

# Shape functions of Hex32

## Coordinates of points in the reference space

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In[2]:= x = {{(*1*){-1, -1, -1}, (*2*){1, -1, -1}, (*3*){1, 1, -1}, (*4*){-1, 1, -1}, (*5*)  
{-1, -1, 1}, (*6*){1, -1, 1}, (*7*){1, 1, 1}, (*8*){-1, 1, 1}, (*9*){-1/3, -1, -1},  
(*10*){1/3, -1, -1}, (*11*){1, -1/3, -1}, (*12*){1, 1/3, -1}, (*13*){1/3, 1, -1},  
(*14*){-1/3, 1, -1}, (*15*){-1, 1/3, -1}, (*16*){-1, -1/3, -1}, (*17*)  
{-1/3, -1, 1}, (*18*){1/3, -1, 1}, (*19*){1, -1/3, 1}, (*20*){1, 1/3, 1}, (*21*)  
{1/3, 1, 1}, (*22*){-1/3, 1, 1}, (*23*){-1, 1/3, 1}, (*24*){-1, -1/3, 1}, (*25*)  
{-1, -1, -1/3}, (*26*){-1, -1, 1/3}, (*27*){1, -1, -1/3}, (*28*){1, -1, 1/3},  
(*29*){1, 1, -1/3}, (*30*){1, 1, 1/3}, (*31*){-1, 1, -1/3}, (*32*){-1, 1, 1/3}};
```

## Shape functions

```
In[3]:= group1 = {9, 10, 13, 14, 17, 18, 21, 22}; (* points with r=+-1/3 *)  
group2 = {11, 12, 15, 16, 19, 20, 23, 24}; (* points with s=+-1/3 *)
```

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In[5]:= ShapeFunc[n_] :=  
If[n ≤ 8,  $\frac{1}{64} (1 + r x[n, 1]) (1 + s x[n, 2]) (1 + t x[n, 3]) (9 r^2 + 9 s^2 + 9 t^2 - 19)$ ,  
If[MemberQ[group1, n],  $\frac{9}{64} (1 - r^2) (1 + 9 r x[n, 1]) (1 + s x[n, 2]) (1 + t x[n, 3])$ ,  
If[MemberQ[group2, n],  $\frac{9}{64} (1 + r x[n, 1]) (1 - s^2) (1 + 9 s x[n, 2]) (1 + t x[n, 3])$ ,  
 $\frac{9}{64} (1 + r x[n, 1]) (1 + s x[n, 2]) (1 - t^2) (1 + 9 t x[n, 3])$ ]]];
```

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In[6]:= AllShapeFunc = Table[ShapeFunc[m], {m, 32}];
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In[7]:= AllShapeFunc // MatrixForm
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Out[7]//MatrixForm=
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$$\begin{pmatrix} \frac{1}{64} (1-r)(1-s)(1-t)(-19+9r^2+9s^2+9t^2) \\ \frac{1}{64} (1+r)(1-s)(1-t)(-19+9r^2+9s^2+9t^2) \\ \frac{1}{64} (1+r)(1+s)(1-t)(-19+9r^2+9s^2+9t^2) \\ \frac{1}{64} (1-r)(1+s)(1-t)(-19+9r^2+9s^2+9t^2) \\ \frac{1}{64} (1-r)(1-s)(1+t)(-19+9r^2+9s^2+9t^2) \\ \frac{1}{64} (1+r)(1-s)(1+t)(-19+9r^2+9s^2+9t^2) \\ \frac{1}{64} (1+r)(1+s)(1+t)(-19+9r^2+9s^2+9t^2) \\ \frac{1}{64} (1-r)(1+s)(1+t)(-19+9r^2+9s^2+9t^2) \\ \frac{9}{64} (1-3r)(1-r^2)(1-s)(1-t) \\ \frac{9}{64} (1+3r)(1-r^2)(1-s)(1-t) \\ \frac{9}{64} (1+r)(1-3s)(1-s^2)(1-t) \\ \frac{9}{64} (1+r)(1+3s)(1-s^2)(1-t) \\ \frac{9}{64} (1+3r)(1-r^2)(1+s)(1-t) \\ \frac{9}{64} (1-3r)(1-r^2)(1+s)(1-t) \\ \frac{9}{64} (1-r)(1+3s)(1-s^2)(1-t) \\ \frac{9}{64} (1-r)(1-3s)(1-s^2)(1-t) \\ \frac{9}{64} (1-3r)(1-r^2)(1-s)(1+t) \\ \frac{9}{64} (1+3r)(1-r^2)(1-s)(1+t) \\ \frac{9}{64} (1+r)(1-3s)(1-s^2)(1+t) \\ \frac{9}{64} (1+r)(1+3s)(1-s^2)(1+t) \\ \frac{9}{64} (1+3r)(1-r^2)(1+s)(1+t) \\ \frac{9}{64} (1-3r)(1-r^2)(1+s)(1+t) \\ \frac{9}{64} (1-r)(1+3s)(1-s^2)(1+t) \\ \frac{9}{64} (1-r)(1-3s)(1-s^2)(1+t) \\ \frac{9}{64} (1-r)(1-s)(1-3t)(1-t^2) \\ \frac{9}{64} (1-r)(1-s)(1+3t)(1-t^2) \\ \frac{9}{64} (1+r)(1-s)(1-3t)(1-t^2) \\ \frac{9}{64} (1+r)(1-s)(1+3t)(1-t^2) \\ \frac{9}{64} (1+r)(1+s)(1-3t)(1-t^2) \\ \frac{9}{64} (1+r)(1+s)(1+3t)(1-t^2) \\ \frac{9}{64} (1-r)(1+s)(1-3t)(1-t^2) \\ \frac{9}{64} (1-r)(1+s)(1+3t)(1-t^2) \end{pmatrix}$$

