployment Rate Unemployment Rate Unemployment Rate Unemployment Rate Unemployment Rate Unemployees (Nonfarm) Job Openings: Total Nonfarm dlog Hires: Total Nonfarm base Weekly Economic Index S&P 500 VIX Dutstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Retail & Food Sales Industrial Production index Dase Dallas Fed: Current General Business Activity base Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	- Control of the cont	U
New Private Housing Permits Manufacturers New Orders: Durable Goods Capacity Utilization: Total Index Idlog Capacity Utilization: Total Index Glog Capacity Utilization: Total Index Glog Total Construction Spending Effective Federal Funds Rate Treasury Yield 10Y Treasury Yield 11Y base Vehicle Sales Unemployment Rate All Employees (Nonfarm) Job Openings: Total Nonfarm dlog Hires: Total Nonfarm base Weekly Economic Index S&P 500 VIX Dutstanding Real Estate Loans Outstanding Credit Card Balances U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index New York Fed: Business Conditions Manufacturing Survey base Philadelphia Fed: Future Capital Expenditures Survey base	9	O
Manufacturers New Orders: Durable Goods Capacity Utilization: Total Index dlog Total Construction Spending Effective Federal Funds Rate Treasury Yield 10Y base Treasury Yield 11Y base Vehicle Sales Unemployment Rate dlog All Employees (Nonfarm) Job Openings: Total Nonfarm dlog Hires: Total Nonfarm base Weekly Economic Index S&P 500 VIX base Outstanding Real Estate Loans Outstanding Credit Card Balances U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity base Dallas Fed: Current General Business Activity base Dallas Fed: Current General Business Activity base Dallas Fed: Current General Business Survey base Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base		9
Capacity Utilization: Total Index Total Construction Spending Effective Federal Funds Rate Dase Treasury Yield 10Y Dase Treasury Yield 1Y Dase Vehicle Sales Unemployment Rate All Employees (Nonfarm) Job Openings: Total Nonfarm Hires: Total Nonfarm Base Weekly Economic Index S&P 500 VIX Dutstanding Real Estate Loans Outstanding Credit Card Balances U.S. Dollar Index Dase Verage Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index Dase Dallas Fed: Current General Business Activity Dase Philadelphia Fed: Future Capital Expenditures Survey Dase Dase Freasury Yield 10Y Dase Treasury Yield 10Y Dase Total Rate Dase Dase Treasury Yield 10Y Dase Treasury Yeld 10Y Dase Treasury Treasury Dase Treasury		9
Total Construction Spending Effective Federal Funds Rate Treasury Yield 10Y base Treasury Yield 1Y base Vehicle Sales Unemployment Rate All Employees (Nonfarm) Job Openings: Total Nonfarm dlog Hires: Total Nonfarm base Weekly Economic Index S&P 500 VIX Outstanding Real Estate Loans Outstanding Credit Card Balances Gust U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base Dase Treasury Yield 10Y base Dase Dase Treasury Yield 10Y base Dase Dase Dase Dallas Fed: Current General Business Activity base Dase Das		dlog
Effective Federal Funds Rate Treasury Yield 10Y base Treasury Yield 1Y base Vehicle Sales Unemployment Rate All Employees (Nonfarm) Job Openings: Total Nonfarm dlog Hires: Total Nonfarm base Weekly Economic Index S&P 500 VIX base Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	Capacity Utilization: Total Index	dlog
Treasury Yield 10Y Treasury Yield 1Y base Vehicle Sales Unemployment Rate Unemployment Rate All Employees (Nonfarm) Job Openings: Total Nonfarm dlog Hires: Total Nonfarm base Weekly Economic Index S&P 500 VIX base Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	Total Construction Spending	dlog
Treasury Yield 1Y Vehicle Sales Unemployment Rate Unemployment Rate All Employees (Nonfarm) Job Openings: Total Nonfarm Hires: Total Nonfarm Base Weekly Economic Index S&P 500 VIX Base Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Dase Philadelphia Fed: Future Capital Expenditures Survey Dalse	Effective Federal Funds Rate	base
Vehicle Sales Unemployment Rate All Employees (Nonfarm) Job Openings: Total Nonfarm Hires: Total Nonfarm Base Weekly Economic Index S&P 500 VIX Base Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Base Philadelphia Fed: Future Capital Expenditures Survey base Philadelphia Fed: Future Capital Expenditures Survey base	Treasury Yield 10Y	base
Unemployment Rate All Employees (Nonfarm) Job Openings: Total Nonfarm Hires: Total Nonfarm Base Weekly Economic Index S&P 500 VIX Base Outstanding Real Estate Loans Outstanding Credit Card Balances Gt. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index Red Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Base Philadelphia Fed: Future Capital Expenditures Survey Base Dalse Base Dallas Fed: Future Capital Expenditures Survey Base Dalse Base Dallas Fed: Future Capital Expenditures Survey Base Dalse	Treasury Yield 1Y	base
All Employees (Nonfarm) Job Openings: Total Nonfarm Hires: Total Nonfarm Weekly Economic Index S&P 500 VIX Dutstanding Real Estate Loans Outstanding Credit Card Balances Gt. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index Red Business Activity New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	Vehicle Sales	base
Job Openings: Total Nonfarm Hires: Total Nonfarm base Weekly Economic Index S&P 500 VIX Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index base U.S. Dollar Index base Average Weeks Unemployed Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	Unemployment Rate	dlog
Hires: Total Nonfarm Weekly Economic Index S&P 500 VIX Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales KC Fed Labor Market Index Consumer Confidence (OECD) Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	All Employees (Nonfarm)	dlog
Weekly Economic Index S&P 500 VIX base Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Retail & Food Sales Retail & Food Sales KC Fed Labor Market Index Consumer Confidence (OECD) Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	Job Openings: Total Nonfarm	dlog
S&P 500 VIX base Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Base Retail & Food Sales RC Fed Labor Market Index Consumer Confidence (OECD) Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Base Philadelphia Fed: Future Capital Expenditures Survey base	Hires: Total Nonfarm	base
S&P 500 VIX base Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Base Retail & Food Sales RC Fed Labor Market Index Consumer Confidence (OECD) Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Base Philadelphia Fed: Future Capital Expenditures Survey base	Weekly Economic Index	base
Outstanding Real Estate Loans Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Base Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Base Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Base Philadelphia Fed: Future Capital Expenditures Survey Base		dlog
Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Base Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Base Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Base Philadelphia Fed: Future Capital Expenditures Survey Base Dales Base Base Base Base Base Base Base Ba	VIX	base
Outstanding Credit Card Balances St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Base Retail & Food Sales Retail & Food Sales Consumer Confidence (OECD) Base Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Base Philadelphia Fed: Future Capital Expenditures Survey Base Dales Base Base Base Base Base Base Base Ba	Outstanding Real Estate Loans	dlog
St. Louis Fed Financial Stress Index U.S. Dollar Index Average Weeks Unemployed Base Retail & Food Sales Retail & Food Sales RC Fed Labor Market Index Consumer Confidence (OECD) Base Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Base Philadelphia Fed: Future Capital Expenditures Survey Base		9
Average Weeks Unemployed base Retail & Food Sales dlog KC Fed Labor Market Index base Consumer Confidence (OECD) base Industrial Production index dlog PCE Price Index dlog New York Fed: Business Conditions Manufacturing Survey base Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	St. Louis Fed Financial Stress Index	9
Retail & Food Sales dlog KC Fed Labor Market Index base Consumer Confidence (OECD) base Industrial Production index dlog PCE Price Index dlog New York Fed: Business Conditions Manufacturing Survey base Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	U.S. Dollar Index	base
Retail & Food Sales dlog KC Fed Labor Market Index base Consumer Confidence (OECD) base Industrial Production index dlog PCE Price Index dlog New York Fed: Business Conditions Manufacturing Survey base Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	Average Weeks Unemployed	base
KC Fed Labor Market Index Consumer Confidence (OECD) Industrial Production index PCE Price Index New York Fed: Business Conditions Manufacturing Survey Dallas Fed: Current General Business Activity Philadelphia Fed: Future Capital Expenditures Survey base	9 1 1	dlog
Consumer Confidence (OECD) base Industrial Production index dlog PCE Price Index dlog New York Fed: Business Conditions Manufacturing Survey base Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	KC Fed Labor Market Index	U
Industrial Production index dlog PCE Price Index dlog New York Fed: Business Conditions Manufacturing Survey base Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base		base
PCE Price Index dlog New York Fed: Business Conditions Manufacturing Survey base Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base	,	
New York Fed: Business Conditions Manufacturing Survey base Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base		U
Dallas Fed: Current General Business Activity base Philadelphia Fed: Future Capital Expenditures Survey base		9
Philadelphia Fed: Future Capital Expenditures Survey base		
	v	
	Chicago Fed National Activity Index	base

