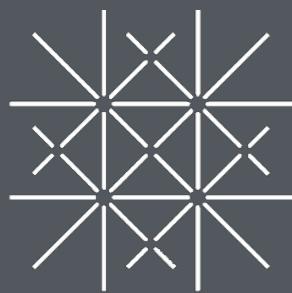


# **Harnessing simulated experience**

Dirk U. Wulff

Bounded Rationality Winter School @ TAPMI, Manipal, 2020



UNI  
BASEL



# Simulating decisions from experience

**Per-option sample size**

10

In decisions from experience, people have to sample from each option so you need to determine the average (per-option) sample size each agent takes.

**CPT - alpha**

1.4

This controls an individual's sensitivity to payoffs (alpha: 0 (low sensitivity to payoffs) - 2 (very high sensitivity)).

**CPT - lambda**

2.15

This controls an individual's loss aversion (lambda: 1 (loss neutral) - 3 (very loss averse))

**CPT - gamma**

0.65

This controls how sensitive people are to changes in probability and consequently the degree to which they overweight or underweight rare events (gamma: 0 (overweighting) - 2 (underweighting))

**Recency**

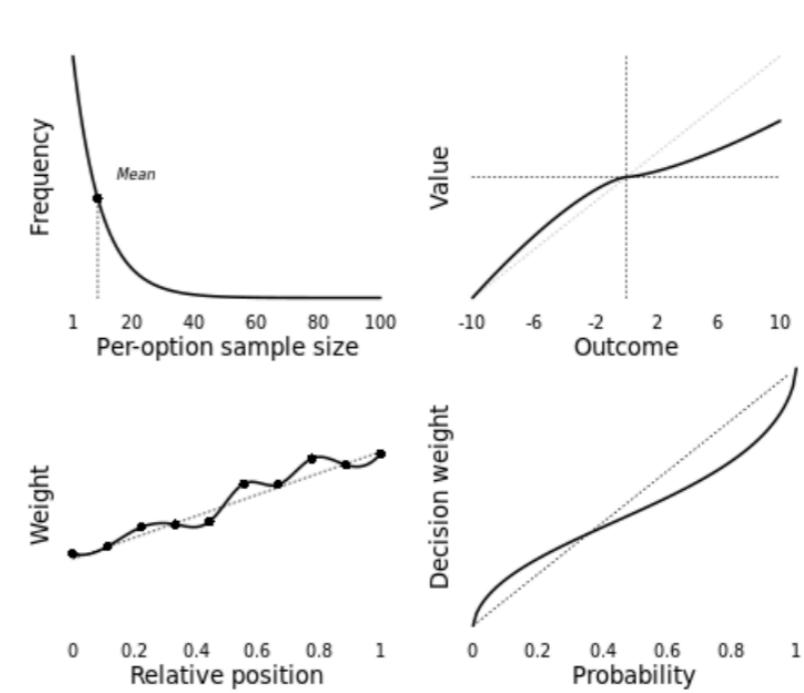
0.6

This controls how much weight each observed sample gets and whether early samples get more weight (primacy), later samples get more weight (recency), or they get equal weight (recency: -1 (primacy) - 1 (recency)).

**Noise**

0.625

This controls the amount of random noise added to the outcomes (0 (no noise) - 1 (large noise)).

