VORONOI DIAGRAMS



April 2016

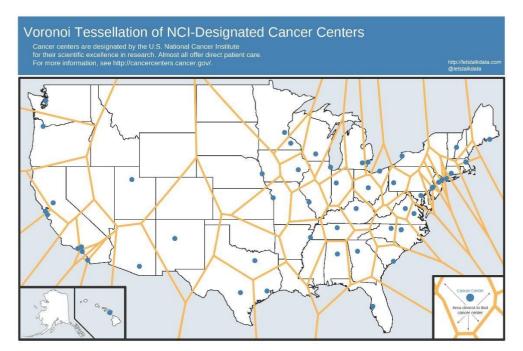
Johan Blomme

Leenstraat 11 – 8340 Damme-Sijsele

URL: www.johanblomme.net Email: j.blomme@telenet.be

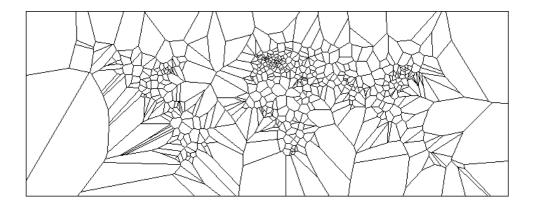
A Voronoi diagram is a partitioning of a plane into regions based on distance to points in a specific subset of the plane. That set of points (called seeds, sites, or generators) is specified beforehand, and for each seed there is a corresponding region consisting of all points closer to that seed than to any other. These regions are called Voronoi cells.

Example :



1 Introduction

```
Example 1 : read in a point shapefile to be converted to a Voronoi diagram
library(rgdal)
dsn <- system.file("vectors", package = "rgdal")[1]</pre>
cities <- readOGR(dsn=dsn, layer="cities")</pre>
str(cities)
  str(cities)
Formal class 'SpatialPointsDataFrame' [package "sp"] with 5 slots
..@ data :'data.frame': 606 obs. of 4 variables:
....$ NAME : Factor w/ 602 levels "Abidjan","Abu Zaby",..: 368 34 472 322 419 593 390
194 263 115 .
194 263 115 ...
....$ COUNTRY : Factor w/ 165 levels "Afghanistan",..: 124 124 124 1
4 124 ...
....$ POPULATION: num [1:606] 468000 416000 5825000 152000 1160000 ...
....$ CAPITAL : Factor w/ 2 levels "N","Y": 1 1 1 1 1 1 1 1 1 1 ...
...@ coords.nrs : num(0)
                           : Factor w/ 165 levels "Afghanistan",..: 124 124 124 124 124 124 124 153 12
  ..@ coords.nrs : num(0)
..@ coords : num [1:606, 1:2] 33.1 40.6 30.5 150.8 56.2 ...
... - attr(*, "dimnames")=List of 2
... ... $ : NULL
... ... $ : chr [1:2] "coords.x1" "coords.x2"
..@ bbox : num [1:2, 1:2] -165.3 -53.2 177.1 78.2
... - attr(*, "dimnames")=List of 2
... ... $ : chr [1:2] "coords.x1" "coords.x2"
... ... $ : chr [1:2] "min" "max"
..@ proj4string:Formal class 'CRS' [package "sp"] with 1 slot
... ..@ projargs: chr "+proj=longlat +datum=WGS84 +no_defs +ellps=WGS84 +towgs84=0,0,0"
Function to create voronoi polygons (originally developed by Carson Farmer) :
this (modified) function accepts vectors of coordinates (expected in order x, y) as
well as a SPDF (see http://stackoverflow.com/questions/12156475)
# Carson's Voronoi polygons function
library(deldir)
voronoipolygons <- function(x) {</pre>
   require (deldir)
   require(sp)
  if (.hasSlot(x, 'coords')) {
     crds <- x@coords
   } else crds <- x</pre>
   z \leftarrow deldir(crds[,1], crds[,2])
   w <- tile.list(z)</pre>
   polys <- vector(mode='list', length=length(w))</pre>
   for (i in seq(along=polys)) {
     pcrds <- cbind(w[[i]]$x, w[[i]]$y)</pre>
      pcrds <- rbind(pcrds, pcrds[1,])</pre>
      \verb"polys[[i]] \gets \verb"Polygons(list(Polygon(pcrds))", ID=as.character(i)")
   SP <- SpatialPolygons(polys)</pre>
   voronoi <- SpatialPolygonsDataFrame(SP, data=data.frame(x=crds[,1],</pre>
                                                                                             y=crds[,2],
                     row.names=sapply(slot(SP, 'polygons'),
                     function(x) slot(x, 'ID'))))
v <- voronoipolygons(cities)</pre>
class(v)
> class(v)
[1] "SpatialPolygonsDataFrame"
attr(,"package")
[1] "sp"
```



