

eduPIC: an introductory particle based code for radio-frequency plasma simulation MANUAL

Zoltán Donkó, Aranka Derzsi, Máté Vass, Benedek Horváth,
Sebastian Wilczek, Botond Hartmann, Peter Hartmann

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1 Introduction

eduPIC is an open source “starting tool” that intends to assist the education and research of those interested in particle based plasma simulations. Our intention has been to keep this code as simple and as transparent as possible; optimization and further development is left for the interested readers. Therefore, the code that we provide has a length of ~ 1000 lines, in a single file. Besides the "simulation core" the code includes some discharge diagnostics features, which can be further expanded.

The code focuses on Capacitively Coupled Plasmas (CCPs) and is based on the Particle-in-Cell/Monte Carlo Collisions (PIC/MCC) technique – an introduction to this technique and the description of the physical basis of the eduPIC code has been provided in [1] and is not repeated in this Manual. For a complete understanding of the operation of the code the description of the code parts provided in this Manual should be simultaneously studied with the respective parts of Ref. [1].

The code is of the type "1d3v", meaning that the physical setting assumes a 1-dimensional spatial variation of the discharge characteristics (within a bounded space), while the particles are traced in the 3-dimensional velocity space. The code includes a basic cross section set for argon (Ar) gas, see [1], discharges in other gases can be simulated with a proper change of the cross section set.

2 Usage

2.1 Compilation

The eduPIC C code has been tested on an Ubuntu Linux computing cluster on nodes equipped with x86-64 based Intel® Xeon and AMD® Threadripper CPUs. The compilation of the C code can be performed with both `icpc` Intel C++ compiler (ver. 2021.1.2, part of the freely available Intel oneAPI Base Toolkit) and `g++` from the GNU Compiler Collection (ver. 9.3.0). Best performance was achieved on Intel architecture using:

```
icpc -fast -o edupic eduPIC.cc
```

2.2 Program execution and files created

The code can be invoked in a terminal window as

```
./edupic arg1
```

To start a new simulation, running an initialization cycle is required by setting `arg1` to 0, i.e. executing

```
./edupic 0
```

In this case, seeding of a number of initial particles (1000 of both species, as default), the simulation of a single radio-frequency (RF) cycle and saving of the state of the system (to a binary file `picdata.bin`) is executed.

The code can be run, subsequently, for any number of additional RF cycles specified by `arg1`, e.g., for 500 cycles, as

```
./edupic 500
```

In this run, the previously saved state of the system is restored, the given number of RF cycles is simulated, and at the end of the run, the state of the system is saved. This procedure can be repeated any number of times, the simulation always continues from the previously saved state of the system. During these runs, the time evolution of the number of superparticles is stored in a file named `conv.dat`, but no other data (results) are saved. The content of this file is illustrated in figure 1 for the reference conditions listed in table 1. The code simulates a CCP driven by a single-frequency excitation voltage waveform.

Table 1: Set of “default” parameters for the reference simulation run. (The parameters have these values in the code that can be downloaded.)

Quantity	Symbol	In the code	Value
Driving voltage amplitude	V_0	VOLTAGE	250 V
Driving frequency	f	FREQUENCY	13.56 MHz
Superparticle weight	W	WEIGHT	7×10^4
Electrode gap	L	L	25 mm
Ar pressure	p	PRESSURE	10 Pa
Gas temperature	T_g	TEMPERATURE	350 K
Number of grid points	N_g	N_G	400
Number of time steps / RF cycle	N_t	N_T	4000

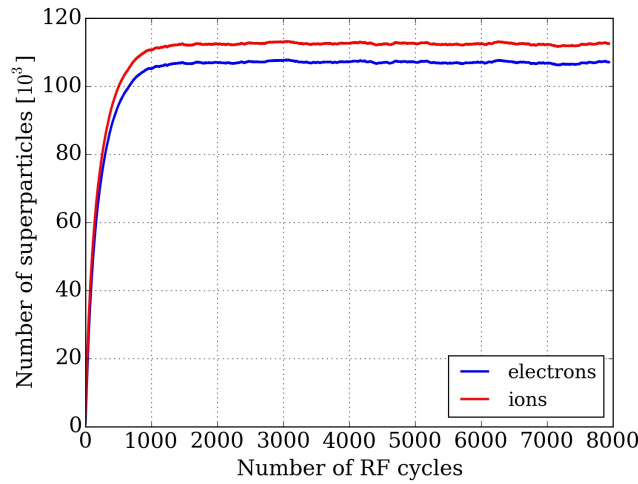


Figure 1: The number of superparticles as a function of the number of RF cycles (file: `conv.dat`). Discharge conditions: argon $p = 10$ Pa, $L = 25$ mm, $T_g = 350$ K, $V = 250$ V and $f = 13.56$ MHz [1].

As one can observe in figure 1, the number of superparticles grows in the simulation from the initial value of 1000 to $\approx 110\,000$ during ~ 1500 RF cycles. The number of RF periods to reach convergence depends strongly on the discharge conditions (e.g., pressure, electrode gap).

Measurements on the system should be executed only after reaching convergence. The measurement mode can be activated by specifying a second command line argument `m` when the code is invoked, e.g., a measurement for 1000 RF cycles is carried out as

```
./edupic 1000 m
```

Here, all built-in diagnostics are turned on. The number of RF cycles for which measurements are run affects the quality of the statistics of the results. Therefore, we recommend using at least ~ 1000 RF cycles to obtain results with good signal to noise ratio. When measurements on the system are taken, the code saves the data into the files listed in table 2.

<code>density.dat</code>	Time-averaged density distributions of electrons (second column) and ions (third column) as a function of the position (first column)
<code>eepf.dat</code>	Time-averaged EEPF in the central 10% spatial domain of the discharge (second column) as a function of the energy (first column). The data are normalized corresponding to (the discretized form of) $\int f(\varepsilon)\sqrt{\varepsilon}d\varepsilon = 1$
<code>ifed.dat</code>	Time-averaged IFEDF at the powered (second column) and grounded (third column) electrode as a function of the energy (first column). The data are normalized corresponding to (the discretized form of) $\int F(\varepsilon)d\varepsilon = 1$
<code>pot_xt.dat</code>	Spatio-temporal distribution of the potential
<code>efield_xt.dat</code>	Spatio-temporal distribution of the electric field
<code>ne_xt.dat</code>	Spatio-temporal distribution of the electron density
<code>ni_xt.dat</code>	Spatio-temporal distribution of the ion density
<code>je_xt.dat</code>	Spatio-temporal distribution of the electron current density
<code>ji_xt.dat</code>	Spatio-temporal distribution of the ion current density
<code>powere_xt.dat</code>	Spatio-temporal distribution of the power absorption by the electrons
<code>poweri_xt.dat</code>	Spatio-temporal distribution of the power absorption by the ions
<code>meanee_xt.dat</code>	Spatio-temporal distribution of the mean electron energy
<code>meanei_xt.dat</code>	Spatio-temporal distribution of the mean ion energy
<code>ioniz_xt.dat</code>	Spatio-temporal distribution of the ionization rate

Table 2: Data files created by the eduPIC code in “measurement” mode.

The “xt files” that store the spatio-temporal variation of the given quantities contain a number of rows equal to the number of spatial grid points N_G . The number of columns represents the temporal variation of these quantities. In order to improve the signal to noise ratio of the data, the number of time steps per RF cycle, N_T , is binned to a lower number, N_{XT} . The number of time steps binned for the xt files can be set by the variable N_{BIN} in the code.

Care should be taken to ensure that (i) N_T is an integer multiple of N_{BIN} and that (ii) N_{BIN} is an integer multiple of N_{SUB} . This latter requirement ensures that information is gathered into each element of the xt matrices for the same number of ion time steps.

All the output data are in SI units, except for the mean electron energy, as well as for the EEPF and the IFEDF, for which eV units are used.

Following a run in the “measurement” mode, the code saves a file named `info.txt`. This file contains the operation parameters and simulation settings as a record of the run. The file also displays information about the stability and accuracy conditions. First, the conditions concerning the relation of the grid spacing to the Debye length, the relation of the time step to the electron plasma frequency, and the collision probabilities during a time step.

Whenever any of these checks fail, an error message is issued and no further diagnostics data are saved. It is very important to realise that the evaluation of the stability and accuracy criteria is meaningful only when measurements are taken over the converged state. The initial setting of the simulation parameters (like the grid size and the number of the time steps) is normally based on an educated guess, these parameters can be refined later according to the information contained in `info.txt`. In case of need of modifications of the parameter settings, the code has to be re-compiled, the simulation has to be re-converged, and the stability and accuracy criteria have to be checked again.

In case the above conditions are met, the diagnostics data listed above are saved to the respective files, and the maximum electron energy for which the Courant–Friedrichs–Lewy condition still holds at the actual values of N_G and N_T , is also displayed in `info.txt`. To make sure that this condition holds for the *vast majority* of the electrons, one has to confirm that the EEPF decays to a small value at this energy. This is not done automatically in the code, the procedure is left to the user. We advise to observe the EEPF obtained in the center of the plasma, and to use a threshold value of $f(\varepsilon) \sim 10^{-6} \text{ eV}^{-3/2}$. For a more rigorous check, the complete space- and time-resolved EEPF should be considered.

Additional information about the particle characteristics at the electrodes and about the power absorption by

the electrons and ions is also saved to `info.txt` at the end of the simulation. The latter is computed as the spatial and temporal average of the product $j(x,t)E(x,t)$. This product is also saved to the files `powere_xt.dat` and `poweri_xt.dat` (corresponding to the power absorption rate by the electrons and ions, respectively) with spatial and temporal resolution.

Without any change to the code (including the parameter settings) the simulation should result the same data as plotted in figures 10–13 of [1]. Such a "test run" is recommended in order to get acquainted with the compilation and the running of the code to the converged state, and to carry out measurements.

3 Description of the code

Below, we provide a detailed description of the individual parts of the eduPIC code. No additional explanation is given in the cases where variables or operations are explained by comments in the code lines.

