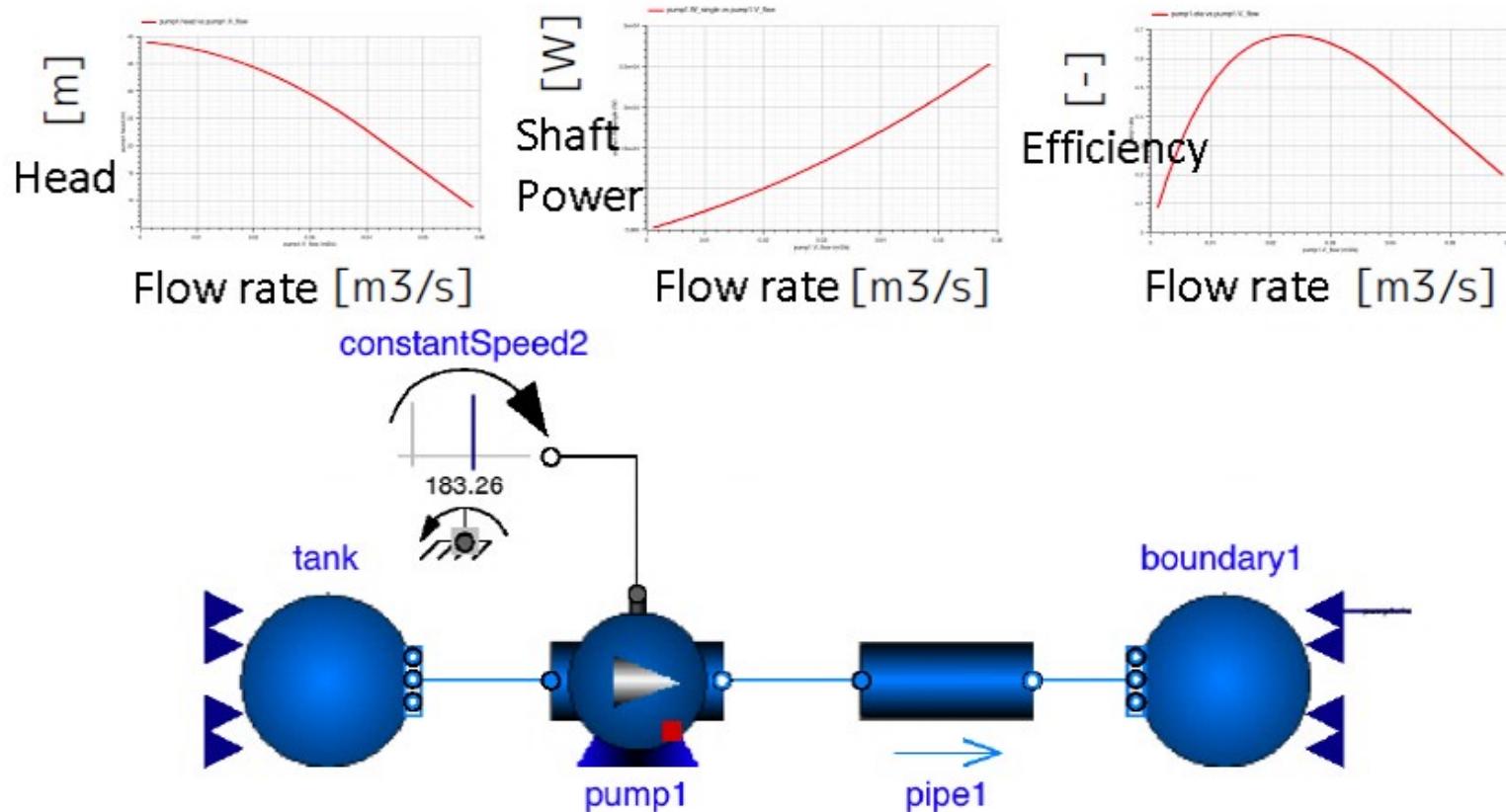


Modelica.Fluid.Machines

About the centrifugal pump model



2019/05/25 11th Modelica Library Study Meeting
finback

This document introduces a study of the centrifugal pump model included in Modelica.Fluid.Machines of the Modelica Standard Library, based on information obtained from source code and other sources. This pump model models the operation of the pump using head characteristics and power characteristics or efficiency characteristics obtained from pump manufacturers' data sheets and experiments.

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Basic knowledge of centrifugal pump

- Centrifugal Pump state variables
- Performance curve of centrifugal pump (characteristics at standard rotation speed)
- Performance conversion formula of centrifugal pump (characteristics when rotating speed is changed)
- Parallel connection of centrifugal pumps
- Effective suction head

(Centrifugal pump) State variables

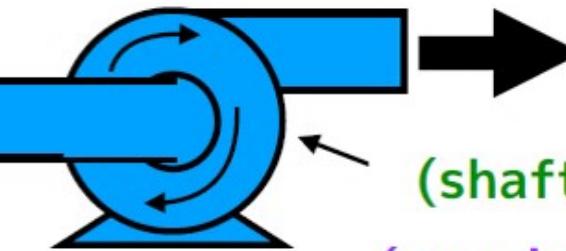
(mass flow rate)

$m_{flow\ single}$ [kg/s]



(suction pressure)

$port_a.p(start = p_{a_start})$ [Pa]



(discharge pressure)

$port_b.p(start = p_{b_start})$ [Pa]

(shaft torque) τ [Nm]

(angular velocity) ω [rad/s]

(volumetric flow rate)

$$V_{flow\ single} = \frac{m_{flow\ single}}{\rho} \quad [\text{m}^3/\text{s}]$$

(rotational speed)

$$N = \frac{60}{2\pi} \omega \quad [\text{rpm}]$$

(head)

$$head = \frac{dp_{pump}}{\rho g} \quad [\text{m}]$$

(pressure increase)

$$dp_{pump} = port_b.p - port_a.p \quad [\text{Pa}]$$

(power consumption),(shaft power)

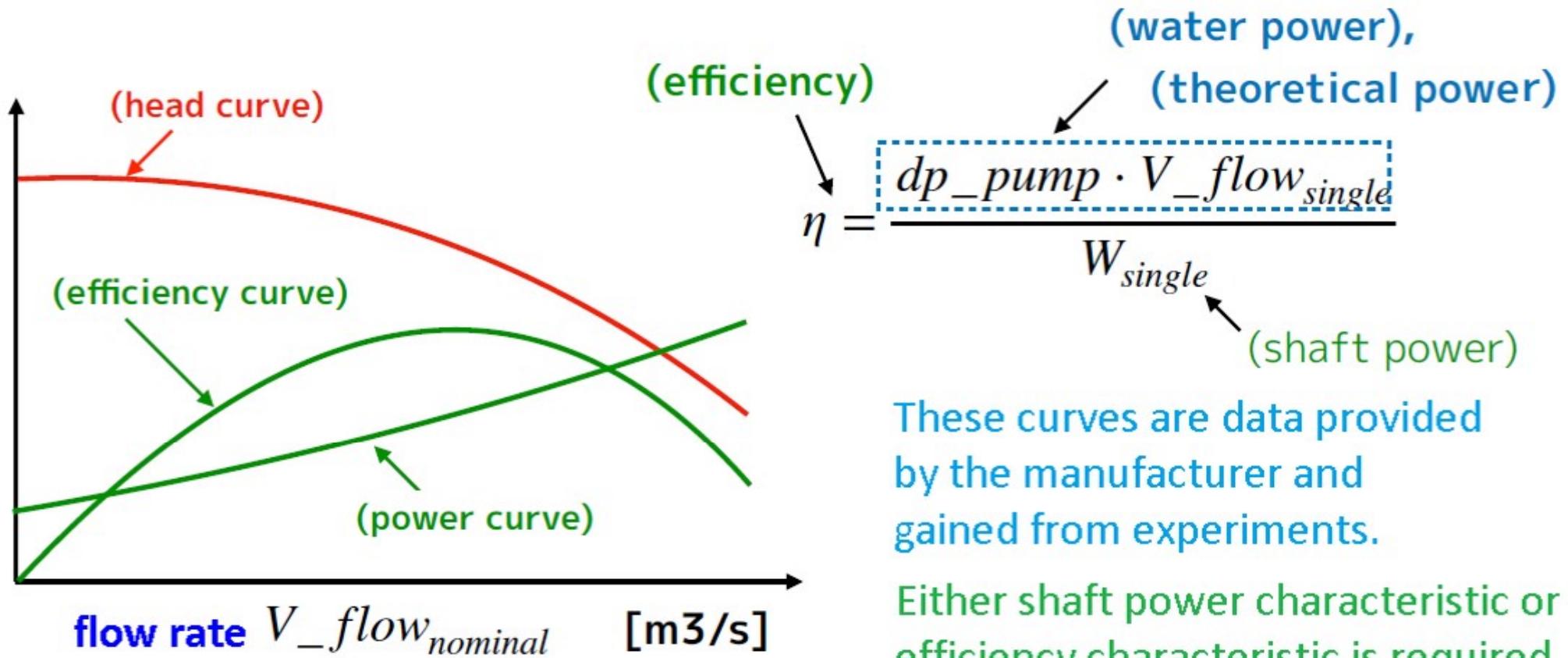
$$W_{single} = \omega \tau \quad [\text{W}]$$

$\rho = \text{medium}.d$ [kg/m³] (density)

g [m/s²]: (acceleration of gravity)

Performance curve of centrifugal pump (characteristics at standard rotation speed)

Reference speed $N = N_{nominal}$ of pumps in Japan



Head characteristics **(head curve)**

$$head_{nominal} = \text{flowCharacteristic}(V_{flow_{nominal}}) \quad [\text{m}]$$

Shaft power characteristics **(power curve)**

$$W_{nominal} = \text{powerCharacteristic}(V_{flow_{nominal}}) \quad [\text{W}]$$

Efficiency characteristics **(efficiency curve)**

$$\eta_{nominal} = \text{efficiencyCharacteristic}(V_{flow_{nominal}})$$

Performance conversion formula for centrifugal pumps (characteristics when rotating speed is changed)

volumetric flow rate

$$V_{flow\ single} = \left(\frac{N}{N_{nominal}} \right) V_{flow\ nominal}$$

Speed ratio

$$\left(\frac{N}{N_{nominal}} \right)$$

(head)

$$head = \left(\frac{N}{N_{nominal}} \right)^2 head_{nominal}$$

(power consumption), (shaft power)

$$W_{single} = \left(\frac{N}{N_{nominal}} \right)^3 \frac{\rho}{\rho_{nominal}} W_{nominal}$$

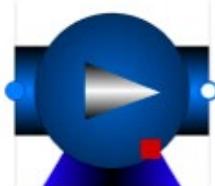
The above equation is obtained on the assumption that the efficiency η does not change even when the rotational speed changes.

$$\eta = \eta_{nominal}$$

$$\Leftrightarrow \frac{\rho \cdot g \cdot head \cdot V_{flow\ single}}{W_{single}} = \frac{\rho_{nominal} \cdot g \cdot head_{nominal} \cdot V_{flow\ nominal}}{W_{nominal}}$$

$$\Leftrightarrow W_{single} = \frac{\rho}{\rho_{nominal}} \frac{head \cdot V_{flow\ single}}{head_{nominal} \cdot V_{flow\ nominal}} W_{nominal} = \frac{\rho}{\rho_{nominal}} \left(\frac{N}{N_{nominal}} \right)^3 W_{nominal}$$

Parallel connection of centrifugal pumps



$n_{Parallel}$ Pumps are connected in parallel.

