

# controllable-refinement

Version 7.9

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The type system based on STLC, introducing user-controllable type refinement. Meta type variables are  $A, B$ . Meta predicate variable is  $P$ . A type with predicate write as  $A_P$ , introduce predicate write as  $P_+$ , eliminate write as  $P_-$ ,  $P_{\gamma+}$  for anyway introduce,  $P_{\gamma-}$  for anyway eliminate.

- verify-predicate

$$\frac{\Gamma, f : A_P \rightarrow B, x : A_P}{fx : B}$$

- introduce-predicate

$$\frac{\Gamma, f : (p : A_{P_+}) \rightarrow B, x : A}{fx : B, x : A_P, p : A}$$

- eliminate-predicate

$$\frac{\Gamma, f : (p : A_{P_-}) \rightarrow B, x : A_P}{fx : B, x : A, p : A_P}$$

- anyway-introduce-predicate

$$\frac{\Gamma, f : A_{P_{\gamma+}} \rightarrow B, x : A}{fx : B, x : A_P} \quad \frac{\Gamma, f : A_{P_{\gamma+}} \rightarrow B, x : A_P}{fx : B, x : A_P}$$

- anyway-eliminate-predicate

$$\frac{\Gamma, f : A_{P_{\gamma-}} \rightarrow B, x : A_P}{fx : B, x : A} \quad \frac{\Gamma, f : A_{P_{\gamma-}} \rightarrow B, x : A}{fx : B, x : A}$$

Notice that it can be extended to with polymorphism without changing previous definition.

## 1 extension: related predicate

Sometime we would like to update related predicate, for example:

```
(: open (-> (file {writable readable})))  
(: write (-> (file {writable}) void))  
(: close (-> (file {+close}) void))  
  
(let ([file (open "xxx")])  
  (write file "hello")  
  (close file)  
  (write file "hello"))
```

where `+close` also means `?-readable` `?-writable`. This extension is quite simple, we can add related predicate information into environment, rewrite predicates of type while parsing type.