Inclusion of the header files required.

```
1 #include <stdio>
2 #include <stdlib>
3 #include <string>
4 #include <stdbool>
5 #include <cmath>
6 #include <ctime>
7 #include <random>
```

Defining the default function name space

```
1 using namespace::std;
```

Declaration of mathematical and physical constants.

```
1 const double PI = 3.141592653589793; // mathematical constant Pi
2 const double TWO_PI = 2.0 * PI; // two times Pi
3 const double E_CHARGE = 1.60217662e-19; // electron charge [C]
4 const double EV_TO_J = E_CHARGE; // eV <-> Joule conversion factor
5 const double E_MASS = 9.10938356e-31; // mass of electron [kg]
6 const double AR_MASS = 6.63352090e-26; // mass of argon atom [kg]
7 const double MU_ARAR = AR_MASS / 2.0; // reduced mass of two argon atoms [kg]
8 const double K_BOLTZMANN = 1.38064852e-23; // Boltzmann's constant [J/K]
9 const double EPSILON0 = 8.85418781e-12; // permittivity of free space [F/m]
```

Declaration of constants that control the execution of the simulation. These include the discharge conditions (frequency, voltage, pressure, electrode gap and temperature), as well as the resolution of the temporal and spatial grids, the superparticle weight, the electrode area assumed in the simulation as well as the number of electron and ion superparticles that are seeded within the discharge gap upon the initialization of the simulation. The electrode area is needed only to connect the number of superparticles and the density of the real particles, see [1]. The number specified here (1 cm², in line 9) should be kept unchanged.

```
1 const int N_G = 400; // number of grid points
2 const int N_T = 4000; // time steps within an RF period
3 const double FREQUENCY = 13.56e6; // driving frequency [Hz]
4 const double VOLTAGE = 250.0; // voltage amplitude [V]
5 const double L = 0.025; // electrode gap [m]
6 const double PRESSURE = 10.0; // gas pressure [Pa]
7 const double TEMPERATURE = 350.0; // background gas temperature [K]
8 const double WEIGHT = 7.0e4; // weight of superparticles
9 const double ELECTRODE_AREA = 1.0e-4; // (fictive) electrode area [m^2]
10 const int N_INIT = 1000; // number of initial electrons and ions
```

Additional constants derived from the parameters specified above. `DT_E` and `DT_I` are the time steps of electrons and ions. `DT_E` is also the basic time step of for the PIC/MCC cycle (shown in figure 2). The two time steps are related via the subcyclng parameter `N_SUB`: ions are treated only in every `N_SUB`-th time step, which is possible due to their higher mass with respect to the electrons. Subcyclng accelerates the computation considerably. The same time step for electrons and ions is recovered at `N_SUB=1`. Too large values for `N_SUB` are to be avoided as the accuracy of the calculations can degrade when ions are not treated frequently enough (see the stability and accuracy criteria discussed in [1]).

DX is the division of the (uniform) computational grid. The inverse of this quantity INV_DX is also defined here as in many cases division by DX is required in the computations. In these cases, the computationally more efficient operation of multiplication by INV_DX is carried out.

```

1 const double PERIOD      = 1.0 / FREQUENCY;           // RF period length [s]
2 const double DT_E        = PERIOD / (double)(N_T);    // electron time step [s]
3 const int     N_SUB      = 20;                       // ions move only in these
   cycles (subcycling)
4 const double DT_I        = N_SUB * DT_E;              // ion time step [s]
5 const double DX          = L / (double)(N_G - 1);    // spatial grid division [m]
6 const double INV_DX      = 1.0 / DX;                 // inverse of spatial grid size
   [1/m]
7 const double GAS_DENSITY = PRESSURE / (K_BOLTZMANN * TEMPERATURE); // background gas density [1/m
   ^3]
8 const double OMEGA       = TWO_PI * FREQUENCY;       // angular frequency [rad/s]

```

Some important constants related to the cross sections of elementary processes and declaration of arrays for the cross section data. Lines 1–6 define the number of elementary processes considered (in this case 5) and the identifiers of these processes. Lines 7–8 specify the energy thresholds for the inelastic electron - Ar atom collision processes, while in lines 9–14 the data structures for the storage of cross section data are declared.

```

1 const int     N_CS        = 5;                       // total number of processes / cross sections
2 const int     E_ELA       = 0;                       // process identifier: electron/elastic
3 const int     E_EXC       = 1;                       // process identifier: electron/excitation
4 const int     E_ION       = 2;                       // process identifier: electron/ionization
5 const int     I_ISO       = 3;                       // process identifier: ion/elastic/isotropic
6 const int     I_BACK      = 4;                       // process identifier: ion/elastic/
   backscattering
7 const double  E_EXC_TH    = 11.5;                   // electron impact excitation threshold [eV]
8 const double  E_ION_TH    = 15.8;                   // electron impact ionization threshold [eV]
9 const int     CS_RANGES   = 1000000;                // number of entries in cross section arrays
10 const double  DE_CS       = 0.001;                  // energy division in cross section arrays [eV]
11 ]
12 typedef float cross_section[CS_RANGES];              // cross section array
13 cross_section sigma[N_CS];                            // set of cross section arrays
14 cross_section sigma_tot_e;                             // total macroscopic cross section of
   electrons
15 cross_section sigma_tot_i;                             // total macroscopic cross section of ions

```

Declaration of the `particle_vector` type for arrays that store the space and velocity coordinates of the various particles. These arrays have a size `MAX_NP`, this is the maximum number of superparticles. `N_e` and `N_i` are the actual numbers of the electron and ion superparticles (initialized with zero values). These values should never exceed `MAX_NP` during the simulation runs.

```

1 const int     MAX_N_P     = 1000000;                 // maximum number of particles (electrons /
   ions)
2 typedef double particle_vector[MAX_N_P];              // array for particle properties
3 int           N_e         = 0;                       // number of electrons
4 int           N_i         = 0;                       // number of ions
5 particle_vector x_e, vx_e, vy_e, vz_e;               // coordinates of electrons (one spatial,
   three velocity components)
6 particle_vector x_i, vx_i, vy_i, vz_i;               // coordinates of ions (one spatial, three
   velocity components)

```

Declaration of the spatial grid and the quantities calculated at the points of this grid. `efield`, `potential`, `e_density`, and `i_density` store the values of the electric field, the potential, the electron density, and the ion density, respectively, in the given time step. `cumul_e_density` and `cumul_i_density` accumulate the electron and the ion density during the simulation run and are used for the computation of the time averaged values of these quantities (via dividing them by the number of time steps of the whole simulation) at the saving of these data to the file `density.dat` by the function `save_density()` (see later).

```

1 typedef double xvector[N_G];                         // array for quantities defined at grid points
2 xvector        efield, pot;                          // electric field and potential
3 xvector        e_density, i_density;                  // electron and ion densities
4 xvector        cumul_e_density, cumul_i_density;      // cumulative densities

```

Counters for the electrons and ions that reach the powered and grounded electrodes during the simulation run. These quantities can be used for the calculation of particle fluxes to the electrodes.

```

1 typedef unsigned long long int Ullong;                // compact name for 64 bit unsigned integer
2 Ullong         N_e_abs_pow = 0;                       // counter for electrons absorbed at the
   powered electrode
3 Ullong         N_e_abs_gnd = 0;                       // counter for electrons absorbed at the
   grounded electrode
4 Ullong         N_i_abs_pow = 0;                       // counter for ions absorbed at the powered
   electrode
5 Ullong         N_i_abs_gnd = 0;                       // counter for ions absorbed at the grounded
   electrode

```

Declaration of the quantities needed for the calculation of the electron energy probability function (EEPF). Data for this function are accumulated in the array `eepf`, which is initialized with zero values, accumulates data during the simulation run, and is normalized properly upon saving of the data by the function `save_eepf()` (see later).

```
1 const int      N_EEPF = 2000;                // number of energy bins in Electron Energy
    Probability Function (EPPF)
2 const double  DE_EEPF = 0.05;               // resolution of EEPF [eV]
3 typedef double eepf_vector[N_EEPF];         // array for EEPF
4 eepf_vector eepf = {0.0};                   // time integrated EEPF in the center of the
    plasma
```

Declaration of the quantities needed for the calculation of the ion flux-energy distribution (IFED) function. Data for this function are accumulated in two arrays corresponding the two electrodes (`ifed_pow` and `ifed_gnd`), which are normalized properly upon saving of the data. The values of the mean energy of the ions reaching both electrodes are also derived from these functions in the function `save_ifed()` (see later).

```
1 const int      N_IFED = 200;                // number of energy bins in Ion Flux-Energy
    Distributions (IFEDs)
2 const double  DE_IFED = 1.0;               // resolution of IFEDs [eV]
3 typedef int    ifed_vector[N_IFED];         // array for IFEDs
4 ifed_vector ifed_pow = {0};                // IFED at the powered electrode
5 ifed_vector ifed_gnd = {0};                // IFED at the grounded electrode
6 double        mean_i_energy_pow;           // mean ion energy at the powered electrode
7 double        mean_i_energy_gnd;           // mean ion energy at the grounded electrode
```

Declarations related to the data for the spatio-temporal maps, which are computed for several discharge characteristics. These data reside in two-dimensional arrays, which are initialized with zero values. The number of grid points in space is the same as for the main simulation grid (`N_G`), the number of grid points in time is reduced with respect to the number of time steps (`N_T`) by a factor of `N_BIN`. This binning can optimise the trade-off between time-resolution and signal to noise ratio of the data.

```
1 const int N_BIN = 20;                      // number of time steps binned for the XT
    distributions
2 const int N_XT = N_T / N_BIN;              // number of spatial bins for the XT
    distributions
3 typedef double xt_distr[N_G][N_XT];        // array for XT distributions (decimal numbers)
4 xt_distr pot_xt = {0.0};                   // XT distribution of the potential
5 xt_distr efield_xt = {0.0};                // XT distribution of the electric field
6 xt_distr ne_xt = {0.0};                    // XT distribution of the electron density
7 xt_distr ni_xt = {0.0};                    // XT distribution of the ion density
8 xt_distr ue_xt = {0.0};                    // XT distribution of the mean electron
    velocity
9 xt_distr ui_xt = {0.0};                    // XT distribution of the mean ion velocity
10 xt_distr je_xt = {0.0};                    // XT distribution of the electron current
    density
11 xt_distr ji_xt = {0.0};                    // XT distribution of the ion current density
12 xt_distr powere_xt = {0.0};                // XT distribution of the electron powering (
    power absorption) rate
13 xt_distr poweri_xt = {0.0};                // XT distribution of the ion powering (power
    absorption) rate
14 xt_distr meanee_xt = {0.0};                // XT distribution of the mean electron energy
15 xt_distr meanei_xt = {0.0};                // XT distribution of the mean ion energy
16 xt_distr counter_e_xt = {0.0};             // XT counter for electron properties
17 xt_distr counter_i_xt = {0.0};             // XT counter for ion properties
18 xt_distr ioniz_rate_xt = {0.0};            // XT distribution of the ionisation rate
```

