

$$(\frac{l \sin (\theta(t))}{2}-l \cos (\beta(t))) \hat{\mathbf{i}}_{\mathbf{S y s}}+(-l \sin (\beta(t))-\frac{l \cos (\theta(t))}{2}) \hat{\mathbf{j}}_{\mathbf{S y s}} \quad (1)$$

$$(\frac{l \sin (\phi(t))}{2}+l \cos (\beta(t))) \hat{\mathbf{i}}_{\mathbf{S y s}}+(l \sin (\beta(t))-\frac{l \cos (\phi(t))}{2}) \hat{\mathbf{j}}_{\mathbf{S y s}} \quad (2)$$

$$(l \sin (\beta(t)) \frac{d}{d t} \beta(t)+\frac{l \cos (\theta(t)) \frac{d}{d t} \theta(t)}{2}) \hat{\mathbf{i}}_{\mathbf{S y s}}+(\frac{l \sin (\theta(t)) \frac{d}{d t} \theta(t)}{2}-l \cos (\beta(t)) \frac{d}{d t} \beta(t)) \hat{\mathbf{j}}_{\mathbf{S y s}} \quad (3)$$

$$(-l \sin (\beta(t)) \frac{d}{d t} \beta(t)+\frac{l \cos (\phi(t)) \frac{d}{d t} \phi(t)}{2}) \hat{\mathbf{i}}_{\mathbf{S y s}}+(\frac{l \sin (\phi(t)) \frac{d}{d t} \phi(t)}{2}+l \cos (\beta(t)) \frac{d}{d t} \beta(t)) \hat{\mathbf{j}}_{\mathbf{S y s}} \quad (4)$$

$$\frac{l\left(\hat{\mathbf{i}}_{\mathbf{S y s}}\left(2 \sin (\beta(t)) \frac{d^2}{d t^2} \beta(t)-\sin (\theta(t))\left(\frac{d}{d t} \theta(t)\right)^2+2 \cos (\beta(t))\left(\frac{d}{d t} \beta(t)\right)^2+\cos (\theta(t)) \frac{d^2}{d t^2} \theta(t)\right)+\hat{\mathbf{j}}_{\mathbf{S y s}}\left(2 \sin (\beta(t))\left(\frac{d}{d t} \beta(t)\right)^2+\sin (\theta(t)) \frac{d^2}{d t^2} \theta(t)-2 \cos (\beta(t)) \frac{d^2}{d t^2} \beta(t)+\cos (\theta(t))\left(\frac{d}{d t} \theta(t)\right)^2\right)\right)}{2} \quad (5)$$

$$\frac{l\left(\hat{\mathbf{i}}_{\mathbf{S y s}}\left(-2 \sin (\beta(t)) \frac{d^2}{d t^2} \beta(t)-\sin (\phi(t))\left(\frac{d}{d t} \phi(t)\right)^2-2 \cos (\beta(t))\left(\frac{d}{d t} \beta(t)\right)^2+\cos (\phi(t)) \frac{d^2}{d t^2} \phi(t)\right)+\hat{\mathbf{j}}_{\mathbf{S y s}}\left(-2 \sin (\beta(t))\left(\frac{d}{d t} \beta(t)\right)^2+\sin (\phi(t)) \frac{d^2}{d t^2} \phi(t)+2 \cos (\beta(t)) \frac{d^2}{d t^2} \beta(t)+\cos (\phi(t))\left(\frac{d}{d t} \phi(t)\right)^2\right)\right)}{2} \quad (6)$$

$$\left(-\frac{g l m_1 \sin (\theta(t))}{2}\right) \hat{\mathbf{k}}_{\mathbf{S y s}}=\left(\frac{l^2 m_1 \frac{d^2}{d t^2} \theta(t)}{12}\right) \hat{\mathbf{k}}_{\mathbf{S y s}} \quad (7)$$

$$\hat{\mathbf{0}} \quad (8)$$

$$\left(\frac{l \sin (\theta(t))}{2}\right) \hat{\mathbf{i}}_{\mathbf{S y s}}+\left(-\frac{l \cos (\theta(t))}{2}\right) \hat{\mathbf{j}}_{\mathbf{S y s}} \quad (9)$$

$$\frac{l m_1\left(\hat{\mathbf{i}}_{\mathbf{S y s}}\left(2 \sin (\beta(t)) \frac{d^2}{d t^2} \beta(t)-\sin (\theta(t))\left(\frac{d}{d t} \theta(t)\right)^2+2 \cos (\beta(t))\left(\frac{d}{d t} \beta(t)\right)^2+\cos (\theta(t)) \frac{d^2}{d t^2} \theta(t)\right)+\hat{\mathbf{j}}_{\mathbf{S y s}}\left(2 \sin (\beta(t))\left(\frac{d}{d t} \beta(t)\right)^2+\sin (\theta(t)) \frac{d^2}{d t^2} \theta(t)-2 \cos (\beta(t)) \frac{d^2}{d t^2} \beta(t)+\cos (\theta(t))\left(\frac{d}{d t} \theta(t)\right)^2\right)\right)}{2} \quad (10)$$

$$\frac{\left(\sin (\beta(t))\left(\frac{d}{d t} \beta(t)\right)^2+\frac{\sin (\theta(t)) \frac{d^2}{d t^2} \theta(t)}{2}+\cos (\beta(t)) \frac{d}{d t}-\beta(t)+\cos (\theta(t))\left(\frac{d}{d t} \theta(t)\right)^2\right) \sin (\theta(t))}{2}+\frac{\left(\sin (\beta(t)) \frac{d^2}{d t^2} \beta(t)+\frac{\sin (\theta(t))\left(\frac{d}{d t} \theta(t)\right)^2}{2}+\cos (\beta(t))\left(\frac{d}{d t} \beta(t)\right)^2+\frac{\cos (\theta(t)) \frac{d^2}{d t^2} \theta(t)}{2}\right) \cos (\theta(t))}{2}=51 \quad (11)$$