Table 2: Imported Monthly Data - Leading Economic Variables

We additionally import quarterly data for our variables of interest. While this model can be used for nowcasting other data, here we will use import GDP, its components, as well as several other major macroeconomic variables of interest.

Variable	Stationary Form
GDP	dlog
Consumption	$d\log$
Consumption: Goods	$d\log$
Consumption: Goods: Durable	dlog
Consumption: Goods: Durable: Motor Vehicles & Parts	dlog
Consumption: Goods: Durable: Furnishings & Durable Household Equipment	dlog
Consumption: Goods: Durable: Recreational Goods & Services	dlog
Consumption: Goods: Durable: Other Durable Goods	dlog
Consumption: Goods: Nondurable Goods	dlog
Consumption: Goods: Nondurable Goods: Food & Beverages for Off-Premises Use	dlog
Consumption: Goods: Nondurable Goods: Clothing	dlog
Consumption: Goods: Nondurable Goods: Gasoline & Energy Goods	dlog
Consumption: Goods: Nondurable Goods: Other Nondurable Goods	dlog
Consumption: Services	$d\log$
Consumption: Services: Housing & Utilities	$d\log$
Consumption: Services: Health Care	$d\log$
Consumption: Services: Transportation	$d\log$
Consumption: Services: Recreation	$d\log$
Consumption: Services: Food Services & Accommodations	dlog
Consumption: Services: Financial Services	$d\log$
Consumption: Services: Other Services	$d\log$
Consumption: Services: Nonprofit Services	dlog
Gross Private Domestic Investment	$d\log$
Gross Private Domestic Investment: Nonresidential Investment	dlog
Gross Private Domestic Investment: Nonresidential Investment: Structures	$d\log$
Gross Private Domestic Investment: Nonresidential Investment: Equipment	$d\log$
Gross Private Domestic Investment: Nonresidential Investment: Intellectual Property	$d\log$
Gross Private Domestic Investment: Residential Investment	$d\log$
Gross Private Domestic Investment: Change in Private Inventories	base
Net Exports	base
Exports	$d\log$
Exports: Exported Goods	$d\log$
Exports: Exported Services	$d\log$
Imports	$d\log$
Imports: Imported Goods	$d\log$
Imports: Imported Services	$d\log$
Government Spending	$d\log$
Government Spending: Federal	$d\log$
Government Spending: State & Local	$d\log$
Delinquency Rate on Residential Mortgages	base
Delinquency Rate on Credit Cards	base
Delinquency Rate on Commercial & Industrial Loans	base

Table 3: Imported Quarterly Data

Finally, we import additional monthly data that may be of interest to forecast, but are not leading indicators that we will use in our principal components analysis.

Variable Stationary Form

Table 4: Other Imported Monthly Data

Most datasets have already been deseasonalized if necessary by their original source. We deseasonalize the remaining series by using the U.S. Census Bureau's seasonal adjustment package, X13-ARIMA-SEATS. We interface with it by using the seasonal package implementation in R (Sax and Eddelbuettel 2018).