Declaration of additional variables for diagnostics and program control purposes. Lines 1–2 contain variables that allow computation of the mean energy of the electrons in the centre of the discharge gap. `N_e_coll` and `N_i_coll` count the total number of collision of electron and ion superparticles, these are used in the computation of the collision frequencies of the two species. The variables in line 6 are used in the `main()` function of the code. The Boolean flag `measurement_mode` allows data collection (measurements on the system) when it is set to `true`. Measurements should be carried out only after reaching the converged state of the simulation.

```
1 double        mean_energy_accu_center = 0; // mean electron energy accumulator in the
    center of the gap
2 Ullong        mean_energy_counter_center = 0; // mean electron energy counter in the center
    of the gap
3 Ullong        N_e_coll = 0;                 // counter for electron collisions
4 Ullong        N_i_coll = 0;                 // counter for ion collisions
5 double        Time;                         // total simulated time (from the beginning of
    the simulation)
6 int           cycle, no_of_cycles, cycles_done; // current cycle and total cycles in the run,
    cycles completed
7 int           arg1;                         // used for reading command line arguments
8 char          st0[80];                      // used for reading command line arguments
9 FILE          *datafile;                    // used for saving data
10 bool          measurement_mode;             // flag that controls measurements and data
    saving
```

The code utilizes the Mersenne Twister (MT) 19937 random number generator (RNG), included in the C++ standard library (beginning with version C++ 11). The same RNG is used to generate random samples (i) from the uniform distribution on the [0,1) interval for several purposes, and (ii) from the normal distribution for assigning velocity components of background gas atoms in thermal equilibrium (Maxwell-Boltzmann distribution), when potential collision partners have to be selected in the case of ion-atom collisions. The MT generator is initialized with the standard C++ random device.

```

1 //-----//
2 // C++ Mersenne Twister 19937 generator //
3 // R01(MTgen) will generate uniform distribution over [0,1) interval //
4 // RMB(MTgen) will generate Maxwell-Boltzmann distribution (of gas atoms) //
5 //-----//
6
7 std::random_device rd{};
8 std::mt19937 MTgen(rd{});
9 std::uniform_real_distribution<> R01(0.0, 1.0);
10 std::normal_distribution<> RMB(0.0, sqrt(K_BOLTZMANN * TEMPERATURE / AR_MASS));

```

Pre-calculation and filling of the cross section arrays for the electrons. The calculation is based on the analytic forms provided by Phelps and Petrović [2]. This set includes the elastic momentum transfer cross section, one (lumped) excitation cross section that represents the sum of all excitation cross sections, and the ionization cross section. The data are stored in the arrays in units of m^2 , as a function of the energy of the electron in the laboratory frame. The energy resolution of the data is DE_CS.

Via storing the data in pre-calculated arrays one can avoid the need for evaluating very frequently the quite complicated analytic forms, this way improving computational efficiency.

```

1 //-----//
2 // electron cross sections: A V Phelps & Z Lj Petrovic, PSST 8 R21 (1999) //
3 //-----//
4
5 void set_electron_cross_sections_ar(void){
6     int i;
7     double en, qmel, qexc, qion;
8
9     printf(">> eduPIC: Setting e- / Ar cross sections\n");
10    for(i=0; i<CS_RANGES; i++){
11        if (i == 0) {en = DE_CS;} else {en = DE_CS * i;} // electron energy
12        qmel = fabs(6.0 / pow(1.0 + (en/0.1) + pow(en/0.6, 2.0), 3.3)
13                - 1.1 * pow(en, 1.4) / (1.0 + pow(en/15.0, 1.2)) / sqrt(1.0 + pow(en/5.5, 2.5) + pow(en
14                /60.0, 4.1)))
15                + 0.05 / pow(1.0 + en/10.0, 2.0) + 0.01 * pow(en, 3.0) / (1.0 + pow(en/12.0, 6.0));
16        if (en > E_EXC_TH)
17            qexc = 0.034 * pow(en-11.5, 1.1) * (1.0 + pow(en/15.0, 2.8)) / (1.0 + pow(en/23.0, 5.5))
18                + 0.023 * (en-11.5) / pow(1.0 + en/80.0, 1.9);
19        else
20            qexc = 0;
21        if (en > E_ION_TH)
22            qion = 970.0 * (en-15.8) / pow(70.0 + en, 2.0) + 0.06 * pow(en-15.8, 2.0) * exp(-en/9);
23        else
24            qion = 0;
25        sigma[E_ELA][i] = qmel * 1.0e-20; // cross section for e- / Ar elastic collision
26        sigma[E_EXC][i] = qexc * 1.0e-20; // cross section for e- / Ar excitation
27        sigma[E_ION][i] = qion * 1.0e-20; // cross section for e- / Ar ionization
28    }
29 }

```

Pre-calculation and filling of the cross section arrays for the argon ions. The calculation is based on the analytic forms provided by A. V. Phelps [3]. The data are stored as a function of the energy in the centre-of-mass reference frame, in units of m^2 . The energy resolution of the data is DE_CS.

```

1 //-----//
2 // ion cross sections: A. V. Phelps, J. Appl. Phys. 76, 747 (1994) //
3 //-----//
4
5 void set_ion_cross_sections_ar(void){
6     int i;
7     double e_com, e_lab, qmom, qback, qiso;
8
9     printf(">> eduPIC: Setting Ar+ / Ar cross sections\n");
10    for(i=0; i<CS_RANGES; i++){
11        if (i == 0) {e_com = DE_CS;} else {e_com = DE_CS * i;} // ion energy in the center of
12        mass frame of reference // ion energy in the laboratory
13        e_lab = 2.0 * e_com; // ion energy in the laboratory
14        frame of reference
15        qmom = 1.15e-18 * pow(e_lab, -0.1) * pow(1.0 + 0.015 / e_lab, 0.6);
16        qiso = 2e-19 * pow(e_lab, -0.5) / (1.0 + e_lab) + 3e-19 * e_lab / pow(1.0 + e_lab / 3.0, 2.0);
17        qback = (qmom-qiso) / 2.0;
18        sigma[I_ISO][i] = qiso; // cross section for Ar+ / Ar isotropic part of elastic
19        scattering // cross section for Ar+ / Ar isotropic part of elastic
20        sigma[I_BACK][i] = qback; // cross section for Ar+ / Ar backward elastic scattering
21    }
22 }

```

```

18 }
19 }

```

Calculation of the total macroscopic cross sections (which are the sum of all cross sections for a given species, multiplied with the gas density) for both species: upon the computation of the collision probabilities of the particles these total macroscopic cross sections are used and it is computationally more efficient to pre-calculate these arrays at the beginning of the simulation run.

```

1 //-----//
2 // calculation of total cross sections for electrons and ions //
3 //-----//
4
5 void calc_total_cross_sections(void){
6     int i;
7
8     for(i=0; i<CS_RANGES; i++){
9         sigma_tot_e[i] = (sigma[E_ELA][i] + sigma[E_EXC][i] + sigma[E_ION][i]) * GAS_DENSITY; // total
10        // macroscopic cross section of electrons
11        sigma_tot_i[i] = (sigma[I_ISO][i] + sigma[I_BACK][i]) * GAS_DENSITY; // total
12        // macroscopic cross section of ions
13    }
14 }

```

Test of the cross sections: the use of this function is optional, it writes all the different cross sections to a data file (`cross_sections.dat`), from which the energy dependent cross sections can be plotted and inspected. It is advisable to use this feature of the code after changing the cross section set.

```

1 //-----//
2 // test of cross sections for electrons and ions //
3 //-----//
4
5 void test_cross_sections(void){
6     FILE * f;
7     int i,j;
8
9     f = fopen("cross_sections.dat","w"); // cross sections saved in data file: cross_sections.dat
10    for(i=0; i<CS_RANGES; i++){
11        fprintf(f,"%12.4f ",i*DE_CS);
12        for(j=0; j<N_CS; j++) fprintf(f,"%14e ",sigma[j][i]);
13        fprintf(f,"\n");
14    }
15    fclose(f);
16 }

```

Finding of the maximum of the collision frequencies for the electrons and for the ions, based on their total collision cross sections. These quantities are needed for checking the maximum collision probability per time step of the respective species. These probabilities have to be kept low in order to minimise the chance of more than one collision per time step (see the section on stability and accuracy in [1]). The values corresponding to the actual simulation settings appear in the file `info.txt`.

```

1 //-----//
2 // find upper limit of collision frequencies //
3 //-----//
4
5 double max_electron_coll_freq (void){
6     int i;
7     double e,v,nu,nu_max;
8     nu_max = 0;
9     for(i=0; i<CS_RANGES; i++){
10        e = i * DE_CS;
11        v = sqrt(2.0 * e * EV_TO_J / E_MASS);
12        nu = v * sigma_tot_e[i];
13        if (nu > nu_max) {nu_max = nu;}
14    }
15    return nu_max;
16 }
17
18 double max_ion_coll_freq (void){
19     int i;
20     double e,g,nu,nu_max;
21     nu_max = 0;
22     for(i=0; i<CS_RANGES; i++){
23        e = i * DE_CS;
24        g = sqrt(2.0 * e * EV_TO_J / MU_ARAR);
25        nu = g * sigma_tot_i[i];
26        if (nu > nu_max) nu_max = nu;
27    }
28    return nu_max;
29 }