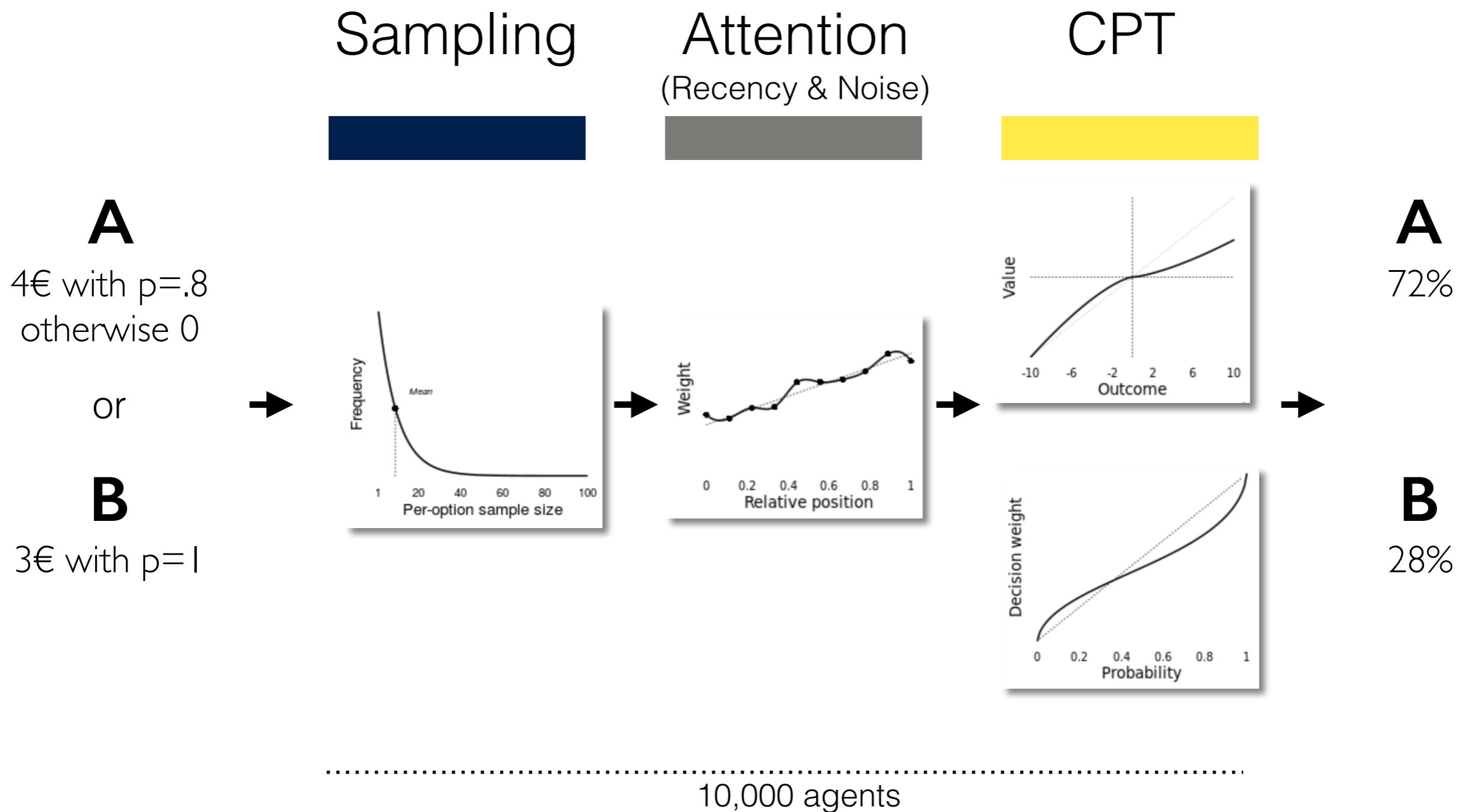


MSE  
.05

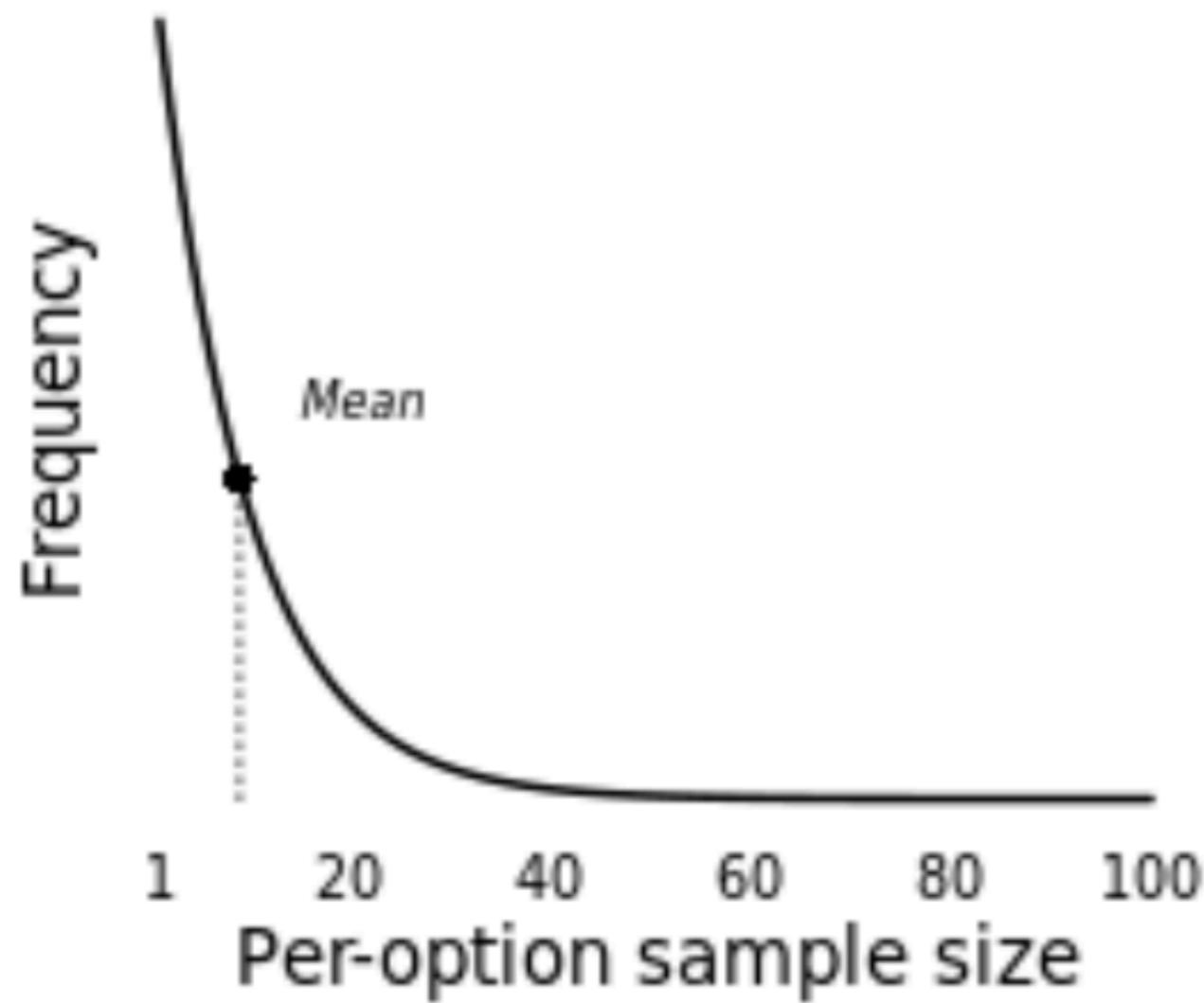


MSE Descript.	Under-weighting	CPT TK92
.118	.47	.569

# Simulating decisions from experience



# Sampling



The 10,000 agents sample according to an exponential distribution.

You control the mean of this distribution, which defines the **average per-option sample size**.

# Sampling

---

**A**

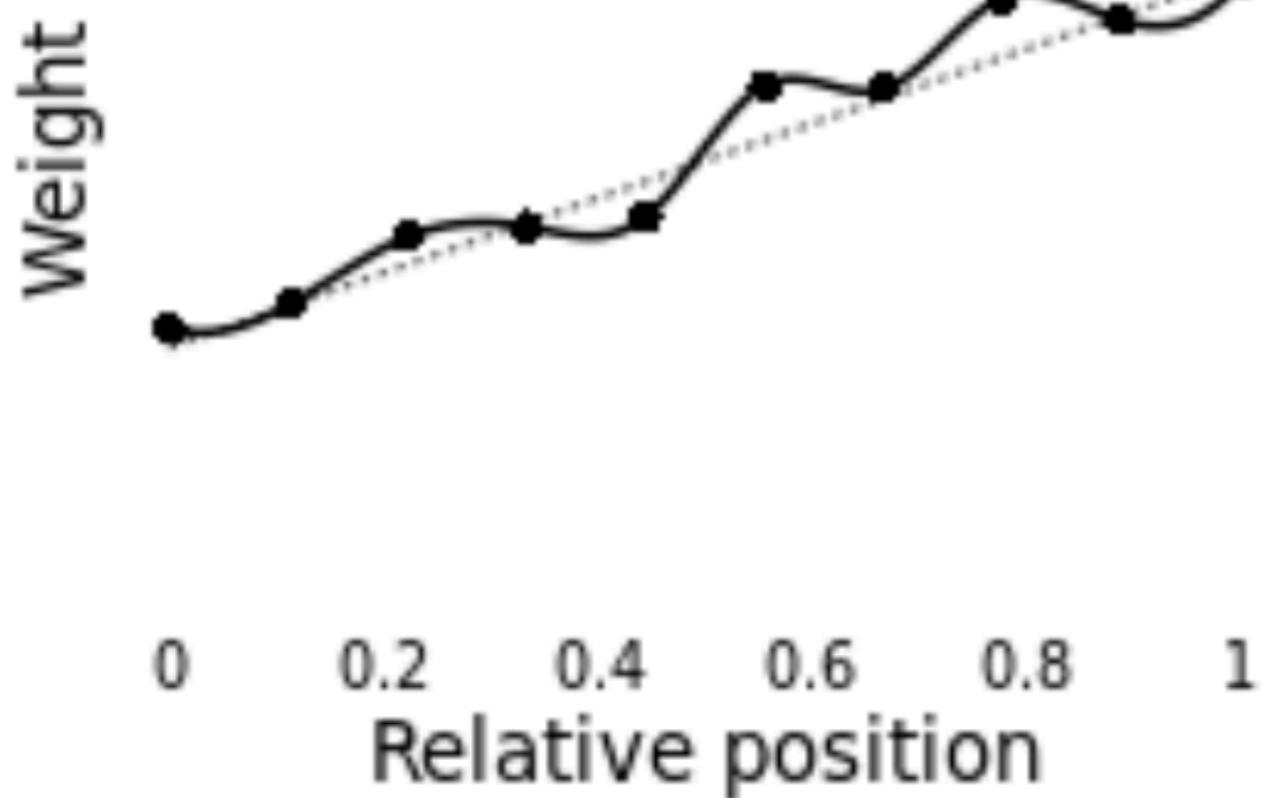
4€ with  $p=.8$   
otherwise 0

**B**

3€ with  $p=1$

*“More sampling means less (as-if) underweighting”*

# Attention



After sampling the agents reweighs the samples to reflect random noise and recency (primacy).

You control the **degree of recency** (or primacy) **and noise**.

