## CSE 321 - Homework 4

Due date: 25/12/2022, 23:59

1. 20 pts. Consider a computer game with a 2D map with axes  $A(A_1, A_2, ..., A_n)$  and  $B(B_1, B_2, ..., B_m)$ . The goal is to start from  $A_1B_1$ , move step by step to arrive at  $A_nB_m$ , and reach the highest possible score. At each coordinate the player arrives, they gain a (positive) number of game points. Additionally, there is a rule that restricts the movements. If the player is at  $A_iB_j$ , their next move should be either  $A_iB_{j+1}$  or  $A_{i+1}B_j$ , and no other movement is possible.

## **Example:**

Input: n = 4, m = 3Game map:

	$B_1$	$B_2$	$B_3$
$A_1$	25	30	25
$A_2$	45	15	11
$A_3$	1	88	15
$A_4$	9	4	23

Output:

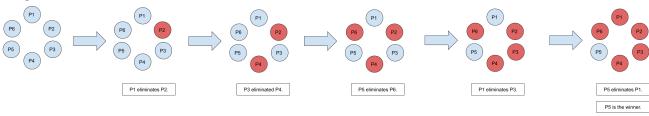
*Route*:  $A_1B_1 \rightarrow A_2B_1 \rightarrow A_2B_2 \rightarrow A_3B_2 \rightarrow A_3B_3 \rightarrow A_4B_3$ 

Points: 25 + 45 + 15 + 88 + 15 + 23 = 211

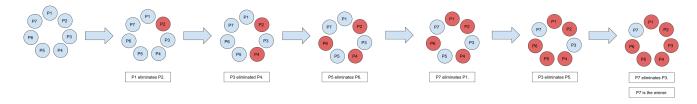
Design a brute-force algorithm to find the sequence of steps to reach the maximum number of total points.

- 2. 20 pts. Design a decrease and conquer algorithm that finds the median of an unsorted array.
- Consider a game with n players  $\{P_1, P_2, ..., P_n\}$ . The players are lined up circularly and at each step, a player eliminates the nearest player on their left. The game starts with  $P_1$ 's move.  $P_1$  eliminates  $P_2$ . Then the next player in the line,  $P_3$ , makes a move and eliminates  $P_4$ . In the end, only one player is left and that player wins the game. Examine the following examples to understand the game better.

Example: n = 6



## Example: n = 7



- (a) *10 pts*. Design an algorithm that finds the winner of the game, by using a circular linked list. Make sure your algorithm runs in linear time.
- (b) 20 pts. Design a decrease-and-conquer algorithm that finds the winner of the game. Make sure your algorithm runs in logarithmic time.
- 4. **20 pts.** Ternary search is a search algorithm similar to binary search but it requires the array to be divided into 3 parts instead of 2 parts at each step. The time complexity of ternary search is  $O(log_3n)$  while the time complexity of binary search is  $O(log_2n)$ . It seems like there is an improvement in terms of time complexity since  $log_3n < log_2n$ .

Compare the time complexities of these two algorithms. Explain how the divisor affects the complexity of the search algorithm. Assuming the array has n elements, what does the time complexity of the algorithm become if we divide it into n parts at the beginning?

- 5. Learn about interpolation search and answer the following questions.
  - (a) 5 pts. What is the best-case scenario of interpolation search? What is the time complexity of it?
  - (b) 5 pts. What is the difference between interpolation search and binary search in terms of the manner of work and the time complexity? Middle of the complexity?

## **Important Notes**

- For the first 3 problems, implement your solution in Python3. Write a driver function to test each of these algorithms. Inputs should be randomly generated (by using *random* library) or taken from the user (you may assume that the inputs are proper). Gather all of the python code in a single .py file. Do not use external libraries or functions to implement a part of the solution. Pay attention to clean coding.
- Write a report explaining the reasoning behind the algorithms you coded and analyze the worst-case time complexity of each of them. This report should also include your answers to Question 4 and Question 5. Write your report by using a program like MS Office and then convert it to a single PDF file. Pictures of handwritten works are **not accepted**.
- Upload two files only, a .py file and a .pdf file, **not a .zip or a .rar file**.