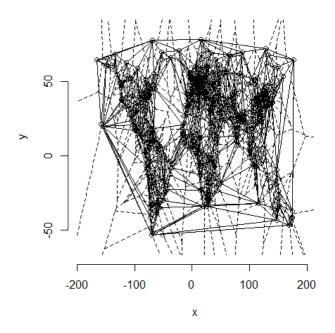
Alternative way to create Voronoi diagram with library deldir.

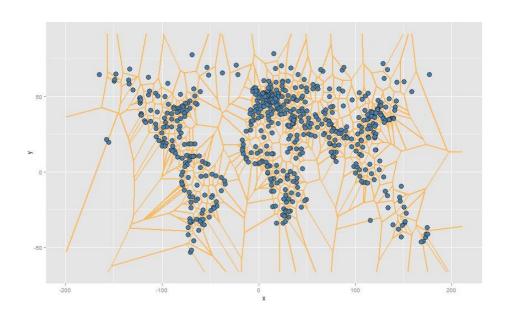
```
library(deldir)
v_ <- deldir(cities$coords.x1,cities$coords.x2)
class(v_)</pre>
```

> class(v_)

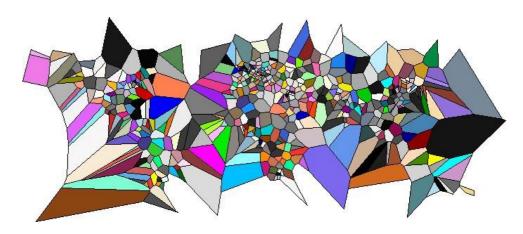
[1] "deldir"

 $plot(v_{-})$

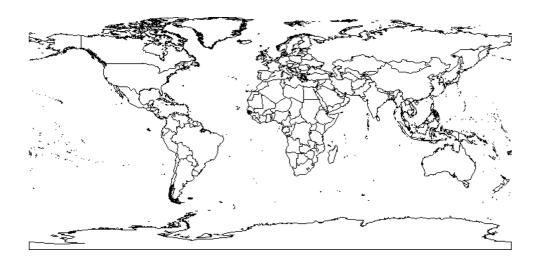




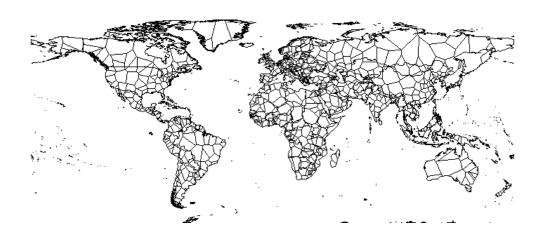
```
# plot the polygons of a Voronoi tesselation instead of segments
# convert line segments to spatialpolygons objects
# see http://stackoverflow.com/questions/24311304
# function to convert line segments in $dirsgs to spatialpolygons
voronoi <- v
voronoi$dirsgs <- v_$dirsgs
library(rgeos)
11 <- apply(voronoi$dirsgs, 1, FUN=function(X) {</pre>
 readWKT(sprintf("LINESTRING(%s %s, %s %s)", X[1], X[2], X[3], X[4]))
11 <- apply(v $dirsgs, 1, FUN=function(X) {</pre>
 readWKT(sprintf("LINESTRING(%s %s, %s %s)", X[1], X[2], X[3], X[4]))
# convert SpatialLines list to SpatialPolygons object
pp <- gPolygonize(ll)</pre>
class(pp)
> class(pp)
[1] "SpatialPolygons"
attr(,"package")
[1] "sp"
# plot
set.seed=11
plot(pp, col=sample(colors(), length(pp)))
```



```
# read shapefile of the world
setwd("c:/R/Rdata")
world <- readOGR(".","TM_WORLD_BORDERS_SIMPL-0.3")
class(world)
> class(world)
[1] "spatialPolygonsDataFrame"
attr(,"package")
[1] "sp"
plot(world)
```



final <- gIntersection(world, v, byid=TRUE)
plot(final)</pre>



final2 <- gIntersection(world,pp,byid=TRUE)
plot(final2,col=sample(colors(), length(pp)))</pre>