```


Upon the initialization of the simulation this function seeds an equal number (`nseed`) of electron and ion superparticles at random positions within the electrode gap, with zero initial velocity.

```

1 //-----//
2 // initialization of the simulation by placing a given number of //
3 // electrons and ions at random positions between the electrodes //
4 //-----//
5
6 void init(int nseed){
7     int i;
8
9     for (i=0; i<nseed; i++){
10         x_e[i] = L * R01(MTgen); // initial random position of the electron
11         vx_e[i] = 0; vy_e[i] = 0; vz_e[i] = 0; // initial velocity components of the electron
12         x_i[i] = L * R01(MTgen); // initial random position of the ion
13         vx_i[i] = 0; vy_i[i] = 0; vz_i[i] = 0; // initial velocity components of the ion
14     }
15     N_e = nseed; // initial number of electrons
16     N_i = nseed; // initial number of ions
17 }

```

Execution of an electron – Ar atom collision. The arguments of the function contain the position and the velocity components of the colliding electron, as well as an index related to its energy, which can be used for retrieving the values of the cross sections of the processes in which the given particle can participate. In lines 14-20, the relative velocity (based on the cold gas approximation, i.e., assuming stationary target atoms) and the velocity of the center of mass reference frame (w) are computed. This is followed in lines 24-28 by the determination of the Euler angles of the projectile. In the following part of the function the type of the process is chosen in a stochastic manner and depending on the type of the collision to take place (elastic, excitation, or ionization) the scattering and azimuth angles are set. In the case of excitation and ionization, the threshold energy is subtracted from the energy in the center of mass frame (lines 48 / 54). In the case of ionization, the sharing of the remaining kinetic energy between the ejected and scattered electrons is defined in lines 55 and 56. Subsequently, the scattering and azimuth angles for the ejected electron are generated and this electron is scattered. Finally, the new (ejected) electron and the new ion are added to the list of electrons and ions, respectively (lines 70-79). In the final, common branch of the function (lines 82-99) the incoming electron is scattered (in the case of all processes).

```

1 //-----//
2 // e / Ar collision (cold gas approximation) //
3 //-----//
4
5 void collision_electron (double xe, double *vxe, double *vye, double *vze, int eindex){
6     const double F1 = E_MASS / (E_MASS + AR_MASS);
7     const double F2 = AR_MASS / (E_MASS + AR_MASS);
8     double t0,t1,t2,rnd;
9     double g,g2,gx,gy,gz,wx,wy,wz,theta,phi;
10    double chi,eta,chi2,eta2,sc,cc,se,ce,st,ct,sp,cp,energy,e_sc,e_ej;
11
12    // calculate relative velocity before collision & velocity of the centre of mass
13
14    gx = (*vxe);
15    gy = (*vye);
16    gz = (*vze);
17    g = sqrt(gx * gx + gy * gy + gz * gz);
18    wx = F1 * (*vxe);
19    wy = F1 * (*vye);
20    wz = F1 * (*vze);
21
22    // find Euler angles
23
24    if (gx == 0) {theta = 0.5 * PI;}
25    else {theta = atan2(sqrt(gy * gy + gz * gz),gx);}
26    if (gy == 0) {
27        if (gz > 0){phi = 0.5 * PI;} else {phi = - 0.5 * PI;}
28    } else {phi = atan2(gz, gy);}
29    st = sin(theta);
30    ct = cos(theta);
31    sp = sin(phi);
32    cp = cos(phi);
33
34    // choose the type of collision based on the cross sections
35    // take into account energy loss in inelastic collisions
36    // generate scattering and azimuth angles
37    // in case of ionization handle the 'new' electron
38
39    t0 = sigma[E_ELA][eindex];
40    t1 = t0 + sigma[E_EXC][eindex];
41    t2 = t1 + sigma[E_ION][eindex];
42    rnd = R01(MTgen);
43    if (rnd < (t0/t2)){ // elastic scattering
44        chi = acos(1.0 - 2.0 * R01(MTgen)); // isotropic scattering
45        eta = TWO_PI * R01(MTgen); // azimuthal angle
46    } else if (rnd < (t1/t2)){ // excitation

```

```

47     energy = 0.5 * E_MASS * g * g; // electron energy
48     energy = fabs(energy - E_EXC_TH * EV_TO_J); // subtract energy loss for excitation
49     g = sqrt(2.0 * energy / E_MASS); // relative velocity after energy loss
50     chi = acos(1.0 - 2.0 * R01(MTgen)); // isotropic scattering
51     eta = TWO_PI * R01(MTgen); // azimuthal angle
52 } else { // ionization
53     energy = 0.5 * E_MASS * g * g; // electron energy
54     energy = fabs(energy - E_ION_TH * EV_TO_J); // subtract energy loss of ionization
55     e_ej = 10.0 * tan(R01(MTgen) * atan(energy/EV_TO_J / 20.0)) * EV_TO_J; // energy of the ejected
    electron
56     e_sc = fabs(energy - e_ej); // energy of scattered electron after the collision
57     g = sqrt(2.0 * e_sc / E_MASS); // relative velocity of scattered electron
58     g2 = sqrt(2.0 * e_ej / E_MASS); // relative velocity of ejected electron
59     chi = acos(sqrt(e_sc / energy)); // scattering angle for scattered electron
60     chi2 = acos(sqrt(e_ej / energy)); // scattering angle for ejected electrons
61     eta = TWO_PI * R01(MTgen); // azimuthal angle for scattered electron
62     eta2 = eta + PI; // azimuthal angle for ejected electron
63     sc = sin(chi2);
64     cc = cos(chi2);
65     se = sin(eta2);
66     ce = cos(eta2);
67     gx = g2 * (ct * cc - st * sc * ce);
68     gy = g2 * (st * cp * cc + ct * cp * sc * ce - sp * sc * se);
69     gz = g2 * (st * sp * cc + ct * sp * sc * ce + cp * sc * se);
70     x_e[N_e] = xe; // add new electron
71     vx_e[N_e] = wx + F2 * gx;
72     vy_e[N_e] = wy + F2 * gy;
73     vz_e[N_e] = wz + F2 * gz;
74     N_e++;
75     x_i[N_i] = xe; // add new ion
76     vx_i[N_i] = RMB(MTgen); // velocity is sampled from background thermal
    distribution
77     vy_i[N_i] = RMB(MTgen);
78     vz_i[N_i] = RMB(MTgen);
79     N_i++;
80 }
81
82 // scatter the primary electron
83
84 sc = sin(chi);
85 cc = cos(chi);
86 se = sin(eta);
87 ce = cos(eta);
88
89 // compute new relative velocity:
90
91 gx = g * (ct * cc - st * sc * ce);
92 gy = g * (st * cp * cc + ct * cp * sc * ce - sp * sc * se);
93 gz = g * (st * sp * cc + ct * sp * sc * ce + cp * sc * se);
94
95 // post-collision velocity of the colliding electron
96
97 (*vxe) = wx + F2 * gx;
98 (*vye) = wy + F2 * gy;
99 (*vze) = wz + F2 * gz;
100 }

```

Execution of an Ar^+ – argon collision. The arguments of the function contain the velocity components of both the projectile ion and the target atom. In lines 13-19, the relative velocity between these two particles and the velocity of the center of mass frame are calculated. In lines 21-26, the Euler angles of the incoming particle are determined, and subsequently, in lines 30-37 the type of scattering (isotropic / backscattering) is determined based on the cross sections and a random number. The scattering angle is chosen accordingly in lines 34/36, while the azimuth angle is set in line 38. Finally, the ion is scattered and the components of its new velocity vector are calculated and are returned by the function.

```

1 //-----//
2 // Ar+ / Ar collision //
3 //-----//
4
5 void collision_ion (double *vx_1, double *vy_1, double *vz_1,
6                   double *vx_2, double *vy_2, double *vz_2, int e_index){
7     double g,gx,gy,gz,wx,wy,wz,rnd;
8     double theta,phi,chi,eta,st,ct,sp,cp,sc,cc,se,ce,t1,t2;
9
10    // calculate relative velocity before collision
11    // random Maxwellian target atom already selected (vx_2,vy_2,vz_2 velocity components of target atom
    come with the call)
12
13    gx = (*vx_1)-(*vx_2);
14    gy = (*vy_1)-(*vy_2);
15    gz = (*vz_1)-(*vz_2);
16    g = sqrt(gx * gx + gy * gy + gz * gz);
17    wx = 0.5 * ((*vx_1) + (*vx_2));
18    wy = 0.5 * ((*vy_1) + (*vy_2));
19    wz = 0.5 * ((*vz_1) + (*vz_2));
20

```

```

21 // find Euler angles
22
23 if (gx == 0) {theta = 0.5 * PI;} else {theta = atan2(sqrt(gy * gy + gz * gz),gx);}
24 if (gy == 0) {
25     if (gz > 0){phi = 0.5 * PI;} else {phi = - 0.5 * PI;}
26 } else {phi = atan2(gz, gy);}
27
28 // determine the type of collision based on cross sections and generate scattering angle
29
30 t1 = sigma[I_IS0][e_index];
31 t2 = t1 + sigma[I_BACK][e_index];
32 rnd = R01(MTgen);
33 if (rnd < (t1 / t2)){ // isotropic scattering
34     chi = acos(1.0 - 2.0 * R01(MTgen)); // scattering angle
35 } else { // backward scattering
36     chi = PI; // scattering angle
37 }
38 eta = TWO_PI * R01(MTgen); // azimuthal angle
39 sc = sin(chi);
40 cc = cos(chi);
41 se = sin(eta);
42 ce = cos(eta);
43 st = sin(theta);
44 ct = cos(theta);
45 sp = sin(phi);
46 cp = cos(phi);
47
48 // compute new relative velocity
49
50 gx = g * (ct * cc - st * sc * ce);
51 gy = g * (st * cp * cc + ct * cp * sc * ce - sp * sc * se);
52 gz = g * (st * sp * cc + ct * sp * sc * ce + cp * sc * se);
53
54 // post-collision velocity of the ion
55
56 (*vx_1) = wx + 0.5 * gx;
57 (*vy_1) = wy + 0.5 * gy;
58 (*vz_1) = wz + 0.5 * gz;
59 }