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In[8]:= substitution = {
  (1 - r) → rm, (1 - s) → sm, (1 - t) → tm,
  (1 + r) → rp, (1 + s) → sp, (1 + t) → tp,
  (1 - 3 r) → r3m, (1 - 3 s) → s3m, (1 - 3 t) → t3m,
  (1 + 3 r) → r3p, (1 + 3 s) → s3p, (1 + 3 t) → t3p,
  (1 - r2) → rr, (1 - s2) → ss, (1 - t2) → tt,
  9 r2 → rr9, 9 s2 → ss9, 9 t2 → tt9
};

In[9]:= interp = AllShapeFunc /. substitution;
Print[CForm[interp]]

List((rm*sm*tm*(-19 + rr9 + ss9 + tt9))/64.,(rp*sm*tm*(-19 + rr9 + ss9 +
  tt9))/64.,(rp*sp*tm*(-19 + rr9 + ss9 + tt9))/64.,(rm*sp*tm*(-19 + rr9 + ss9 +
  tt9))/64.,(rm*sm*tp*(-19 + rr9 + ss9 + tt9))/64.,(rp*sm*tp*(-19 + rr9 + ss9 +
  tt9))/64.,(rp*sp*tp*(-19 + rr9 + ss9 + tt9))/64.,(rm*sp*tp*(-19 + rr9 + ss9 +
  tt9))/64.,(9*r3m*rr*sm*tm)/64.,(9*r3p*rr*sm*tm)/64.,(9*rp*s3m*ss*tm)/64.,(9*rp*s3p*ss*tm)/64.,(9*
  r3p*rr*sp*tm)/64.,(9*r3m*rr*sp*tm)/64.,(9*rm*s3p*ss*tm)/64.,(9*rm*s3m*ss*tm)/64.,(9*r3m*rr*sm*tp)/
  64.,(9*r3p*rr*sm*tp)/64.,(9*rp*s3m*ss*tp)/64.,(9*rp*s3p*ss*tp)/64.,(9*r3p*rr*sp*tp)/64.,(9*r3m*rr*
  sp*tp)/64.,(9*rm*s3p*ss*tp)/64.,(9*rm*s3m*ss*tp)/64.,(9*rm*sm*t3m*tt)/64.,(9*rm*sm*t3p*tt)/64.,(9*
  rp*sm*t3m*tt)/64.,(9*rp*sm*t3p*tt)/64.,(9*rp*sp*t3m*tt)/64.,(9*rp*sp*t3p*tt)/64.,(9*rm*sp*t3m*tt)/
  64.,(9*rm*sp*t3p*tt)/64.)

