

# Hybrid-EP + Junction Tree Demo

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## Computing the log normalizing constant of the G-Wishart density

Consider the G-Wishart density, which has the following form:

$$f(\Omega \mid G) \propto |\Omega|^{(\delta-2)/2} \exp(-\text{tr}(\Omega\Lambda)/2),$$

Here,  $\Omega, \Lambda$  are  $p \times p$  non-negative definite matrices, and  $\delta > 2$  is the degrees of freedom. The normalizing constant is typically intractable, and the algorithm that we develop in this package targets this quantity.

**Case 1:**  $p = 30$ .

Define the following problem settings. We first randomly initialize the  $30 \times 30$  adjacency matrix representation of the graph  $G$ .

```
library(graphml)
set.seed(1234)
p = 30
Adj = matrix(rbinom(p^2,1,0.15), p, p)
Adj = Adj + t(Adj)
diag(Adj) = 0
Adj[Adj==1]=0
Adj[Adj==2]=1
diag(Adj) = 1
```

Next, we define the following degrees of freedom and scale matrix.

```
b = 500
Y = matrix(rnorm(p*500), nrow = 500, ncol = p)
Lambda = t(Y)%*%Y
```

Next, we compute the edge matrix which is needed for the junction tree part of the Hybrid-EP + JT algorithm.

```
# compute the edge matrix
EdgeMat = graphml::getEdgeMat(Adj)
```

Finally, we compute the Hybrid-EP + JT approximation to the log normalizing constant.

```

start_time <- Sys.time()
hyb_approx = graphml::hybridJT(Adj, EdgeMat, b, Lambda, 1000)
end_time <- Sys.time()
hyb_approx

```

```
## [1] -7450.699
```

```
end_time - start_time
```

```
## Time difference of 0.023839 secs
```

We compare this to Atay's method.

```

start_time <- Sys.time()
atay_approx = BDgraph::gnorm(Adj, b, Lambda, 1000)
end_time <- Sys.time()
atay_approx

```

```
## [1] -7428.426
```

```
end_time - start_time
```

```
## Time difference of 0.09324002 secs
```

We observe that the two estimates are quite close to each other, and that the Hybrid-EP + JT method is faster.

**Case 2:**  $p = 60$ .

```

library(graphml)
set.seed(1234)
p = 60
Adj = matrix(rbinom(p^2,1,0.15), p, p)
Adj = Adj + t(Adj)
diag(Adj) = 0
Adj[Adj==1]=0
Adj[Adj==2]=1
diag(Adj) = 1
b = 500
Y = matrix(rnorm(p*500), nrow = 500, ncol = p)
Lambda = t(Y)%*%Y
# compute the edge matrix
EdgeMat = graphml::getEdgeMat(Adj)

```

Finally, we compute the Hybrid-EP + JT approximation to the log normalizing constant.

```
start_time <- Sys.time()
hyb_approx = graphml::hybridJT(Adj, EdgeMat, b, Lambda, 1000)
end_time <- Sys.time()
hyb_approx
```

```
## [1] -15170.04
```

```
end_time - start_time
```

```
## Time difference of 0.09867001 secs
```

We compare this to Atay's method.

```
start_time <- Sys.time()
atay_approx = BDgraph::gnorm(Adj, b, Lambda, 1000)
end_time <- Sys.time()
atay_approx
```

```
## [1] -Inf
```

```
end_time - start_time
```

```
## Time difference of 1.531597 secs
```

We observe that Atay's method fails to give a finite estimate, while the Hybrid-EP + JT quickly produces a sensible approximation.