(suction pressure)

port_a.p



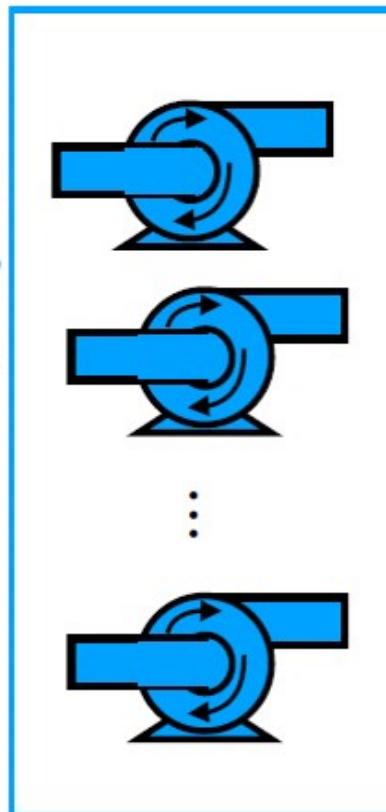
(mass flow rate)

$$m_{flow} = \text{port_a}.m_{flow}$$

(start = m_{flow}_{start}) [kg/s]

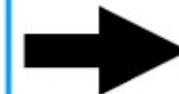
(volumetric flow rate)

$$V_{flow} = \frac{m_{flow}}{\rho} \quad [\text{m}^3/\text{s}]$$



(discharge pressure)

port_b.p



One pump

$$m_{flow_{single}} = \frac{m_{flow}}{n_{Parallel}}$$

$$V_{flow_{single}} = \frac{V_{flow}}{n_{Parallel}}$$

$$W_{single}$$

(power consumption), (shaft power)

$$W_{total} = W_{single} \cdot n_{Parallel} \quad [\text{W}]$$

Method of calculating the net positive suction head (available net positive suction head)

Indicator to determine whether cavitation occurs

Calculation formula of this model

$$\text{NPSPa} = \frac{\text{Inlet static pressure}}{\text{Inlet saturation vapor pressure}} - 1$$

$$\text{NPDPa} = \frac{\text{Discharge port static pressure}}{\text{Outlet saturation vapor pressure}} - 1$$

$$\text{NPSHa} = \text{NPSPa} / (\text{Suction port density} \times \text{Gravity})$$

Wikipedia

<https://ja.wikipedia.org/wiki/%E6%9C%89%E5%8A%B9%E5%90%B8%E8%BE%BC%E3%81%BF%E3%83%98%E3%83%83%E3%83%89>

Effective suction head

It is a physical quantity indicating the difference between the pressure of the liquid in the pipe and the vapor pressure of the liquid at that temperature in an arbitrary cross section of the liquid pipe such as water or oil pressure.

p_0 Water pressure

p_v Base pressure at liquid temperature T1

ρ Fluid density

Δz Height difference between water surface and position 1

h_L Head loss

$$NPSH_A = \frac{p_0 - p_v}{\rho g} + \Delta z - h_L$$

available net positive suction head

Available effective suction head obtained by subtracting the recommended pressure head of liquid from all heads of pump suction

$$(NPSH)_{AVA} = \left(\frac{p_s}{\rho_s} + \frac{u_s^2}{2} - \frac{p_v}{\rho_s} \right) \cdot g^{-1}$$

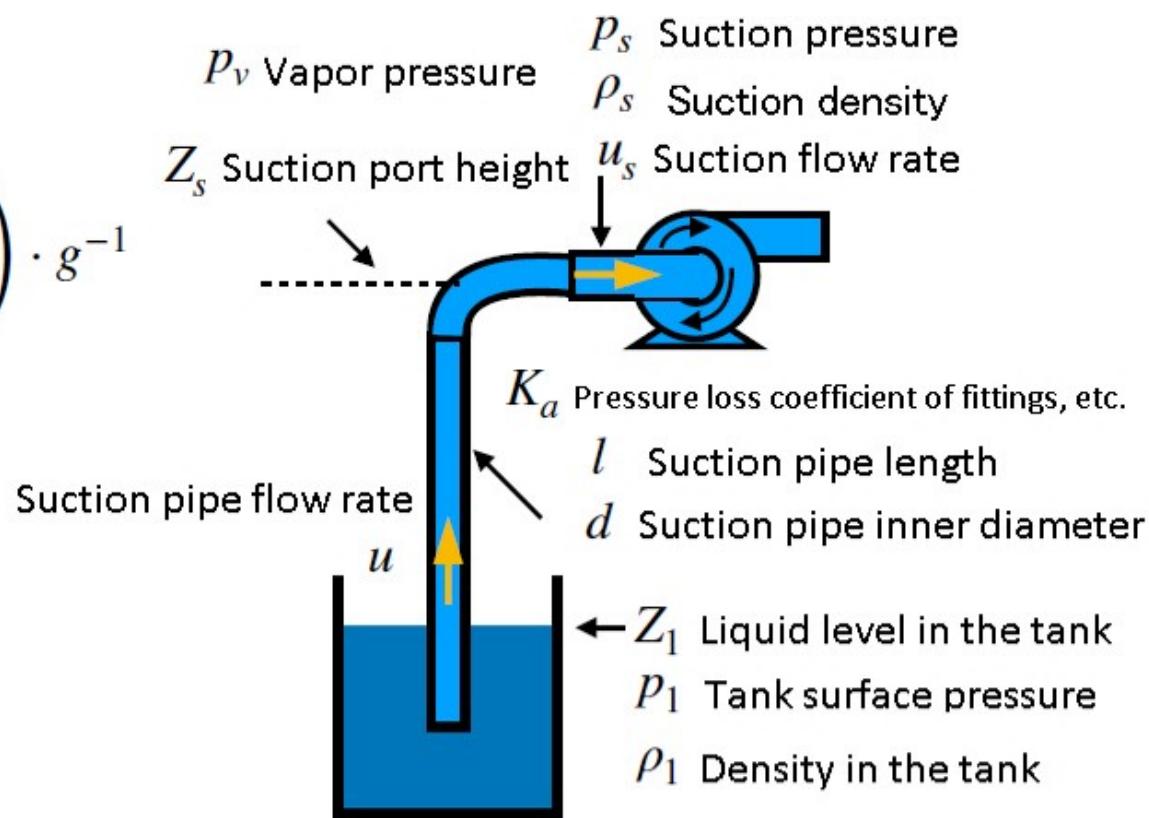
$$= (Z_1 - Z_s) + \left(\frac{p_1}{\rho_1} - \sum F - \frac{p_v}{\rho_s} \right) \cdot g^{-1}$$

Energy conservation equation

$$g \cdot Z_1 + \frac{p_1}{\rho_1} = g \cdot Z_s + \frac{p_s}{\rho_s} + \frac{u_s^2}{2} + \sum F$$

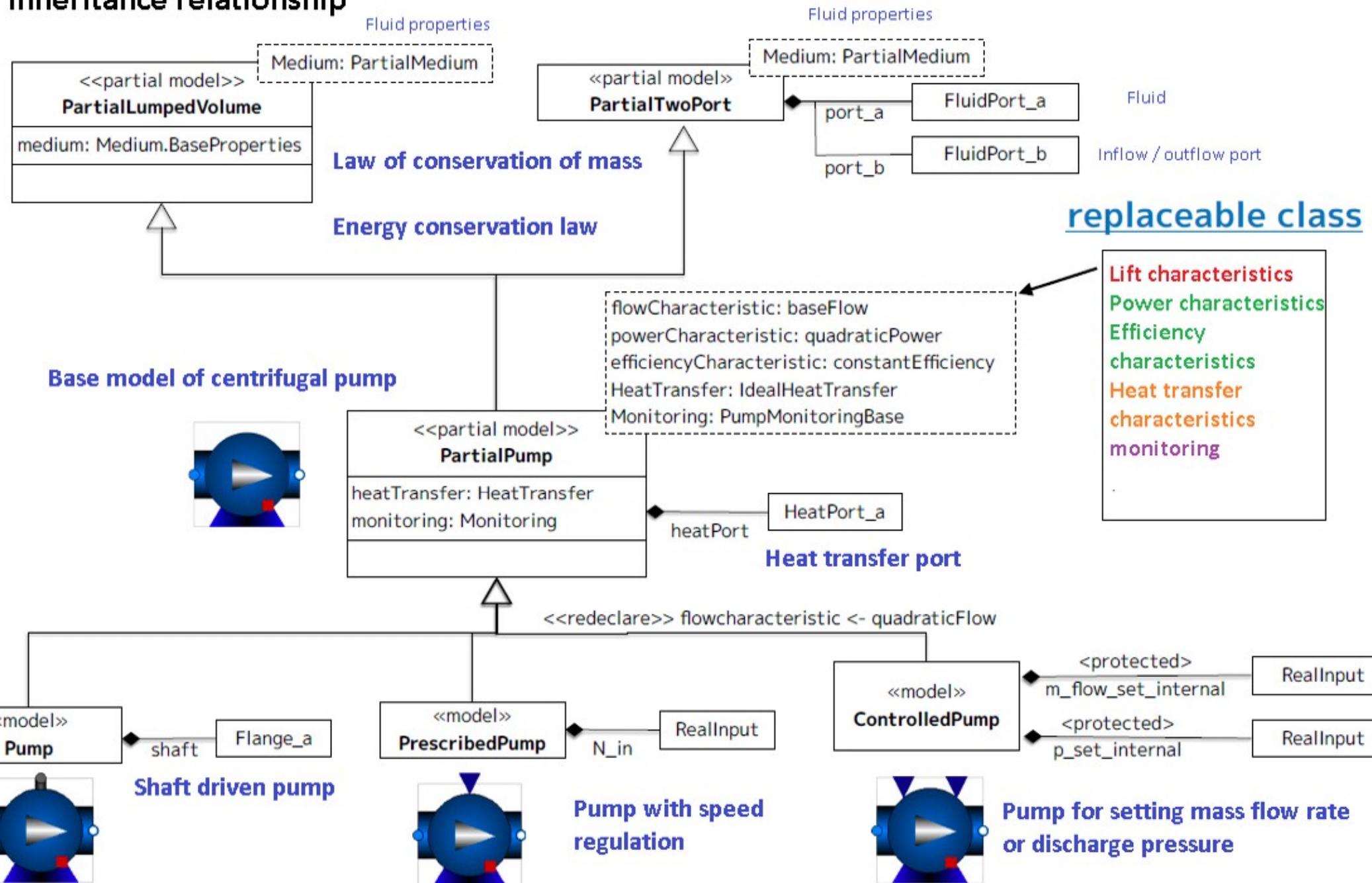
Energy lost due to friction, etc.