# Attention



**A**

4€ with p=.8  
otherwise 0

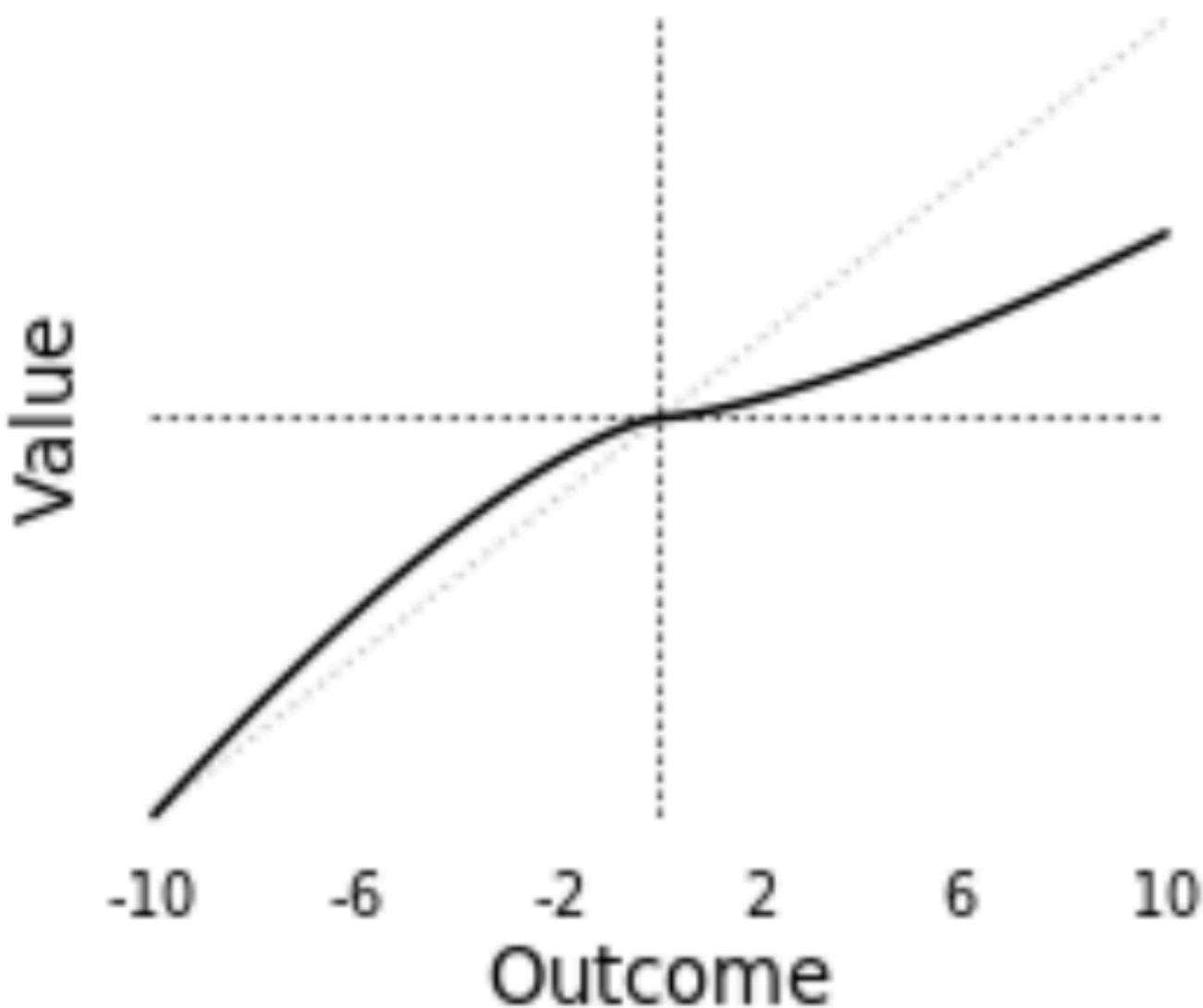
**B**

3€ with p=1

*“More recency (primacy) and noise  
means more (as-if) underweighting”*

# CPT

(Cumulative prospect theory)



Finally, decisions are made according to CPTs value and probability weighting function.

In the value function, you control the **degree of risk (alpha) and loss aversions (lambda)**.

# CPT

(Cumulative prospect theory)

**A**

4€ with p=.8  
otherwise 0

**B**

3€ with p=1

*“More risk aversion (alpha) decreases  
the weight of extreme outcomes”*

# CPT

(Cumulative prospect theory)

**A**

4€ with p=.8  
otherwise 0

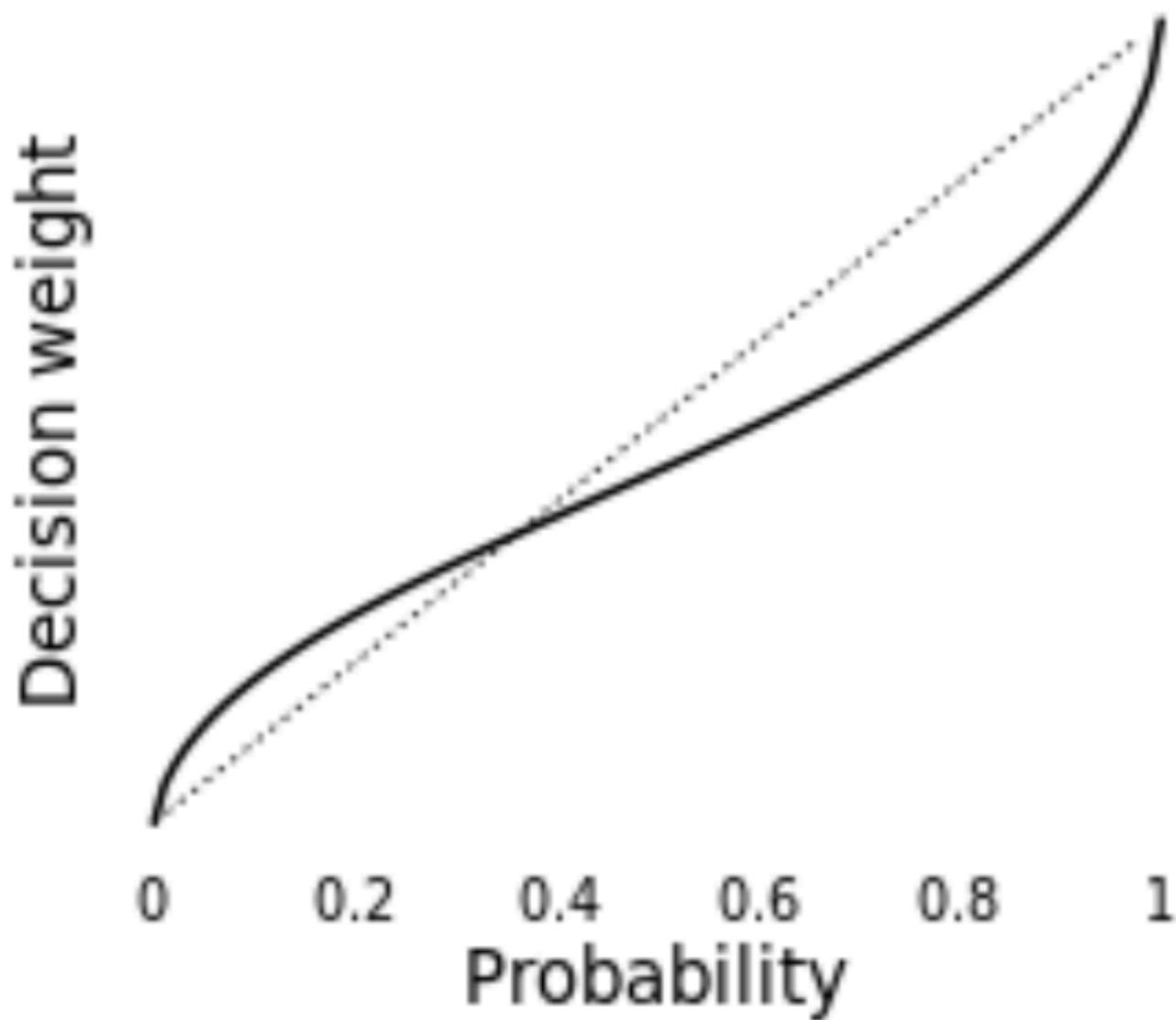
**B**

3€ with p=1

*“More loss aversion (alpha) amplifies the weight of negative outcomes”*

# CPT

(Cumulative prospect theory)



Finally, decisions are made according to CPTs value and probability weighting function.

In the weighting function, you control the **degree of over- and under-weighting of rare events (gamma)**.

# CPT

(Cumulative prospect theory)

**A**

4€ with  $p=.8$   
otherwise 0

**B**

3€ with  $p=1$

*“Higher gamma  
means less underweighting”*

# Interactive 1

# bit.ly/tapmi2020

## I The description-experience gap ☰



### Interactive 1 - 5min

Go to this [site](#) to try out risky choices based on experience and description. **Don't sample for too long.**

### Interactive 2 - 5min

Please enter your intuitions about how people explore using this [survey](#).

## References

Wulff, D. U., Mergenthaler-Canseco, M., & Hertwig, R. (2018). A meta-analytic review of two modes of learning and the description-experience gap. *Psychological bulletin*, 144(2), 140-176.

Hertwig, R., Wulff, D. U., & Mata, R. (2018). Three gaps and what they may mean for risk preference. *Philosophical Transactions of the Royal Society B*, 374(1766), 20180140.

