The Effect of the Aging Lens on Color Vision

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The goal of this **colorSpec** vignette is to simulate the effect of age on human color vision. The colored figures are best viewed by an observer with age of 32 years, and on a display calibrated for sRGB.

The Human Lens

It is well known that the lens in the human eye does not transmit all wavelengths equally; the transmission at short wavelengths is less, which means the lens is yellowish. In the UV there is very little transmission; which is a good thing since the lens protects the retina from UV damage. It is also well known that the lens gets yellower with age. When making these colored images it is appropriate to use the CIE 1931 color matching functions (CMFs). Unfortunately I could not find the average age of the observers used to establish the 1931 standard observer (there were 17 of them). But it is known that the average age of the observers used to create the CIE 1964 standard observer is 32 years, see [Pok87]. So we'll take 32 years for the CIE 1931 standard observer as well. Featured functions in this vignette are: linearize(), lensAbsorbance(), extradata(), applyspec(), and calibrate().

Start the R session and load the colorSpec package,

```
library( colorSpec )
library( spacesXYZ )  # for function standardXYZ()
library( spacesRGB )  # for functions RGBfromXYZ() and plotPatchesRGB()
```

Compute and plot lens transmittance at 32 and 64 years using the model in [Pok87].

```
lens.trans = linearize( lensAbsorbance( c(32,64), wave=380:780 ) )
par( omi=c(0,0,0,0), mai=c(0.6,0.7,0.3,0.2) )
plot( lens.trans, color='black', lty=1:2, main=FALSE, legend='topleft' )
```

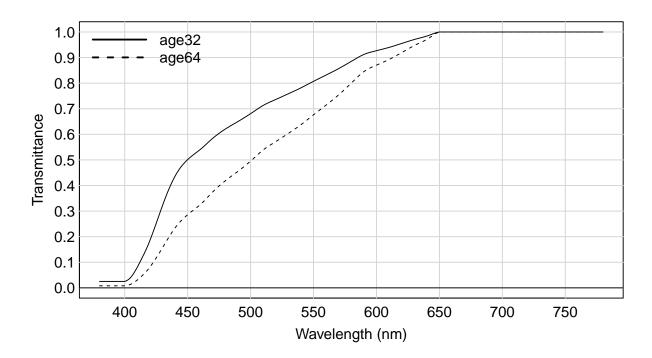


Figure 1: Human Lens Transmittance at age=32 and age=64

To compare the color appearance at age 64 to that at age 32, we need the transmittance at age 64 relative to that at age 32. We know that object lens.trans is a matrix, so use the standard R matrix subset operation to extract each spectrum. Then perform the division and plot the ratio.

```
lens.64 = lens.trans[ ,2] / lens.trans[ ,1]
lens.64 = colorSpec( lens.64, wavelength(lens.trans), 'transmittance' )
specnames(lens.64) = "trans.64 / trans.32"
par( omi=c(0,0,0,0), mai=c(0.6,0.7,0.3,0.2) )
plot( lens.64, main=TRUE, legend=FALSE, ylab='Relative Transmittance', col='black' )
```

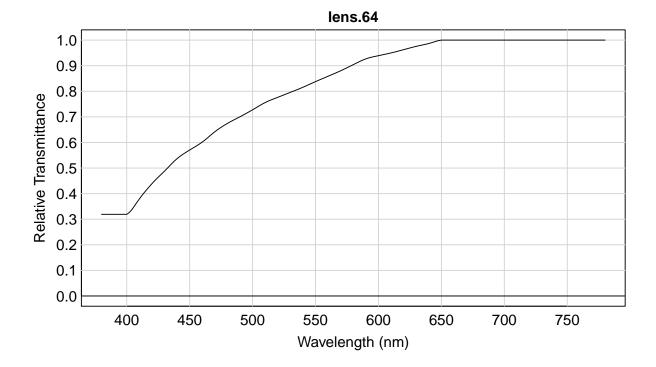


Figure 2: Human Lens Transmittance at age 64 relative to age 32

Think of this curve as defining a pair of glasses with a yellowish tint. In this vignette, going from an age of 32 years to 64 years is equivalent to putting on these tinted glasses.

