Design Theory of Relational DBr.

- · What makes a good database?
 - · Normalization
 - · Avoid "anomalies"

Functional Dependencies (FD)

· A FD is a constraint between two set of attributes of a relation.

·Given R, a set of attributes X in R is said to functionally determine another set of attributes Y in R (X > Y) iff 2 tiples have the same values of attributes X then they must have the same values for attributes Y.

We write them as:

A. ... An > B. ... Bm Attributes written as list.

Example: title Le ar 1977 124 Star Wars Sci Fi Carrie Fisher Fox Star Wars 1977 124 Sci Fi Fox Mark Hamill Star Wars 1977 Sci Fi Fox 124 Harrison Ford 175 The God father 1972 Drama Paramount Robert Duvall The God ather 1972 175 Drama Marlon Brandon Paramount 1979 Apocalypse Now 153 War Zoetrope Marlon Brandon I claim by design that title, year -> lenght, genre, studioName title, year /> starName Superkey (SK) A set of attributes of A...Angis a superkey of Riff A...Angis a Candidate ken (key) A candidate key is a superker that is minimal: There is no proper subset of C of AA...And s.t. C > R One candidate Key becomes the Primary Key!

For our example:

- · All attributes of R are always a SK
- · title, year, starhame is a candidate title, year, star Name -> R

· Any superset of a candidate key is

Leasoning about FD's.

. aiven a relation R two sets of FDs

A & B are equivalent if.

The set of instances of 12 that satisfy A is exactly the same that

- · A follows from B if every instance of 12 that satisfies Balso satisfies A.
- A & B are equivalent ild.

 A follows B and B follows A

Armstrong's Axioms (3.2 page 81)

Given relation 12 with subsels of attributes X, Y, Z CR

Reflexivity (Trivial)
YCX then X > Y

Argmentation: If X => Y then XZ => YZ for any Z

Transituity:

If X > Y, Y > Z then X > Z

Additional Rules. They can be derived from axioms.

Union:

If X > Y, X > Z then X > YZ Decomposition

If X => YZ then X => Y and X => Z

Ex:

Y Z -> Z

 $\times \rightarrow \forall$

 $\times \rightarrow 2$

Derive Union from axioms X => 17, X => 12 XS -> AS Agmontation Augmentation. $\times \rightarrow \times 2$ X -> X Z -> YZ y Transituity X -> Y -Derve decomposition Y2 -> Y y Reflexivity.

Transitivity

(3.2.4) Closure of attributes Given a relation R and a set of of FDs, what other FDs can be computed from a set of FDs f? The closure of a set of attributes

A...An denoted $\{A_1...A_n\}^{\dagger}$ is the set of attr. that can be derived from A...An A Suisa Hard to do and error prone via axioms! 1) Rewrite FDs in f in canonical form 2) X
A1. An 3) for each B1... Bm. C in FDs if B1. Bm EX and CXX add C to X 1) Repeat (3) until X does not change X is h A, ... Any+

Ex; R(ABCDE) AB-C BC -> A f= \ AB→C BC→AD D→E CE→B BC > D D->E CE-B Compute 4B3+ X & AB First pass: $x \in ABC$ $fd\underline{1}$ $X \in ABCDE$ fd3 $X \in ABCDE$ all attributes hence X will change any more (AB)+ = 4 ABCDEY AB is a SK of R. Is it a candidate Key? Closure of attr. can help us find CKs of a relation: Compute hart land 413iyt

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Closure of set of FDs Given a set of FDs, its closure It is the set of all FDs derived from f. 1=/ A >B A > C E f+ \ \ B→C Two sets A&B of FDs are equivalent iff. A = B + $\begin{cases} A \rightarrow B \\ B \rightarrow C \end{cases} = \begin{cases} A \rightarrow B \\ A \rightarrow C \end{cases}$

Ne can easily test if $X \Rightarrow Y \in f^+$ $X \Rightarrow Y \in f^+$ iff $Y \subseteq X^+$ using f.

 Basis of a relation

Given a relation R and FDs f we say that any set g s.t. ft = gt is a basis of R.

Minimal Basis of FDs. (3.2.7)

Any relation R has many equivalent set of FDs. (many basis-es)

To avoid an exposion of FDs we usually use a minimal basis

A minimal basis B of a relation R is a basis of R s.t.