Spektor, M., & Wulff, D. U. (in prep.) Strategic information search. Manuscript in preparation.

Wulff, D. U., Hills, T. T., & Hertwig, R. (2015). Online product reviews and the description-experience gap. *Journal of Behavioral Decision Making*, 28(3), 214-223.

## II Harnessing simulated experiences ☰

7.34	+5.97%	▲	100.08	120,000
7.89	+2.13%	▲	564.23	900,000
7.45	+6.43%	▲	765.90	600,000

### Interactive 1 - 20min

Go to this [site](#) to explore the cognitive underpinnings of decisions from experience.

When you think you have found the best mix of cognitive components go to this [survey](#) to enter your predictions.

### Interactive 2 - 20min

Try out each of the risk intervention tools below (simply click on them). Only explore the tool. **Don't answer the questions** posed to after you've made the decisions.

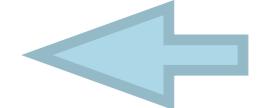


When you have explore all risk intervention tools, go to this [survey](#) to share your impression on each of the tools.

## References

Kaufmann, C., Weber, M., & Haisley, E. (2013). The role of experience sampling and graphical displays on one's investment risk appetite. *Management science*, 59(2), 323-340.

Hertwig, R., & Wulff, D. U. (in prep.). Learning From Experience and Description: Two Powerful Yet Imperfect Teachers of Risk Cognition. Invited by *Nature Human Behavior*.



Censored

Censored

Censored

# **USING SIMULATED EXPERIENCES**

*Can experience be used to  
help people understand risks?*

# Experience triggers more accurate probability judgments than description

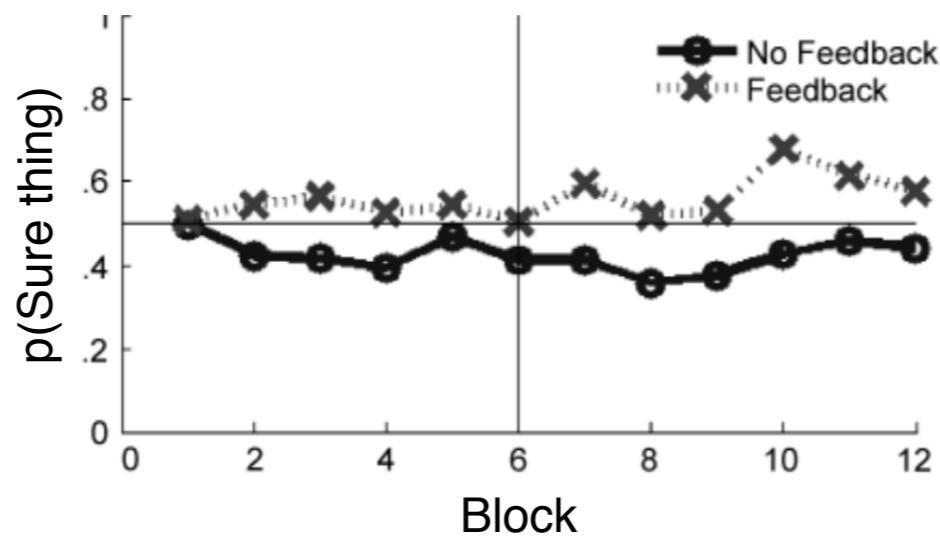
*'How many days do you estimate that it will rain in a ten-day period in each of the four cities?'*

		Kent	Talbot	Somerset	Harford
Objective probability		<b>0.30</b>	<b>0.90</b>	<b>0.60</b>	<b>0.10</b>
Mean observed probability	Description	0.30	0.90	0.60	0.10
	Experience	0.29	0.91	0.61	0.09
	SD	0.17	0.08	0.14	0.09
Mean frequency judgments	Description	<b>0.38</b>	<b>0.80</b>	<b>0.43</b>	<b>0.34</b>
	SD	0.24	0.20	0.25	0.22
	Experience	<b>0.32</b>	<b>0.81</b>	<b>0.57</b>	<b>0.26</b>
	SD	0.18	0.16	0.22	0.18
p-value for different means		.205	.733	.005	.059
p-value for different variances		.155	.203	.869	.352

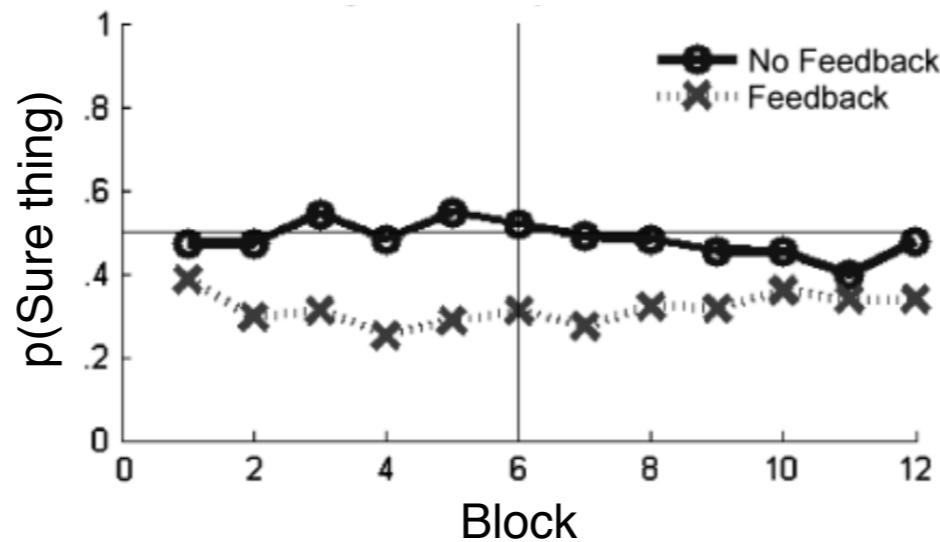
# Experience ‘debiases’

