

# controllable-refinement

Version 7.8

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The type system based on STLC, introducing user-controllable type refinement. Meta type variables are  $A, B$ . Meta predicate variable is  $P$ . A type with predicate write as  $A_P$ , introduce predicate write as  $P_+$ , eliminate write as  $P_-$ ,  $P_{?+}$  for anyway introduce,  $P_{?-}$  for anyway eliminate.

- verify-predicate

$$\frac{\Gamma, f : A_P \rightarrow B, x : A_P}{fx : B}$$

- introduce-predicate

$$\frac{\Gamma, f : (p : A_{P_+}) \rightarrow B, x : A}{fx : B, x : A_P, p : A}$$

- eliminate-predicate

$$\frac{\Gamma, f : (p : A_{P_-}) \rightarrow B, x : A_P}{fx : B, x : A, p : A_P}$$

- anyway-introduce-predicate

$$\frac{\Gamma, f : A_{P_{?+}} \rightarrow B, x : A}{fx : B, x : A_P} \quad \frac{\Gamma, f : A_{P_{?+}} \rightarrow B, x : A_P}{fx : B, x : A_P}$$

- anyway-eliminate-predicate

$$\frac{\Gamma, f : A_{P_{?-}} \rightarrow B, x : A_P}{fx : B, x : A} \quad \frac{\Gamma, f : A_{P_{?-}} \rightarrow B, x : A}{fx : B, x : A}$$

Notice that it can be extended to with polymorphism without changing previous definition.