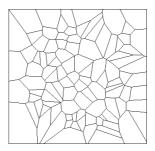


Example 2 : input is vectors of x, y coordinates
dat <- data.frame(x=runif(100), y=runif(100))
str(dat)</pre>

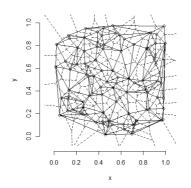
> str(dat)

'data.frame': 100 obs. of 2 variables: \$ x: num 0.284 0.521 0.818 0.303 0.309 ... \$ y: num 0.95 0.106 0.436 0.618 0.528 ...

v2 <- voronoipolygons(dat)
plot(v2)</pre>



library(deldir)
v3 <- deldir(dat\$x,dat\$y)
plot(v3)</pre>



(2) Working with voronoi polygons

```
R script : "c:/R/Rdata/voronoi.R"
# hospitals West Flanders : estimate the population served by hospitals
# note : remove sites with duplicate lat/long, which would break the
  voronoi algorithm !
# e.g. sites <- sites[!duplicated(sites$latitude), ]</pre>
# input of x, y coordinates in csv-file
setwd("c:/R/Rdata")
hospitals <- read.csv("ziekenhuizen_wvl_geocoded.csv",header=T,sep=",")
str(hospitals)
> str(hospitals)
                        37 obs. of 4 variables:
'data.frame':
 $ address: Factor w/ 37 levels "AZ Alma Campus Sijsele Gentsesteenweg 132 8340 Sijsele",..:
1 2 3 5 4 6 7 8 9 12 ...
             : num 51.2 51.2 51.2 50.8 50.8 ...
 $ long : num 3.32 2.93 2.91 3.26 3.27 ...
 $ accuracy: Factor w/ 4 levels "hospital","locality",..: 4 2 1 3 3 4 3 1 3 1 ...
head(hospitals)
> head(hospitals)
> head(hospitals)

AZ Alma Campus Sijsele Gentsesteenweg 132 8340 Sijsele 51.20156 3.321246 sublocality_level_1

AZ Damiaan Campus H. Hart Gauwelozestraat 100 8400 Oostende 51.21543 2.928656 locality

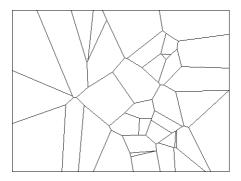
AZ Damiaan Campus Sint-Jozef Nieuwpoortsesteenweg 57 8400 Oostende 51.22322 2.906011 hospital

AZ Groeninge Campus O.-L. Vrouw Reepkaai 4 8500 Kortrijk 50.82971 3.260921 street_address

AZ Groeninge Campus Maria's Voorzienigheid Loofstraat 43 8500 Kortrijk 50.81991 3.267864 street_address

AZ Groeninge Campus Sint-Maarten Burg. Vercruysselaan 5 8500 Kortrijk 50.81949 3.257708 sublocality_level_1
coords <- as.data.frame(cbind(hospitals$long,hospitals$lat))</pre>
class(coords)
> class(coords)
[1] "data.frame"
str(coords)
> str(coords)
'data.frame':
                        37 obs. of 2 variables:
 $ v1: num 3.32 2.93 2.91 3.26 3.27 ...
 $ v2: num 51.2 51.2 51.2 50.8 50.8 ...
names(coords) <- c("long","lat")</pre>
vp <- voronoipolygons(coords)</pre>
class(vp)
> class(vp)
[1] "SpatialPolygonsDataFrame"
attr(,"package")
[1] "sp"
```

plot(vp)