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## Derivative of shape functions

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In[11]:= AllDerivShapeWrtR = D[AllShapeFunc, r];
AllDerivShapeWrtS = D[AllShapeFunc, s];
AllDerivShapeWrtT = D[AllShapeFunc, t];

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In[14]:= AllDerivShapeWrtR // MatrixForm
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Out[14]//MatrixForm=
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$$\begin{pmatrix} \frac{9}{32} (1-r) r (1-s) (1-t) - \frac{1}{64} (1-s) (1-t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} r (1+r) (1-s) (1-t) + \frac{1}{64} (1-s) (1-t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} r (1+r) (1+s) (1-t) + \frac{1}{64} (1+s) (1-t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1-r) r (1+s) (1-t) - \frac{1}{64} (1+s) (1-t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1-r) r (1-s) (1+t) - \frac{1}{64} (1-s) (1+t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} r (1+r) (1-s) (1+t) + \frac{1}{64} (1-s) (1+t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} r (1+r) (1+s) (1+t) + \frac{1}{64} (1+s) (1+t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1-r) r (1+s) (1+t) - \frac{1}{64} (1+s) (1+t) (-19+9r^2+9s^2+9t^2) \\ -\frac{9}{32} (1-3r) r (1-s) (1-t) - \frac{27}{64} (1-r^2) (1-s) (1-t) \\ -\frac{9}{32} r (1+3r) (1-s) (1-t) + \frac{27}{64} (1-r^2) (1-s) (1-t) \\ \frac{9}{64} (1-3s) (1-s^2) (1-t) \\ \frac{9}{64} (1+3s) (1-s^2) (1-t) \\ -\frac{9}{32} r (1+3r) (1+s) (1-t) + \frac{27}{64} (1-r^2) (1+s) (1-t) \\ -\frac{9}{32} (1-3r) r (1+s) (1-t) - \frac{27}{64} (1-r^2) (1+s) (1-t) \\ -\frac{9}{64} (1+3s) (1-s^2) (1-t) \\ -\frac{9}{64} (1-3s) (1-s^2) (1-t) \\ -\frac{9}{32} (1-3r) r (1-s) (1+t) - \frac{27}{64} (1-r^2) (1-s) (1+t) \\ -\frac{9}{32} r (1+3r) (1-s) (1+t) + \frac{27}{64} (1-r^2) (1-s) (1+t) \\ \frac{9}{64} (1-3s) (1-s^2) (1+t) \\ \frac{9}{64} (1+3s) (1-s^2) (1+t) \\ -\frac{9}{32} r (1+3r) (1+s) (1+t) + \frac{27}{64} (1-r^2) (1+s) (1+t) \\ -\frac{9}{32} (1-3r) r (1+s) (1+t) - \frac{27}{64} (1-r^2) (1+s) (1+t) \\ -\frac{9}{64} (1+3s) (1-s^2) (1+t) \\ -\frac{9}{64} (1-3s) (1-s^2) (1+t) \\ -\frac{9}{64} (1-s) (1-3t) (1-t^2) \\ -\frac{9}{64} (1-s) (1+3t) (1-t^2) \\ \frac{9}{64} (1-s) (1-3t) (1-t^2) \\ \frac{9}{64} (1-s) (1+3t) (1-t^2) \\ \frac{9}{64} (1+s) (1-3t) (1-t^2) \\ \frac{9}{64} (1+s) (1+3t) (1-t^2) \\ -\frac{9}{64} (1+s) (1-3t) (1-t^2) \\ -\frac{9}{64} (1+s) (1+3t) (1-t^2) \end{pmatrix}$$