```

Solving the Poisson equation. The spatial distribution of the potential and the electric field are computed based on the spatial distribution of the space charge density (ρ_{o1}) and the potential applied to the (powered) electrode situated at the grid point 0. By default, a simple single-frequency (cosine) excitation waveform is used (line 16). The potential of the other (grounded) electrode, situated at the grid point N_G-1 is set to zero (line 17). Lines 21-31 implement the calculation of the potential based on the Thomas-algorithm. Subsequently, the electric field is derived in lines 35-37.

```

1 //-----//
2 // solve Poisson equation (Thomas algorithm) //
3 //-----//
4
5 void solve_Poisson (xvector rho1, double tt){
6     const double A = 1.0;
7     const double B = -2.0;
8     const double C = 1.0;
9     const double S = 1.0 / (2.0 * DX);
10    const double ALPHA = -DX * DX / EPSILON0;
11    xvector g, w, f;
12    int i;
13
14    // apply potential to the electrodes - boundary conditions
15
16    pot[0] = VOLTAGE * cos(OMEGA * tt); // potential at the powered electrode
17    pot[N_G-1] = 0.0; // potential at the grounded electrode
18
19    // solve Poisson equation
20
21    for(i=1; i<=N_G-2; i++) f[i] = ALPHA * rho1[i];
22    f[1] -= pot[0];
23    f[N_G-2] -= pot[N_G-1];
24    w[1] = C/B;
25    g[1] = f[1]/B;
26    for(i=2; i<=N_G-2; i++){
27        w[i] = C / (B - A * w[i-1]);
28        g[i] = (f[i] - A * g[i-1]) / (B - A * w[i-1]);
29    }
30    pot[N_G-2] = g[N_G-2];
31    for (i=N_G-3; i>0; i--) pot[i] = g[i] - w[i] * pot[i+1]; // potential at the grid points
32    // between the electrodes
33
34    // compute electric field
35
36    for(i=1; i<=N_G-2; i++) efield[i] = (pot[i-1] - pot[i+1]) * S; // electric field at the grid points
37    // between the electrodes
38    efield[0] = (pot[0] - pot[1]) * INV_DX - rho1[0] * DX / (2.0 * EPSILON0); // powered
39    // electrode
40    efield[N_G-1] = (pot[N_G-2] - pot[N_G-1]) * INV_DX + rho1[N_G-1] * DX / (2.0 * EPSILON0); // grounded

```

```

38 } electrode

```

Main simulation cycle that accomplishes the steps that are executed in every time step, according to figure 2. The main loop (for cycle in line 19) covers the time steps in the $[0, \dots, N_T-1]$ range.

Step 1 is the computation of the charged particle densities at the grid points. This is accomplished in lines 25-33 for the electrons. The densities at the outermost grid points are multiplied by a factor of two, since data for these points are collected from spatial domains that are of half size as compared to the rest of the grid points (lines 32-33). The computed density distribution is used for updating the cumulative distribution in line 34. The same calculations are carried out for the positive ions in lines 36-46, but only in every N_SUB -th time step (ion subcycling.)

Step 2 (lines 51-52) computes the charge density distribution at the grid points and calls the function that solves the Poisson equation.

Steps 3 and 4 of the PIC-MCC cycle are merged in the forthcoming part of the function. The calculation of the electric field present at the location of the electrons (lines 57-61) the consequent acceleration and displacement of the electrons is computed here (lines 94-95). The latter corresponds to the leapfrog integration scheme. The measurements of various discharge characteristics (that depend directly on the characteristics of the particles, e.g. their velocity and energy) are also integrated into this part of the code. For the electrons, the mean velocity (`ue_xt`), the mean energy (`meane_xt`), and the ionization rate (`ioniz_rate_xt`) are measured with spatial and temporal resolution (line 67-80). Data for each electron contribute to two entries of the specific arrays (that correspond to the grid points that surround the given electron, similarly to the calculation of the density). Data for the EEPF (Electron Energy Probability Function) in the central 10% domain of the discharge are also collected here (lines 84-88). The same calculation is conducted for the positive ions in lines 98-126, with the difference that no ionization rate for the ions and no energy distribution function in the centre of the discharge are computed.

Step 5 is contained in lines 130-172. Here, the particles, which left the computational domain (after being moved in the previous step) are identified. The electrons that arrive to the powered/grounded electrode are counted using the variables `N_e_abs_pow` and `N_e_abs_gnd`, and are subsequently removed from the arrays of coordinates (lines 136-139). In the second part of this code section, the same procedure is executed for the positive ions. For the ions, additionally, the flux-energy distribution function is accumulated here (lines 151-154 / 159-162): the energy of the arriving ions is calculated and an element of the array `ifed_pow` or `ifed_gnd` is incremented accordingly.

Step 6 (check and execution of collisions) is contained in lines 176-187 for electrons and in lines 189-208 for ions. The calculation of collision probability requires the determination (i) of the energy and the velocity of the particles in the case of the electrons and (ii) of the energy in the center of mass reference frame and the relative velocity in the case of ions. In the latter case, this requires sampling a random background gas atom, with Maxwell-Boltzmann velocity distribution; the velocity components are generated in lines 191-193. Whenever the comparison between a random number with uniform distribution (`R01(MTgen)`) and the collision probability (`p_coll`) indicates the occurrence of a collision, the corresponding function is called in line 184 (for electrons) and in line 204 (for ions).

At the end of the function (lines 210-220), data for the spatio-temporal distributions of some discharge characteristics are collected. In line 222, runtime information is printed to the terminal screen about the actual RF cycle number and the superparticle numbers, in line 224 the same data are saved to the `datafile = conv.dat`.

```

1 //-----//
2 // simulation of one radiofrequency cycle //
3 //-----//
4
5 void do_one_cycle (void){
6     const double DV      = ELECTRODE_AREA * DX;
7     const double FACTOR_W = WEIGHT / DV;
8     const double FACTOR_E = DT_E / E_MASS * E_CHARGE;
9     const double FACTOR_I = DT_I / AR_MASS * E_CHARGE;
10    const double MIN_X    = 0.45 * L; // min. position for EEPF collection
11    const double MAX_X    = 0.55 * L; // max. position for EEPF collection
12    int k, t, p, energy_index;
13    double g, g_sqr, gx, gy, gz, vx_a, vy_a, vz_a, e_x, energy, nu, p_coll, v_sqr, velocity;
14    double mean_v, c0, c1, c2, rate;
15    bool out;
16    xvector rho;
17    int t_index;
18

```

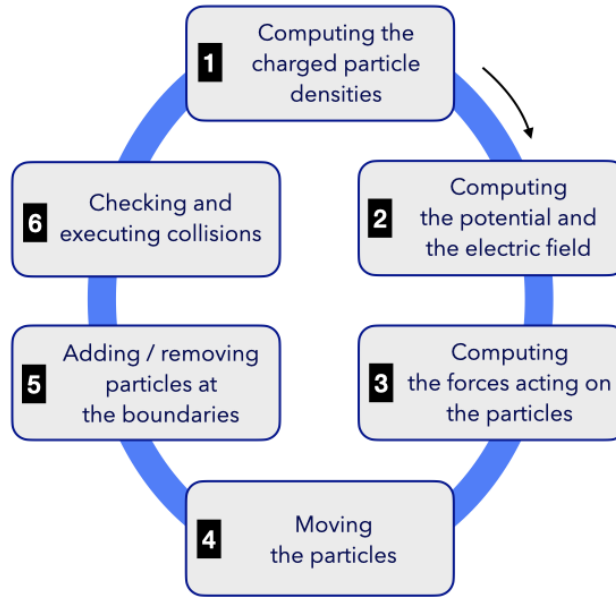


Figure 2: Steps of the basic PIC/MCC cycle [1]

```

19  for (t=0; t<N_T; t++){           // the RF period is divided into N_T equal time intervals (time step
    DT_E)
20      Time += DT_E;                // update of the total simulated time
21      t_index = t / N_BIN;         // index for XT distributions
22
23      // step 1: compute densities at grid points
24
25      for(p=0; p<N_G; p++){         // electron density - computed in
    every time step
26          for(k=0; k<N_e; k++){
27              c0 = x_e[k] * INV_DX;
28              p = int(c0);
29              e_density[p] += (p + 1 - c0) * FACTOR_W;
30              e_density[p+1] += (c0 - p) * FACTOR_W;
31          }
32          e_density[0] *= 2.0;
33          e_density[N_G-1] *= 2.0;
34          for(p=0; p<N_G; p++) cumul_e_density[p] += e_density[p];
35
36          if ((t % N_SUB) == 0) {    // ion density - computed in
    every N_SUB-th time steps (subcycling)
37              for(p=0; p<N_G; p++) i_density[p] = 0;
38              for(k=0; k<N_i; k++){
39                  c0 = x_i[k] * INV_DX;
40                  p = int(c0);
41                  i_density[p] += (p + 1 - c0) * FACTOR_W;
42                  i_density[p+1] += (c0 - p) * FACTOR_W;
43              }
44              i_density[0] *= 2.0;
45              i_density[N_G-1] *= 2.0;
46          }
47          for(p=0; p<N_G; p++) cumul_i_density[p] += i_density[p];
48
49          // step 2: solve Poisson equation
50
51          for(p=0; p<N_G; p++) rho[p] = E_CHARGE * (i_density[p] - e_density[p]); // get charge density
52          solve_Poisson(rho,Time); // compute potential and
    electric field
53
54          // steps 3 & 4: move particles according to electric field interpolated to particle positions
55
56          for(k=0; k<N_e; k++){      // move all electrons in every time step
57              c0 = x_e[k] * INV_DX;
58              p = int(c0);
59              c1 = p + 1.0 - c0;
60              c2 = c0 - p;
61              e_x = c1 * efield[p] + c2 * efield[p+1];
62
63              if (measurement_mode) {
64
65                  // measurements: 'x' and 'v' are needed at the same time, i.e. old 'x' and mean 'v'
66
67                  mean_v = vx_e[k] - 0.5 * e_x * FACTOR_E;
  