$$\sum F = \left(4f \cdot \frac{l}{d} + \sum K_a \right) \cdot \frac{u^2}{2}$$



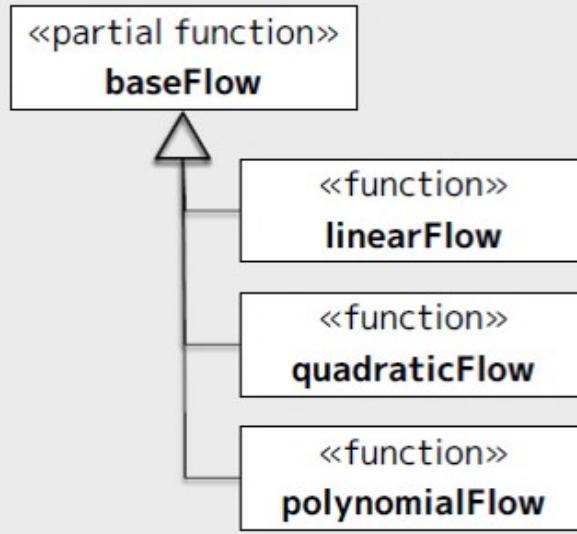
- In the above formula, consider the path from the liquid level to the suction port
- There is a slightly different definition in either use the static pressure or use the total pressure of the suction port in the evaluation

Inheritance relationship



replaceable class (1)

(head curve) Lift characteristics



Head is linear with flow

$$\text{head}_{\text{nominal}} = c_1 + V_{\text{flow}}_{\text{nominal}} \cdot c_2$$

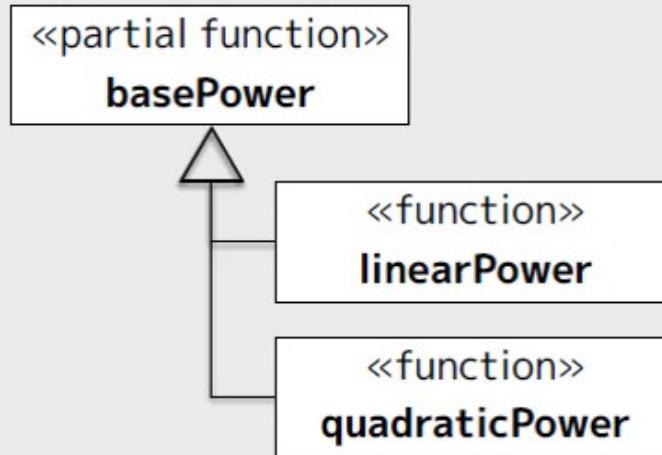
Second-order polynomial of the lift flow rate

$$\text{head}_{\text{nominal}} = c_1 + V_{\text{flow}}_{\text{nominal}} \cdot c_2 + V_{\text{flow}}_{\text{nominal}}^2 \cdot c_3$$

The head is the order polynomial of the flow rate

$$\text{head} = \sum_{i=1}^{n+1} V_{\text{flow}}^{i-1} \cdot c_i$$

(power curve) Shaft power characteristics



Shaft power is linear with flow

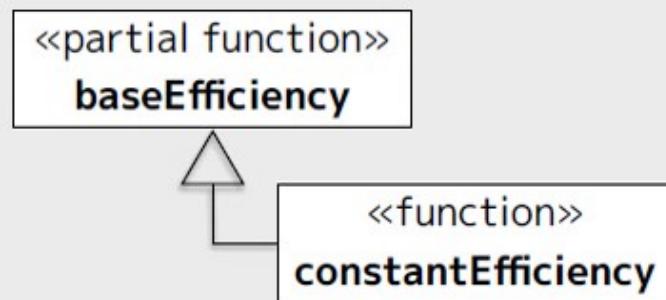
$$W_{\text{nominal}} = c_1 + V_{\text{flow}}_{\text{nominal}} \cdot c_2$$

Shaft power is 2nd order polynomial of flow rate

$$W_{\text{nominal}} = c_1 + V_{\text{flow}}_{\text{nominal}} \cdot c_2 + V_{\text{flow}}_{\text{nominal}}^2 \cdot c_3$$

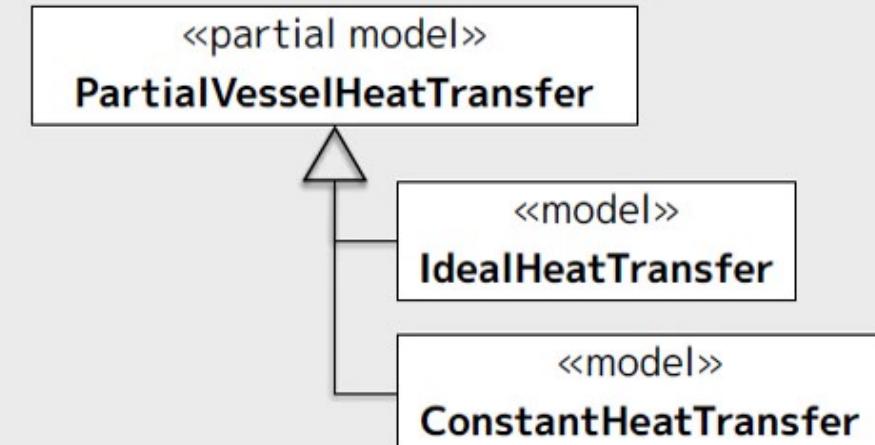
replaceable class (2)

Efficiency characteristics (efficiency curve)

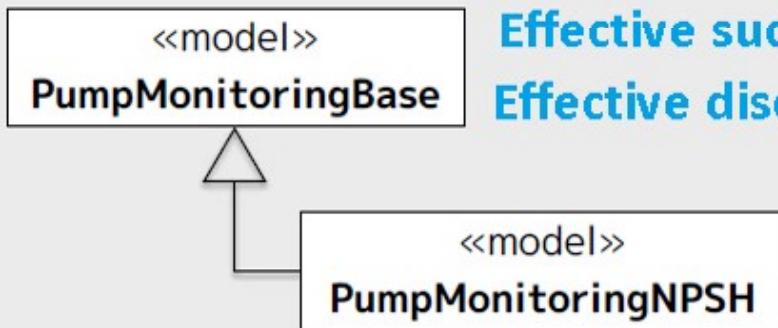


Default $\eta = 0.8$
Efficiency is constant $\eta = \eta_{nominal}$

Heat transfer characteristics (heat transfer)



Pump monitoring



Effective suction lift

Effective suction pressure
Effective discharge pressure

$NPSHa$
 $NPSPa$
 $NPDPa$

NPSPa

Difference between inlet static pressure at inlet and saturated vapor pressure

NPDPa

Difference between static pressure at outlet and outlet saturated vapor pressure

$$NPSHa = \frac{NPSPa}{\rho_{in} \cdot g}$$

assertPositiveDifference(p, p_sat) Algorithm

```

algorithm
  dp := p - p_sat;
  assert(p >= p_sat, message);
end assertPositiveDifference;
  
```

Difference between static pressure and vapor pressure

PartialPump (Base model of centrifugal pump)

- (parameters)
- (homotopy transformation)
- actual models
- simplified models
- (mass balances)
- (energy balance)

(parameters)

| Parameters | unit | unit definition | default |
|-------------------------|--------|---|----------------|
| N_nominal | rpm | Reference speed | |
| rho_nominal | kg/m3 | Reference density | Medium default |
| V | m3 | Pump volume | 0 [m3] |
| nParallels | table? | Number of parallel pumps | 1 [table?] |
| chekcValve | | true: Use check valve function | false |
| use_PowerCharacteristic | | true:Using shaft power characteristics false: Use efficiency characteristics | false |
| use_HeatTransfer | | true: Consider heat transfer | false |
| show_NPSHa | | true: NPSHa Output (obsolete) | false |

(initial values)

$$p_a_{start} = system.p_{start}$$

Suction pressure

$$p_b_{start} = p_a_{start}$$

Discharge pressure

$$m_flow_{start} = system.m_flow_{start}$$

Mass flow

$$V_flow_{single_init} = \frac{m_flow_{start}}{\rho_{nominal} \cdot n_{Parallel}}$$

Homotopy
transformation simplified
It is used in the model

$$\delta_{head_init} = flowCharacteristic(V_flow_{single_init}) - flowCharacteristic(0)$$

(homotopy transformation)

When solving a system of nonlinear equations by iterative calculation at the initialization stage of a simulation, the model is continuously converted from a model (simplified models) from which a solution can be easily obtained to an actual model

homotopy operator

$$y = \text{homotopy}(\text{actual} = \text{actual}, \text{simplified} = \text{simplified})$$

$$\Leftrightarrow y = \text{actual} \cdot \lambda + \text{simplified} \cdot (1 - \lambda), \quad \lambda = 0 \rightarrow 1$$

Since the formulas for flow rate, head, shaft power, and efficiency are nonlinear equations, homotopy conversion is performed.

Flow rate equation

```
// Flow equations
```

```
V_flow = homotopy(m_flow/rho, ←  
                    m_flow/rho_nominal); ←
```

actual model

simplified model

actual models (1)

volumetric flow rate

$$V_{flow} = \frac{m_{flow}}{\rho}$$

$$V_{flow_single} = \frac{V_{flow}}{nParallel}$$

Constants and the curve coordinate variables of the check valve function

constant unitHead = 1

constant unitMassFlowRate = 1

final constant unit_m_flow = 1

s Initial value of s = $\frac{m_flow_{start}}{\text{unit_m_flow}}$

(head)

No check valve function $checkValve = false$

$$head = \left(\frac{N}{N_{nominal}} \right)^2 \text{flowCharacteristic} \left(V_{flow_single} \left(\frac{N_{nominal}}{N} \right) \right), s = 0$$

With check valve function $checkValve = true$

$$head = \begin{cases} \left(\frac{N}{N_{nominal}} \right)^2 \text{flowCharacteristic} \left(V_{flow_single} \left(\frac{N_{nominal}}{N} \right) \right), & s > 0 \\ \left(\frac{N}{N_{nominal}} \right)^2 \text{flowCharacteristic}(0) - s \cdot \text{unitHead}, & s \leq 0 \end{cases}$$

$$V_{flow_single} = \begin{cases} s \cdot \frac{\text{unitMassFlowRate}}{\rho}, & s > 0 \\ 0, & s \leq 0 \end{cases} \Leftrightarrow s = \frac{\rho \cdot V_{flow_single}}{\text{unitMassFlowRate}}$$

actual models (2)

(power curve) (power consumption), (shaft power)

Using shaft power
characteristics

use_powerCharacteristic = true

$$W_{single} = \left(\frac{N}{N_{nominal}} \right)^3 \frac{\rho}{\rho_{nominal}} \text{powerCharacteristic} \left(V_{flow_{single}} \frac{N_{nominal}}{N} \right)$$

$$\eta = \frac{dp_{pump} \cdot V_{flow_{single}}}{W_{single}}$$

Use efficiency
characteristics

use_powerCharacteristic = false

$$\eta = \text{efficiencyCharacteristic} \left(V_{flow_{single}} \left(\frac{N_{nominal}}{N} \right) \right)$$

$$W_{single} = \frac{dp_{pump} \cdot V_{flow_{single}}}{\eta}$$

simplified models

(volumetric flow rate)

$$V_{flow} = \frac{m_{flow}}{\rho_{nominal}}$$

(head)

$$head = \frac{N}{N_{nominal}}(\text{flowCharacteristic}(0) + x), \quad x = \begin{cases} \frac{V_{flow_{single}} \cdot \text{delta_head}_{init}}{V_{flow_{single_init}}}, & \text{if } |V_{flow_{single_init}}| > 0 \\ 0, & \text{else} \end{cases}$$

$$V_{flow_{single}} = \frac{s \cdot \text{unitMassFlowRate}}{\rho_{nominal}} \Leftrightarrow s = \frac{V_{flow_{single}}}{\rho_{nominal} \cdot \text{unitMassFlowRate}}$$