3.2 Time Periods

Now we will segment the data by time periods. The imported monthly data will have ragged edges - i.e., some monthly data will be available for later months than others.

We will let T denote the number of dates for which data is available for all data series. τ will denote the number of dates for which data is available for at least one data series. T^* will denote number of dates up to the end-of-quarter month of the τ date. For example, suppose date τ occurs on February. The end-of-quarter month, T^* , will be March (since Q1 runs through the end of March).

In other words, data will be indexed by $t = 1, 2, ..., T, T + 1, ..., \tau, ..., T^*$, where dates T + 1 through τ are the dates for which only some data are available, and dates $\tau + 1$ through T^* are the dates for which no data is available up to the next quarter-ending month.



For our data, we set the dates as follows.

Date	t
2010-01-01	1
2020-12-01	T
2021-03-01	au
2021-03-01	T*

Table 5: Time Periods

3.3 Principal Components Analysis

It is known that a large number of macroeconomic time series are highly correlated; using such covariates as regressors could naturally lead to problems with collinearity and unstable estimates. In addition, it becomes computationally burdensome to analyze data with such a large number of highly correlated variables. Instead, we use principal components analysis (PCA) to shrink our dataset in a way that allows us to retain most of the information in our original data.

Estimation of factors is derived following Stock and Watson (2008). We begin by taking our $T \times N$ data matrix of N monthly leading economic variables, from time 1 through T. The matrix, which we denote X, is normalized to mean 0 and variance 0 across all columns.

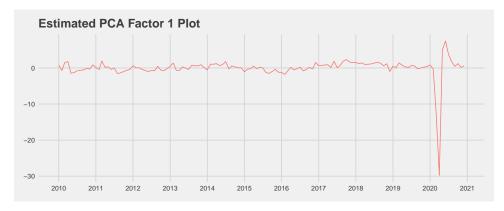
The goal is to minimize the error E below.

$$X = F\Lambda' + E,$$
 where X is the $T \times N$ data matrix,
F is the $T \times N$ matrix of factors,
and Λ is the weighting matrix.

Estimation of factors is derived following Stock and Watson (2008).

$$\widehat{\Lambda}$$
 = eigenvectors of $(X'X)$
 $\widehat{F} = X\widehat{\Lambda}$

Once factors are derived, we perform a qualitative check of the factors. The first factor usually represents the COVID-19 shock. Typically the second factor should give us something similar to the growth rate of GDP or aggregate production, but on a monthly basis. The third and fourth factors may vary but often represent interest rates or consumption. Note that the sign direction of the factors is irrelevant to the modeling process, and they may be switched negated without consequence.





Once factors are derived, we select the optimal number of factors to use in predictive regressions. To do so, we use the information criteria from Bai and Ng (2002). Let R refer to the number of

factors used. We also include alternative specifications of the information criteria from Bai and Ng as a robustness check.

$$IC(R) = MSE + R \times \frac{N+T}{NT} \times log\left(\frac{NT}{N+T}\right)$$

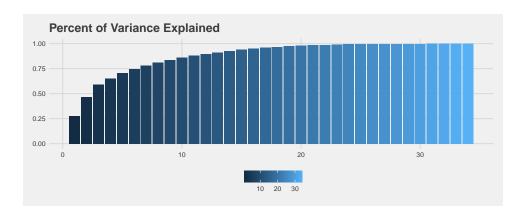


Figure 3: Factor Selection

Factors (R)	Variance Explained	Pct of Total Var Explained	Cumulative Pct	MSE	IC1	IC2	IC3
1	9.50	0.28	0.28	0.72	0.84	0.85	0.82
2	6.46	0.19	0.47	0.53	0.77	0.79	0.73
3	4.17	0.12	0.59	0.40	0.77	0.80	0.72
4	2.07	0.06	0.65	0.34	0.83	0.87	0.76
5	1.91	0.06	0.71	0.29	0.90	0.94	0.81
6	1.36	0.04	0.75	0.25	0.98	1.03	0.87
7	1.17	0.03	0.78	0.21	1.07	1.13	0.94
8	1.05	0.03	0.81	0.18	1.16	1.23	1.01
9	0.82	0.02	0.84	0.16	1.26	1.33	1.09
10	0.76	0.02	0.86	0.14	1.36	1.44	1.17
11	0.68	0.02	0.88	0.12	1.46	1.55	1.26
12	0.60	0.02	0.90	0.10	1.56	1.67	1.34
13	0.52	0.02	0.91	0.09	1.67	1.78	1.43
14	0.49	0.01	0.93	0.07	1.78	1.90	1.52
15	0.44	0.01	0.94	0.06	1.89	2.01	1.61
16	0.39	0.01	0.95	0.05	2.00	2.13	1.71
17	0.30	0.01	0.96	0.04	2.11	2.26	1.80
18	0.26	0.01	0.97	0.03	2.23	2.38	1.90
19	0.22	0.01	0.98	0.02	2.34	2.50	1.99
20	0.19	0.01	0.98	0.02	2.46	2.63	2.09
21	0.16	0.00	0.99	0.01	2.57	2.75	2.19
22	0.12	0.00	0.99	0.01	2.69	2.88	2.29
23	0.10	0.00	0.99	0.01	2.81	3.01	2.39
24	0.08	0.00	0.99	0.01	2.93	3.14	2.49
25	0.05	0.00	1.00	0.00	3.05	3.26	2.60
26	0.04	0.00	1.00	0.00	3.17	3.39	2.70
27	0.03	0.00	1.00	0.00	3.29	3.52	2.80
28	0.02	0.00	1.00	0.00	3.42	3.65	2.91
29	0.02	0.00	1.00	0.00	3.54	3.78	3.01
30	0.01	0.00	1.00	0.00	3.66	3.91	3.11
31	0.01	0.00	1.00	0.00	3.78	4.04	3.22
32	0.00	0.00	1.00	0.00	3.90	4.17	3.32
33	0.00	0.00	1.00	0.00	4.02	4.30	3.42
34	0.00	0.00	1.00	0.00	4.15	4.43	3.53

Table 6: Factor Selection Process

Choosing the IC-minimizing R lets us choose R=2 factors.