```

```

68     counter_e_xt[p][t_index] += c1;
69     counter_e_xt[p+1][t_index] += c2;
70     ue_xt[p][t_index] += c1 * mean_v;
71     ue_xt[p+1][t_index] += c2 * mean_v;
72     v_sqr = mean_v * mean_v + vy_e[k] * vy_e[k] + vz_e[k] * vz_e[k];
73     energy = 0.5 * E_MASS * v_sqr / EV_T0_J;
74     meane_e_xt[p][t_index] += c1 * energy;
75     meane_e_xt[p+1][t_index] += c2 * energy;
76     energy_index = min( int(energy / DE_CS + 0.5), CS_RANGES-1);
77     velocity = sqrt(v_sqr);
78     rate = sigma[E_ION][energy_index] * velocity * DT_E * GAS_DENSITY;
79     ioniz_rate_xt[p][t_index] += c1 * rate;
80     ioniz_rate_xt[p+1][t_index] += c2 * rate;
81
82     // measure EEPF in the center
83
84     if ((MIN_X < x_e[k]) && (x_e[k] < MAX_X)){
85         energy_index = (int)(energy / DE_EEPF);
86         if (energy_index < N_EEPF) {eepf[energy_index] += 1.0;}
87         mean_energy_accu_center += energy;
88         mean_energy_counter_center++;
89     }
90 }
91
92 // update velocity and position
93
94 vx_e[k] -= e_x * FACTOR_E;
95 x_e[k] += vx_e[k] * DT_E;
96 }
97
98 if ((t % N_SUB) == 0) { // move all ions in every N_SUB-th time steps (
subcycling)
99     for(k=0; k<N_i; k++){
100         c0 = x_i[k] * INV_DX;
101         p = int(c0);
102         c1 = p + 1 - c0;
103         c2 = c0 - p;
104         e_x = c1 * efield[p] + c2 * efield[p+1];
105
106         if (measurement_mode) {
107
108             // measurements: 'x' and 'v' are needed at the same time, i.e. old 'x' and mean 'v'
109
110             mean_v = vx_i[k] + 0.5 * e_x * FACTOR_I;
111             counter_i_xt[p][t_index] += c1;
112             counter_i_xt[p+1][t_index] += c2;
113             ui_xt[p][t_index] += c1 * mean_v;
114             ui_xt[p+1][t_index] += c2 * mean_v;
115             v_sqr = mean_v * mean_v + vy_i[k] * vy_i[k] + vz_i[k] * vz_i[k];
116             energy = 0.5 * AR_MASS * v_sqr / EV_T0_J;
117             meane_i_xt[p][t_index] += c1 * energy;
118             meane_i_xt[p+1][t_index] += c2 * energy;
119         }
120
121         // update velocity and position and accumulate absorbed energy
122
123         vx_i[k] += e_x * FACTOR_I;
124         x_i[k] += vx_i[k] * DT_I;
125     }
126 }
127
128 // step 5: check boundaries
129
130 k = 0;
131 while(k < N_e) { // check boundaries for all electrons in every time step
132     out = false;
133     if (x_e[k] < 0) {N_e_abs_pow++; out = true;} // the electron is out at the powered electrode
134     if (x_e[k] > L) {N_e_abs_gnd++; out = true;} // the electron is out at the grounded electrode
135     if (out) { // remove the electron, if out
136         x_e[k] = x_e[N_e-1];
137         vx_e[k] = vx_e[N_e-1];
138         vy_e[k] = vy_e[N_e-1];
139         vz_e[k] = vz_e[N_e-1];
140         N_e--;
141     } else k++;
142 }
143
144 if ((t % N_SUB) == 0) { // check boundaries for all ions in every N_SUB-th time steps (subcycling)
145     k = 0;
146     while(k < N_i) {
147         out = false;
148         if (x_i[k] < 0) { // the ion is out at the powered electrode
149             N_i_abs_pow++;
150             out = true;
151             v_sqr = vx_i[k] * vx_i[k] + vy_i[k] * vy_i[k] + vz_i[k] * vz_i[k];
152             energy = 0.5 * AR_MASS * v_sqr / EV_T0_J;
153             energy_index = (int)(energy / DE_IFED);
154             if (energy_index < N_IFED) {ifed_pow[energy_index]++;} // save IFED at the powered
electrode
155         }
156         if (x_i[k] > L) { // the ion is out at the grounded electrode

```

```

157         N_i_abs_gnd++;
158         out = true;
159         v_sqr = vx_i[k] * vx_i[k] + vy_i[k] * vy_i[k] + vz_i[k] * vz_i[k];
160         energy = 0.5 * AR_MASS * v_sqr / EV_TO_J;
161         energy_index = (int)(energy / DE_IFED);
162         if (energy_index < N_IFED) {ifed_gnd[energy_index]++;} // save IFED at the
grounded electrode
    }
    if (out) { // delete the ion, if out
        x_i[k] = x_i[N_i-1];
        vx_i[k] = vx_i[N_i-1];
        vy_i[k] = vy_i[N_i-1];
        vz_i[k] = vz_i[N_i-1];
        N_i--;
    } else k++;
}
}

// step 6: collisions
for (k=0; k<N_e; k++){ // checking for occurrence of a collision for
all electrons in every time step
    v_sqr = vx_e[k] * vx_e[k] + vy_e[k] * vy_e[k] + vz_e[k] * vz_e[k];
    velocity = sqrt(v_sqr);
    energy = 0.5 * E_MASS * v_sqr / EV_TO_J;
    energy_index = min( int(energy / DE_CS + 0.5), CS_RANGES-1);
    nu = sigma_tot_e[energy_index] * velocity;
    p_coll = 1 - exp(- nu * DT_E); // collision probability for electrons
    if (R01(MTgen) < p_coll) { // electron collision takes place
        collision_electron(x_e[k], &vx_e[k], &vy_e[k], &vz_e[k], energy_index);
        N_e_coll++;
    }
}

if ((t % N_SUB) == 0) { // checking for occurrence of a collision for
all ions in every N_SUB-th time steps (subcycling)
    for (k=0; k<N_i; k++){ // pick velocity components of a random target
        vx_a = RMB(MTgen);
        vy_a = RMB(MTgen);
        vz_a = RMB(MTgen);
        gx = vx_i[k] - vx_a; // compute the relative velocity of the
collision partners
        gy = vy_i[k] - vy_a;
        gz = vz_i[k] - vz_a;
        g_sqr = gx * gx + gy * gy + gz * gz;
        g = sqrt(g_sqr);
        energy = 0.5 * MU_ARAR * g_sqr / EV_TO_J;
        energy_index = min( int(energy / DE_CS + 0.5), CS_RANGES-1);
        nu = sigma_tot_i[energy_index] * g;
        p_coll = 1 - exp(- nu * DT_I); // collision probability for ions
        if (R01(MTgen) < p_coll) { // ion collision takes place
            collision_ion (&vx_i[k], &vy_i[k], &vz_i[k], &vx_a, &vy_a, &vz_a, energy_index);
            N_i_coll++;
        }
    }
}

if (measurement_mode) {
    // collect 'xt' data from the grid
    for (p=0; p<N_G; p++) {
        pot_xt[p][t_index] += pot[p];
        efield_xt[p][t_index] += efield[p];
        ne_xt[p][t_index] += e_density[p];
        ni_xt[p][t_index] += i_density[p];
    }
}

if ((t % 1000) == 0) printf(" c = %8d t = %8d #e = %8d #i = %8d\n", cycle,t,N_e,N_i);
}
fprintf(datafile, "%8d %8d %8d\n", cycle, N_e, N_i);
}

```

Saving (lines 5-29) and loading (lines 35-60) of the “state of the system”. At the end of the simulation of a specified number of RF cycles, all the data that will allow continuing the simulation of the same setting is saved to the binary file `picdata.bin`. These include the time, the number of the RF cycles completed, the number of electron and ion superparticles, as well as all the coordinates of all the particles. Loading these data allows a smooth continuation of the simulation for the next cycles.

```

1 //-----//
2 // save particle coordinates //
3 //-----//
4
5 void save_particle_data(){
6     double d;

```

```

7 FILE * f;
8 char fname[80];
9
10 strcpy(fname,"picdata.bin");
11 f = fopen(fname,"wb");
12 fwrite(&Time,sizeof(double),1,f);
13 d = (double)(cycles_done);
14 fwrite(&d,sizeof(double),1,f);
15 d = (double)(N_e);
16 fwrite(&d,sizeof(double),1,f);
17 fwrite(x_e, sizeof(double),N_e,f);
18 fwrite(vx_e,sizeof(double),N_e,f);
19 fwrite(vy_e,sizeof(double),N_e,f);
20 fwrite(vz_e,sizeof(double),N_e,f);
21 d = (double)(N_i);
22 fwrite(&d,sizeof(double),1,f);
23 fwrite(x_i, sizeof(double),N_i,f);
24 fwrite(vx_i,sizeof(double),N_i,f);
25 fwrite(vy_i,sizeof(double),N_i,f);
26 fwrite(vz_i,sizeof(double),N_i,f);
27 fclose(f);
28 printf(">> eduPIC: data saved : %d electrons %d ions, %d cycles completed, time is %e [s]\n",N_e,N_i,
    cycles_done,Time);
29 }
30
31 //-----//
32 // load particle coordinates //
33 //-----//
34
35 void load_particle_data(){
36     double d;
37     FILE * f;
38     char fname[80];
39
40     strcpy(fname,"picdata.bin");
41     f = fopen(fname,"rb");
42     if (f==NULL) {printf(">> eduPIC: ERROR: No particle data file found, try running initial cycle using
        argument '0'\n"); exit(0); }
43     fread(&Time,sizeof(double),1,f);
44     fread(&d,sizeof(double),1,f);
45     cycles_done = int(d);
46     fread(&d,sizeof(double),1,f);
47     N_e = int(d);
48     fread(x_e, sizeof(double),N_e,f);
49     fread(vx_e,sizeof(double),N_e,f);
50     fread(vy_e,sizeof(double),N_e,f);
51     fread(vz_e,sizeof(double),N_e,f);
52     fread(&d,sizeof(double),1,f);
53     N_i = int(d);
54     fread(x_i, sizeof(double),N_i,f);
55     fread(vx_i,sizeof(double),N_i,f);
56     fread(vy_i,sizeof(double),N_i,f);
57     fread(vz_i,sizeof(double),N_i,f);
58     fclose(f);
59     printf(">> eduPIC: data loaded : %d electrons %d ions, %d cycles completed before, time is %e [s]\n",N_e
        ,N_i,cycles_done,Time);
60 }