- 1) All FDs in Bare in canonical form
- 2) If for any FD we remove one or more aftr. from the left hand side the result is no longer a basis,
- 3) If any FD is removed from B, the result is no longer a basis

ls A a minimal K. with pasis a A= \(B > A \\ C > B \) C -> A 6 C -> B AB -> C <u>8</u>9 AC >B BC->A GNEN FDs in A, can we generate FDs in B? (1), (3), (4), (6) already in A. Can we generate (2), (5), (5), (6)? $\langle A \rangle^+ = \langle A B c \rangle$ > 2 can be generated, and also 3, 8 by using augmentation. (or compute 1AByt, 4ACyt) (5?(13+=4CBA) > yes (3) and 9 (augmentation) can be generated. So from A we can generate B. Hence A is a basis of R

Bis also a basis of R with fds A

BCA

subset

Is A minimal?

- · Can we drop $A \rightarrow B$? $A \rightarrow B$ be generated from $C \rightarrow B$ $B \rightarrow C$ $A \rightarrow B$ so $P \rightarrow B$ cannot be remared.
 - Com we drop B > A?

 B > A be generated from C > B

 B > C

 B > C

 B > C

 B C , so ro, it can not be removed.
 - · Repeat for C→B and B→C.

 Yes, A is minimal

Another Example. Compute its minimal basis 1) Write in caronical form OAC>D OA>C (S) C>D (2) AD >> C (4) A >> D 2) Remove redundant attr. for LHS Test A in (1) Can we generate A form c? 1 cy+ = CD ' 100 Can we generate c form A: 4A7+ = AC... yes Drop (from @ > A > D. (Replace 1) Can us generate A form Di? NO Can we genrate D fam A? Ges. ⇒ A → C (Replace (2))

Now we have. 3 A→C 3 C→D (1) A -> D (2) A -> C (4) A -> D 3 Remove redundant FDr. 1) and 2) are obviously redundant. -> Perrose. can 3 be seweted from 4,5? No. Verp. Can 4 be genrated form (36)? Yes. Remove. can & be generated from 3? No. Veep. Minimal Basis

 $\begin{array}{ccc} \textcircled{3} & A \rightarrow C \\ \textcircled{5} & C \rightarrow D \end{array}$

Projection of FDs (3.2.8) aven R and set F of FDS The projection of Fon R1=TLK is the set of FDs that follows from F that involve only attributes in R1. Algorithm: $T \leftarrow \emptyset$ for each subset X EL compute \(\int \) to every attribute A in \(\int \chi \) \(\int \) add X > A to T iff A E L and A & X (nontrivial)

 $F = \begin{pmatrix} A \rightarrow B \\ B \rightarrow C \\ C \rightarrow D \end{pmatrix}$ Ex: R(ABCD) Compute FDs of MACD R A C D D XXX D XX C D XX D D D D D 3) Remove RHS att not in L. 4) Remove trivial For Result: / AC → D AD → C $A \rightarrow C$ $A \rightarrow D$ $C \rightarrow D$ Is it a minimal basis? No A => D] can be A C => D] generated from \ C => D] A D => C) Prove it!!

Design of Relational DBs (3.3)t: +le 977 Star Wars 124 Sci Fi Fox Carry Fisher Star Wars 977 124 Sci Fi Fox Mark Homill Star Wars 977 124 Sci Fi Fox Harrison Ford 972 The God father 175 Robert Duvall Drama Paramount 972 The God father 175 Marlon Brandon Drama Paramount

FDs: title, year -> length, studio Name

War

Zoetrope

Marlon Brandon

153

1953

Anomalies

Apocalyte Now

- · Redundancy: Unnecessary repeated
- · Update anomalies: If we change one typle we might have to change another: Ex: change length of a movie.
 - · Deletion anomalies: If we delete a typle we might lose other info: Ex: Pensore M. Brandon from Ap. Now.

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Decomposing Relations To deal with anomalies we decompose relations.

Given $R(A_1...A_n)$ a decomposition into $S(B_1...B_m)$ and $T(C_1...C_k)$ s.t.