In[15]:= AllDerivShapeWrts // MatrixForm

Out[15]//MatrixForm=

$$\left( \begin{array}{l} \frac{9}{32} (1-r) (1-s) s (1-t) - \frac{1}{64} (1-r) (1-t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1+r) (1-s) s (1-t) - \frac{1}{64} (1+r) (1-t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1+r) s (1+s) (1-t) + \frac{1}{64} (1+r) (1-t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1-r) s (1+s) (1-t) + \frac{1}{64} (1-r) (1-t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1-r) (1-s) s (1+t) - \frac{1}{64} (1-r) (1+t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1+r) (1-s) s (1+t) - \frac{1}{64} (1+r) (1+t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1+r) s (1+s) (1+t) + \frac{1}{64} (1+r) (1+t) (-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1-r) s (1+s) (1+t) + \frac{1}{64} (1-r) (1+t) (-19+9r^2+9s^2+9t^2) \\ - \frac{9}{64} (1-3r) (1-r^2) (1-t) \\ - \frac{9}{64} (1+3r) (1-r^2) (1-t) \\ - \frac{9}{32} (1+r) (1-3s) s (1-t) - \frac{27}{64} (1+r) (1-s^2) (1-t) \\ - \frac{9}{32} (1+r) s (1+3s) (1-t) + \frac{27}{64} (1+r) (1-s^2) (1-t) \\ \frac{9}{64} (1+3r) (1-r^2) (1-t) \\ \frac{9}{64} (1-3r) (1-r^2) (1-t) \\ - \frac{9}{32} (1-r) s (1+3s) (1-t) + \frac{27}{64} (1-r) (1-s^2) (1-t) \\ - \frac{9}{32} (1-r) (1-3s) s (1-t) - \frac{27}{64} (1-r) (1-s^2) (1-t) \\ - \frac{9}{64} (1-3r) (1-r^2) (1+t) \\ - \frac{9}{64} (1+3r) (1-r^2) (1+t) \\ - \frac{9}{32} (1+r) (1-3s) s (1+t) - \frac{27}{64} (1+r) (1-s^2) (1+t) \\ - \frac{9}{32} (1+r) s (1+3s) (1+t) + \frac{27}{64} (1+r) (1-s^2) (1+t) \\ \frac{9}{64} (1+3r) (1-r^2) (1+t) \\ \frac{9}{64} (1-3r) (1-r^2) (1+t) \\ - \frac{9}{32} (1-r) s (1+3s) (1+t) + \frac{27}{64} (1-r) (1-s^2) (1+t) \\ - \frac{9}{32} (1-r) (1-3s) s (1+t) - \frac{27}{64} (1-r) (1-s^2) (1+t) \\ - \frac{9}{64} (1-r) (1-3t) (1-t^2) \\ - \frac{9}{64} (1-r) (1+3t) (1-t^2) \\ - \frac{9}{64} (1+r) (1-3t) (1-t^2) \\ - \frac{9}{64} (1+r) (1+3t) (1-t^2) \\ \frac{9}{64} (1+r) (1-3t) (1-t^2) \\ \frac{9}{64} (1+r) (1+3t) (1-t^2) \\ \frac{9}{64} (1-r) (1-3t) (1-t^2) \\ \frac{9}{64} (1-r) (1+3t) (1-t^2) \end{array} \right)$$

In[16]:= **AllDerivShapeWrTt // MatrixForm**

Out[16]//MatrixForm=

$$\left( \begin{array}{l} \frac{9}{32} (1-r)(1-s)(1-t)t - \frac{1}{64} (1-r)(1-s)(-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1+r)(1-s)(1-t)t - \frac{1}{64} (1+r)(1-s)(-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1+r)(1+s)(1-t)t - \frac{1}{64} (1+r)(1+s)(-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1-r)(1+s)(1-t)t - \frac{1}{64} (1-r)(1+s)(-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1-r)(1-s)t(1+t) + \frac{1}{64} (1-r)(1-s)(-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1+r)(1-s)t(1+t) + \frac{1}{64} (1+r)(1-s)(-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1+r)(1+s)t(1+t) + \frac{1}{64} (1+r)(1+s)(-19+9r^2+9s^2+9t^2) \\ \frac{9}{32} (1-r)(1+s)t(1+t) + \frac{1}{64} (1-r)(1+s)(-19+9r^2+9s^2+9t^2) \\ -\frac{9}{64} (1-3r)(1-r^2)(1-s) \\ -\frac{9}{64} (1+3r)(1-r^2)(1-s) \\ -\frac{9}{64} (1+r)(1-3s)(1-s^2) \\ -\frac{9}{64} (1+r)(1+3s)(1-s^2) \\ -\frac{9}{64} (1+3r)(1-r^2)(1+s) \\ -\frac{9}{64} (1-3r)(1-r^2)(1+s) \\ -\frac{9}{64} (1-r)(1+3s)(1-s^2) \\ -\frac{9}{64} (1-r)(1-3s)(1-s^2) \\ \frac{9}{64} (1-3r)(1-r^2)(1-s) \\ \frac{9}{64} (1+3r)(1-r^2)(1-s) \\ \frac{9}{64} (1+r)(1-3s)(1-s^2) \\ \frac{9}{64} (1+r)(1+3s)(1-s^2) \\ \frac{9}{64} (1+3r)(1-r^2)(1+s) \\ \frac{9}{64} (1-3r)(1-r^2)(1+s) \\ \frac{9}{64} (1-r)(1+3s)(1-s^2) \\ \frac{9}{64} (1-r)(1-3s)(1-s^2) \\ -\frac{9}{32} (1-r)(1-s)(1-3t)t - \frac{27}{64} (1-r)(1-s)(1-t^2) \\ -\frac{9}{32} (1-r)(1-s)t(1+3t) + \frac{27}{64} (1-r)(1-s)(1-t^2) \\ -\frac{9}{32} (1+r)(1-s)(1-3t)t - \frac{27}{64} (1+r)(1-s)(1-t^2) \\ -\frac{9}{32} (1+r)(1-s)t(1+3t) + \frac{27}{64} (1+r)(1-s)(1-t^2) \\ -\frac{9}{32} (1+r)(1+s)(1-3t)t - \frac{27}{64} (1+r)(1+s)(1-t^2) \\ -\frac{9}{32} (1+r)(1+s)t(1+3t) + \frac{27}{64} (1+r)(1+s)(1-t^2) \\ -\frac{9}{32} (1-r)(1+s)(1-3t)t - \frac{27}{64} (1-r)(1+s)(1-t^2) \\ -\frac{9}{32} (1-r)(1+s)t(1+3t) + \frac{27}{64} (1-r)(1+s)(1-t^2) \end{array} \right)$$