(power curve) (power consumption) (shaft power)

Using shaft power characteristics

$$W_{single} = \frac{N}{N_{nominal}} \frac{V_{flow_{single}}}{V_{flow_{single_init}}} \text{powerCharacteristic}(V_{flow_{single_init}})$$

Using efficiency characteristics

$$\eta = \text{efficiencyCharacteristic}(V_{flow_{string_init}}), \quad W_{single} = \frac{dp_{pump} \cdot V_{flow_{single_init}}}{\eta}$$

**Law of mass
conservation****(mass balances)****PartialLumpedVolume**

$$\frac{dm}{dt} = mb_flow$$

Total mass

$$\frac{dmXi}{dt} = mbXi_flow$$

Ingredients

$$\frac{dmC_{scaled}}{dt} = \frac{mbC_flow}{C_{nominal}}$$

**Additional substances
(Such as fine particles)**

- Left side is zero for stationary analysis (default)

- For a non-stationary analysis, change massDynamics and V>0

[3. Modelica.Fluid Library,](#)

FluidExample2 volume Model reference

<https://www.amane.to/wp-content/uploads/2018/12/ffe08c971d7476d067b0f2910be6dd63.pdf>

PartialPump Connect the advection term and FluidPort.

$$mb_flow = port_a.m_flow + port_b.m_flow$$

Total mass

$$mbXi_flow = port_a.m_flow \cdot \text{actualStream}(port_a.Xi_outflow) + port_b.m_flow \cdot \text{actualStream}(port_b.Xi_outflow)$$

$$port_a.Xi_outflow = medium.Xi$$

Ingredients

$$port_b.Xi_outflow = medium.Xi$$

$$mbC_flow = port_a.m_flow \cdot \text{actualStream}(port_a.C_outflow) + port_b.m_flow \cdot \text{actualStream}(port_b.C_outflow)$$

**Additional
substances**

$$port_a.C_outflow = C$$

$$port_b.C_outflow = C$$

Law of energy conservation (energy balance)

PartialLumpedVolume

$$\frac{dU}{dt} = Hb_flow + Qb_flow + Wb_flow$$

- Left side is zero for stationary analysis (default)
- Change energyDynamics for transient analysis.
Let $V > \{0\}$.

PartialPump

Energy change due to work

$$Wb_flow = W_{total} \text{ (shaft power)}$$

[3. Modelica.Fluid Library](#),

FluidExample2 volume Model reference

<https://www.amane.to/wp-content/uploads/2018/12/ffe08c971d7476d067b0f2910be6dd63.pdf>

heatPort Heat transfer from

$$Qb_flow = heatTransfer.Qflows[1]$$

FluidPort Enthalpy advection from

$$Hb_flow = port_a.m_flow \cdot \text{actualStream}(port_a.h_outflow) \\ + port_b.m_flow \cdot \text{actualStream}(port_b.h_outflow)$$

$$port_a.h_outflow = medium.h$$

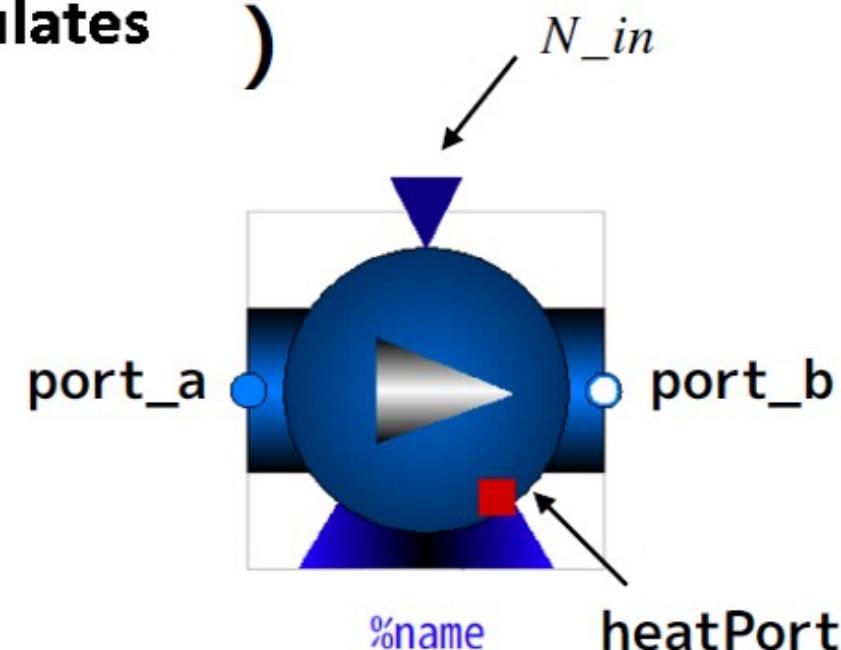
$$port_b.h_outflow = medium.h$$

PrescribedPump (Pump that regulates rotation speed)

Parameters

```
use_N_in = true Input connector N_in    use
    connect(N_in,N_in_internal)
```

```
use_N_in = true Parameters N_const    use
    N_ni_internal = N_const
```



Pump speed N [rpm] Is internally protected | Declared connector $N_{in_internal}$ Is determined.

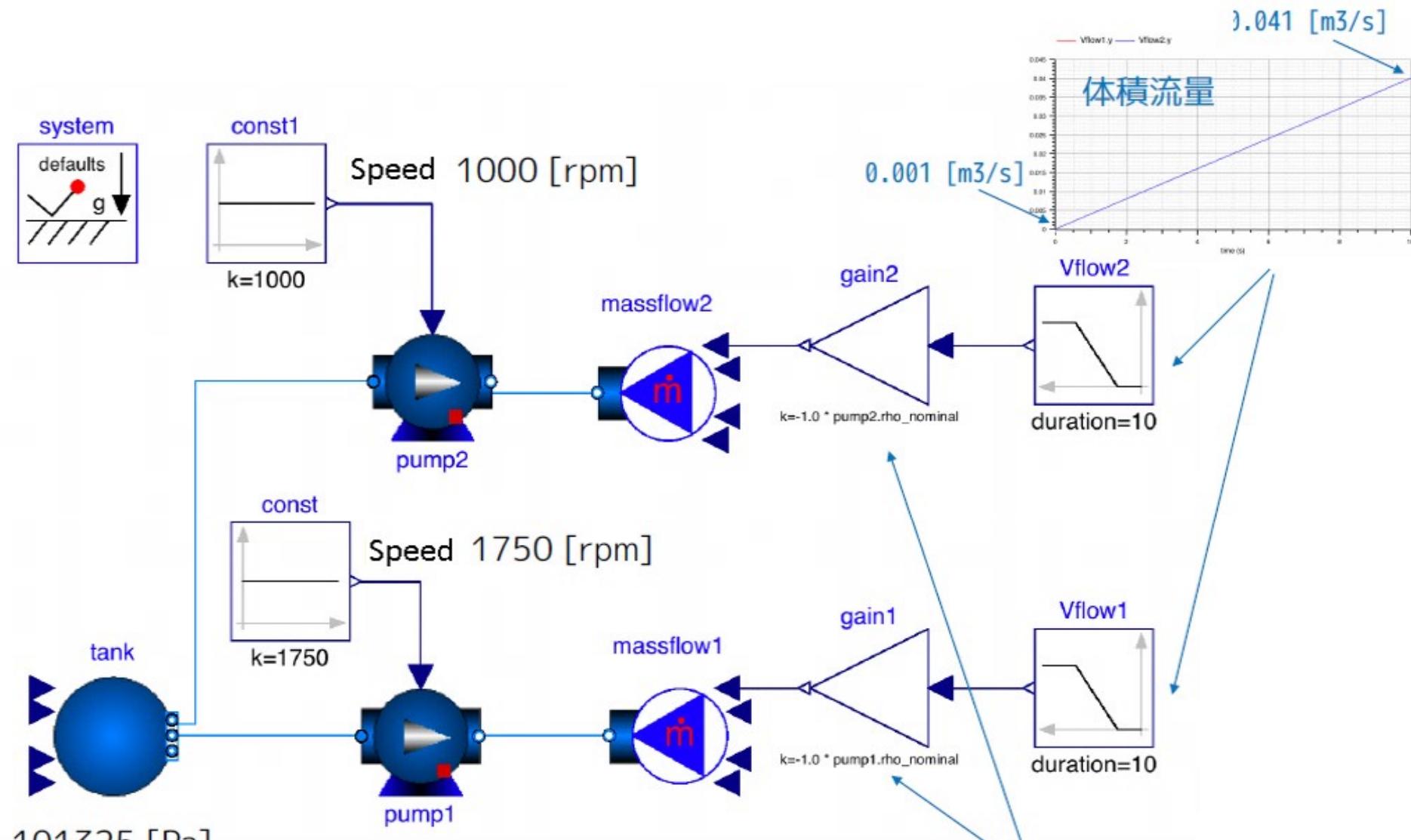
$$N = \max(N_{in_internal}, 1 \times 10^{-3})$$

↑ Limiter (lower limit of rotation speed)

Parameters use_N_in is $N_{in_internal}$ To select the setting method

PumpExample1

PrescribedPump discharge port flow rate Change in 10 sec from 0.001 [m³/s] to 0.041 [m³/s]



Convert volume flow to mass flow by multiplying by density

With the default solver of OpenModelica (1.14.0-dev-26499-g3e12ff2), starting from a volume flow rate of 0 [m³ / s], division by zero. When starting from 0.0001 [m³ / s], the initial solution does not converge.

