Process Sequences



Recurrent Neural Networks

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A lot of the ideas in this lecture come from Andrej Karpathy's blog post on the Unreasonable Effectiveness of RNNs (http://karpathy.github.io/2015/05/21/rnn-effectiveness/). Many of the images and animations were made by Adam Prügel-Bennett.

Recurrent Neural Networks - Motivation

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Recurrent Neural Networks - Motivation

$$x: x^{(1)} \dots x^{(t)} \dots x^{(T_x)}$$

$$y: y^{(1)} \dots y^{(t)} \dots y^{(T_y)}$$

In this example, $T_x = T_y = 7$ but T_x and T_y can be different.

Recurrent Neural Networks

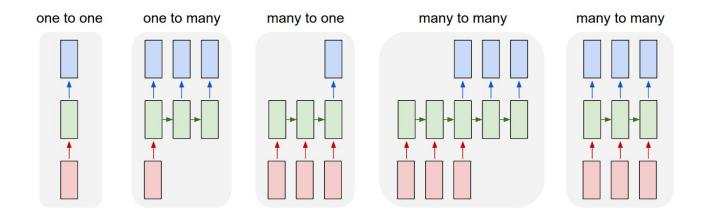


Image from http://karpathy.github.io/2015/05/21/rnn-effectiveness/

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Aside: One Hot Encoding

How can we represent individual words (or other discrete tokens)?

"a" "abbreviations"

0

0

1 0 . . . 0 0 0 0 1

0

"zoology"

"zoom"

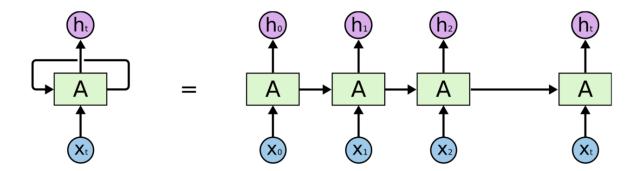
Image from https://ayearofai.com

Why Not a Standard Feed Forward Network?

- For a task such as "Named Entity Recognition" a MLP would have several disadvantages
 - The inputs and outputs may have varying lengths
 - The features wouldn't be shared across different temporal positions in the network
 - Note that 1-D convolutions can be (and are) used to address this, in addition to RNNs more on this in a later lecture
- To interpret a sentence, or to predict tomorrows weather it is necessary to remember what happened in the past
- To facilitate this we would like to add a feedback loop delayed in time

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Recurrent Neural Networks



- RNNs are a family of ANNs for processing sequential data
- RNNs have directed cycles in their computational graphs

Recurrent Neural Networks

RNNs combine two properties which make them very powerful.

- Distributed hidden state that allows them to store a lot of information about the past efficiently. This is because several different units can be active at once, allowing them to remember several things at once.
- Non-linear dynamics that allows them to update their hidden state in complicated ways¹.

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Recurrent Neural Networks

RNNs are Turing complete in the sense they can simulate arbitrary programs².

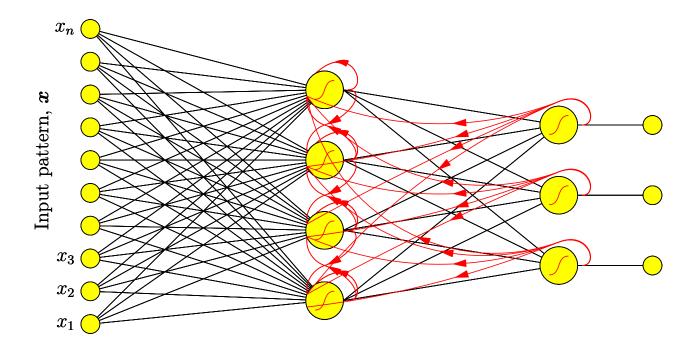
If training vanilla neural nets is optimisation over functions, training recurrent nets is optimisation over programs.

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 $^{^1\}mathrm{Often}$ said to be difficult to train, but this is not necessarily true - dropout can help with overfitting for example

²Don't read too much into this - like universal approximation theory, just because they can doesn't mean its necessarily learnable!

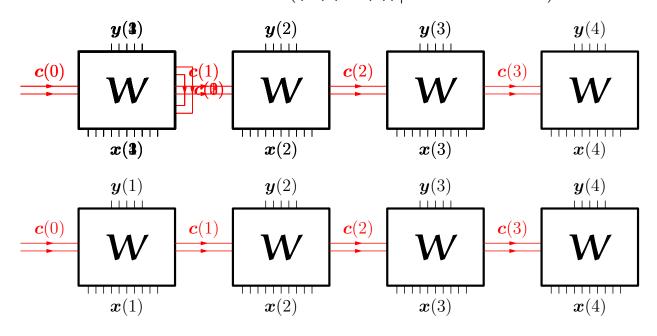
Recurrent Network



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Training Recurrent Networks

• Given a set of inputs $\mathcal{D} = \big((\mathbf{x}(t), \mathbf{y}(t)) \big| t = 1, 2, \ldots, T \big)$