```

Saving of the time-averaged electron and ion density. The function makes use of the cumulative electron density (`cumul_e_density`) and cumulative ion density (`cumul_i_density`) data accumulated in each time step of the simulation. Upon writing to the data file, these data are multiplied by a factor that accounts for the number of accumulation times during the whole simulation (computed in line 11).

```

1 //-----//
2 // save density data //
3 //-----//
4
5 void save_density(void){
6     FILE *f;
7     double c;
8     int m;
9
10    f = fopen("density.dat","w");
11    c = 1.0 / (double)(no_of_cycles) / (double)(N_T);
12    for(m=0; m<N_G; m++){
13        fprintf(f,"%8.5f %12e %12e\n",m * DX, cumul_e_density[m] * c, cumul_i_density[m] * c);
14    }
15    fclose(f);
16 }

```

Saving of the EEPF (Electron Energy Probability Function) to the data file `eepf.dat`. The data are normalized corresponding to (the discretized form of) $\int f(\varepsilon)\sqrt{\varepsilon}d\varepsilon = 1$. Recall that these data represent the central 10% spatial region of the discharge.

```

1 //-----//

```



```

2 // save EEPF data //
3 //-----//
4
5 void save_eepf(void) {
6     FILE *f;
7     int i;
8     double h,energy;
9
10    h = 0.0;
11    for (i=0; i<N_EEPF; i++) {h += eepf[i];}
12    h *= DE_EEPF;
13    f = fopen("eepf.dat","w");
14    for (i=0; i<N_EEPF; i++) {
15        energy = (i + 0.5) * DE_EEPF;
16        fprintf(f,"%e %e\n", energy, eepf[i] / h / sqrt(energy));
17    }
18    fclose(f);
19 }

```

Saving of the time-averaged IFEDF (Ion Flux Energy Distribution Function) at the powered (second column) and grounded (third column) electrode as a function of the energy (first column) to the data file `ifed.dat`. The functions are normalized as $\int F(\varepsilon)d\varepsilon = 1$.

```

1 //-----//
2 // save IFED data //
3 //-----//
4
5 void save_ifed(void) {
6     FILE *f;
7     int i;
8     double h_pow,h_gnd,energy;
9
10    h_pow = 0.0;
11    h_gnd = 0.0;
12    for (i=0; i<N_IFED; i++) {h_pow += ifed_pow[i]; h_gnd += ifed_gnd[i];}
13    h_pow *= DE_IFED;
14    h_gnd *= DE_IFED;
15    mean_i_energy_pow = 0.0;
16    mean_i_energy_gnd = 0.0;
17    f = fopen("ifed.dat","w");
18    for (i=0; i<N_IFED; i++) {
19        energy = (i + 0.5) * DE_IFED;
20        fprintf(f,"%6.2f %10.6f %10.6f\n", energy, (double)(ifed_pow[i])/h_pow, (double)(ifed_gnd[i])/h_gnd);
21        mean_i_energy_pow += energy * (double)(ifed_pow[i]) / h_pow;
22        mean_i_energy_gnd += energy * (double)(ifed_gnd[i]) / h_gnd;
23    }
24    fclose(f);
25 }

```

Saving of the spatio-temporal maps of several discharge characteristics. The list of these was provided in table 2. The raw data accumulated for the various quantities needs specific normalization that is accomplished by the function `norm_all_xt()` in lines 19-58. The normalized distributions are saved by the function `save_xt_1()`, which is called for each of the quantities in the function `save_all_xt()`. These distributions have N_G points in space and N_{XT} points in time, where $N_{XT} = N_T / N_{BIN}$, see earlier.

```

1 //-----//
2 // save XT data //
3 //-----//
4
5 void save_xt_1(xt_distr distr, char *fname) {
6     FILE *f;
7     int i, j;
8
9     f = fopen(fname,"w");
10    for (i=0; i<N_G; i++){
11        for (j=0; j<N_XT; j++){
12            fprintf(f,"%e ", distr[i][j]);
13        }
14        fprintf(f,"\n");
15    }
16    fclose(f);
17 }
18
19 void norm_all_xt(void){
20     double f1, f2;
21     int i, j;
22
23     // normalize all XT data
24
25     f1 = (double)(N_XT) / (double)(no_of_cycles * N_T);
26     f2 = WEIGHT / (ELECTRODE_AREA * DX) / (no_of_cycles * (PERIOD / (double)(N_XT)));
27
28     for (i=0; i<N_G; i++){
29         for (j=0; j<N_XT; j++){

```

```

30     pot_xt[i][j]    *= f1;
31     efield_xt[i][j] *= f1;
32     ne_xt[i][j]     *= f1;
33     ni_xt[i][j]     *= f1;
34     if (counter_e_xt[i][j] > 0) {
35         ue_xt[i][j] = ue_xt[i][j] / counter_e_xt[i][j];
36         je_xt[i][j] = -ue_xt[i][j] * ne_xt[i][j] * E_CHARGE;
37         meanee_xt[i][j] = meanee_xt[i][j] / counter_e_xt[i][j];
38         ioniz_rate_xt[i][j] *= f2;
39     } else {
40         ue_xt[i][j] = 0.0;
41         je_xt[i][j] = 0.0;
42         meanee_xt[i][j] = 0.0;
43         ioniz_rate_xt[i][j] = 0.0;
44     }
45     if (counter_i_xt[i][j] > 0) {
46         ui_xt[i][j] = ui_xt[i][j] / counter_i_xt[i][j];
47         ji_xt[i][j] = ui_xt[i][j] * ni_xt[i][j] * E_CHARGE;
48         meanei_xt[i][j] = meanei_xt[i][j] / counter_i_xt[i][j];
49     } else {
50         ui_xt[i][j] = 0.0;
51         ji_xt[i][j] = 0.0;
52         meanei_xt[i][j] = 0.0;
53     }
54     powere_xt[i][j] = je_xt[i][j] * efield_xt[i][j];
55     poweri_xt[i][j] = ji_xt[i][j] * efield_xt[i][j];
56 }
57 }
58 }
59
60 void save_all_xt(void){
61     char fname[80];
62
63     strcpy(fname, "pot_xt.dat");      save_xt_1(pot_xt, fname);
64     strcpy(fname, "efield_xt.dat");   save_xt_1(efield_xt, fname);
65     strcpy(fname, "ne_xt.dat");       save_xt_1(ne_xt, fname);
66     strcpy(fname, "ni_xt.dat");       save_xt_1(ni_xt, fname);
67     strcpy(fname, "je_xt.dat");       save_xt_1(je_xt, fname);
68     strcpy(fname, "ji_xt.dat");       save_xt_1(ji_xt, fname);
69     strcpy(fname, "powere_xt.dat");   save_xt_1(powere_xt, fname);
70     strcpy(fname, "poweri_xt.dat");   save_xt_1(poweri_xt, fname);
71     strcpy(fname, "meanee_xt.dat");   save_xt_1(meanee_xt, fname);
72     strcpy(fname, "meanei_xt.dat");   save_xt_1(meanei_xt, fname);
73     strcpy(fname, "ioniz_xt.dat");    save_xt_1(ioniz_rate_xt, fname);
74 }

```

The following function generates a simulation report, which is saved to the file `info.dat` and controls the saving of all data for the plasma characteristics. This report includes information about the basic simulation parameters specified by the user (lines 22-32) as well as about some of the computed primary plasma parameters (lines 34-39).

Subsequently, some of the stability and accuracy criteria of the simulation are evaluated according to the prescriptions given in section 2.2 of [1]. These are the conditions concerning the relation of the grid spacing to the Debye length, the relation of the time step to the electron plasma frequency, and the collision probabilities during a time step.

