



**3-primary Adams-Novikov spectral sequence for the sphere**

The classes in this chart, representing the ANSS  $E_2$  page, were generated using the 3-primary version of Guozhen Wang's algebraic Novikov program. Solid dots denote copies of  $\mathbb{Z}/3$ . Concentric circles denote copies of  $\mathbb{Z}/9$ . Brown lines of slope 1/3 denote multiplication by  $\alpha_1$ . Blue dashed lines denote  $\beta_1$ -divisible classes. Gray dashed lines indicate  $(\alpha_1, \alpha_1, \dots)$  Massey products.

Higher differentials are complete through the 108 stem, and are inferred from the homotopy groups computed in the green book (Table A3.4). When a differential has a source or target of dimension  $\geq 1$ , in general we do not claim to specify which linear combination is involved. (Similarly, we do not attempt to indicate whether a differential hits a generator, or 2 times the generator.)

The differentials beyond the 108 stem are just the easy differentials propagated via  $\beta_1$ -multiplications. Propagating other differentials, as well as determining new families of differentials, is work in progress.