PrescribedPump Performance settings

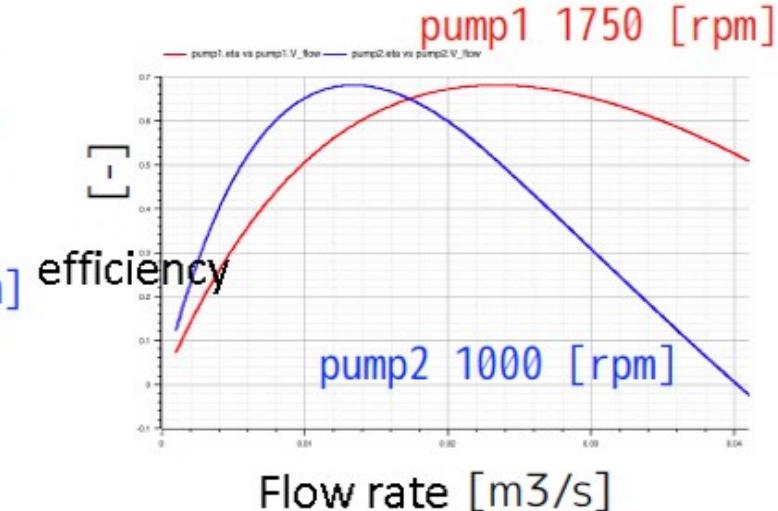
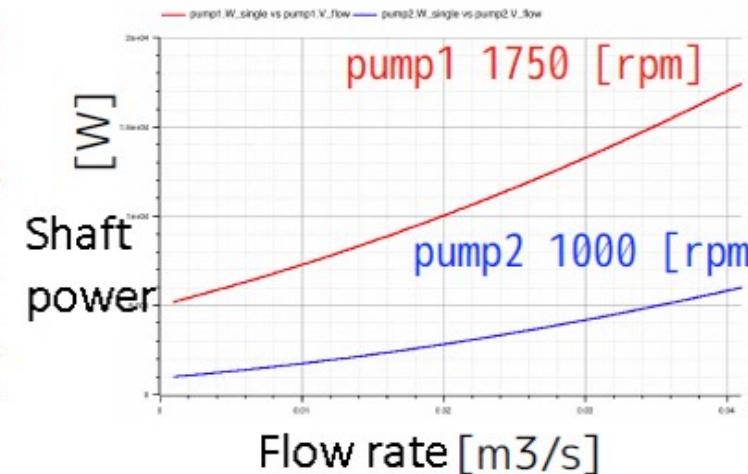
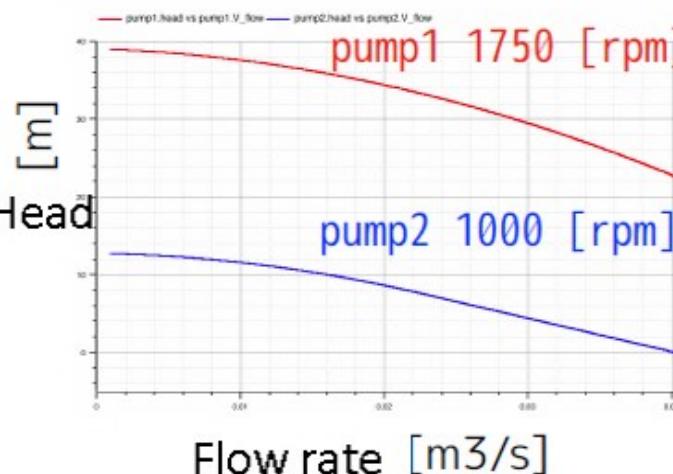
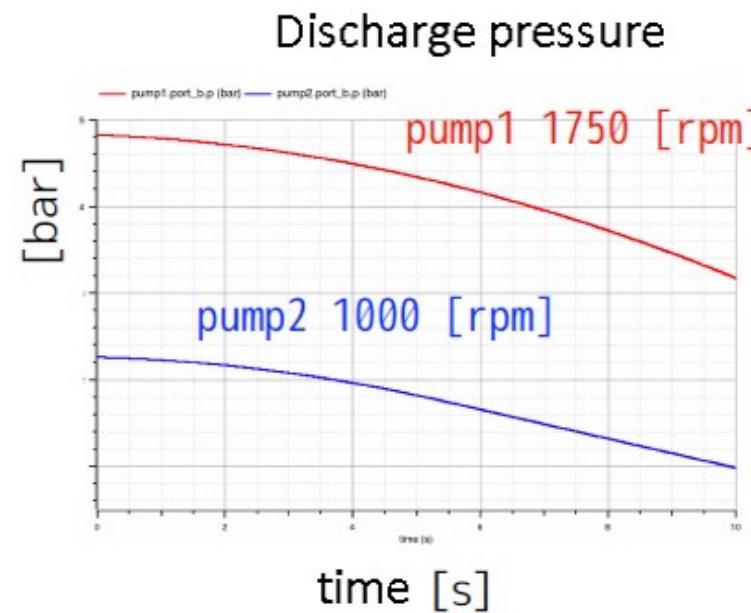
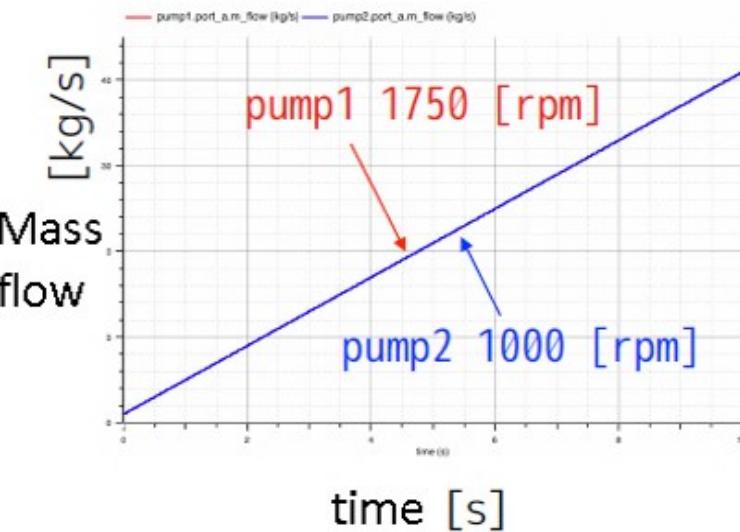
| Flow rate [m ³ /s] | Total head [m] | Base rotation speed 1750 [rpm] | |
|-------------------------------|----------------|--------------------------------|------------|
| | | Shaft power [kW] | efficiency |
| 0.000 | 39.000 | 5.000 | 0.000 |
| 0.034 | 27.400 | 14.700 | 0.620 |
| 0.040 | 22.800 | 14.850 | 0.600 |

```
Modelica.Fluid.Machines.PrescribedPump pump1(
  redeclare package Medium = Medium,
  redeclare function flowCharacteristic =
    Modelica.Fluid.Machines.BaseClasses.PumpCharacteristics.quadraticFlow (
      V_flow_nominal={0,0.034,0.04}, head_nominal={39.0,27.0,22.8}),
  redeclare function powerCharacteristic =
    Modelica.Fluid.Machines.BaseClasses.PumpCharacteristics.quadraticPower (
      V_flow_nominal={0,0.034,0.04}, W_nominal={5000,14700,17000}),
  N_nominal = 1750,           Reference speed 1750 [rpm]
  checkValve = true,         Check valve function enabled
  m_flow_start = 0.0001,     Initial mass flow rate 0.0001 [kg/s]
  use_N_in = true,          To set the number of revolutions at the input connector
  use_powerCharacteristic = true) annotation( ...); Use shaft power characteristics
```

Head characteristics
Shaft power characteristics

flowCharacteristic and powerCharacteristic can be exchanged for any user-defined function.

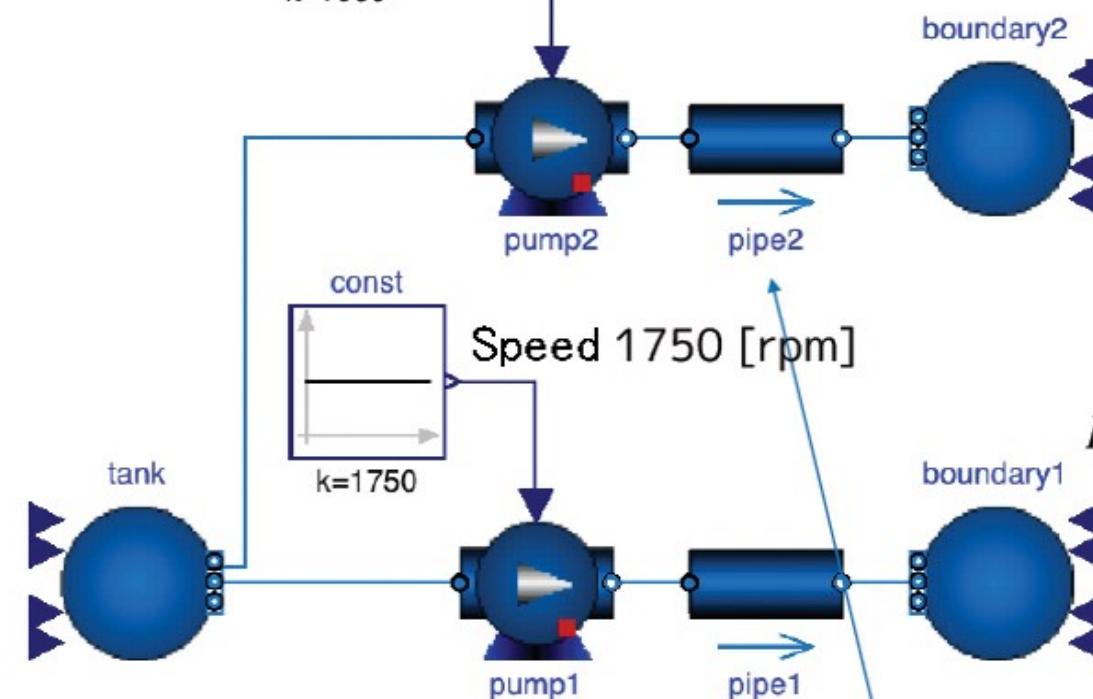
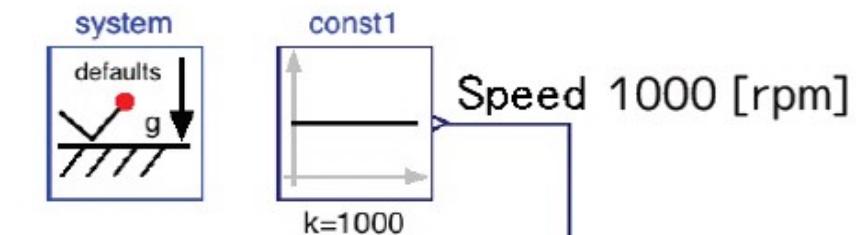
Simulation result



PumpExample2

Connect a pipe to the outlet of the PrescribedPump to change the outlet head.