3.4 Factor VAR

The next step is to model the transition of the factors over time. To do so, we utilize a vector-autoregressive (VAR) process, following Stock and Watson (2016). As before, R will refer to the total number of factors we extracted in the previous section, and f_t^i for i = 1, ..., R will refer to the value of factor i at time t.

We will use a VAR(1) model of the following form.

$$\underbrace{\begin{bmatrix} f_t^1 \\ f_t^2 \\ \vdots \\ f_t^R \end{bmatrix}}_{z_t} = B \underbrace{\begin{bmatrix} f_{t-1}^1 \\ f_{t-1}^2 \\ \vdots \\ f_{t-1}^R \end{bmatrix}}_{z_{t-1}} + C + \underbrace{\begin{bmatrix} v_t^1 \\ v_t^2 \\ \vdots \\ v_t^R \end{bmatrix}}_{v_t},$$

where z_t is the $R \times 1$ matrix of time t factors,

B is the $R \times R$ coefficient matrix,

C is the $R \times 1$ constant matrix,

and v_t is the $R \times 1$ matrix of errors for time t.

We wish to estimate the coefficient matrices B and C. This can be done via OLS estimation. We first rewrite the data as the standard linear equation,

$$\underbrace{\begin{bmatrix} f_1^1 & f_2^2 & \dots & f_2^R \\ f_3^1 & f_3^2 & \dots & f_3^R \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ f_T^1 & f_T^2 & \dots & f_T^R \end{bmatrix}}_{\Gamma} = \underbrace{\begin{bmatrix} 1 & f_1^1 & f_1^2 & \dots & f_1^R \\ 1 & f_2^1 & f_2^2 & \dots & f_2^R \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & f_{T-1}^1 & f_{T-1}^2 & \dots & f_{T-1}^R \end{bmatrix}}_{\Gamma} \underbrace{\begin{bmatrix} C' \\ B' \end{bmatrix}}_{\Lambda} + \underbrace{\begin{bmatrix} v_1^1 & v_2^2 & \dots & v_2^R \\ v_3^1 & v_3^2 & \dots & v_3^R \\ \vdots & & & & \\ v_T^1 & v_T^2 & \dots & v_T^R \end{bmatrix}}_{V},$$

where Γ is the $T-1\times R$ dependent data matrix, Ψ is the $T-1\times R+1$ independent data matrix, Λ is the $R+1\times R$ matrix of coefficient weightings, and V is the $T-1\times R$ matrix of residuals.

The coefficient matrix Λ can be estimated by the standard OLS estimator.

$$\widehat{\Lambda} = (\Psi'\Psi)^{-1}(\Psi'\Gamma)$$

It can then be partitioned to calculate \widehat{B}' and \widehat{C}' , which can then be transposed to derive our estimates of the original coefficient matrices B and C, \widehat{B} and \widehat{C} .

The estimated coefficients in \widehat{B} and \widehat{C} are shown below.

name	constant	f1.l1	f2.l1
f1	-0.00	0.29	-0.03
f2	-0.05	-0.01	0.98

Table 7: Factor VAR Coefficients

Finally, we perform a qualitative check of the fitted values and residuals. It is important that factors that are predictable — i.e., factors 2 and 3, since they represent output — have a good fit. Since factor 1 represents the COVID-19 shock, we should expect that the fit is poor; such a shock should not be predictable simply from the time dynamics of the factors; so if the fit is good, our model is likely overfitted.

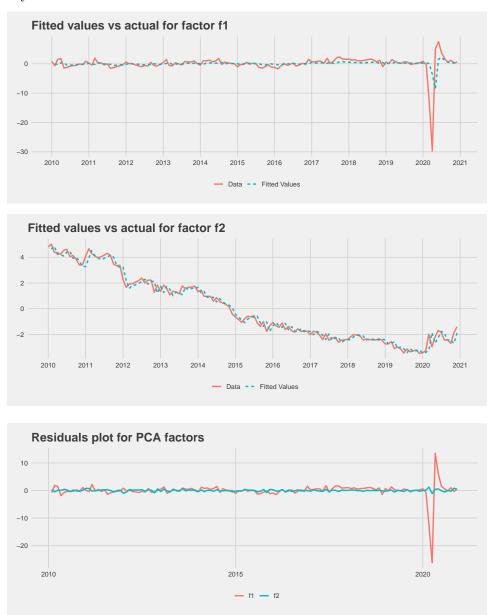


Figure 4: Factor VAR Residuals

Additionally, we expect residuals of the nowcast. Goodness-of-fit statistics are shown below.

varname	MAE	MSE
f1	1.05491706	8.71079660
f2	0.27519652	0.12770368

Table 8: DFM Goodness of Fit

3.5 Dynamic Factor Models

Now let us consider again the monthly leading economic variables which were include in the principal components analysis. We will model these as dynamic factor models (DFMs), i.e. - they are regressed on the factor variables derived from earlier. As before, let x_t^i refer to the time t value for monthly variable x^i , where i = 1, ..., N.

The factor models take the following form:

$$\underbrace{\begin{bmatrix} x_t^1 \\ x_t^2 \\ \vdots \\ x_t^N \end{bmatrix}}_{y_t} = A \underbrace{\begin{bmatrix} f_t^1 \\ f_t^2 \\ \vdots \\ f_t^R \end{bmatrix}}_{z_t} + D + \underbrace{\begin{bmatrix} w_t^1 \\ w_t^2 \\ \vdots \\ w_t^N \end{bmatrix}}_{w_t}$$

where y_t is the $N \times 1$ vector of monthly variables at time t, A is the $N \times R$ coefficient matrix, z_t is the $R \times 1$ vector of factors at time t, D is the $N \times 1$ constant matrix,

and w_t is the $N \times 1$ vector of errors at time t.

