

MITx: 6.041x Introduction to Probability - The Science of Uncertainty

Help



- Unit 0: Overview
- Entrance Survey
- Unit 1: Probability models and axioms
- ▼ <u>Unit 2:</u> <u>Conditioning and</u> independence

Unit overview

Lec. 2: Conditioning and Bayes' rule

Exercises 2 due Feb 2, 2017 20:59 ART

<u>Lec. 3:</u>

<u>Independence</u>

Exercises 3 due Feb 2, 2017 20:59 ART

Solved problems

Problem Set 2

Problem Set 2 due Feb 2, 2017 20:59 ART

Unit 3: Counting

Unit 2: Conditioning and independence > Problem Set 2 > Problem 1 Vertical: Two fivesided dice

Problem 1 Vertical: Two five-sided dice

☐ Bookmark this page

Problem 1: Two five-sided dice

4/4 points (graded)

You roll two five-sided dice. The sides of each die are numbered from 1 to 5. The dice are "fair" (all sides are equally likely), and the two die rolls are independent.

Part (a): Event \boldsymbol{A} is "the total is 10" (i.e., the sum of the results of the two die rolls is 10).

1. Is event $m{A}$ independent of the event "at least one of the dice resulted in a 5"?

2. Is event $m{A}$ independent of the event "at least one of the dice resulted in a 1"?



Part (b): Event \boldsymbol{B} is "the total is 8."

1. Is event $m{B}$ independent of getting "doubles" (i.e., both dice resulting in the same number)?



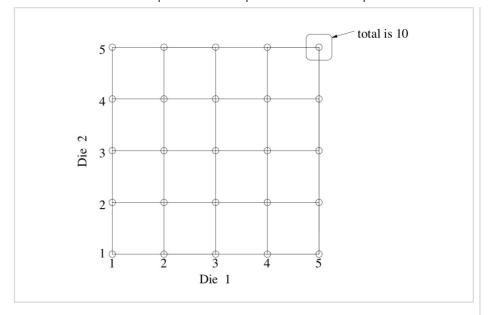
2. Given that the total was 8, what is the probability that at least one of the dice resulted in a 3?

0.666	Answer: 0.66667
-------	------------------------

Answer:

Part (a):

1. No. A mathematical derivation is as follows: Let event $m{A}$ be "the total is 10," and event $m{C}$ be "at least one of the dice resulted in a 5".



Overall, there are 25 possible and equally likely outcomes. For a total of 10, we must get a 5 on both dice. Therefore, out of the 25 outcomes, only one of them will result in a total of 10. Therefore, $\mathbf{P}(A) = \frac{1}{25}$.

Next, for at least one die to result in a 5, we can have 5 on the first die, a 5 on the second die, or a 5 on both dice. This corresponds to 9 possible outcomes and so $\mathbf{P}(C)=\frac{9}{25}$.

We then notice that if we have a total of 10 (event ${\bf A}$), then both dice must have resulted in a 5, and event ${\bf C}$ also occurs. Thus,

$$\mathbf{P}(A\cap C)=\mathbf{P}(A)=rac{1}{25}
eq \mathbf{P}(A)\cdot \mathbf{P}(C)=rac{1}{25}\cdot rac{9}{25}.$$

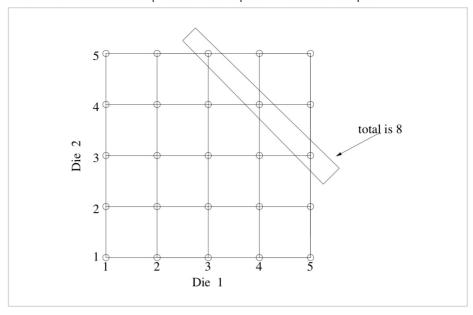
2. No. Let A be the event that "the total is 10", and let D be the event "at least one of the dice resulted in a 1". Similar to event C described in part 1, $\mathbf{P}(D) = \frac{9}{25}$.

Next, let us consider $\mathbf{P}(A\cap D)$. We notice that if one of the dice resulted in a 1, it is impossible to get a total of 10. Therefore, $\mathbf{P}(A\cap D)=\mathbf{P}(\emptyset)=0$, and

$$0 = \mathbf{P}(A \cap D)
eq \mathbf{P}(A) \cdot \mathbf{P}(D) > 0.$$

Part (b):

1. No. Let $m{B}$ be the event "the total is 8" and let $m{E}$ be the event that doubles are obtained.



Event B consists of the three outcomes (3,5), (4,4), and (5,3). Therefore, ${\bf P}(B)=\frac{3}{25}$.

Event $m{E}$ occurs in 5 out of the 25 possible outcomes, and so ${f P}(E)=rac{5}{25}=rac{1}{5}$.

Therefore,

$$\mathbf{P}(B \cap E) = \mathbf{P}(\{(4,4)\}) = rac{1}{25}
eq \mathbf{P}(B) \cdot \mathbf{P}(E) = rac{3}{25} \cdot rac{1}{5}.$$

2.

$$\mathbf{P}(\text{at least one 3 | total is 8}) = \frac{\mathbf{P}(\text{at least one 3 and total is 8})}{\mathbf{P}(\text{total is 8})}$$

$$= \frac{\mathbf{P}(\{(3,5),(5,3)\})}{\mathbf{P}(B)}$$

$$= \frac{2/25}{3/25}$$

$$= \frac{2}{3}.$$

Submit

You have used 1 of 1 attempt

Printable problem set available here.

DISCUSSION

//2017		blem 1 Vertical: Two five-sided dice Problem Set 2 6.041x Courseware edX Click "Show Discussion" below to see discussions on this problem.		
	Discussion Topic: Unit 2/Problem Set 2 / Two five-sided dice	Show Discussion		

© All Rights Reserved



© 2012-2017 edX Inc. All rights reserved except where noted. EdX, Open edX and the edX and Open EdX logos are registered trademarks or trademarks of edX Inc.

















