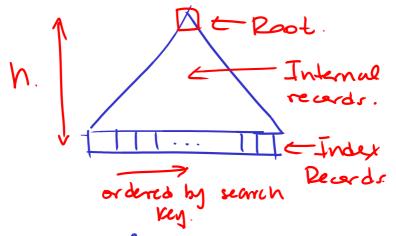
Indexer.

B+-tree

- · Atomakcally Balanced
- · Finder records are at the leaver



- · Every record is a block.
- · Index records from a list
- . They can be traversed in the order of the search key

Internal records

n+1

pointers

ki kz ... kny kn

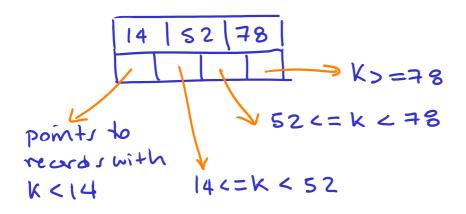
key r.

to other

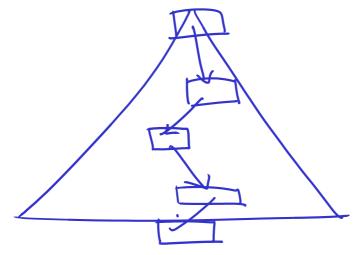
index records.

Example.

Assume n = 3



Index is traversed from not to leaf



We assume noot is always in memory hence, to reach the leaf we read h blocks. Cost of index:

· Cost of reaching the leafs

· Cost of reading the matching records.

Example:

1) Asame Pla, b)

Ta = 5 R

Only one or zero matching tyle:

⇒ We must traverse the index h

rhe leaf either cantains a = 5 or not

Cost of index = h of index.

2) Jaro R

What if all types match?

· We traverse index (cost h)

Reads first leaf.

· We must read all leaves of

Cost of index = h + # leaver -1

To be able to compute the cost of an index we need:

Calalate # of leaf blocks of index proportional to # index records per block.

of Mdex records depends your a) type of index Sparse ss. Dense

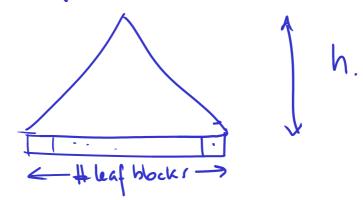
b) Number of types in Rel.

index reards per block depends upon:

- a) size of search lay
- b) occupancy rate =) How much waste space is there in the index (to keep it balanced).

We assume that occupancy rate of inner rodes and leaves is the same as internal rodes.

Hence, height of tree depends upon # of leaf records.



n = max number of search records per block

fill = occupancy rate (between 0-1, but usually around 1/2 to 3/4)

#leaf blocks = [# index records]

For h, we simplify calculations:

Example:

Assume
$$n = 150$$
, $fill = \frac{2}{3}$

How many index records can we store in an index of height 1,2,3,4,5,6.

Let is wary about max # index Records

h # index Peard ()

1 100 =
$$10^2$$

2 100² = 10^4

3 100³ = 10^6

4 100⁵ = 10^9

With 5 block reads we can find a leaf with a given search key in an index of 10 giga-records!!

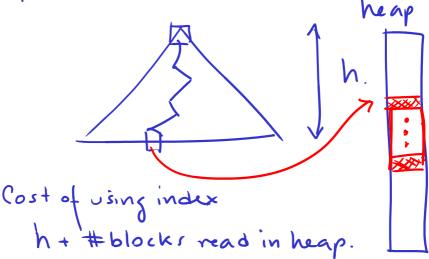
How many search lays do we need to store?

- · Sparse index: B(R)
- · Dense index: [R]

Sparse index is marginally shorter than dense index.

Cost of Using an Index

Sparce Index.



- · We only read one record in index
 - · We read 1 or more blocks from heap

Example.

a)
$$O_{\alpha} = s R$$
 Got = h+1.

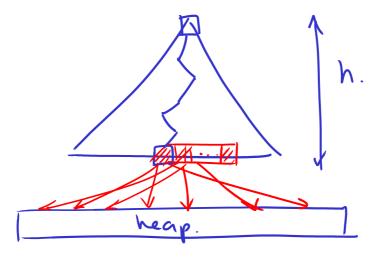
Read block in heap to determine if tiple exists

Assume 50% of tiples match gueny:

Cost = h + B(R)

$$B(R) = \frac{10^6}{10} = \frac{10^5}{2}$$

Dense Index.



Cost:

- · Traverse tree to first leaf: h · Might need to read Ø or more leafs.
- · For every type in result, read one block.

Example.

$$R(a,b)$$
 $|R| = 10^6$ tuples.
heap: 10 tuples per block
Dense index on $R(a)$
Effective index records per block: 100
 $h = 4$ $|B| = 10^5$ blocks.

a)
$$0_{a=s}$$
 R

if type exists: cost = h+1.

if type does not exist: cost = h.

b) Ta>10 R Assume 50% of types match.



We need to scan 50% of them.

#block: in index =
$$\left[\frac{\text{# matching types}}{\text{n. fill}}\right]$$

= $\frac{.5 \cdot 10^6}{10^2}$ = .5.10⁴

$$Cost = h - 1 + 0.5 \cdot 10^4 + 10^6$$
 $\approx 10^6!!$

Approximately 10 times more than Sparse index!

How do we know how many tipler match a given greng?

selectivity (p) = probability that a type in R matches predicate P.

Selectivity of matching a primary Key: Selections of matching a nonprimary vey: We need a distribution. value of search We need to compute proportion of the tuples that match the predicate. Example: R(g,b) · Relation a mitem distribution of · Assume valer of b, min 1, max 100. Selectify (b = 10) = 100.

Selection (b>20) = 19 Selection ty (b>20 and b<30) = 9 Selectivity (b>200) = Ø