In the case when any of these conditions is violated the function writes an error message to the file `info.dat`. When no violation of the conditions is found, the function continues to save further data to files (including the density and energy distributions, and spatio-temporal maps of a number of plasma characteristics (lines 77-81)) and calculates and writes additional diagnostics data to the file `info.dat` (including the fluxes of electrons and ions at both electrodes and the mean ion energy at both electrodes (lines 82-88)), as well as the power density absorbed by both charged species (lines 93-106)).

```

1  //-----//
2  // simulation report including stability and accuracy conditions //
3  //-----//
4
5  void check_and_save_info(void){
6      FILE *f;
7      double plas_freq, meane, kT, debye_length, density, ecoll_freq, icoll_freq, sim_time, e_max, v_max,
8      power_e, power_i, c;
9      int i,j;
10     bool conditions_OK;
11
12     density = cumul_e_density[N_G / 2] / (double)(no_of_cycles) / (double)(N_T); // e density @ center
13     plas_freq = E_CHARGE * sqrt(density / EPSILON0 / E_MASS); // e plasma frequency @
14     center
15     meane = mean_energy_accu_center / (double)(mean_energy_counter_center); // e mean energy @
16     center
17     kT = 2.0 * meane * EV_TO_J / 3.0; // k T_e @ center (
18     approximate)
19     sim_time = (double)(no_of_cycles) / FREQUENCY; // simulated time

```

```

16 ecoll_freq = (double)(N_e_coll) / sim_time / (double)(N_e); // e collision
17 frequency
18 icoll_freq = (double)(N_i_coll) / sim_time / (double)(N_i); // ion collision
19 frequency
20 debye_length = sqrt(EPSILON0 * kT / density) / E_CHARGE; // e Debye length @
21 center
22
23 f = fopen("info.txt", "w");
24 fprintf(f, "##### eduPIC simulation report #####\n");
25 fprintf(f, "Simulation parameters:\n");
26 fprintf(f, "Gap distance = %12.3e [m]\n", L);
27 fprintf(f, "# of grid divisions = %12d\n", N_G);
28 fprintf(f, "Frequency = %12.3e [Hz]\n", FREQUENCY);
29 fprintf(f, "# of time steps / period = %12d\n", N_T);
30 fprintf(f, "# of electron / ion time steps = %12d\n", N_SUB);
31 fprintf(f, "Voltage amplitude = %12.3e [V]\n", VOLTAGE);
32 fprintf(f, "Pressure (Ar) = %12.3e [Pa]\n", PRESSURE);
33 fprintf(f, "Temperature = %12.3e [K]\n", TEMPERATURE);
34 fprintf(f, "Superparticle weight = %12.3e\n", WEIGHT);
35 fprintf(f, "# of simulation cycles in this run = %12d\n", no_of_cycles);
36 fprintf(f, "-----\n");
37 fprintf(f, "Plasma characteristics:\n");
38 fprintf(f, "Electron density @ center = %12.3e [m^-3]\n", density);
39 fprintf(f, "Plasma frequency @ center = %12.3e [rad/s]\n", plas_freq);
40 fprintf(f, "Debye length @ center = %12.3e [m]\n", debye_length);
41 fprintf(f, "Electron collision frequency = %12.3e [1/s]\n", ecoll_freq);
42 fprintf(f, "Ion collision frequency = %12.3e [1/s]\n", icoll_freq);
43 fprintf(f, "-----\n");
44 fprintf(f, "Stability and accuracy conditions:\n");
45 conditions_OK = true;
46 c = plas_freq * DT_E;
47 fprintf(f, "Plasma frequency @ center * DT_E = %12.3f (OK if less than 0.20)\n", c);
48 if (c > 0.2) {conditions_OK = false;}
49 c = DX / debye_length;
50 fprintf(f, "DX / Debye length @ center = %12.3f (OK if less than 1.00)\n", c);
51 if (c > 1.0) {conditions_OK = false;}
52 c = max_electron_coll_freq() * DT_E;
53 fprintf(f, "Max. electron coll. frequency * DT_E = %12.3f (OK if less than 0.05)\n", c);
54 if (c > 0.05) {conditions_OK = false;}
55 c = max_ion_coll_freq() * DT_I;
56 fprintf(f, "Max. ion coll. frequency * DT_I = %12.3f (OK if less than 0.05)\n", c);
57 if (c > 0.05) {conditions_OK = false;}
58 if (conditions_OK == false){
59     fprintf(f, "-----\n");
60     fprintf(f, "** STABILITY AND ACCURACY CONDITION(S) VIOLATED - REFINES SIMULATION SETTINGS! **\n");
61     fprintf(f, "-----\n");
62     fclose(f);
63     printf(">> eduPIC: ERROR: STABILITY AND ACCURACY CONDITION(S) VIOLATED!\n");
64     printf(">> eduPIC: for details see 'info.txt' and refine simulation settings!\n");
65 }
66 else
67 {
68     // calculate maximum energy for which the Courant-Friedrichs-Levy condition holds:
69
70     v_max = DX / DT_E;
71     e_max = 0.5 * E_MASS * v_max * v_max / EV_TO_J;
72     fprintf(f, "Max e- energy for CFL condition = %12.3f [eV]\n", e_max);
73     fprintf(f, "Check EEPF to ensure that CFL is fulfilled for the majority of the electrons!\n");
74     fprintf(f, "-----\n");
75
76     // saving of the following data is done here as some of the further lines need data
77     // that are computed / normalized in these functions
78
79     printf(">> eduPIC: saving diagnostics data\n");
80     save_density();
81     save_eepf();
82     save_ifed();
83     norm_all_xt();
84     save_all_xt();
85     fprintf(f, "Particle characteristics at the electrodes:\n");
86     fprintf(f, "Ion flux at powered electrode = %12.3e [m^-2 s^-1]\n", N_i_abs_pow * WEIGHT /
87     ELECTRODE_AREA / (no_of_cycles * PERIOD));
88     fprintf(f, "Ion flux at grounded electrode = %12.3e [m^-2 s^-1]\n", N_i_abs_gnd * WEIGHT /
89     ELECTRODE_AREA / (no_of_cycles * PERIOD));
90     fprintf(f, "Mean ion energy at powered electrode = %12.3e [eV]\n", mean_i_energy_pow);
91     fprintf(f, "Mean ion energy at grounded electrode = %12.3e [eV]\n", mean_i_energy_gnd);
92     fprintf(f, "Electron flux at powered electrode = %12.3e [m^-2 s^-1]\n", N_e_abs_pow * WEIGHT /
93     ELECTRODE_AREA / (no_of_cycles * PERIOD));
94     fprintf(f, "Electron flux at grounded electrode = %12.3e [m^-2 s^-1]\n", N_e_abs_gnd * WEIGHT /
95     ELECTRODE_AREA / (no_of_cycles * PERIOD));
96     fprintf(f, "-----\n");
97
98     // calculate spatially and temporally averaged power absorption by the electrons and ions
99
100     power_e = 0.0;
101     power_i = 0.0;
102     for (i=0; i<N_G; i++){
103         for (j=0; j<N_XT; j++){
104             power_e += powere_xt[i][j];
105             power_i += poweri_xt[i][j];
106         }
107     }

```

```

100     }
101     power_e /= (double)(N_XT * N_G);
102     power_i /= (double)(N_XT * N_G);
103     fprintf(f,"Absorbed power calculated as <j*E>:\n");
104     fprintf(f,"Electron power density (average)    = %12.3e [W m-3]\n", power_e);
105     fprintf(f,"Ion power density (average)          = %12.3e [W m-3]\n", power_i);
106     fprintf(f,"Total power density(average)          = %12.3e [W m-3]\n", power_e + power_i);
107     fprintf(f,"-----\n");
108     fclose(f);
109 }
110 }

```

The `main()` function controls code execution. The command line arguments are evaluated in lines 17-35. The first argument gives the number of RF cycles to simulate. A zero value of this parameter has a special meaning: in this case a new simulation can be initiated. An accidental initialization and overwriting of previous simulation results is prevented in lines 41-47; here, if a `picdata.bin` file originating from a previous simulation is found in the current folder a warning message is issued in the terminal window and the code is stopped. In case no such file is present in the current folder, the code seeds a given number (`N_INIT`) of electron and ion superparticles within the electrode gap, executes the simulation of a single RF cycle, and saves the state of the system in the function `save_particle_data()` to the file `picdata.bin`.

In case the first command line argument is greater than zero, the code will load the state of the system (saved previously) using the call to `load_particle_data()`. Subsequently, it executes the simulation of the specified number of RF cycles, and saves the state of the system as explained above.

```

1 //-----//
2 // main //
3 // command line arguments: //
4 // [1]: number of cycles (0 for init) //
5 // [2]: "m" turns on data collection and saving //
6 //-----//
7
8 int main (int argc, char *argv[]){
9     printf(">> eduPIC: starting...\n");
10    printf(">> eduPIC: *****\n");
11    printf(">> eduPIC: Copyright (C) 2021 Z. Donko et al.\n");
12    printf(">> eduPIC: This program comes with ABSOLUTELY NO WARRANTY\n");
13    printf(">> eduPIC: This is free software, you are welcome to use, modify and redistribute it\n");
14    printf(">> eduPIC: according to the GNU General Public License, https://www.gnu.org/licenses/\n");
15    printf(">> eduPIC: *****\n");
16
17    if (argc == 1) {
18        printf(">> eduPIC: error = need starting_cycle argument\n");
19        return 1;
20    } else {
21        strcpy(st0,argv[1]);
22        arg1 = atoi(st0);
23        if (argc > 2) {
24            if (strcmp (argv[2],"m") == 0){
25                measurement_mode = true; // measurements will be done
26            } else {
27                measurement_mode = false;
28            }
29        }
30    }
31    if (measurement_mode) {
32        printf(">> eduPIC: measurement mode: on\n");
33    } else {
34        printf(">> eduPIC: measurement mode: off\n");
35    }
36    set_electron_cross_sections_ar();
37    set_ion_cross_sections_ar();
38    calc_total_cross_sections();
39    //test_cross_sections(); return 1;
40    datafile = fopen("conv.dat","a");
41    if (arg1 == 0) {
42        if (FILE *file = fopen("picdata.bin", "r")) { fclose(file);
43            printf(">> eduPIC: Warning: Data from previous calculation are detected.\n");
44            printf("    To start a new simulation from the beginning, please delete all output files
45            before running ./eduPIC 0\n");
46            printf("    To continue the existing calculation, please specify the number of cycles to
47            run, e.g. ./eduPIC 100\n");
48            exit(0);
49        }
50        no_of_cycles = 1;
51        cycle = 1; // init cycle
52        init(N_INIT); // seed initial electrons & ions
53        printf(">> eduPIC: running initializing cycle\n");
54        Time = 0;
55        do_one_cycle();
56        cycles_done = 1;
57    } else {
58        no_of_cycles = arg1; // run number of cycles specified in command line
59        load_particle_data(); // read previous configuration from file
60    }
61 }

```

```

58     printf(">> eduPIC: running %d cycle(s)\n",no_of_cycles);
59     for (cycle=cycles_done+1;cycle<=cycles_done+no_of_cycles;cycle++) {do_one_cycle();}
60     cycles_done += no_of_cycles;
61 }
62 fclose(datafile);
63 save_particle_data();
64 if (measurement_mode) {
65     check_and_save_info();
66 }
67 printf(">> eduPIC: simulation of %d cycle(s) is completed.\n",no_of_cycles);
68 }

```

4 Licence / Disclaimer

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