Lab 5 Exercise - A little Linear Regression

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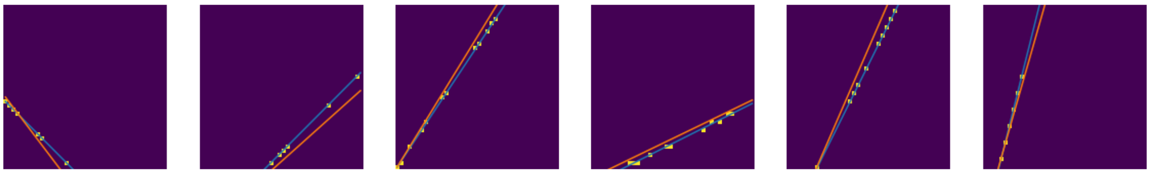
This is the exercise that you need to work through **on your own** after completing the fifth lab session. You'll need to write up your results/answers/findings and submit this to ECS handin as a PDF document along with the other lab exercises near the end of the module (1 pdf document per lab).

You should use *no more* than one side of A4 to cover your responses to *this* exercise. This exercise is worth 5% of your overall module grade.

1 An initial attempt

In the lab exercise you built and trained a couple of CNNs for image classification. Your now going to try something different and build some CNNs for image-to-vector regression task - in particular you're going to implement a network that takes an image of a scatter plot, and predicts the parameters of the line of best fit.



The following code is used to generate the datasets for this task (get it in a useable form here: `https://gist.github.com/jonhare/73a59dcc5416729548a086a983e81f07`):

```
import torch
from torchvision import transforms
from torch.utils.data import Dataset

class MyDataset(Dataset):
  def __init__(self, size=5000, dim=40, random_offset=0):
        super(MyDataset, self).__init__()
        self.size = size
        self.dim = dim
        self.random_offset = random_offset

  def __getitem__(self, index):
      if index >= len(self):
          raise IndexError('{} index out of range'.format(self.__class__.__name__))

      rng_state = torch.get_rng_state()
      torch.manual_seed(index + self.random_offset)

      while True:
        img = torch.zeros(self.dim, self.dim)
        dx = torch.randint(-10,10,(1,),dtype=torch.float)
        dy = torch.randint(-10,10,(1,),dtype=torch.float)
        c = torch.randint(-20,20,(1,), dtype=torch.float)

        params = torch.cat((dy/dx, c))
        xy = torch.randint(0,img.shape[1], (20, 2), dtype=torch.float)
```

```
        xy[:,1] = xy[:,0] * params[0] + params[1]

        xy.round_()
        xy = xy[ xy[:,1] > 0 ]
        xy = xy[ xy[:,1] < self.dim ]
        xy = xy[ xy[:,0] < self.dim ]

        for i in range(xy.shape[0]):
          x, y = xy[i][0], self.dim - xy[i][1]
          img[int(y), int(x)]=1
        if img.sum() > 2:
          break

      torch.set_rng_state(rng_state)
      return img.unsqueeze(0), params

  def __len__(self):
      return self.size

train_data = MyDataset()
val_data = MyDataset(size=500, random_offset=33333)
test_data = MyDataset(size=500, random_offset=99999)
```

1.1 A simple CNN baseline (2 marks)

Implement the following CNN model, and train it using Adam (default parameters) for 100 epochs (use a GPU and be prepared to wait 6 or 7 minutes!). Use shuffled batches of 128 items. State the loss function you're using. **Comment** on the performance of the model.

```
Convolution2D, channels=48, size=3x3, stride=1, padding=1
ReLU
Linear, 128 outputs
ReLU
Linear, 2 outputs
```

2 A second attempt

Clearly the CNN implemented in Section 1 has many parameters in its final hidden layers. One common way of reducing this is to use Global Max Pooling to flatten the feature maps into a vector (called `AdaptiveMaxPool2d` in PyTorch).

2.1 A simple CNN with global pooling (1 mark)

Implement the following CNN model, and train it using Adam (default parameters) for 100 epochs. Use shuffled batches of 128 items. **Comment** on the model performance.

```
Convolution2D, channels=48, size=3x3, stride=1, padding=1
ReLU
Convolution2D, channels=48, size=3x3, stride=1, padding=1
ReLU
Global Max Pool
Linear, 128 outputs
ReLU
Linear, 2 outputs
```

3 Something that actually works?

The two models so far likely have a few issues. We're now going to try and fix this.

3.1 Let's regress (2 marks)

Modify the model from Section 2 as follows:

1. Modify the number of input channels to the first convolutional layer to be 3 instead of 1
2. In the forward pass, before the first convolution, modify the input, `x`, using the following code:

```
idxx = torch.repeat_interleave(
    torch.arange(-20,20, dtype=torch.float).unsqueeze(0) / 40.0,
    repeats=40, dim=0).to(x.device)
idxy = idxx.clone().t()
idx = torch.stack([idxx, idxy]).unsqueeze(0)
idx = torch.repeat_interleave(idx, repeats=x.shape[0], dim=0)
x = torch.cat([x, idx], dim=1)
```

Train the modified model using Adam (default parameters) for 100 epochs. Use shuffled batches of 128 items. **Comment** on the model performance. **Describe** the rationale for the modification that was made.