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In[17]:= derivR = AllDerivShapeWrtR /. substitution;
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Print[CForm[derivR]]
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```
List((9*r*rm*sm*tm)/32. - (sm*tm*(-19 + rr9 + ss9 + tt9))/64.,(9*r*rp*sm*tm)/32. +
  (sm*tm*(-19 + rr9 + ss9 + tt9))/64.,(9*r*rp*sp*tm)/32. + (sp*tm*(-19 + rr9 + ss9 +
  tt9))/64.,(9*r*rm*sp*tm)/32. - (sp*tm*(-19 + rr9 + ss9 + tt9))/64.,(9*r*rm*sm*tp)/32.
  - (sm*tp*(-19 + rr9 + ss9 + tt9))/64.,(9*r*rp*sm*tp)/32. + (sm*tp*(-19 + rr9 + ss9 +
  tt9))/64.,(9*r*rp*sp*tp)/32. + (sp*tp*(-19 + rr9 + ss9 + tt9))/64.,(9*r*rm*sp*tp)/32. -
  (sp*tp*(-19 + rr9 + ss9 + tt9))/64.,(-9*r*r3m*sm*tm)/32. - (27*rr*sm*tm)/64.,(-9*r*r3p*sm*tm)/32.
  + (27*rr*sm*tm)/64.,(9*s3m*ss*tm)/64.,(9*s3p*ss*tm)/64.,(-9*r*r3p*sp*tm)/32.
  + (27*rr*sp*tm)/64.,(-9*r*r3m*sp*tm)/32. -
  (27*rr*sp*tm)/64.,(-9*s3p*ss*tm)/64.,(-9*s3m*ss*tm)/64.,(-9*r*r3m*sm*tp)/32.
  - (27*rr*sm*tp)/64.,(-9*r*r3p*sm*tp)/32. +
  (27*rr*sm*tp)/64.,(9*s3m*ss*tp)/64.,(9*s3p*ss*tp)/64.,(-9*r*r3p*sp*tp)/32.
  + (27*rr*sp*tp)/64.,(-9*r*r3m*sp*tp)/32. -
  (27*rr*sp*tp)/64.,(-9*s3p*ss*tp)/64.,(-9*s3m*ss*tp)/64.,(-9*sm*t3m*tt)/64.,(-9*sm*t3p*tt)/64.,(9*sm*
  t3m*tt)/64.,(9*sm*t3p*tt)/64.,(9*sp*t3m*tt)/64.,(9*sp*t3p*tt)/64.,(-9*sp*t3m*tt)/64.,(-9*sp*t3p*tt)/
  64.)
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In[19]:= derivS = AllDerivShapeWrtS /. substitution;
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```
Print[CForm[derivS]]
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```
List((9*rm*s*sm*tm)/32. - (rm*tm*(-19 + rr9 + ss9 + tt9))/64.,(9*rp*s*sm*tm)/32. -
  (rp*tm*(-19 + rr9 + ss9 + tt9))/64.,(9*rp*s*sp*tm)/32. + (rp*tm*(-19 + rr9 + ss9 +
  tt9))/64.,(9*rm*s*sp*tm)/32. + (rm*tm*(-19 + rr9 + ss9 + tt9))/64.,(9*rm*s*sm*tp)/32.
  - (rm*tp*(-19 + rr9 + ss9 + tt9))/64.,(9*rp*s*sm*tp)/32. - (rp*tp*(-19 + rr9 + ss9 +
  tt9))/64.,(9*rp*s*sp*tp)/32. + (rp*tp*(-19 + rr9 + ss9 + tt9))/64.,(9*rm*s*sp*tp)/32. +
  (rm*tp*(-19 + rr9 + ss9 + tt9))/64.,(-9*r3m*rr*tm)/64.,(-9*r3p*rr*tm)/64.,(-9*rp*s*s3m*tm)/32.
  - (27*rp*ss*tm)/64.,(-9*rp*s*s3p*tm)/32. +
  (27*rp*ss*tm)/64.,(9*r3p*rr*tm)/64.,(9*r3m*rr*tm)/64.,(-9*rm*s*s3p*tm)/32.
  + (27*rm*ss*tm)/64.,(-9*rm*s*s3m*tm)/32. -
  (27*rm*ss*tm)/64.,(-9*r3m*rr*tp)/64.,(-9*r3p*rr*tp)/64.,(-9*rp*s*s3m*tp)/32.
  - (27*rp*ss*tp)/64.,(-9*rp*s*s3p*tp)/32. +
  (27*rp*ss*tp)/64.,(9*r3p*rr*tp)/64.,(9*r3m*rr*tp)/64.,(-9*rm*s*s3p*tp)/32.
  + (27*rm*ss*tp)/64.,(-9*rm*s*s3m*tp)/32. -
  (27*rm*ss*tp)/64.,(-9*rm*t3m*tt)/64.,(-9*rm*t3p*tt)/64.,(-9*rp*t3m*tt)/64.,(-9*rp*t3p*tt)/64.,(9*rp*
  t3m*tt)/64.,(9*rp*t3p*tt)/64.,(9*rm*t3m*tt)/64.,(9*rm*t3p*tt)/64.)
```