We wish to estimate the coefficient matrices A and D. As before, we can do this by estimating this as an OLS equation, writing the data matrices as follows

$$\underbrace{\begin{bmatrix} x_{1}^{1} & x_{2}^{2} & \dots & x_{2}^{N} \\ x_{3}^{1} & x_{3}^{2} & \dots & x_{3}^{N} \\ \vdots & \vdots & \vdots & \vdots \\ x_{T}^{1} & x_{T}^{2} & \dots & x_{T}^{N} \end{bmatrix}}_{\Phi} = \underbrace{\begin{bmatrix} 1 & f_{2}^{1} & f_{2}^{2} & \dots & f_{2}^{R} \\ 1 & f_{3}^{1} & f_{3}^{2} & \dots & f_{3}^{R} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & f_{T}^{1} & f_{T}^{2} & \dots & f_{T}^{R} \end{bmatrix}}_{\Omega} \underbrace{\begin{bmatrix} D' \\ A' \end{bmatrix}}_{W} + \underbrace{\begin{bmatrix} w_{2}^{1} & w_{2}^{2} & \dots & w_{2}^{R} \\ w_{3}^{1} & w_{3}^{2} & \dots & w_{3}^{R} \\ \vdots & & & & \\ w_{T}^{1} & w_{T}^{2} & \dots & w_{T}^{R} \end{bmatrix}}_{W} \tag{1}$$

As before we can estimate A and D with the standard OLS estimator.

$$\begin{bmatrix} \widehat{A} \\ \widehat{D} \end{bmatrix} = (\Omega'\Omega)^{-1}(\Omega'\Phi)$$

Estimated coefficients for \widehat{A} and \widehat{D} are below.

name	constant	f1	f2
mpce	0.00	0.00	0.00
pid	0.00	-0.00	-0.00
hpi	0.00	0.00	-0.00
houst	0.01	0.01	0.00
hsold	0.01	0.01	-0.00
hpermits	0.01	0.01	0.00
mnodg	0.00	0.01	0.00
cu	0.00	0.00	0.00
cons	0.00	0.00	-0.00
ffr	0.59	0.03	-0.19
t10y	2.27	0.05	0.12
t01y	2.27	0.05	0.12
vsales	15.97	0.22	-0.66
ue	-0.00	-0.03	-0.00
emp	0.00	0.00	0.00
jolts	0.01	0.01	0.00
joltshires	5092.23	76.79	-237.79
wei	1.62	0.20	0.32
spy	0.01	0.00	-0.00
vix	17.97	-1.06	0.58
loansre	0.00	-0.00	-0.00
loanscc	0.01	0.00	0.00
stlfsi	-0.26	-0.11	0.01
usd	103.78	-0.25	-3.98
uemean	29.67	0.31	2.39
advsales	0.00	0.01	0.00
kclfi	-0.47	0.06	-0.39
csent	99.78	0.04	-0.48
ipi	0.00	0.00	0.00
pcepi	0.00	0.00	0.00
snyfed	6.18	2.62	0.45
stxfed	2.41	3.20	-0.42
sphfed	21.05	0.79	-2.01
cfnai	-0.07	0.55	0.03

Table 9: Estimated DFM Coefficients

We perform a qualitative check of the in-sample fit, as well as a quantitative review of the goodness-of-fit. The graphs of the fitted plots are located in the appendix.

varname	MAE	MSE
advsales	0.00681700	0.00020334
cfnai	0.36903356	0.27036238
cons	0.00874305	0.00012286
csent	0.50626866	0.53380208
cu	0.00436350	0.00003752
emp	0.00322143	0.00002934
ffr	0.45792142	0.31938201
houst	0.06789934	0.00687780
hpermits	0.04018905	0.00252555
hpi	0.00283978	0.00001484
hsold	0.05934842	0.00625653
ipi	0.00424971	0.00003517
jolts	0.03721109	0.00222811
joltshires	181.73239948	96498.38944195
kclfi	0.24643515	0.14334688
loanscc	0.01446534	0.00232917
loansre	0.00205168	0.00000718
mnodg	0.03046160	0.00195612
mpce	0.00398986	0.00004756
pcepi	0.00099362	0.00000163
pid	0.00568376	0.00010923
snyfed	7.94863047	117.54305779
sphfed	6.28492044	59.99217775
spy	0.02204606	0.00105937
stlfsi	0.30078983	0.18293519
stxfed	11.10721115	206.94180326
t01y	0.47459205	0.35835789
t10y	0.47459205	0.35835789
ue	0.03299664	0.00210707
uemean	2.85275382	14.92402251
usd	3.41528094	18.62528877
vix	4.18377189	34.34071432
vsales	0.90633502	1.55183331
wei	1.13491434	4.56123577

Table 10: DFM Goodness of Fit

3.6 State-Space Setup

Now, combining our equations for the DFM and the VAR, we have the below system.

$$z_t = Bz_{t-1} + Cx + v_t$$
$$y_t = Az_t + w_t$$

This system is now fully specified and in state-space form. The first equation is our state (or transition) equation. The second equation is our measurement equation.

We use our estimated values B, C, A, and D calculated in our previous two sections. To run the Kalman Filter, we will want to create the actual data matrices for z_t and y_t . z_t can be constructed as before, using data for factors from time 1 through T. However, unlike in the previous two sections, we will want to create y_t matrices not for just time periods 1 through T, but now for time periods 1 through τ . Elements in y_t may be set to any value for missing observations; the process of Kalmam filtration will render this choice irrelevant.