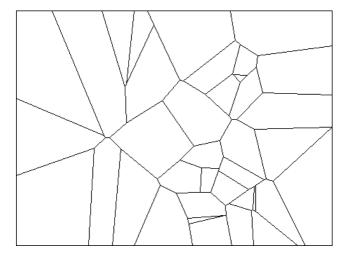
```
# convert coords into SpatialPoints
 points <- SpatialPoints(coords)</pre>
 class (points)
 > class(points)
 [1] "SpatialPoints"
 attr(,"package")
 [1] "sp"
 str(points)
 > str(points)
 Formal class 'SpatialPoints' [package "sp"] with 3 slots
     ..@ coords : num [1:37, 1:2] 3.32 2.93 2.91 3.26 3.27 ...
     ....- attr(*, "dimnames")=List of 2
     .. .. ..$ : NULL
     .. .. ..$ : chr [1:2] "V1" "V2"
     ..@ bbox
                                    : num [1:2, 1:2] 2.67 50.78 3.42 51.34
     ....- attr(*, "dimnames")=List of 2
     .....$ : chr [1:2] "V1" "V2"
     .....$ : chr [1:2] "min" "max"
     ..@ proj4string:Formal class 'CRS' [package "sp"] with 1 slot
     .. .. ..@ projargs: chr NA
 # create SpatialPointsDataFrame of points
 spdf <- SpatialPointsDataFrame(points,hospitals)</pre>
 class(spdf)
 > class(spdf)
 [1] "SpatialPointsDataFrame"
 attr(,"package")
 [1] "sp"
 str(spdf)
> str(spdf)
Formal class 'SpatialPointsDataFrame' [package "sp"] with 5 slots
...@ data :'data.frame': 37 obs. of 4 variables:
....$ address : Factor w/ 37 levels "AZ Alma campus Sijsele Gentsesteenweg 132 8340 Sijsele",..: 1 2 3 5 4 6 7 8 9 12 ...
...$ lat : num [1:37] 51.2 51.2 51.2 51.2 50.8 50.8 ...
....$ long : num [1:37] 3.32 2.93 2.91 3.26 3.27 ...
....$ accuracy: Factor w/ 4 levels "hospital","locality",..: 4 2 1 3 3 4 3 1 3 1 ...
...@ coords.nrs : num(0)
...@ coords : num [1:37, 1:2] 3.32 2.93 2.91 3.26 3.27 ...
.... - attr(*, "dimnames")=List of 2
.....$ : chr
....$ : chr
[1:2] "V1" "V2"
...@ bbox : num [1:2, 1:2] 2.67 50.78 3.42 51.34
.... - attr(*, "dimnames")=List of 2
.....$ : chr
....$ : chr
[1:2] "V1" "V2"
....$ : chr
....$ : chr
[1:2] "V1" "V2"
....$ : chr
....$ : chr
[1:2] "v1" "w2"
....$ : chr
....$ : chr
[1:2] "v1" "w2"
....$ : chr
....$ : chr
[1:2] "v1" "v2"
....$ : chr
....$ : chr
[1:2] "v1" "v2"
....$ : chr
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[1:2] "v1" "v2"
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[1:2] "v1" "v2"
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....$ : chr
[1:2] "v1" "v2"
....$ : chr
....$ : chr
[1:2] "v1" "v2"
....$ : chr
....$ : chr
[1:2] "v1" "v2"
```

voronoiPolys <- voronoipolygons(spdf)</pre> class(voronoiPolys)

> class(voronoiPolys)

[1] "SpatialPolygonsDataFrame" attr(,"package") [1] "sp"

plot(voronoiPolys)

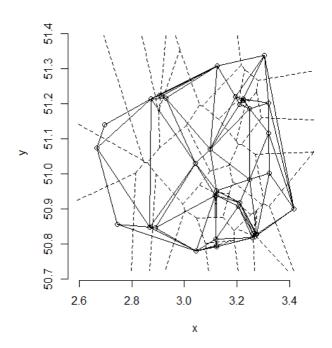


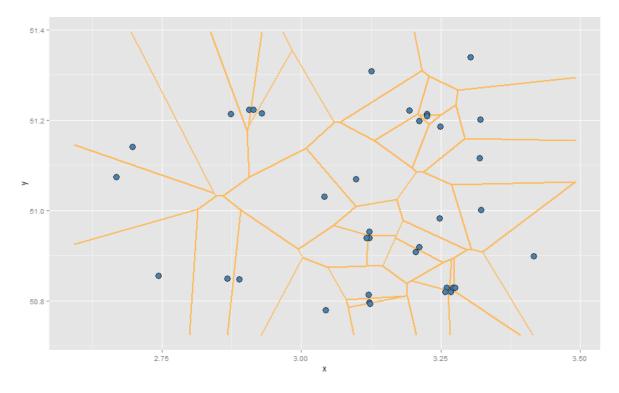
library(deldir) v_ <- deldir(spdf@data\$long,spdf@data\$lat)</pre> class(v_)

> class(v_)

[1] "deldir"

plot(v_)