1) {A, ... An } = 1B, .. Bm } U 1 C1 ... Cx }
and

2) S = TB1...Bm & and T = TC1...CK &

We can decompose Movies into S(title, year, length, genre, statio Name)

T (title, year, star Name)

Call this Movies 2

		Ja.	
1 title	Ye ar	s _y a,	
Star Wars	1977	Carry Fisher	
Star Wars	1977	Mark Homill	$=$ \top
Star Wars	1977	Harrison Ford	٠.
The Godfather	1972	Robert Duvall	
The God ather	1972	Marlon Brandon	
Apocalyse Now	1953	Marlon Brandon	
l ' '	ı	1	ı

Call this Movies 3

Good de compositions.

Green a relation R we want to decompose it into two relations S and T s.t.

- 1) P = SMT lossless join
- 2) The projection of FDs Fr of R into S (F's) and T (FT)

sorts fies:
$$(F_S \cup F_T)^+ = F_R^+$$

Dependency preserving.

Boyce Codd Normal Form (BCNF)

A relation R is in BCNF iff
for every FD

A...An > B...Bm

A...An > B...Bm

A...An is a Superkey.

GB...Bm) S/AI...An) (it is trivial.

£x;

Movies is not BCNF

title, year -> lenght, studio Name
is a not a SK of Movies

If a relation R:s not BCNF then decompose into relations R... Rn s.t R, \bowtie Rz... \bowtie Rn = R \Rightarrow Loss-less join decomposition.

Algorithm to de compose into BCNF relations

Given R and set F of FDs:

R is not BCNF.

1) Choose one FD X > Y not in BCNF 2). De compose:

$$P_{i} = \sqrt{\times j^{+}} \times \Rightarrow Y$$

$$P_{2} = \times \cup (P - P_{i})$$

- 3) Compute FDs for R, and Bz (projection of FDs of R into P1, P2)
- 4) If R1 or R2 are not BCNF recursively decompose.

Guaranteed to be lossless join but not FD preserving.

Any non BCNF relation has a BCNF loss-less join decomposition but not a BCNF FD preserving de composition. Ex: e(TCH) $H \rightarrow C$ TC 9H. not BCNF. H-> C HU 1TCH-HC3 4 H3+= HC

any 2 att rel 7. HT FDs FDs is BCNF HC HC HT HTC -H H2

111 $H \rightarrow C$ R1 = HC FD1 = 1 H-3C) De composition P= HT FD2= 0 Not FD preserving lost TC >H.

3rd Normal Form (3NF)

If we cannot decompose a relation into BCNF relations that are FD preserving we are happy if they can be decompose into 3NF relations.

Any relation R with a set of FDs F has a 3NF decomposition that is loss-less join and FD preserving.

Δ relation R with FDs Fisin 3NF

if for every FD

A1...An → B1...Bm

- · it is a: SK or for all
- · C ∈ {B₁...B_m} is either C ∈ {A₁...A_n}

er C is part of some candidate key.

Ex: B(ABCDE) Isit 3NF? AB -> C AB rota Sk. is C partofa Ck? Need to compte candidate keys of R · Heuristic: AE never on righthand side of > always part of a key Use closure of attr. to compute SKs. all combination of atter. closure AE BCD AEBCD BC BP AE BC D AE BD C AE all SK. AEB C D AECDB AECBD AED AED . > Candidate Keyr. JAEC

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Back to testing if Ris 3NF.

AB > C cis part of CK. V

C > B Cis not SK. but

B is part of CK.

A > D A is not SK.

D is not part of CK

>> 2 is not 3NF.

Decomposition of a Relation into 3NF relations that is loss-less join and FD preserving: (Synthesis alg 3.5.2)

Given R with set of FDs F

- 1) Find G, a minimal basis of F
- 2) For each FD A...An → B in G.
 add a relation with schema
 A...An B with FD

 $A_1 \dots A_N \rightarrow B$

3) If none of the added relations in step 2 is a SK of R (i.e. does not contain a candidate key of R) then add another relation whose schema is a key of R.

4) Simplify: if the attributes of a subrelation are a subset of another subrelation => merge them.

i.e. delete subset relation and add its FDs to other relation.

120 = AD

None of them contains a SK.

(see previous exercise, you can verify it by computing 42:3t)

We know its begs are AEB and AEC We need only one. So add

with A >D

R4=AEB with no FDs.

But Re is a subset of R1

So we merge them?