Specifically, we construct the matrices below.

$$z_t = \begin{bmatrix} f_t^1 \\ f_t^2 \\ \vdots \\ f_t^R \end{bmatrix}, \forall t \in 1, \dots, T$$

$$y_t = \begin{bmatrix} x_t^1 \text{ if available, otherwise 0} \\ x_t^2 \text{ if available, otherwise 0} \\ \vdots \\ x_t^N \text{ if available, otherwise 0} \end{bmatrix}, \forall t \in 1, \dots, \tau$$

For Kalman filtration, we also require an assumed distribution on v_t and w_t . We assume that v_t is distributed normally with mean 0 and constant diagonal covariance matrix denoted Q, with diagonal entries calculated by taking the average squared values of the residuals of the VAR.

We also assume w_t is distributed normally with mean 0. However, we no longer specify the covariance matrix as constant, but as the time-dependent matrices R_t . For $t \in 1, ..., T+1$, we let R_t be a diagonal covariance matrix with diagonal entries calcualted by taking the average squared values of the residuals of the DFM. For $t \in T+1, ..., \tau$, we let the diagonal elements of R_t be equal to infinity if the corresponding element of y_t is missing for that time period; and equal to the average squared value of the residual if otherwise.

$$v_t \sim \mathcal{N}(0, Q)$$
$$w_t \sim \mathcal{N}(0, R_t)$$

3.7 Kalman Filtration

Now that our state-space model is fully specified, we can begin the Kalman filter recursions.

$$z_t = Bz_{t-1} + Cx + v_t$$
$$y_t = Az_t + Dx + w_t$$
$$v_t \sim \mathcal{N}(0, Q)$$
$$w_t \sim \mathcal{N}(0, R_t)$$

To solve this programmatically, we will need the previously estimated matrices A, B, C, and D; the matrices z_t from 1 through T; the matrices y_t from 1 through τ ; the covariance matrix Q; and finally, the covariance matrices R_t from 1 through τ .

We initialize the Kalman filter with the following standard assumptions.

$$\mathbf{z}_{0|0} = 0$$

$$\mathbf{CovZ} = 0$$

Now for $t = 1, ..., \tau$, we iterate through the Kalman filter recursions and iteratively calculate the values below.

$$\mathbf{z}_{t|t-1} = B\mathbf{z}_{t-1|t-1} + C$$

$$\mathbf{Cov}\mathbf{Z}_{t|t-1} = B\mathbf{Cov}\mathbf{Z}_{t-1|t-1} + Q$$

$$\mathbf{y}_{t|t-1} = A\mathbf{z}_{t|t-1} + D$$

$$\mathbf{Cov}\mathbf{Y}_{t|t-1} = A\mathbf{Cov}\mathbf{Z}_{t|t-1}A' + R_t$$

$$P_t = \mathbf{Cov}\mathbf{Z}_{t|t-1}A'\mathbf{Cov}\mathbf{Y}_{t|t-1}^{-1}$$

$$\mathbf{z}_{t|t} = \mathbf{z}_{t|t-1} + P_t(\mathbf{y}_t - \mathbf{y}_{t|t-1})$$

$$\mathbf{Cov}\mathbf{Z}_{t|t} = \mathbf{Cov}\mathbf{Z}_{t|t-1} - P_t(\mathbf{Cov}\mathbf{Y}_{t|t-1})P_t'$$

Note that the during recursions $T+1, \ldots \tau$, the infinite values in the R_t matrix will cause infinite values in the $\mathbf{CovY}_{t|t-1}$ matrix. This may prevent standard computational methods from computing the inverse of the matrix needed in the step for calculation of $\mathbf{CovZ}_{t|t}$. Alternative methods, such as a Cholesky decomposition before inversion, are used to subvert this problem.

The Kalman filter allows us to recover all the time t conditional state matrices $z_{t|t}$ that have been adjusted for information from the monthly datasets. However, of more interest to us is the value of the state matrices when conditioned on all data available at time τ , $z_{t|\tau}$. This can be recovered by using the Kalman smoother.

Recursively iterating over $t = \tau - 1, \dots, 1$, we calculate the following values.

$$S_t = \mathbf{Cov} \mathbf{Z}_{t|t} B' \mathbf{Cov} \mathbf{Z}_{t+1|t}^{-1}$$

$$\mathbf{z}_{t|\tau} = \mathbf{z}_{t|t} + S_t (\mathbf{z}_{t+1|\tau} - \mathbf{z}_{t+1|t})$$

$$\mathbf{Cov} \mathbf{Z}_{t|\tau} = \mathbf{Cov} \mathbf{Z}_{t|t} - S_t (\mathbf{Cov} \mathbf{Z}_{t+1|t} - \mathbf{Cov} \mathbf{Z}_{t+1|\tau}) S'_t$$

These values $\mathbf{z}_{t|\tau}$ will serve as our estimates of the state variables (i.e., the PCA factors) from time 1 through τ .

Finally, we want to forecast the state vector $z_{t|\tau}$ for $t = \tau + 1, \ldots, T^*$. This can be done through the typical Kalman filter forecasting step.

Recursively iterating over $t = \tau + 1, \dots, T^*$, we calculate the following values.

$$\mathbf{z}_{t|\tau} = B\mathbf{z}_{t-1|\tau} + C$$

$$\mathbf{Cov}\mathbf{Z}_{t|\tau} = B\mathbf{Cov}\mathbf{Z}_{t-1|\tau}B' + Q$$

$$\mathbf{y}_{t|\tau} = A\mathbf{z}_{t|\tau} + D$$

$$\mathbf{Cov}\mathbf{Y}_{t|\tau} = A\mathbf{Cov}\mathbf{Z}_{t|\tau}A' + R_0$$

Combining the calculations for $\mathbf{z}_{t|\tau}$ with the ones derived from the Kalman smoother, we will now be able to obtain the full time series for the factors from time 1 through time T^* .



3.8 Nowcast Step

Now that we have our Kalman-smoothed and forecasted factors from time 1 through time T^* , we will be able to use these as covariates to model any monthly time series that we have.

We begin by aggregating these monthly factors into quarterly data by taking a simple monthly average for each factor over each quarter.

