

Question 1.

a.

$$IPS_{P_1} = \frac{\text{Clock rate}}{CPI} = \frac{3 \times 10^9}{1.5} = 2 \times 10^9$$

$$IPS_{P_2} = \frac{2.5 \times 10^9}{1.0} = 2.5 \times 10^9$$

$$IPS_{P_3} = \frac{4.0 \times 10^9}{2.2} = 1.818 \times 10^9$$

So processor P2 has highest performance.

b.

$$\text{Number of cycles}_{P_1} = \text{Clock rate} \times \text{Time} = 3 \times 10^9 \times 10 = 3 \times 10^{10} \text{ cycles}$$

$$\text{Number of cycles}_{P_2} = 2.5 \times 10^9 \times 10 = 2.5 \times 10^{10} \text{ cycles}$$

$$\text{Number of cycles}_{P_3} = 4.0 \times 10^9 \times 10 = 4.0 \times 10^{10} \text{ cycles}$$

$$\text{Number of instructions}_{P_1} = IPS \times \text{Time} = 2 \times 10^9 \times 10 = 2 \times 10^{10} \text{ instructions}$$

$$\text{Number of instructions}_{P_2} = 2.5 \times 10^9 \times 10 = 2.5 \times 10^{10} \text{ instructions}$$

$$\text{Number of instructions}_{P_3} = 1.818 \times 10^9 \times 10 = 1.818 \times 10^{10} \text{ instructions}$$

c.

$$\begin{aligned} \text{Clock rate}_2 &= \frac{\text{ClockCycles}_2}{\text{Time}_2} = \frac{\text{Instructions} \times CPI_2}{\text{Time}_2} = \frac{\text{Instructions} \times 1.2 \times CPI_1}{0.7 \times \text{Time}_1} \\ &= \frac{1.2 \times \text{Clock rate}_1}{0.7} = 1.71 \times \text{Clock rate}_1 \end{aligned}$$

Question 2.

a.

$$IPC_{P_1} = \frac{\text{No. Instructions}}{\text{Clock rate} \times \text{Time}} = \frac{20 \times 10^9}{3 \times 10^9 \times 7} = 0.952$$

$$IPC_{P_2} = \frac{30 \times 10^9}{2.5 \times 10^9 \times 10} = 1.2$$

$$IPC_{P_3} = \frac{90 \times 10^9}{4.0 \times 10^9 \times 9} = 2.5$$

b.

$$Clock\ rate_{p_2} = \frac{Clock\ cycle}{Time} = \frac{Instructions}{Time \times IPC} = \frac{30 \times 10^9}{7 \times 1.2} = 3.57\ GHz$$

c.

$$No.\ Instruction_{p_{2\ new}} = \frac{No.\ Instruction_{p_2} \times Time_{p_3}}{Time_{p_2}} = \frac{30 \times 10^9 \times 9}{10} = 27 \times 10^9$$

Question3.

a.

$$CPU\ Time_{p_1} = \frac{10^6 \times (0.1 \times 1 + 0.2 \times 2 + 0.5 \times 3 + 0.2 \times 3)}{2.5 \times 10^9} = 1.04\ ms$$

$$CPU\ Time_{p_2} = \frac{10^6 \times 2}{3 \times 10^9} = 0.667\ ms$$

So the P2 is faster

b.

$$Global\ CPI_{p_1} = 0.1 \times 1 + 0.2 \times 2 + 0.5 \times 3 + 0.2 \times 3 = 2.6$$

$$Global\ CPI_{p_2} = 2$$

c.

$$Clock_{p_1} = 10^6 \times 2.6 = 2.6 \times 10^6\ clock\ cycles$$

$$Clock_{p_2} = 2 \times 10^6\ clock\ cycles$$

Question 4.

$$Exe.\ time = \frac{Instructions \times CPI}{Clock\ rate} = \frac{1000 \times (0.2 \times 2.5 + 0.1 \times 1 + 0.2 \times 2 + 0.5 \times 2)}{2 \times 10^9} = 9.5 \times 10^{-7}\ seconds$$

$$Average\ CPI = 0.2 \times 2.5 + 0.1 \times 1 + 0.2 \times 2 + 0.5 \times 2 = 1.9$$

$$t_2 = \frac{1000 \times \left(\frac{0.2 \times 2.5}{2} + 0.1 \times 1 + 0.2 \times 2 + 0.5 \times 2 \right)}{2 \times 10^9} = 8.25\ s$$

$$Speedup: \frac{t_1}{t_2} = \frac{9.5}{8.25} = 1.15$$

Question 5.

$$Original\ model\ CPI: 0.25 \times 4 + 0.02 \times 20 + 0.73 \times 1.33 = 2.3709$$

$$Alternative\ 1: 0.25 \times 4 + 0.02 \times 2 + 0.73 \times 1.33 = 2.0109$$

$$Alternative\ 2: 0.25 \times 2.5 + 0.02 \times 20 + 0.73 \times 1.33 = 1.9959$$

So alternative model 2 is faster

$$\frac{H_2}{H_1} = \frac{CPI_1}{CPI_2} = \frac{2.0109}{1.9959} = 1.0075$$

Question 6.

a.

$$\frac{Time_1}{Time_2} = \frac{CPI_1}{CPI_2} = \frac{50 \times 10^6 \times 1 + 110 \times 10^6 \times 1 + 80 \times 10^6 \times 4 + 160 \times 10^6 \times 2}{50 \times 10^6 \times NewCPI_{FP} + 110 \times 10^6 \times 1 + 80 \times 10^6 \times 4 + 160 \times 10^6 \times 2}$$

$$= \frac{8 \times 10^8}{50 \times 10^6 \times NewCPI_{FP} + 7.5 \times 10^8} = 2$$

\Rightarrow No solution

b.

$$\frac{Time_1}{Time_2} = \frac{8 \times 10^8}{80 \times 10^6 \times NewCPI_{L/S} + 4.8 \times 10^8} = 2$$

\Rightarrow No solution

c.

$$\frac{Time_2}{Time_1} = \frac{CPI_2}{CPI_1}$$

$$= \frac{50 \times 10^6 \times 1 \times 0.6 + 110 \times 10^6 \times 1 \times 0.6 + 80 \times 10^6 \times 4 \times 0.7 + 160 \times 10^6 \times 2 \times 0.7}{50 \times 10^6 \times 1 + 110 \times 10^6 \times 1 + 80 \times 10^6 \times 4 + 160 \times 10^6 \times 2}$$

$$= \frac{5.44 \times 10^8}{8 \times 10^8} = 0.68$$

\Rightarrow The exe. time is reduced 32%