```
In[21]:= derivT = AllDerivShapeWrtT /. substitution;
```

```
Print[CForm[derivT]]
```

```
List((9*rm*sm*t*tm)/32. - (rm*sm*(-19 + rr9 + ss9 + tt9))/64.,(9*rp*sm*t*tm)/32.
- (rp*sm*(-19 + rr9 + ss9 + tt9))/64.,(9*rp*sp*t*tm)/32. - (rp*sp*(-19
+ rr9 + ss9 + tt9))/64.,(9*rm*sp*t*tm)/32. - (rm*sp*(-19 + rr9 + ss9 +
tt9))/64.,(9*rm*sm*t*tp)/32. + (rm*sm*(-19 + rr9 + ss9 + tt9))/64.,(9*rp*sm*t*tp)/32.
+ (rp*sm*(-19 + rr9 + ss9 + tt9))/64.,(9*rp*sp*t*tp)/32. + (rp*sp*(-19
+ rr9 + ss9 + tt9))/64.,(9*rm*sp*t*tp)/32. + (rm*sp*(-19 + rr9 + ss9 +
tt9))/64.,(-9*r3m*rr*sm)/64.,(-9*r3p*rr*sm)/64.,(-9*rp*s3m*ss)/64.,(-9*rp*s3p*ss)/64.,(-9*r3p*rr*sp)
/64.,(-9*r3m*rr*sp)/64.,(-9*rm*s3p*ss)/64.,(-9*rm*s3m*ss)/64.,(9*r3m*rr*sm)/64.,(9*r3p*rr*sm)/64.,(9
*rp*s3m*ss)/64.,(9*rp*s3p*ss)/64.,(9*r3p*rr*sp)/64.,(9*r3m*rr*sp)/64.,(9*rm*s3p*ss)/64.,(9*rm*s3m*
ss)/64.,(-9*rm*sm*t*t3m)/32. - (27*rm*sm*tt)/64.,(-9*rm*sm*t*t3p)/32. +
(27*rm*sm*tt)/64.,(-9*rp*sm*t*t3m)/32. - (27*rp*sm*tt)/64.,(-9*rp*sm*t*t3p)/32. +
(27*rp*sm*tt)/64.,(-9*rp*sp*t*t3m)/32. - (27*rp*sp*tt)/64.,(-9*rp*sp*t*t3p)/32. +
(27*rp*sp*tt)/64.,(-9*rm*sp*t*t3m)/32. - (27*rm*sp*tt)/64.,(-9*rm*sp*t*t3p)/32. + (27*rm*sp*tt)/64.)
```