In this section, we will use these now-quarterly factors to forecast our quarterly subcomponents of GDP. As discussed in the data import section, these have been transformed for stationarity, typically by taking a log-difference.

Variable
Consumption: Goods: Durable: Motor Vehicles & Parts
Consumption: Goods: Durable: Furnishings & Durable Household Equipment
Consumption: Goods: Durable: Recreational Goods & Services
Consumption: Goods: Durable: Other Durable Goods
Consumption: Goods: Nondurable Goods: Food & Beverages for Off-Premises Use
Consumption: Goods: Nondurable Goods: Clothing
Consumption: Goods: Nondurable Goods: Gasoline & Energy Goods
Consumption: Goods: Nondurable Goods: Other Nondurable Goods
Consumption: Services: Housing & Utilities
Consumption: Services: Health Care
Consumption: Services: Transportation
Consumption: Services: Recreation
Consumption: Services: Food Services & Accommodations
Consumption: Services: Financial Services
Consumption: Services: Other Services
Consumption: Services: Nonprofit Services
Gross Private Domestic Investment: Nonresidential Investment: Structures
Gross Private Domestic Investment: Nonresidential Investment: Equipment
Gross Private Domestic Investment: Nonresidential Investment: Intellectual Property
Gross Private Domestic Investment: Residential Investment
Gross Private Domestic Investment: Change in Private Inventories
Exports: Exported Goods
Exports: Exported Services
Imports: Imported Goods
Imports: Imported Services
Government Spending: Federal
Government Spending: State & Local

Table 11: Quarterly Data Covariates

We will notate each of these gdp subcomponents as y^i and M as the total number of covariates, so that i = 1, ..., M.

Note that many higher-level components of GDP (including GDP itself) are *not* forecasted directly in this step; these will be forecasted later by aggregating their subcomponents.

Now we will specify that these GDP subcomponents follow a DFM-AR(1) model; i.e., they will be functions of the monthly-aggregated factors as well as the first lag of themselves.

$$y_t^i = \beta \begin{bmatrix} 1 \\ y_{t-1}^i \\ f_t^1 \\ \vdots \\ f_t^R \end{bmatrix} + e_t$$

The β coefficients can be estimated with a typical OLS process, where the training data is constituted of the y_t^i quarterly covariates, the lagged quarterly covariates y_{t-1}^i , and the quarterly-aggregated factor variables. The data is cut off at the date for which the any data on the quarterly covariates are missing.

After estimation, we then use the same model to forecast forward the y_t^i quarterly, up through time τ . The forecasted results are as follows.

Variable	2021Q1	2021Q2
Consumption: Goods: Durable: Motor Vehicles & Parts	0.03	0.01
Consumption: Goods: Durable: Furnishings & Durable Household Equipment	0.04	0.01
Consumption: Goods: Durable: Recreational Goods & Services	0.02	0.02
Consumption: Goods: Durable: Other Durable Goods	0.06	0.00
Consumption: Goods: Nondurable Goods: Food & Beverages for Off-Premises Use	0.01	0.00
Consumption: Goods: Nondurable Goods: Clothing	0.05	-0.00
Consumption: Goods: Nondurable Goods: Gasoline & Energy Goods	0.03	-0.01
Consumption: Goods: Nondurable Goods: Other Nondurable Goods	0.02	0.01
Consumption: Services: Housing & Utilities	0.00	0.00
Consumption: Services: Health Care	0.03	0.00
Consumption: Services: Transportation	0.06	-0.00
Consumption: Services: Recreation	0.07	-0.00
Consumption: Services: Food Services & Accommodations	0.06	-0.01
Consumption: Services: Financial Services	0.00	0.00
Consumption: Services: Other Services	0.03	0.01
Consumption: Services: Nonprofit Services	-0.03	0.01
Gross Private Domestic Investment: Nonresidential Investment: Structures	0.01	0.00
Gross Private Domestic Investment: Nonresidential Investment: Equipment	0.03	0.01
Gross Private Domestic Investment: Nonresidential Investment: Intellectual Property	0.02	0.01
Gross Private Domestic Investment: Residential Investment	0.02	0.01
Gross Private Domestic Investment: Change in Private Inventories	86.54	71.82
Exports: Exported Goods	0.03	0.01
Exports: Exported Services	0.03	0.01
Imports: Imported Goods	0.03	0.01
Imports: Imported Services	0.05	0.01
Government Spending: Federal	-0.00	0.00
Government Spending: State & Local	0.00	0.00

Table 12: DFM-AR(1) Forecasted GDP Subcomponents

We can then backtransform the data so that the units are in base values. After backtransformation, we are ready to aggregate these up to higher-level GDP components. In particular, we calculate the variables below.

Variable
GDP
Consumption
Consumption: Goods
Consumption: Goods: Durable
Consumption: Goods: Nondurable Goods
Consumption: Services
Gross Private Domestic Investment
Gross Private Domestic Investment: Nonresidential Investment
Net Exports
Exports
Imports
Government Spending

Table 13: Summable Quarterly Data Covariates

These are calculated using the standard GDP aggregation equations, e.g., net exports – imports, and so on. Finally, we convert these into annualized percentage change, as this is the standard format in which GDP subcomponents are reported in. The results are reported in the next section.

We also use a similar DFM-AR(1) specification to forecast out other economic variables of interest, with results reported in the next section.

4 RESULTS 22

4 Results

Our final nowcasts of GDP and its subcomponents are below. All units are reported in terms of annualized percentage change (seasonally adjusted) except for change in private inventories and net exports, which are reported in terms of billions of real 2012 dollars.

