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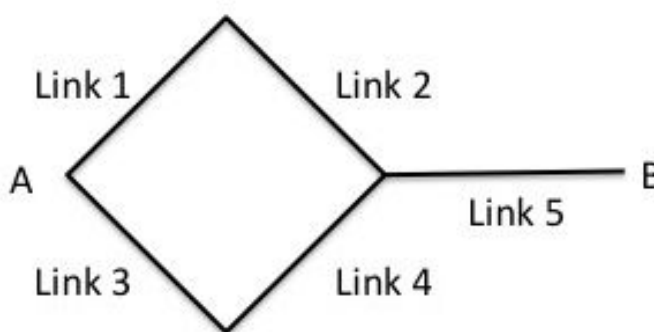
## Problem 2 Vertical: A reliability problem

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### Problem 2: A reliability problem

4/4 points (graded)

Consider the communication network shown in the figure below and suppose that each link can fail with probability  $p$ . Assume that failures of different links are independent.



1. Assume that  $p = 1/3$ . Find the probability that there exists a path from **A** to **B** along which no link has failed. (Give a numerical answer.)



2. Given that exactly one link in the network has failed, find the probability that there exists a path from **A** to **B** along which no link has failed. (Give a numerical answer.)




You have used 1 of 2 attempts

Correct (4/4 points)

DISCUSSION

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What's wrong about this thought

discussion posted 5 days ago by **GuusKoning**

If you know that exactly one link failed, then for getting no path, that link has to be number 5. That link has a change of 1/3 to get failed. In all other occasions there's a path, so the probability much be  $1 - 1/3 = 2/3$

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1 response

**papastauf**

5 days ago

Once you know that exactly one link has failed, the a priori probabilities of failure must be updated. Now you know that one link has failed and four links have not failed. Since the a prior unconditional probabilities of failure were the same for each link, the conditional probabilities of failure for each link in the new conditional universe must also be uniform. What are those probabilities?

Think about your new sample space, in which you know that exactly one link has failed. What happens to the probability of failure of the other links? How many possibilities of the total (the sample space itself) would lead the system works? Hope it helps.

posted 4 days ago by **Schots**

Not sure I understand these responses. In particular, why should the prior probabilities of each link's failure be updated given that one has already failed. Is the probability of failure in this case not an intrinsic property of the link itself rather than our belief about its failure rate? Are you suggesting that  $5 \times 1/3$  should now be allocated over the remaining 4 links? Doesn't seem intuitive to me, but I'm learning not to necessarily trust my intuition.

posted 3 days ago by **DJamesW**

@papastauf and @Schauts ... Thanks for clarifying my thinking on this. Question 2 is actually quite straightforward.



posted 2 days ago by **soloke**

@papastauf.. Nice explanation.. I couldn't have explained any better..



posted a day ago by **lakshmikant**

Thanks @soloke (and others); gave me encouragement to go with first impression! Didn't see it as a re-allocation of priors but I suppose it was. In other words intuition won in this case.



posted a day ago by **DJamesW**

Looks like we don't need to calculate the probability of failure of the links. We just need to count how many scenarios there are with exactly one failed link, and of these how many would satisfy the requirement. As all scenarios should have the same probability there should be no need to do any calc's?



posted a day ago by **Alfred2014**

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