PrescribedPump The performance setting is the same as Example1.



$$p_{amb} = 101325 \text{ [Pa]}$$

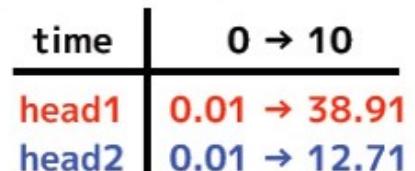
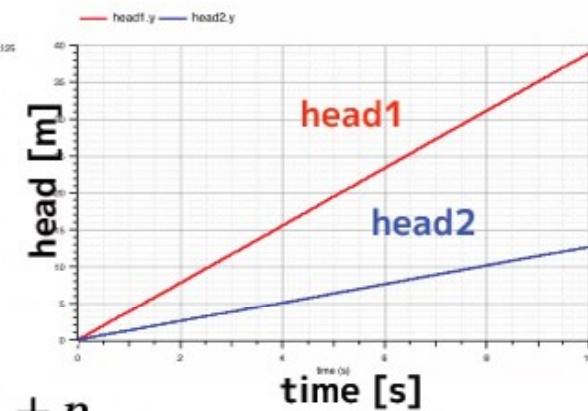
$$T_{amb} = 293.15 \text{ [K]}$$

$$\text{diameter} = 0.1 \text{ [m]}$$

$$\text{length} = 20 \text{ [m]}$$

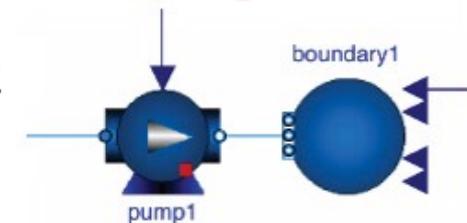
Convert head to pressure
 $p = \rho g \cdot \text{head} + p_{amb}$

$$p = \rho g \cdot \text{head} + p_{amb}$$

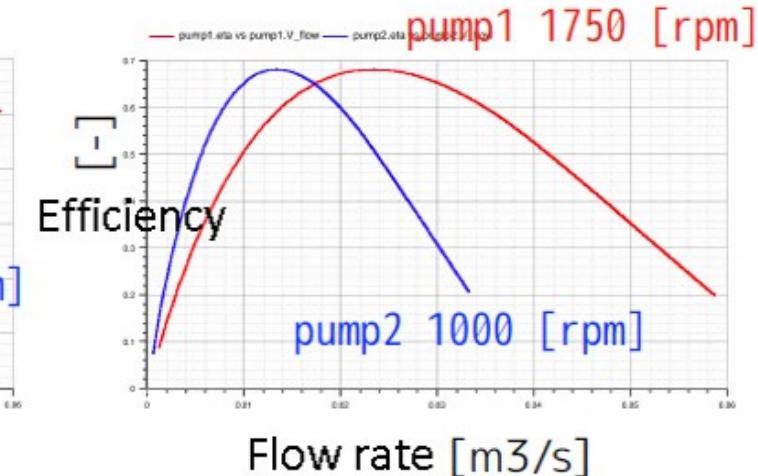
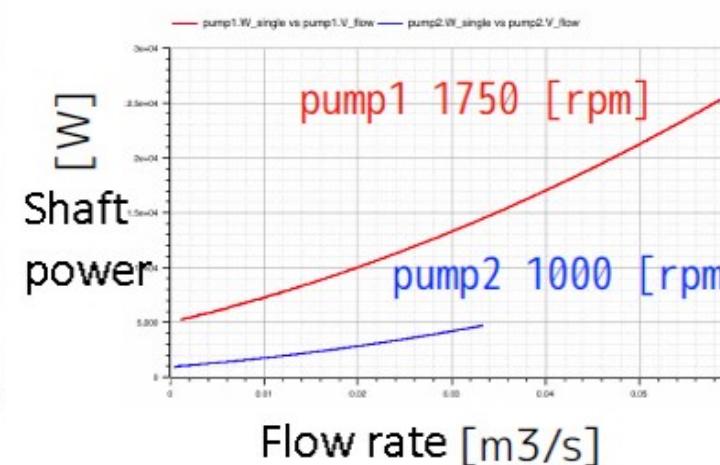
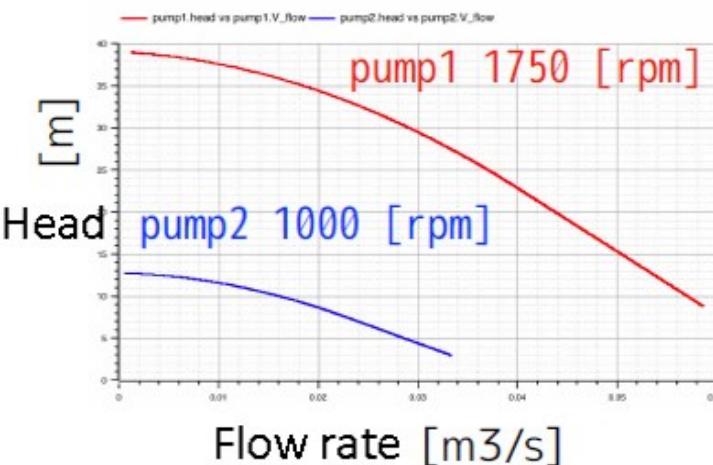
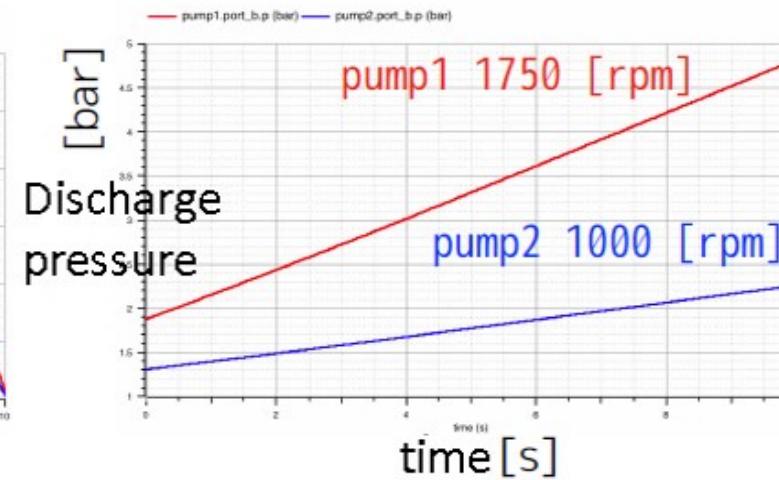
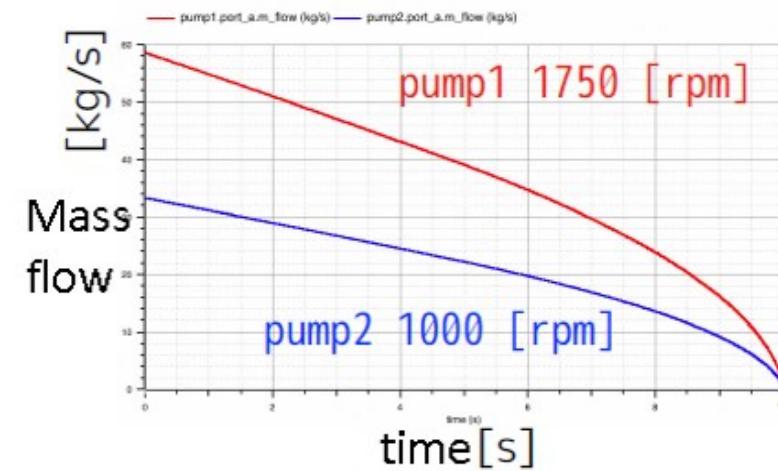


The discharge port side of the pump is internally a volume model, so connecting a flow model such as staticpipe is more stable.

When pump and Boundary_pT are directly connected, Initial solution (time = 0) is hard to converge



Simulation results



Pump (Shaft driven pump)

A pump that connects the shaft and sets the speed and power

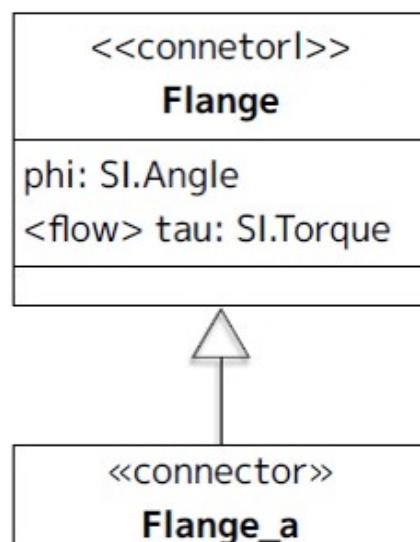
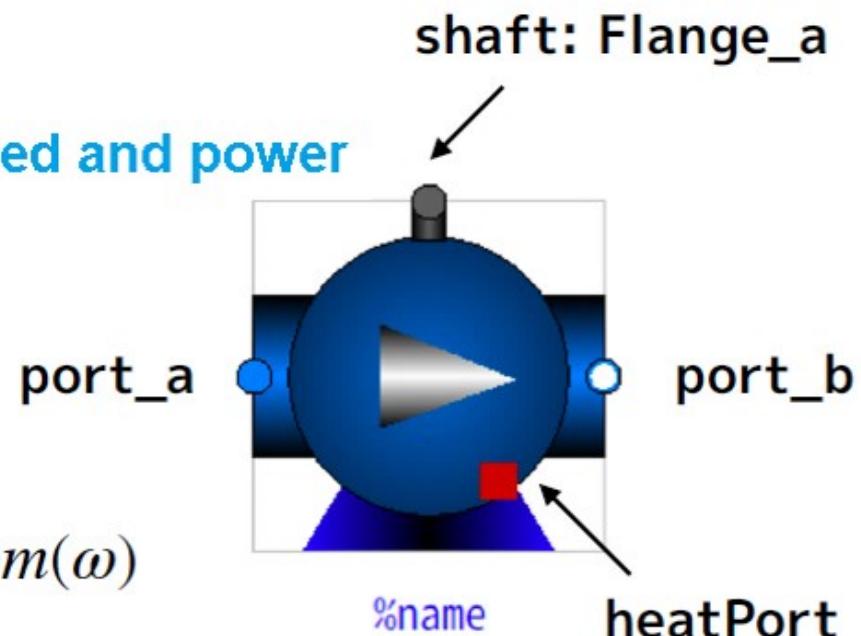
$$\varphi = \text{shaft}.phi \quad [\text{rad}]: \text{rotation angle}$$

$$\omega = \frac{d\varphi}{dt} \quad [\text{rad/s}]: \text{angular velocity}$$

$$N = \text{Modelica.SIUnits.Conversions.to_rpm}(\omega)$$

$$W_{\text{single}} = \omega \cdot \text{shaft}.tau \quad [\text{W}]: \text{Shaft power}$$