Variable	2021Q1	2021Q2
GDP	10.44	1.46
Consumption	15.35	1.74
Goods	12.96	2.86
Durable	22.28	5.57
Motor Vehicles & Parts	11.45	4.41
Furnishings & Durable Household Equipment	18.55	3.01
Recreational Goods & Services	7.18	9.99
Other Durable Goods	24.88	1.09
Nondurable Goods	3.10	1.07
Food & Beverages for Off-Premises Use	4.09	0.94
Clothing	20.78	-1.57
Gasoline & Energy Goods	13.82	-3.36
Other Nondurable Goods	6.27	3.57
Services	9.01	1.01
Housing & Utilities	1.05	1.21
Health Care	13.51	1.48
Transportation	27.97	-1.12
Recreation	34.63	-1.30
Food Services & Accommodations	29.34	-3.73
Financial Services	1.88	1.14
Other Services	13.02	2.58
Nonprofit Services	-12.50	5.96
Gross Private Domestic Investment	12.35	3.11
Nonresidential Investment	13.31	4.68
Structures	4.58	1.70
Equipment	13.62	5.21
Intellectual Property	7.37	5.37
Residential Investment	10.38	5.75
Change in Private Inventories	86.54	71.82
Net Exports	-1169.32	-1189.32
Exports	20.68	2.60
Exported Goods	14.22	2.06
Exported Services	12.55	4.18
Imports	19.64	4.04
Imported Goods	13.21	3.75
Imported Services	22.64	6.12
Government Spending	-0.11	0.49
Federal	-0.97	0.52
State & Local	0.27	0.46
ancha — annualized % change		

apchg = annualized % change

Table 14: Nowcasts for GDP and Subcomponents (Annualized Percent Change)

We also report nowcasts of other variables of interest, including other quarterly variables, as well

4 RESULTS 23

as all monthly variables used in this process. Note that because these variables are ragged-edge in nature, there may be "blank" columns. These columns simply indicate that historical data already exists for those columns. Only nowcasts produced by the model are reported.

Variable	2021Q1	2021Q2
Delinquency Rate on Residential Mortgages	2.95	3.15
Delinquency Rate on Credit Cards	2.15	2.17
Delinquency Rate on Commercial \& Industrial Loans	1.26	1.23

Table 15: Nowcasts for Other Quarterly Variables

4 RESULTS 24

Variable	2021M1	2021M2	2021M3	2021M4	2021N
PCE (apchg)		3.87	-6.74	2.80	2.
PCE: Goods (apchg)		6.26	-4.34	5.20	5.1
PCE: Goods: Durable Goods (apchg)		9.90	-4.16	8.46	8.4
PCE: Goods: Nondurable Goods (apchg)		4.46	-4.44	3.57	3.
PCE: Services (apchg)		2.76	-7.85	1.68	1.0
Personal Income (apchg)		2.45	10.10	3.17	3.
Disposable Personal Income (apchg)		2.25	11.51	3.12	3.
Personal Outlays (apchg)		5.40	-5.63	4.28	4.1
Personal Savings (apchg)		4.69	131.40	13.08	13.
Personal Savings Rate		0.23	0.25	0.25	0.3
Case-Shiller Housing Price Index	236.63	237.63	238.62	239.63	240.0
Housing Starts	200.00	1597.32	1576.29	1589.83	1603.4
Houses Sold		932.38	930.71	939.11	947.0
New Private Housing Permits		1905.10	1894.72	1911.02	1927.
Manufacturers New Orders: Durable Goods		258049.51	255071.38	255989.21	256902.5
Capacity Utilization: Total Index		75.66	75.12	75.17	75.5
Total Construction Spending		1529170.10	1533916.06	1541414.89	1548958.
Effective Federal Funds Rate		1029170.10	0.07	0.07	0.0
Secured Overnight Financing Rate			0.04	0.04	0.0
Treasury Yield 10Y			1.52	1.55	1.4
Treasury Yield 30Y			$\frac{1.32}{2.36}$	$\frac{1.33}{2.37}$	2.3
Treasury Yield 5Y			0.87	0.90	0.9
Treasury Yield 2Y			0.33	0.90 0.36	0.:
Treasury Yield 1Y			0.33	0.30	0
Treasury Yield 6M			0.10	0.10	0
Treasury Yield 3M			0.03	0.10	0.0
Treasury Yield 1M			0.04	0.00 0.04	0.0
Treasury Yield 20Y			$\frac{0.02}{2.13}$	$\frac{0.04}{2.14}$	2.
Treasury Yield 7Y			1.17	$\frac{2.14}{1.20}$	1.5
Vehicle Sales			16.29	1.20 16.64	16.0
			6.54	6.50	6.4
Unemployment Rate			0.54 142179.81		142500.
All Employees (Nonfarm) Job Openings: Total Nonfarm		6978.31	6916.29	142340.43 6965.34	7014.4
Hires: Total Nonfarm		5353.00	5198.73	5344.14	5348.
S&P 500		ə ə əə.00	5196.75	3904.80	3941.
VIX				3904.80 17.47	3941.6 17.4
			9 19	2.94	
Outstanding Real Estate Loans (apchg)			3.13 1.55	4.93	2.9
Outstanding Credit Card Balances (apchg)					4.3
Housing Prices: New Listed Prices (apchg)			12.09	12.34	12.5
St. Louis Fed Financial Stress Index			-0.13	-0.29	-0.5
U.S. Dollar Index			108.18	107.96	108.
Average Weeks Unemployed		4.07	26.73	27.18	27.
Retail & Food Sales (apchg)		4.97	-8.36	3.59	3
KC Fed Labor Market Index		100.05	-0.17	-0.07	-0.0
Consumer Confidence (OECD)		100.27	100.24	100.28	100.5
PCE Price Index (apchg)		1.57	1.00	1.51	1.
New York Fed: Business Conditions Manufacturing Survey			2.39	6.36	6.3
Dallas Fed: Current General Business Activity			-1.06	3.46	3.4
Philadelphia Fed: Future Capital Expenditures Survey			22.30	23.31	23.3

apchg = annualized % change

Table 16: Nowcasts for All Monthly Variables

Appendices

A DFM Fitted Plots