...description-based choices

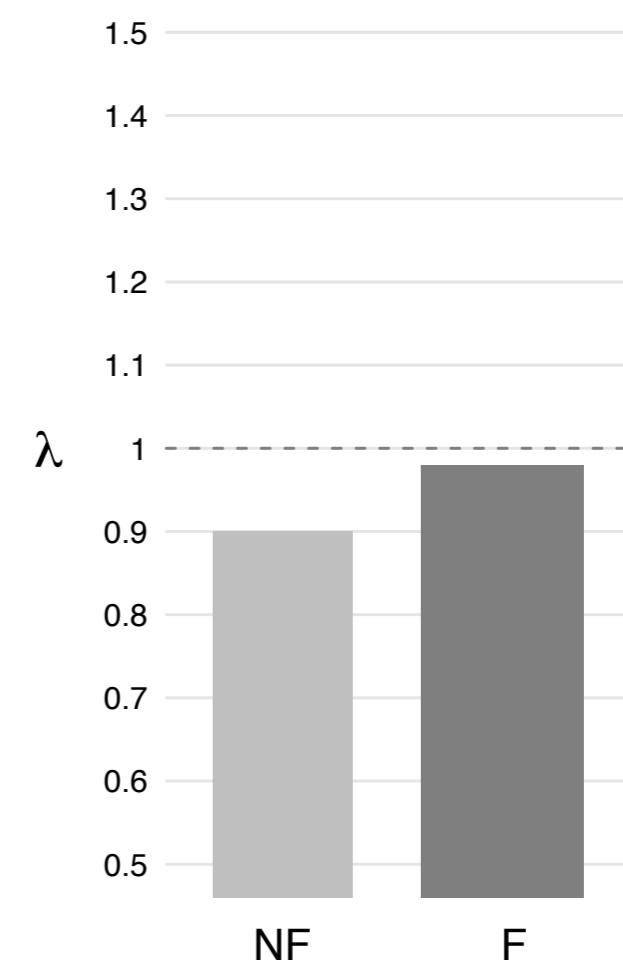
A \$3 for sure



B \$4 with .8



$$w = e^{-(\log(p))^\gamma}$$

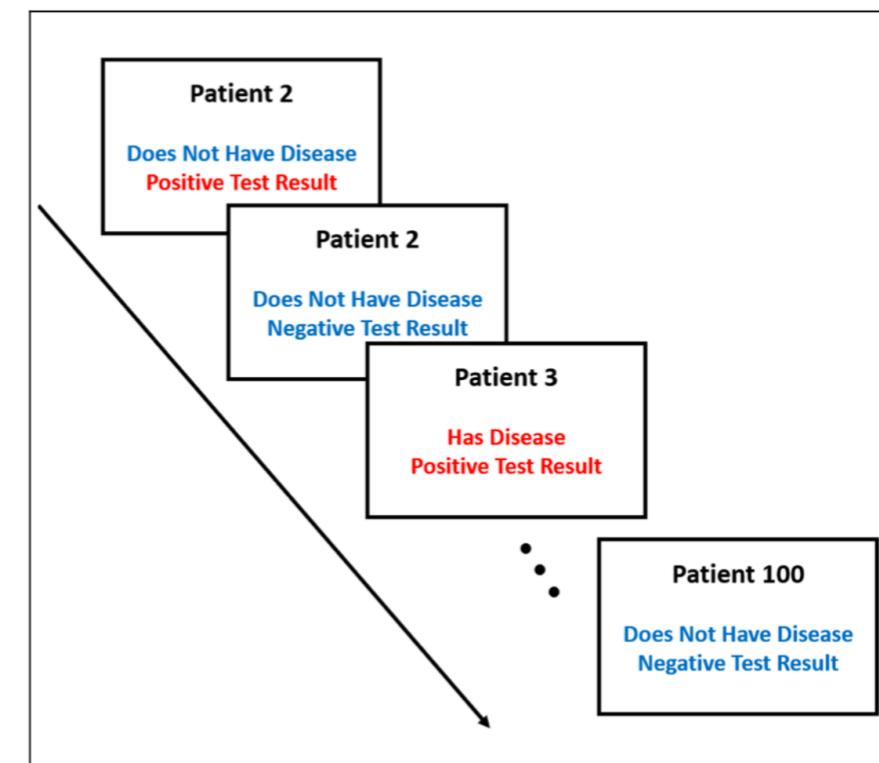


# Format benefits of experience in medical diagnosis

*Description*

	Polykronisia	Zymbosis
Disease prevalence (%)	2.00	1.00
Test properties (%)		
Sensitivity	100.00	100.00
Specificity	91.84	89
False-alarm rate	8.16	11.11
PPV	20.00	8.33
NPV	100.00	100.00
Frequency (experience format)		
Disease/positive test	2	1
Disease/negative test	0	0
No disease/positive test	8	11
No disease/negative test	90	88

*Experience*



# Format benefits of experience in medical diagnosis

	Description		Experience	
	Younger	Older	Younger	Older
PPV error				
Polykronesia	58.30 (29.01)	51.67 (31.42)	19.15 (26.53)	7.78 (18.07)
Zymbosis	64.53 (37.77)	57.93 (39.51)	10.81 (21.22)	9.29 (19.64)
NPV error				
Polykronesia	26.03 (39.03)	26.03 (39.03)	5.51 (16.15)	8.45 (18.48)
Zymbosis	15.83 (29.18)	27.97 (39.13)	2.84 (4.92)	8.39 (16.70)
Self-assessment				
Confidence	2.75 (1.03)	2.87 (1.20)	3.43 (0.93)	3.28 (1.28)
Difficulty	3.75 (0.87)	3.75 (0.81)	3.05 (1.01)	3.10 (1.11)
Belief in accuracy	3.20 (0.85)	3.20 (0.82)	3.55 (1.06)	3.50 (0.78)
Self v. physician	6.45 (2.72)	6.63 (2.68)	6.38 (2.39)	5.75 (2.44)

# Interactive 1

# bit.ly/tapmi2020

## I The description-experience gap ☰



### Interactive 1 - 5min

Go to this [site](#) to try out risky choices based on experience and description. **Don't sample for too long.**

### Interactive 2 - 5min

Please enter your intuitions about how people explore using this [survey](#).

## References

Wulff, D. U., Mergenthaler-Canseco, M., & Hertwig, R. (2018). A meta-analytic review of two modes of learning and the description-experience gap. *Psychological bulletin*, 144(2), 140-176.

Hertwig, R., Wulff, D. U., & Mata, R. (2018). Three gaps and what they may mean for risk preference. *Philosophical Transactions of the Royal Society B*, 374(1766), 20180140.

Spektor, M., & Wulff, D. U. (in prep.) Strategic information search. Manuscript in preparation.

Wulff, D. U., Hills, T. T., & Hertwig, R. (2015). Online product reviews and the description-experience gap. *Journal of Behavioral Decision Making*, 28(3), 214-223.

## II Harnessing simulated experiences ☰

7.34	+5.97%	▲	100.08	120,000
7.89	+2.13%	▲	564.23	900,000
7.45	+6.43%	▲	765.90	600,000

### Interactive 1 - 20min

Go to this [site](#) to explore the cognitive underpinnings of decisions from experience.

When you think you have found the best mix of cognitive components go to this [survey](#) to enter your predictions.

### Interactive 2 - 20min

Try out each of the risk intervention tools below (simply click on them). Only explore the tool. **Don't answer the questions** posed to after you've made the decisions.



When you have explore all risk intervention tools, go to this [survey](#) to share your impression on each of the tools.

## References

Kaufmann, C., Weber, M., & Haisley, E. (2013). The role of experience sampling and graphical displays on one's investment risk appetite. *Management science*, 59(2), 323-340.

Hertwig, R., & Wulff, D. U. (in prep.). Learning From Experience and Description: Two Powerful Yet Imperfect Teachers of Risk Cognition. Invited by *Nature Human Behavior*.