$$N = \frac{60}{2\pi}\omega \quad [\text{rpm}]: \text{Speed}$$



Modelica.Mechanics.Rotationlas.Interfaces.Flange

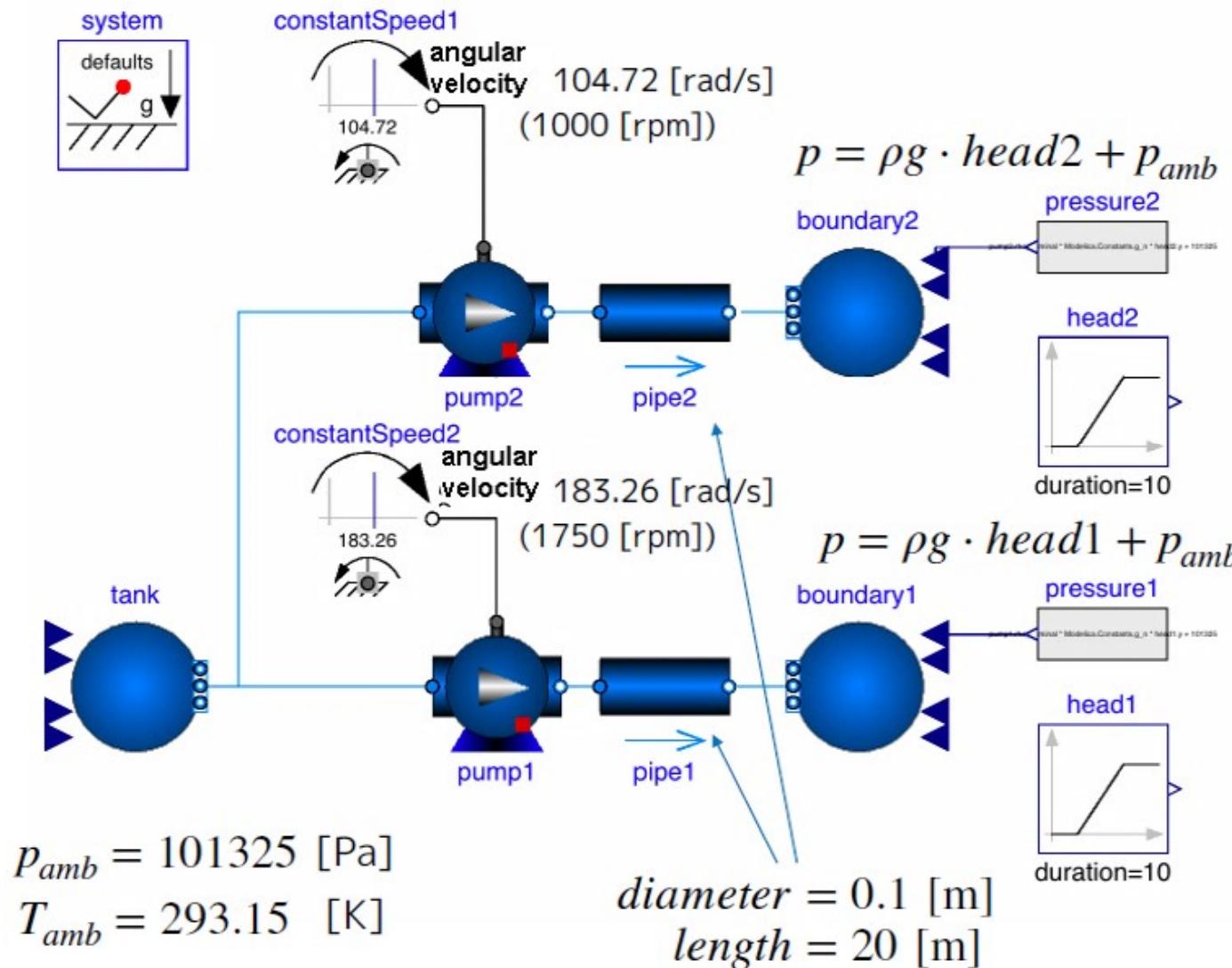
$$\varphi = \text{shaft}.phi \quad [\text{rad}]: \text{rotation angle}$$

$$\tau = \text{shaft}.tau \quad [\text{Nm}]: \text{torque}$$

Modelica.Mechanics.Rotationlas.Interfaces.Flange_a

PumpExample3

As in PumpExample2, connect a pipe to the outlet of the Pump and change the head at the outlet.



| time | 0 → 10 |
|-------|--------------------------|
| head1 | $0.01 \rightarrow 38.91$ |
| head2 | $0.01 \rightarrow 12.71$ |

Pump Performance settings

Reference speed 1750 [rpm]

| Flow rate [m ³ /s] | Total head [m] | Shaft power [kW] | efficiency |
|-------------------------------|----------------|------------------|------------|
| 0.000 | 39.000 | 5.000 | 0.000 |
| 0.034 | 27.400 | 14.700 | 0.620 |
| 0.040 | 22.800 | 14.850 | 0.600 |

```

Modelica.Fluid.Machines.Pump pump1(
  redeclare package Medium = Medium,
  redeclare function flowCharacteristic =
    Modelica.Fluid.Machines.BaseClasses.PumpCharacteristics.quadraticFlow(
      V_flow_nominal={0,0.034,0.04}, head_nominal = {39.0, 27.0, 22.8}), Lift characteristics
  redeclare function powerCharacteristic =
    Modelica.Fluid.Machines.BaseClasses.PumpCharacteristics.quadraticPower(
      V_flow_nominal={0,0.034,0.04}, W_nominal={5000,14700,17000}), Shaft power
    characteristics
  redeclare model Monitoring = Modelica.Fluid.Machines.BaseClasses.PumpMonitoring.PumpMonitoringNPSH,
  N_nominal = 1750, Reference speed 1750 [rpm]
  checkValve = true, Check valve function enabled
  m_flow_start = 1, Initial mass flow rate1 [kg/s]
  use_powerCharacteristic = true) Use shaft power characteristics
  annotation( ...);

```

ControlledPump (Mass flow rate / discharge pressure regulation pump)

Pump to set mass flow or discharge pressure

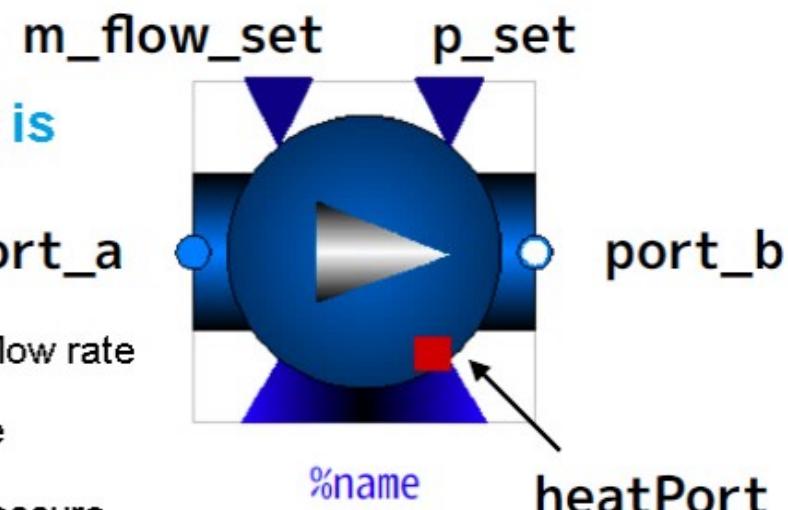
Used when the importance of pump characteristics is secondary

Pump head characteristics are parameters

$m_flow_{nominal}$ [kg/s]: Reference value of discharge flow rate

$p_a_{nominal}$ [Pa]: Suction pressure reference value

$p_b_{nominal}$ [Pa]: Reference value of discharge pressure



Only to set in. (See next slide)

How to set flow rate and discharge pressure

`control_m_flow_set = true`

Control mass flow.

`use_m_flow_set = true`

If so, control with the input connector `m_flow_set`.

`false`

Then the mass flow becomes the parameter `m_flownominal`

`control_m_flow_set = false`

Control the discharge pressure.

`use_p_set = true`

If so, control with the input connector `p_set`.

`false`

Then, the discharge pressure becomes the parameter `p_bnominal`.

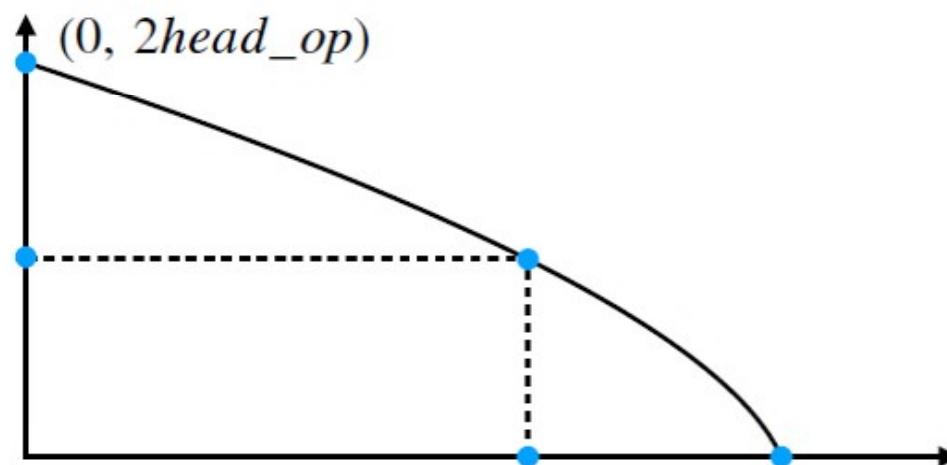
ControlledPump Head characteristics

$$V_{flow_op} = \frac{m_{flow_nominal}}{\rho_{nominal}}$$

$$head_{op} = \frac{p_b_{nominal} - p_a_{nominal}}{\rho_{nominal}g}$$

$$v_{flow_nominal} = \{0, V_{flow_op}, 1.5V_{flow_op}\}$$

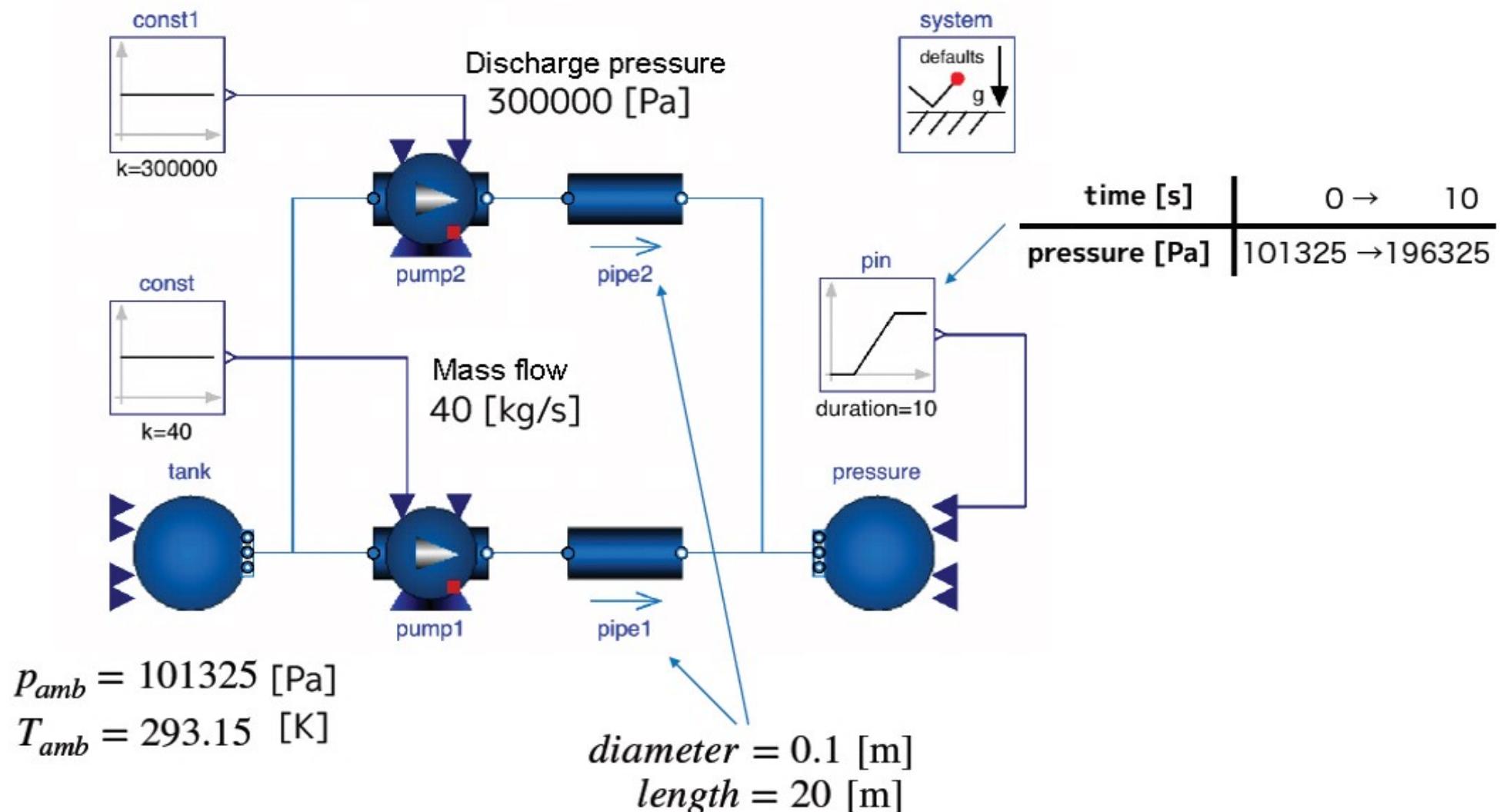
$$head_{nominal} = \{2head_{op}, head_{op}, 0\}$$



- The head characteristics as described above are set inside the model.
- In this model, the relationship between pressure differential and flow is determined by the piping system behind the pump.
Do not follow this property.