The Macbeth ColorChecker with Observer Age 32

We first read the spectra of the *ColorChecker* target. This data has been kindly provided in CGATS format by [Pas]. *ColorChecker* is a Registered Trademark of X-Rite, and X-Rite is a Trademark.

```
path = system.file( 'extdata/targets/CC_Avg30_spectrum_CGATS.txt', package='colorSpec')
MacbethCC = readSpectra( path, wave=wavelength(lens.64) )
MacbethCC = MacbethCC[ order(MacbethCC$SAMPLE_ID), ]
print( extradata(MacbethCC), row.names=F )
SAMPLE_ID
             SAMPLE_NAME
                                 Munsell
                                                   ISCC-NBS_Name LEFT TOP
                                                                           WIDTH HEIGHT
                             3YR 3.7/3.2
                                                                    7
                                                                         9
                                                                              29
         1
               dark skin
                                                  moderate brown
                                                                                     29
         2
              light skin 2.2YR 6.47/4.1
                                            light reddish brown
                                                                    40
                                                                         9
                                                                              29
                                                                                     29
         3
                blue sky 4.3PB 4.95/5.5
                                                   moderate blue
                                                                    73
                                                                         9
                                                                              29
                                                                                     29
         4
                 foliage 6.7GY 4.2/4.1
                                           moderate olive green
                                                                  106
                                                                         9
                                                                              29
                                                                                     29
                                                                  139
         5
                                                                         9
                                                                              29
                                                                                     29
             blue flower 9.7PB 5.47/6.7
                                                    light violet
            bluish green
         6
                               2.5BG 7/6
                                             light bluish green
                                                                  172
                                                                         9
                                                                              29
                                                                                     29
         7
                                                                    7
                                                                       42
                                                                              29
                                                                                     29
                  orange
                                5YR 6/11
                                                   strong orange
         8
           purplish blue
                            7.5PB 4/10.7
                                            strong purplish blue
                                                                   40
                                                                       42
                                                                              29
                                                                                     29
                                                                       42
         9
            moderate red
                               2.5R 5/10
                                                    moderate red
                                                                   73
                                                                              29
                                                                                     29
        10
                  purple
                                  5P 3/7
                                                     deep purple
                                                                  106
                                                                       42
                                                                              29
                                                                                     29
                             5GY 7.1/9.1
        11
            yellow green
                                             strong yellow green
                                                                  139
                                                                        42
                                                                              29
                                                                                     29
        12 orange yellow
                             10YR 7/10.5
                                            strong orange yellow
                                                                  172
                                                                       42
                                                                              29
                                                                                     29
        13
                    Blue 7.5PB 2.9/12.7
                                             vivid purplish blue
                                                                    7
                                                                       75
                                                                              29
                                                                                     29
        14
                   Green 0.25G 5.4/8.65 strong yellowish green
                                                                   40
                                                                       75
                                                                              29
                                                                                     29
        15
                                                                       75
                                                                              29
                                                                                     29
                                 5R 4/12
                                                      strong red
                                                                   73
```

```
5Y 8/11.1 vivid yellow 106 75
                                                           29
16
       Yellow
       Magenta
17
                2.5RP 5/12 strong reddish purple 139 75
                                                           29
        Cyan 5B 5/8 strong greenish blue 172 75
                                                     29
18
                                                           29
                                      white 7 108
19
       white
                   N9.5/
                                                           29
                                  light gray 40 108
20
    neutral 8
                                                           29
                     N8/
                                                     29
                         light medium gray 73 108 29
21 neutral 6.5
                   N6.5/
                                                           29
22 neutral 5
                    N5/
                               medium gray 106 108 29
                                                           29
23 neutral 3.5
                   N3.5/
                                  dark gray 139 108 29
                                                           29
24
        black
                     N2/
                                       black 172 108
                                                     29
                                                           29
```

Note that MacbethCC is organized as 'df.row' and contains extra data for each spectrum, notably the coordinates of the patch rectangle.