Censored

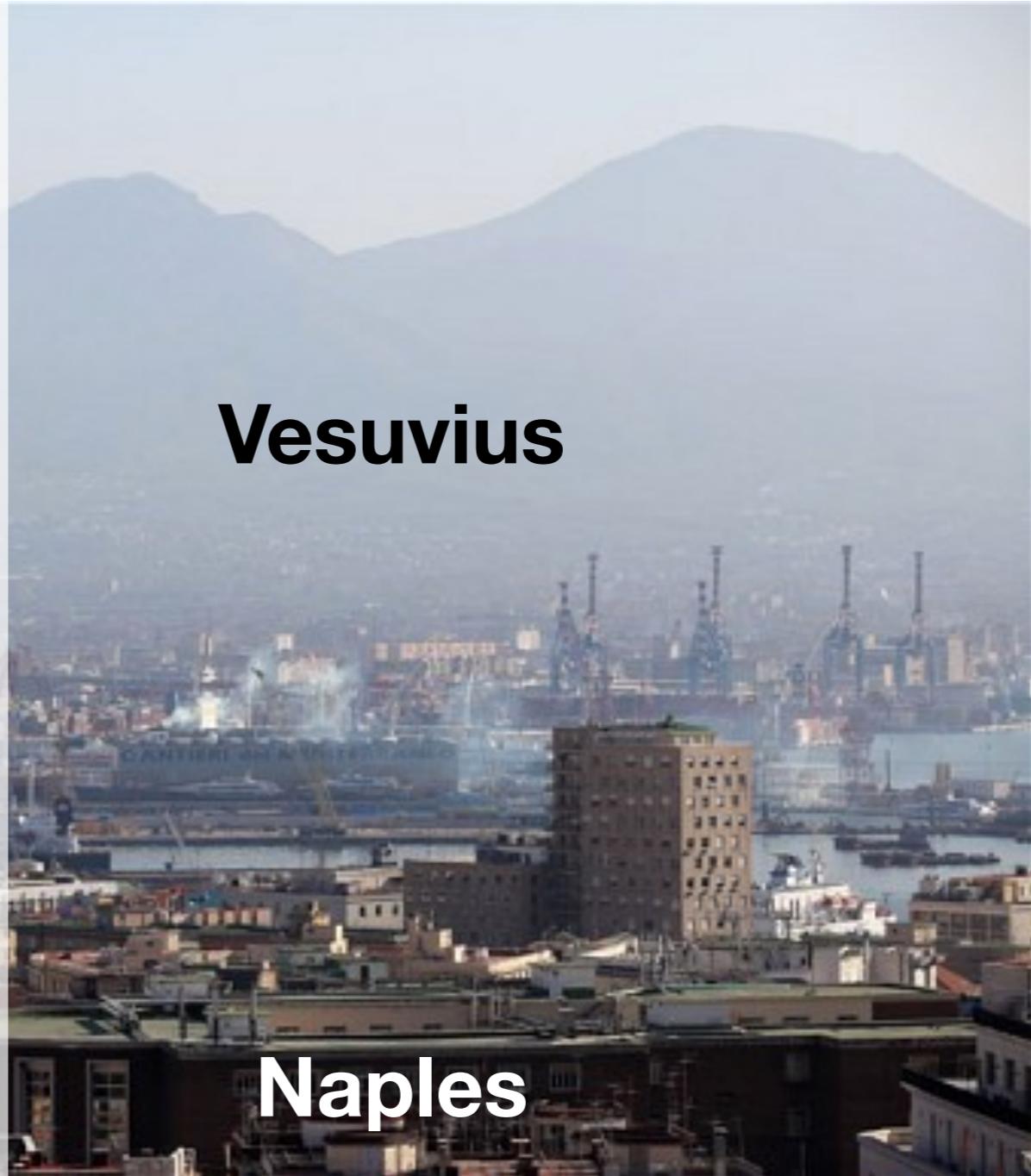
Censored

# The Weight of Experience

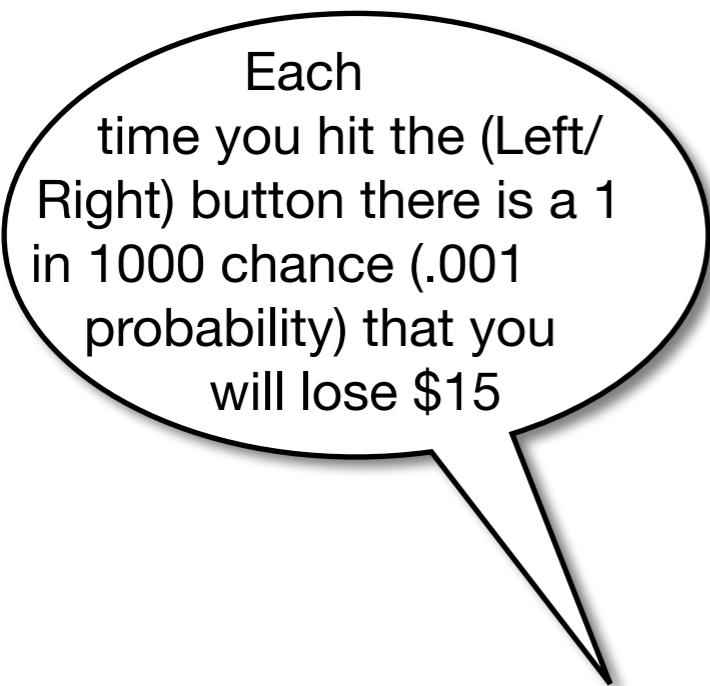
“A crisis could start today. The trouble is that nobody would be able to tell how long it would last, what type of eruption it would be, or how the event would evolve”

“There would be no modern precedent for an evacuation of this magnitude. This is why the Vesuvius is the most dangerous volcano of the world.”

Giuseppe Mastrolorenzo,  
Vesuvius Volcano Observatory  
(Nature, 2011)