PumpExample4

ControlledPump example. pump1 sets the mass flow rate to 40 [kg / s], and pump2 sets the discharge pressure to 300000 [Pa]. The pressure at the outlet of pipe1 and pipe2 is changed from 101325 [Pa] to 196325 [Pa] in 10 seconds.



ControlledPump Performance settings

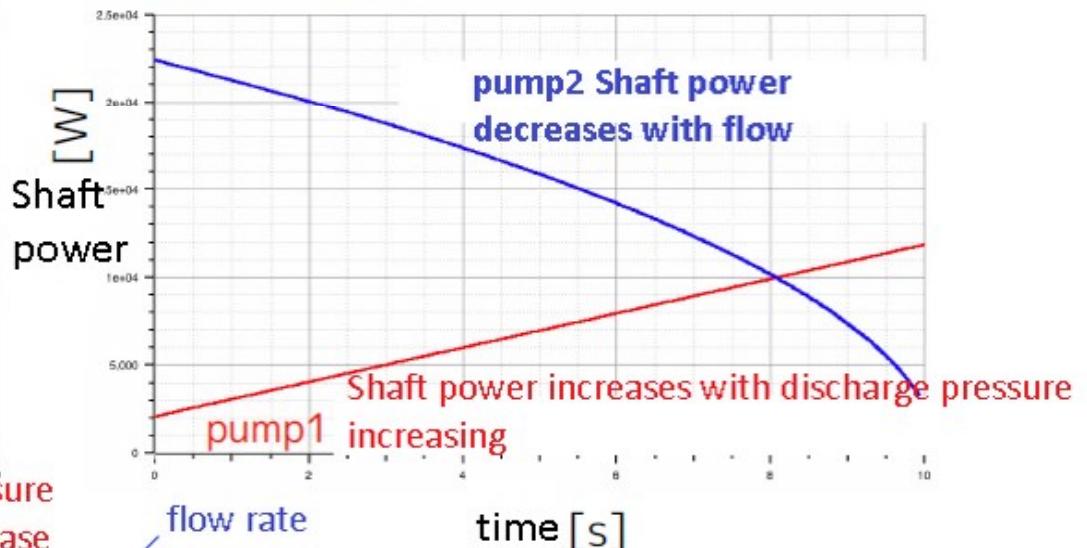
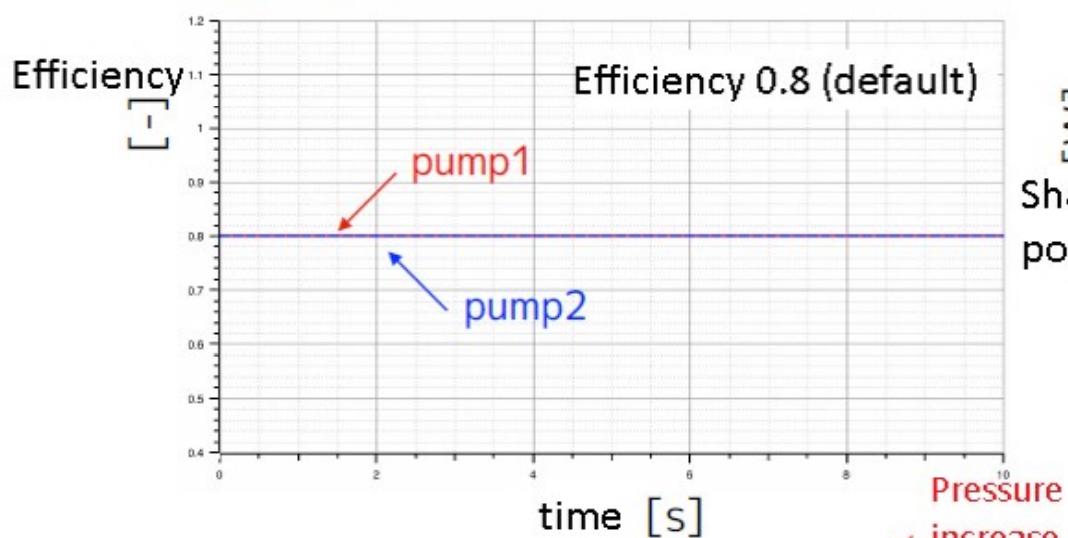
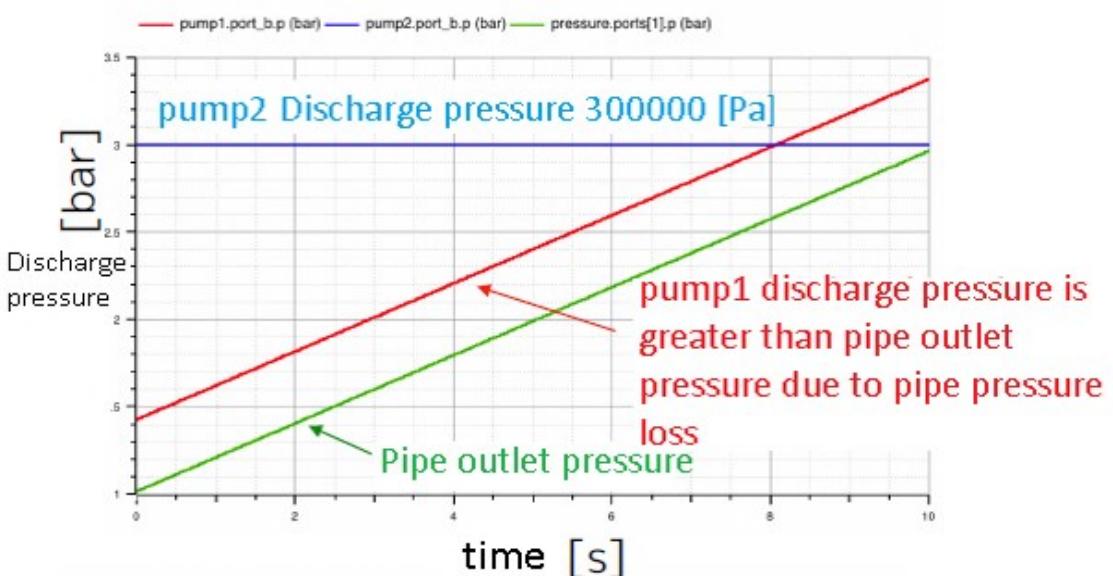
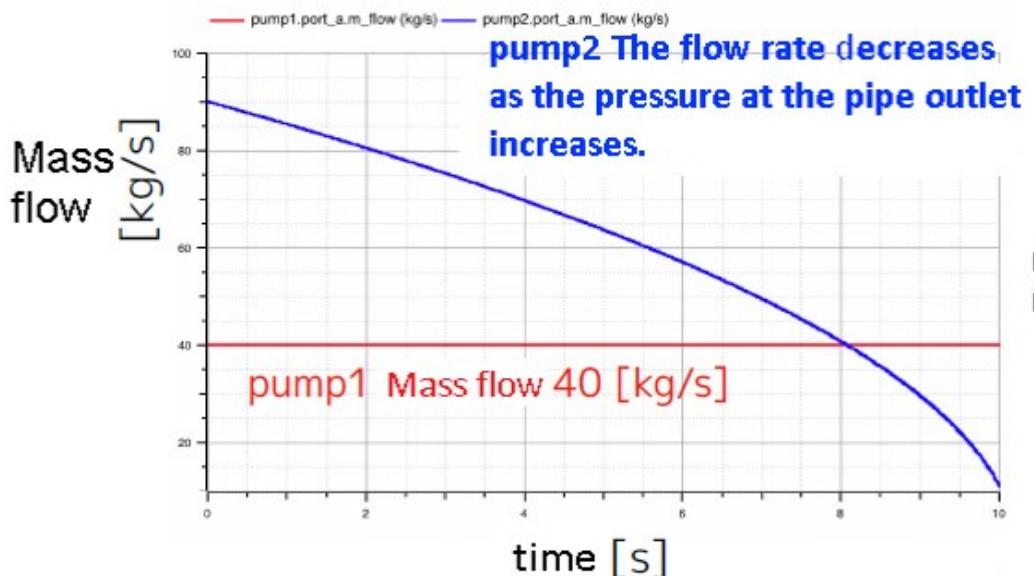
pump1 setting Specify the mass flow rate with the input connector
Specify the flow rate (control_m_flow = true by default)

```
Modelica.Fluid.Machines.ControlledPump pump1(  
  redeclare package Medium = Medium,  
  m_flow_nominal = 40,      ] [kg/s]: Reference value of discharge flow rate  
  p_a_nominal = 101325,     ] [Pa]: Suction pressure reference value  
  p_b_nominal = 351325,     ] [Pa]: Reference value of discharge pressure  
  use_m_flow_set = true)  Use mass flow input connectors  
  annotation( ...);
```

pump2 setting Input connector regulates discharge pressure

```
Modelica.Fluid.Machines.ControlledPump pump2(  
  redeclare package Medium = Medium,  
  control_m_flow = false,   ← Specify pressure  
  m_flow_nominal = 40,      ] [kg/s]: Reference value of discharge flow rate  
  p_a_nominal = 101325,     ] [Pa]: Suction pressure reference value  
  p_b_nominal = 351325,     ] [Pa]: Reference value of discharge pressure  
  use_p_set = true)        Use input connector for discharge pressure  
  annotation(...);
```

simulation result



$$\eta = \frac{dp_{pump} \cdot V_{flow_single}}{W_{single}}$$

efficiency

pressure increase

flow rate

Shaft power

Conclusion

The Modelica.Fluid.Machines pump model models the operation of the pump using a head characteristic and a shaft power characteristic or an efficiency characteristic.

- The head characteristic, head power characteristic, and efficiency characteristic are replaceable functions and can be replaced with user-defined functions.
- The discharge side of the pump is a volume model. By setting the pump volume V [m³], massDynamics, and energyDynamics as parameters, unsteady mass conservation and energy conservation can be considered.
- Calculations such as NPSHa can be made by setting a Monitoring model.
- Pump can connect to Modelica.Mechanics.Rotational Flange connector.
- Specify the rotation speed with PrescribedPump, Real connector or parameter.
- ControlledPump is used when the characteristics of the pump are not sufficient, and specifies the mass flow rate or discharge pressure.

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