Now build the "material responder" from Illuminant D65 and the 1931 CMFs:

```
D65.eye = product( D65.1nm, "artwork", xyz1931.1nm, wave=wavelength(lens.64) )

# calibrate so the perfect-reflecting-diffuser is the 'official XYZ'

# scale XYZ independently

prd = neutralMaterial( 1, wavelength(lens.64) )

D65.eye = calibrate( D65.eye, stimulus=prd, response=standardXYZ('D65'), method='scaling' )
```

Calculate XYZ and then RGB:

```
XYZ = product( MacbethCC, D65.eye, wave=wavelength(lens.64) )
RGB = RGBfromXYZ( XYZ, space='sRGB', which='scene' )$RGB # this is *signal* sRGB
# add the rectangle data to RGB, so they can be plotted in proper places
patches = extradata(MacbethCC)
patches$RGB = RGB
patches.first = patches # save this reference object for later
# display in proper location, and use the sRGB display transfer function
par( omi=c(0,0,0,0), mai=c(0.2,0.2,0.2,0.2) )
plotPatchesRGB( patches, space='sRGB', which='signal', back='gray20', labels=FALSE )
```

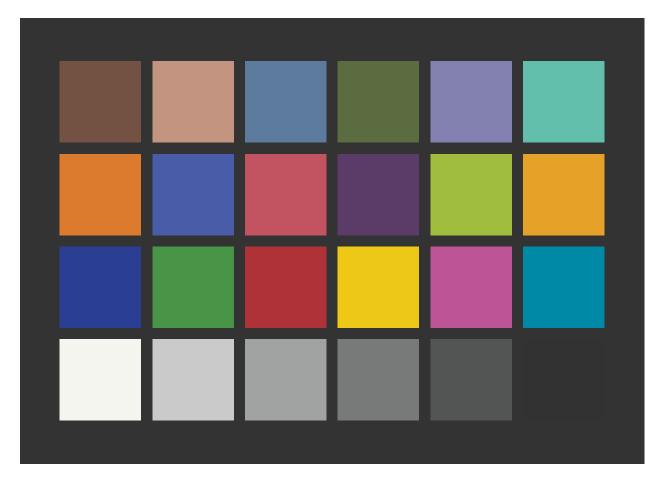


Figure 3: Rendering with Illuminant D65 and xyz1931.1nm, at age=32

This figure has the colors as perceived by the 1931 standard observer.

The Macbeth ColorChecker with Observer Age 64

Make new responder by inserting the hypothetical pair of tinted glasses (defined by lens.64 in Figure 2) between target and the eye, and then recalculate RGBs.

```
D65.eye.64 = applyspec( D65.eye, function(y) {lens.64 * y} )
XYZ = product( MacbethCC, D65.eye.64, wave=wavelength(lens.64) )
patches = extradata(MacbethCC)
patches$RGB = RGBfromXYZ( XYZ, space='sRGB', which='scene' )$RGB # this is *signal* sRGB
par( omi=c(0,0,0,0), mai=c(0.2,0.2,0.2,0.2) )
plotPatchesRGB( patches, space='sRGB', which='signal', back='gray20', labels=FALSE )
```



Figure 4: Rendering with Illuminant D65 and xyz1931.1nm, at age=64 without adaptation

As expected, the result has a yellow tint. Now make a plot that compares the effective responsivities.

```
# the effective responsivities for age=32
par( omi=c(0,0,0,0), mai=c(0.6,0.7,0.3,0.2) )
specnames( D65.eye ) = sprintf( "%s.32", c('x','y','z') )
plot( D65.eye, lty=1, legend='top' )
# the effective responsivities for age=64
specnames( D65.eye.64 ) = sprintf( "%s.64", c('x','y','z') )
plot( D65.eye.64, lty=2, add=TRUE, legend='topright' )
```