• Minimise an error (here MSE, but your choice):

$$E(\boldsymbol{W}) = \sum_{\text{RNNs}}^{I} \|\boldsymbol{y}(t) - \boldsymbol{f}(\boldsymbol{x}(t), \boldsymbol{c}(t-1) | \boldsymbol{W}) \|^{2}$$

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An RNN is just a recursive function invocation

- y(t) = f(x(t), c(t-1)|W)
- ullet and the state $oldsymbol{c}(t) = oldsymbol{g}(oldsymbol{x}(t), oldsymbol{c}(t-1) | oldsymbol{W})$
- If the output y(t) depends on the input x(t-2), then prediction will be

$$f(x(t), g(x(t-1), g(x(t-2), g(x(t-3)|W)|W)|W)|W)$$

• it should be clear that the gradients of this with respect to the weights can be found with the chain rule

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What is the state update g()?

- It depends on the variant of the RNN!
 - Elman
 - Jordan
 - LSTM
 - GRU

Elman Networks ("Vanilla RNNs")

$$egin{aligned} m{h}_t &= \sigma_h(m{W}_{ih}m{x}_t + m{b}_{ih} + m{W}_{hh}m{h}_{t-1} + m{b}_{hh}) \ m{y}_t &= \sigma_y(m{W}_ym{h}_t + m{b}_y) \end{aligned}$$

- σ_h is usually tanh
- σ_y is usually identity (linear) the y's could be regressed values or logits
- the state h_t is referred to as the "hidden state"
- the output at time t is a projection of the hidden state at that time
- the hidden state at time t is a summation of a projection of the input and a projection of the previous hidden state

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Going deep: Stacking RNNs

- RNNs can be trivially stacked into deeper networks
- It's just function composition:

$$\mathbf{y}(t) = \mathbf{f}_2(\mathbf{f}_1(\mathbf{x}(t), \mathbf{c}_2(t-1)|\mathbf{W}_1), \mathbf{c}_2(t-1)|\mathbf{W}_2)$$

- The output of the inner RNN at time t is fed into the input of the outer RNN which produces the prediction y
- Also note: RNNs are most often not used in isolation it's quite common to process the inputs and outputs with MLPs (or even convolutions)

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Example: Character-level language modelling

- We'll end with an example: an RNN that learns to 'generate' English text by learning to predict the next character in a sequence
- This is "Character-level Language Modelling"

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Example: Character-level language modelling

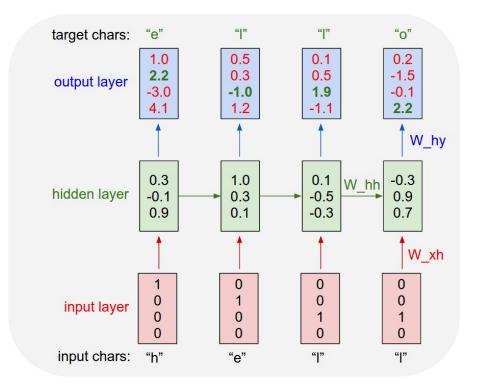


Image from http://karpathy.github.io/2015/05/21/rnn-effectiveness/

Training a Char-RNN

- The training data is just text data (e.g. sequences of characters)
- The task is unsupervised (or rather self-supervised): given the previous characters predict the next one
 - All you need to do is train on a reasonable sized corpus of text
 - Overfitting could be a problem: dropout is very useful here

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Sampling the Language Model

- Once the model is trained what can you do with it?
- if you feed it an initial character it will output the logits of the next character
- you can use the logits to select the next character and feed that in as the input character for the next timestep
- how do you 'sample' a character from the logits?
 - you could pick the most likely (maximum-likelihood solution), but this
 might lead to generated text with very low variance (it might be boring
 and repetitive)
 - you could treat the softmax probabilities defined by the logits as a categorical distribution and sample from them
 - you might increase the 'temperature', T, of the softmax to make the distribution more diverse (less 'peaky'): $q_i = \frac{\exp{(z_i/T)}}{\sum_j \exp{(z_j/T)}}$

A lot of the ideas in this lectu on the input c(t-1), g(x) is (x(t-2), g(t-1) - W) lged snllhomitpon" ares Mnt Net) the

Onaafed a tre the sidisicters of to prediction couponet on the logits its venvows usts sevouvd be this in as useuled at on in the pan Lerate'atectsrray to paet inputs D = Pxxpraition the rople, the next

vog the state atite

- Sampled from a single layer RNN³.

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³LSTM, 128 dim hidden size, with linear input projection to 8-dimensions and output to the number of characters (84). Trained on the text of these slides for 50 epochs.