# The Weight of Experience



Early

**Warning**

Repeated Choice

Late

Repeated Choice

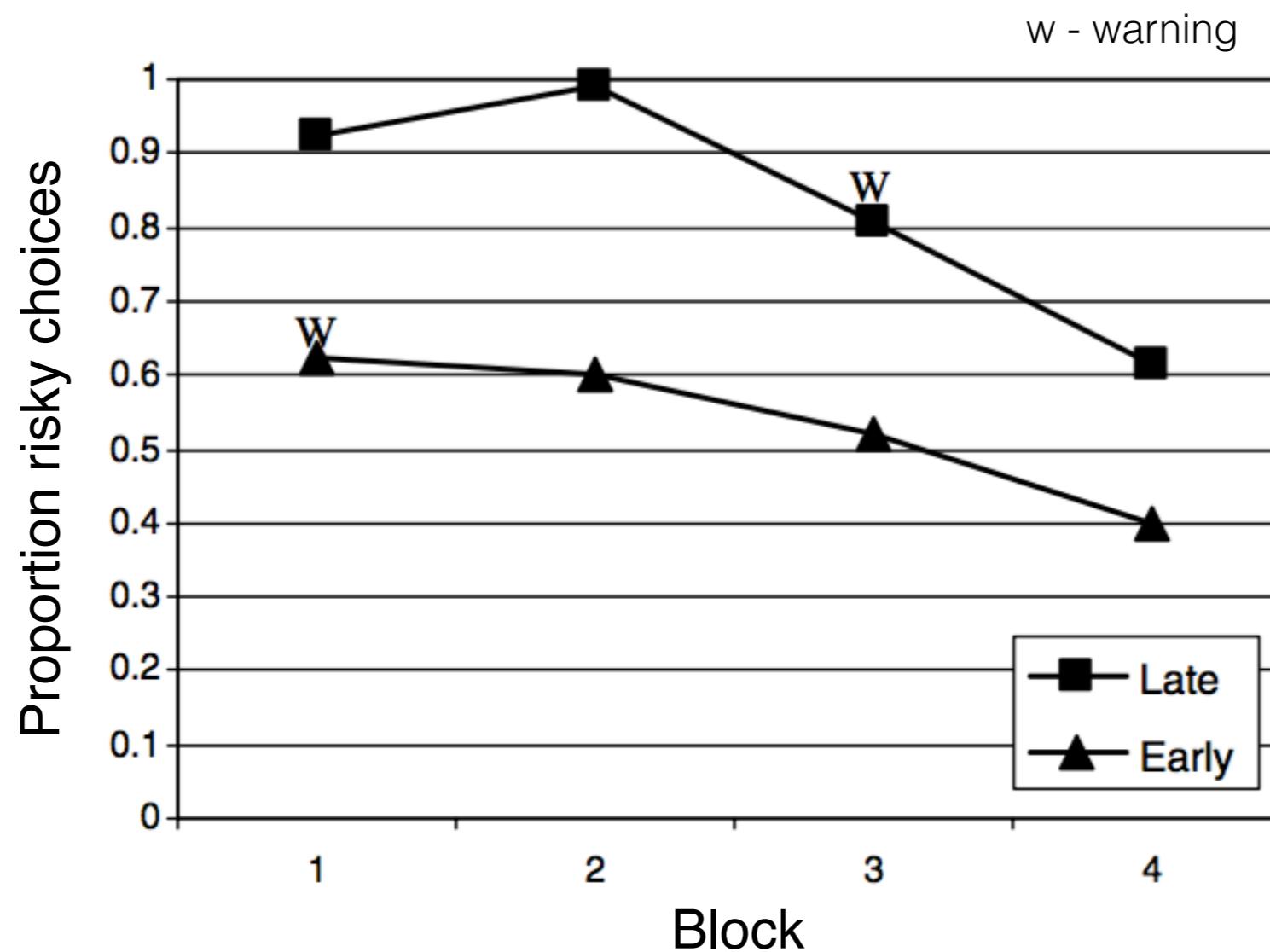
**Warning**

Repeated Choice

**A**  
\$0.1  
for sure

**B**  
\$0.13 w/ 99.9%  
or  
-\$15 w/ 0.1%

# The Weight of Experience



# 4 epistemic states

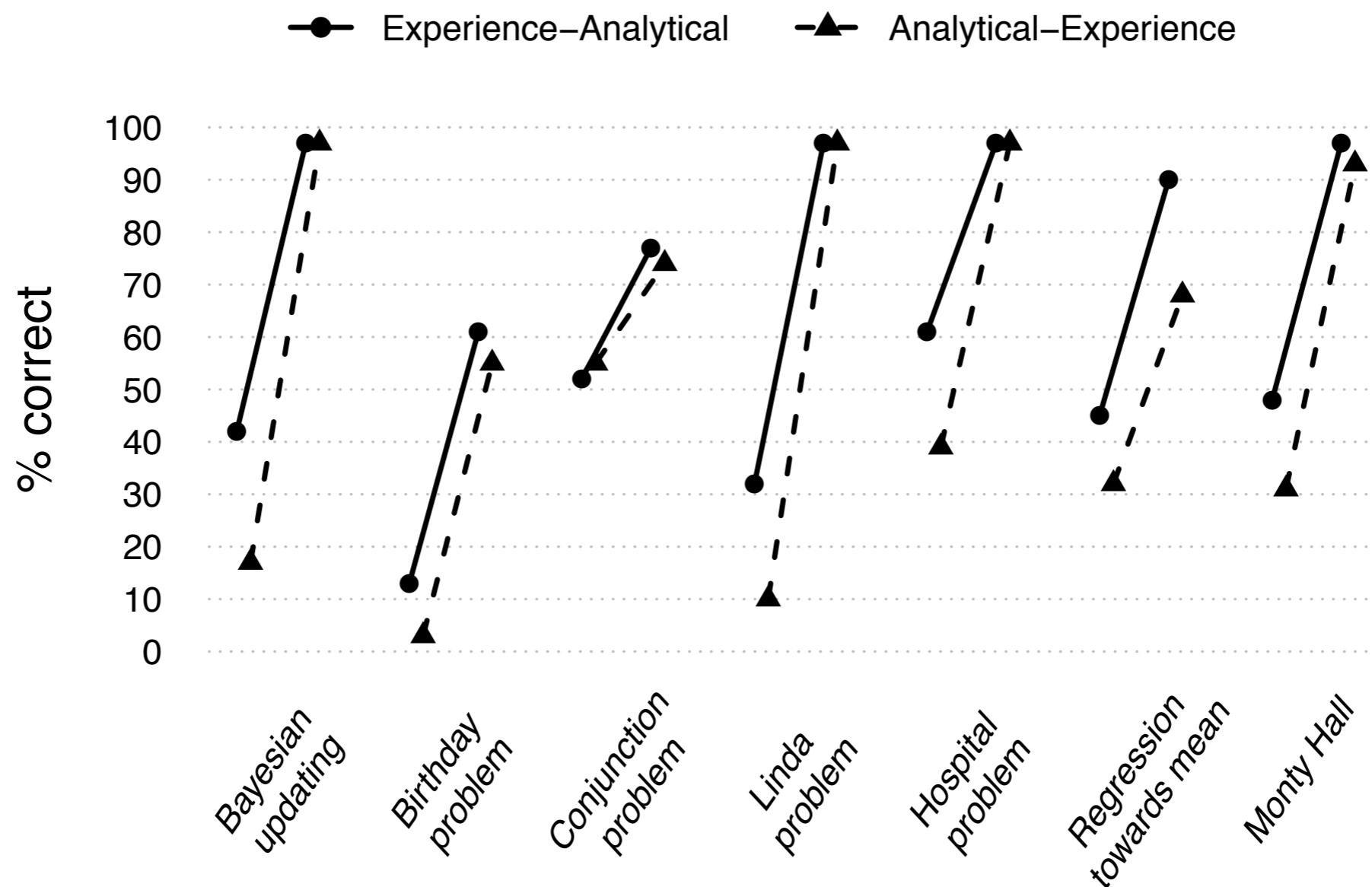
Experience -      Description -

Experience +      Description -

Experience -      Description +

Experience +      Description +

# Experience improves probabilistic inference



# Conclusions

- 1** Modes of learning shape risk perception and behavior
- 2** Experience weighs heavier than description.
- 3** Experience may foster a better understandings of probabilities
- 4** Good risk communication probably requires both experience and description.



**Ralph  
Hertwig**  
*MPI for Human  
Development*

# Appendix

# Asset allocation

Kaufmann, Weber, & Haisley (2013)

**Fund A is a risk-free asset.** It has a guaranteed annual return of **3.35% for sure**. If you invest the full \$100 in Fund A, you will have a return of \$118 in five years, net of fees.

**Fund B is a risky asset.** It has an expected annual return of **8.92% with an annual standard deviation of 15.89%**. If you invest the full \$100 in that asset, you will have an expected final outcome of \$153 in five years. However, the actual return is not known. It could be higher or lower. In 70 out of 100 cases your final wealth will be between \$100 and \$208 and in 95 out of 100 cases between \$72 and \$289.

Amount to invest in Fund A **30**

Amount to invest in Fund B **70**

Fund A



Fund B

**Based on your allocation, your expected return in 5 years is: \$136**

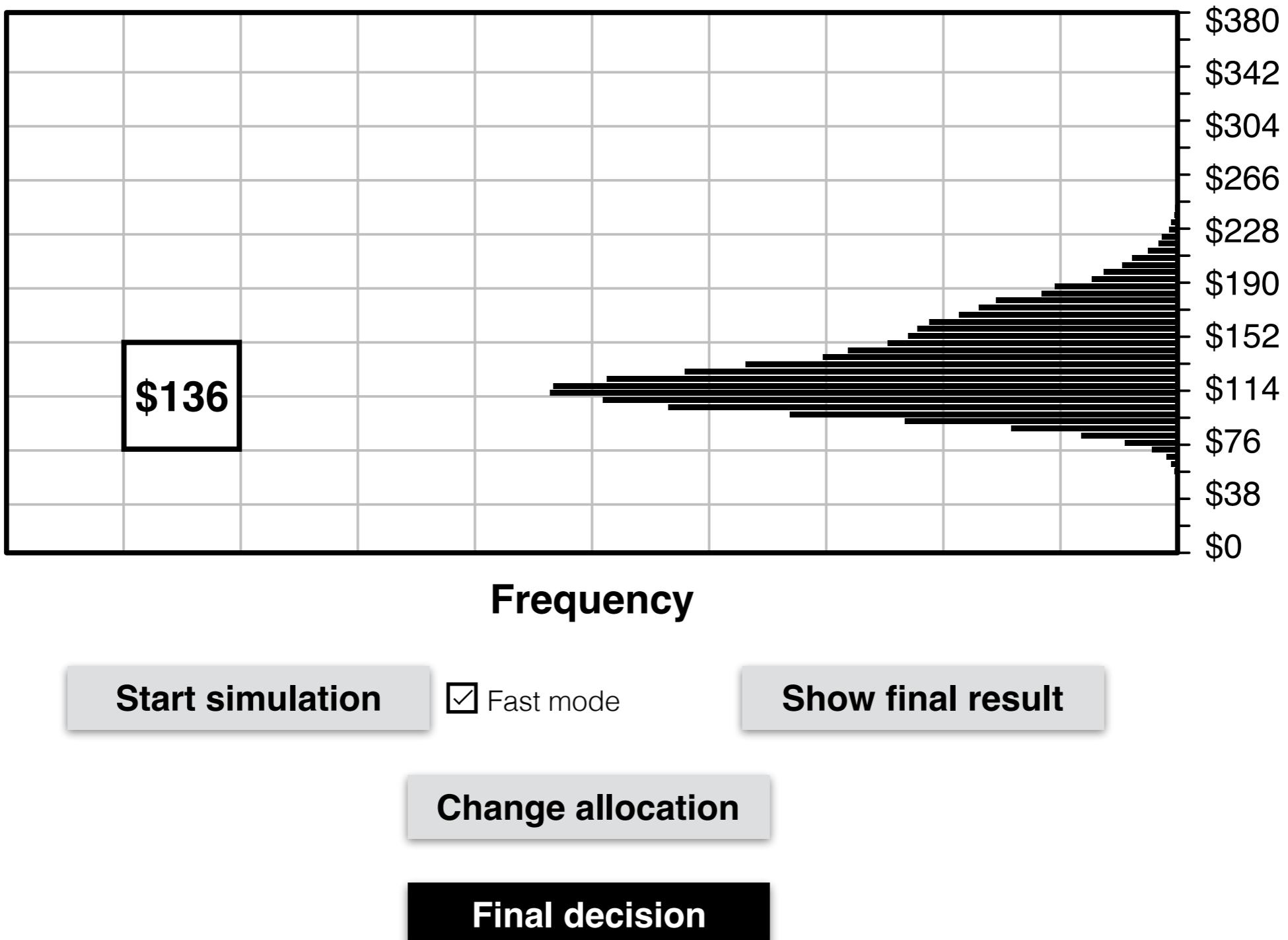
In 70 out of 100 cases your return will be between \$109 and \$163.