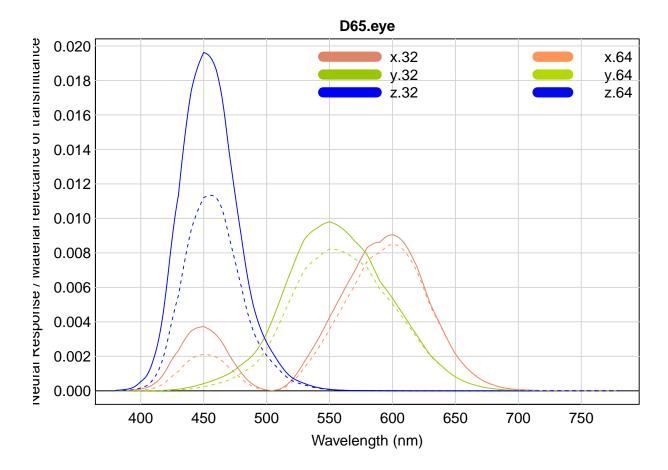


Figure 5: comparison of effective responsivities, at age=32 and age=64

But these figures are only appropriate for the instant in time that the change was made, and before the eye and brain have had the time to adapt. In electronic camera terms, there is no "white balance" yet.

So now calibrate and adapt to D65 using the *Bradford Method*. This method is regarded as being a good model for the way that the human eye and brain achieve *color constancy*, see [Lin].

```
prd = neutralMaterial( 1, wavelength(lens.64) )

XYZ.D65 = spacesXYZ::standardXYZ('D65')

D65.eye.64 = calibrate( D65.eye.64, stimulus=prd, response=XYZ.D65, method='Bradford' )

XYZ = product( MacbethCC, D65.eye.64, wave=wavelength(lens.64) )

patches = extradata(MacbethCC)

patches$RGB = RGBfromXYZ( XYZ, space='sRGB' )$RGB  # this is *signal* sRGB

par( omi=c(0,0,0,0), mai=c(0.2,0.2,0.2,0.2) )

plotPatchesRGB( patches, space='sRGB', which='signal', back='gray20', labels=FALSE )
```

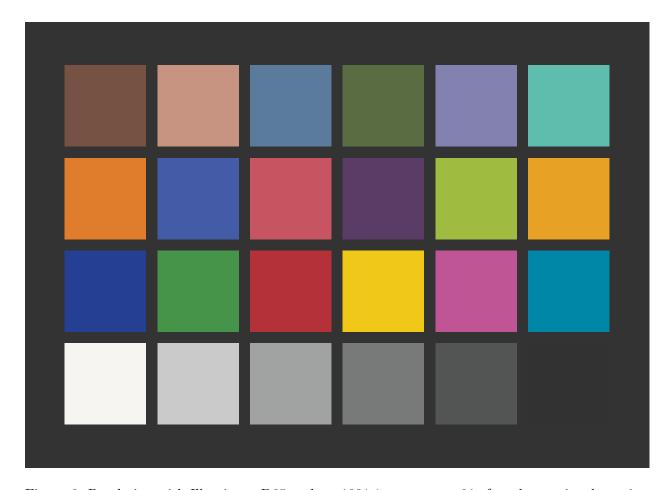


Figure 6: Rendering with Illuminant D65 and xyz1931.1nm, at age=64 after chromatic adaptation

The tint is now gone. But it hard to compare colors in this figure with the ones way back in Figure 3. So combine the original age=32 rendering with the age=64 rendering by splitting each square into 2 triangles.

```
par( omi=c(0,0,0,0), mai=c(0.2,0.2,0.2,0.2) )
# draw full squares from Figure 3
plotPatchesRGB( patches.first, space='sRGB', back='gray20', labels=F )
# overwrite the squares with triangles by setting shape= and add=
plotPatchesRGB( patches, space='sRGB', labels=F, shape='bottomright', add=T )
```

