

Lab Sheet 3 Answers

Elliot Potts
ep15449@my.bristol.ac.uk

March 10, 2017

We will indicate the value of the variable a after the n^{th} iteration of the loop body using a subscript, or none if it's value doesn't change throughout the program. e.g.

y_4 is the value of y after the loop body has been executed 4 times.

0.0.1 Hypothesis

We want to show that:

$$\forall x. \forall y_0. (x > 0 \wedge y_0 > 0) \rightarrow z_n = x^{y_0}$$

$$\frac{x > 0 \quad y_0 > 0}{z_n = x^{y_0}}$$

0.0.2 Proof

By inspection of the code:

1. $z_0 = x$
2. $x_i = x$
3. $z_{i+1} = z_i \times x$
4. $y_{i+1} = y_i - 1$

Perform induction over y_0 . Base case. Let $y = 1$
 $(x > 0 \wedge 1 > 0) \rightarrow z_n = x^1$