In 95 out of 100 cases your return will be between \$95 and \$203.

Final  
decision

# Asset allocation

Kaufmann, Weber, & Haisley (2013)



# Inference Problems

## in Hogarth & Soyer (2011)

### 1. Bayesian Updating (Gigerenzer et al., 2007, version)

Assume you conduct breast cancer screening using mammography in a certain region. You know the following information about the women in this region:

The probability that a woman has breast cancer is 1% (prevalence).

If a woman has breast cancer, the probability that she tests positive is 90% (sensitivity).

If a woman does not have breast cancer, the probability that she nevertheless tests positive is 9% (false-positive rate).

A woman—chosen at random—gets breast screening, and the test results show that she has cancer. What is the probability that she has cancer?

- a) The probability that she has breast cancer is about 81%.
- b) Out of 10 women with a positive mammogram, about 9 have breast cancer.
- c) Out of 10 women with a positive mammogram, about 1 has breast cancer.
- d) The probability that she has breast cancer is about 1%.

### 2. Birthday Problem

In a group that has 25 people in it, what is the probability that 2 or more people have the same birthday?

### 3. Conjunction Problem

A project has 7 parts. The success of the project depends on the success of these parts. In order to be successful, all its parts need to be successful.

Assume that each part is independent from the others and each has a 75% success rate.

What is the probability that the project will be successful?

### 4. Linda Problem (Tversky & Kahneman, 1983)

Jessica is 31 years old, single, candid, and very promising. She graduated in philosophy. As a student, she was anxious about discrimination issues and social justice and also took part in antinuclear demonstrations.

Assign a rank to the following statements from most probable to least probable:

- a) Jessica works in a bookstore and takes yoga classes.
- b) Jessica is active in the feminist movement.
- c) Jessica is a psychiatric social worker.
- d) Jessica is a member of the League of Women Voters.
- e) Jessica is a bank teller.
- f) Jessica is an insurance salesperson.
- g) Jessica is a bank teller and is active in the feminist movement.

### 5. The Hospital Problem (Tversky & Kahneman, 1974)

A certain town is served by two hospitals. In the larger hospital, about 45 babies are born each day. In the smaller hospital, about 15 babies are born each day. As you know, about 50 percent of all babies are girls. However, the exact percentage varies from day to day. Sometimes it may be higher than 50 percent, sometimes lower. For a period of 1 year, each hospital recorded the days on which more than 60 percent of the babies born were girls.

Which hospital do you think recorded more such days?

- a) the larger hospital?
- b) the smaller hospital?
- c) about the same for both hospitals?

### 6. Regression Toward the Mean

A class of students enters in a TOEFL exam (it is a standardized test of English language). One of the students gets a better result than 90% of the class.

The same class, including the person who had done better than 90% of his class, enters another TOEFL exam. Past data suggest that the correlation between the scores of the different exams is about 0.8.

Which statement is correct?

- a) It is more likely that the student in question now gets a better ranking.
- b) It is more likely that the student in question now gets a worse ranking.
- c) The chances that the student gets a better ranking or a worse one are approximately equal.

### 7. Monty Hall Problem

There are three doors: A, B, and C. We randomly selected one of them and put a Ferrari behind it. There is nothing behind the remaining two doors.

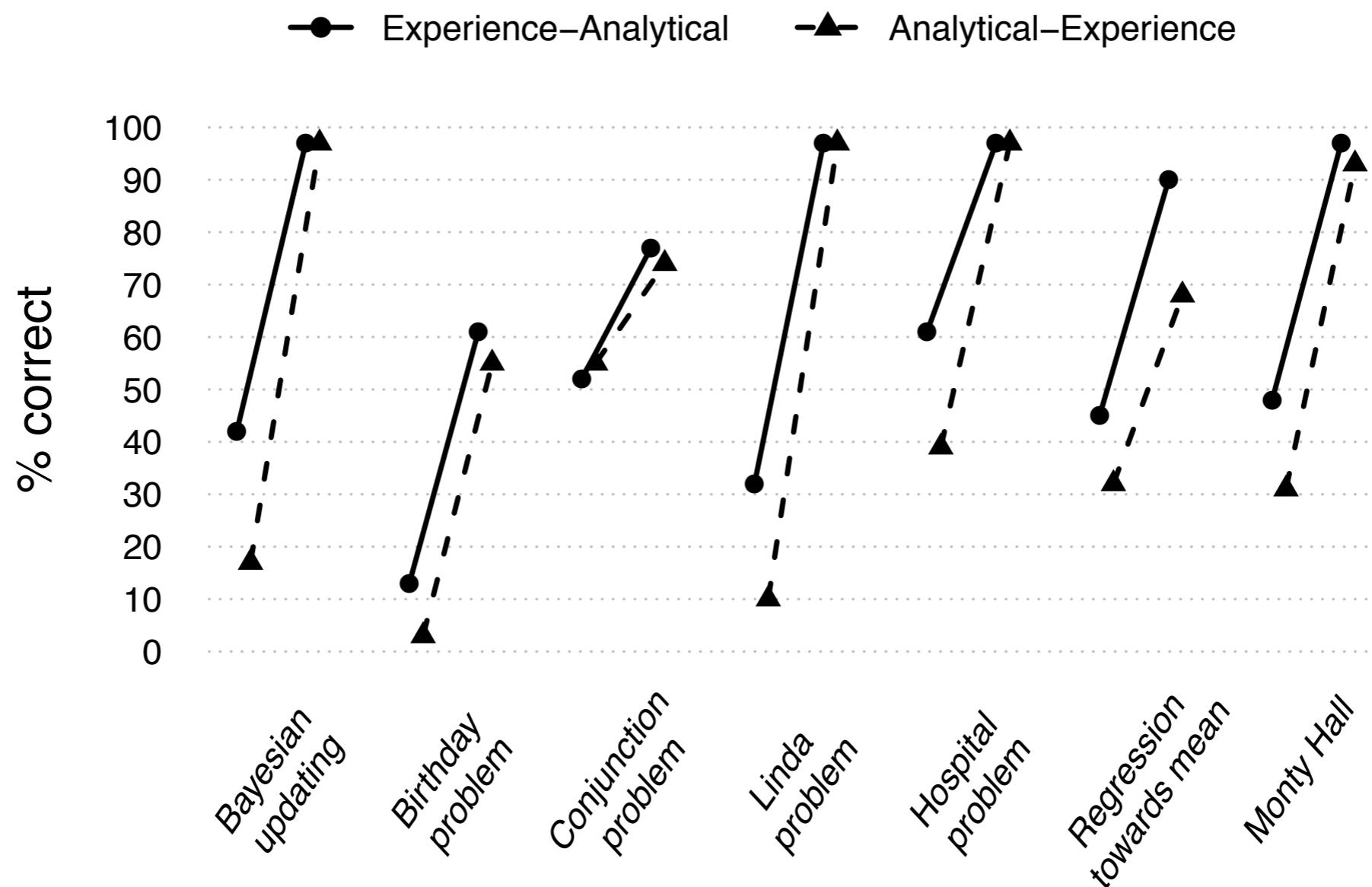
You will select a door, and we will open it. You will win the game if there is Ferrari behind it.

Now select a door. (The participant makes a selection, say A).

Before we open the door you selected, we open B and show you that there is nothing behind it. Now two doors remain: A and C. Behind one of them is a Ferrari. Given this situation, please state if you would like to

- a) Stay with your original selection
- b) Change to the other door

# Experience improves probabilistic inference



# Linear position weighting in autonomous sampling and flat in regulated sampling