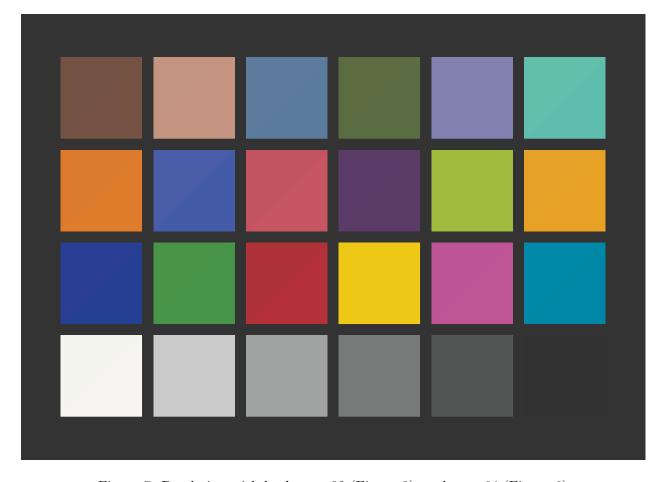


Figure 7: Rendering with both age=32 (Figure 3), and age=64 (Figure 6)

The top-left triangle has the color from Figure 3 and the bottom-right triangle has the color from Figure 6. There are minor differences in the **Red** and **Magenta** patches, and some smaller differences in a few others.

Here are the responsivity functions *after* adaptation:

```
par( omi=c(0,0,0,0), mai=c(0.6,0.7,0.3,0.2) )
plot( D65.eye, lty=1, legend='top', main=FALSE )
plot( D65.eye.64, lty=2, add=TRUE, legend='topright' )
```

REFERENCES REFERENCES

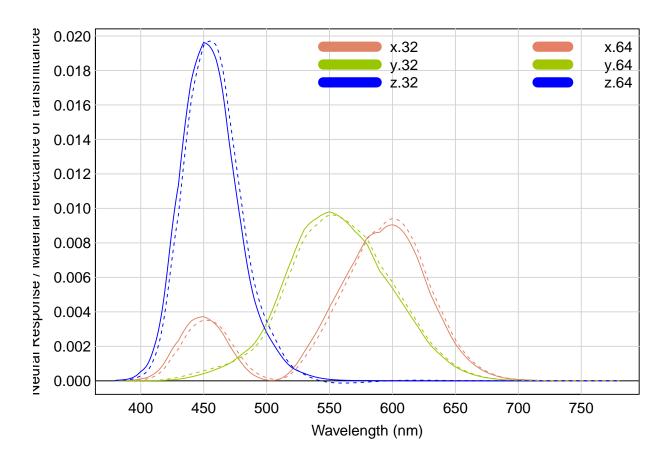


Figure 8: comparison of effective responsivities

So despite the fairly radical yellowing of the lens with age (in Figure 2), this adaptation model shows that the perceived colors are not all that different. Great!

References

- [Lin] Lindbloom, Bruce. How the Chromatic Adaptation Calculator Works. http://brucelindbloom.com/index.html?ChromAdaptCalcHelp.html.
- [Pas] Pascale, Danny. The ColorChecker, page 2. http://www.babelcolor.com/colorchecker-2.htm.
- [Pok87] Pokorny, Joel, Vivianne C. Smith, and Margaret Lutze. Aging of the Human Lens. *Applied Optics*, Vol. 26, No. 8, 15 April 1987. Table I. Page 1439.

Appendix

This document was prepared December 7, 2019 with the following configuration:

- R Under development (unstable) (2019-12-03 r77513), i386-w64-mingw32
- Running under: Windows 7 (build 7601) Service Pack 1
- Matrix products: default

REFERENCES

- Base packages: base, datasets, grDevices, graphics, methods, stats, utils
- Other packages: colorSpec 1.1-1, knitr 1.26, spacesRGB 1.2-2, spacesXYZ 1.0-4

• Loaded via a namespace (and not attached): MASS 7.3-51.4, Rcpp 1.0.3, compiler 4.0.0, digest 0.6.22, evaluate 0.14, highr 0.8, htmltools 0.4.0, magrittr 1.5, microbenchmark 1.4-7, rlang 0.4.1, rmarkdown 1.18, rootSolve 1.8.1, stringi 1.4.3, stringr 1.4.0, tools 4.0.0, xfun 0.11, yaml 2.2.0