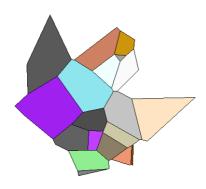
```
# plot the polygons of a Voronoi tesselation instead of segments
# convert line segments to spatialpolygons objects

voronoi <- v_
voronoi$dirsgs <- v_$dirsgs
library(rgeos)

11 <- apply(voronoi$dirsgs, 1, FUN=function(X) {
   readWKT(sprintf("LINESTRING(%s %s, %s %s)", X[1], X[2], X[3], X[4]))
})

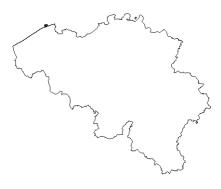
# convert SpatialLines list to SpatialPolygons object
pp <- gPolygonize(11)</pre>
```

```
# plot
set.seed=11
plot(pp, col=sample(colors(), length(pp)))
```



plot voronoi polygons (vor) and hospitals (coords)

```
# read shapefile of Belgium
library(rgdal)
belgium <- readOGR(".","BEL_adm0")
plot(belgium)</pre>
```



class(belgium)

```
> class(belgium)
```

[1] "SpatialPolygonsDataFrame"
attr(,"package")

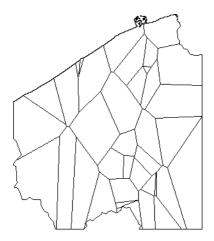
[1] "sp"

final <- gIntersection(belgium, voronoiPolys, byid=TRUE)
class(final)</pre>

> class(final)

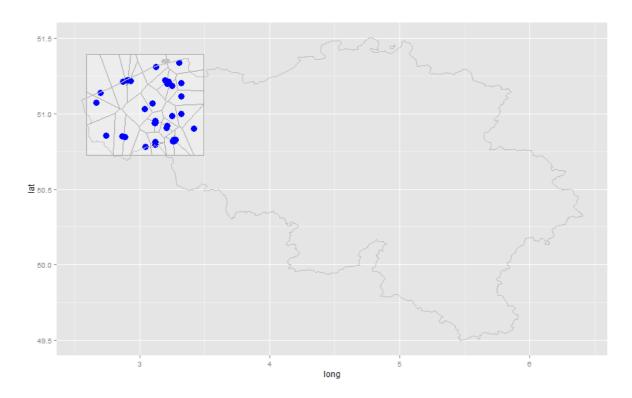
[1] "SpatialPolygons"
attr(,"package")
[1] "sp"

plot(final)



```
# convert voronoiPolys and shapefile Belgium into data frames to plot with ggplot2
vor <- fortify(voronoiPolys)
bel <- fortify(belgium)</pre>
```

HospAndVor



```
# plot voronoi diagram and population dots
# shapefile België mét veld voor populatie
library(rgdal)
library(maptools)
setwd("c:/R/Rdata")
belgie <- readOGR(".", "newbelgie")</pre>
plot(belgie)
```



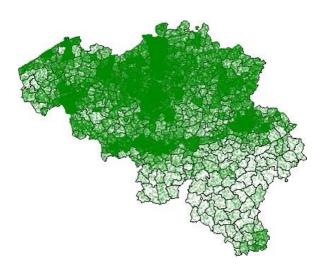
str(belgie@data)

```
> str(belgie@data)
'data.frame': 589 obs. of 21 variables:
$ ID_4 : int 3 4 5 11 12 15 16 17 21 27 ...
$ ID_0 : int 22 22 22 22 22 22 22 22 22 ...
$ ISO : Factor w/ 1 level "BEL": 1 1 1 1 1 1 1 1 1 1 ...
$ NAME_0 : Factor w/ 1 level "Belgium": 1 1 1 1 1 1 1 1 1 1 ...
$ ID_1 : int 1 1 1 1 1 1 1 1 1 1 ...
$ ID_1 : int 1 1 1 1 1 1 1 1 1 1 ...
$ NAME_1 : Factor w/ 3 levels "Bruxelles", "Vlaanderen", ...: 2 2 2 2 2 2 2 2 2 2 ...
$ ID_2 : int 1 1 1 1 1 1 1 1 1 1 1 ...
$ NAME_2 : Factor w/ 11 levels "Antwerpen", "Brabant wallon", ...: 1 1 1 1 1 1 1 1 1 ...
$ NAME_2 : Factor w/ 11 levels "Antwerpen", "Brabant wallon", ...: 1 1 1 1 1 1 1 1 1 ...
$ NAME_3 : int 1 1 1 1 1 1 1 1 1 1 1 ...
$ NAME_4 : Factor w/ 43 levels "Aslst", "Antwerpen", ...: 2 2 2 2 2 2 2 2 2 2 2 ...
$ NAME_4 : Factor w/ 588 levels "X&caussinnes" ...: 152 267 568 19 85 270 493 84 344 466 ...
$ VARNAME_4 : Factor w/ 41 levels "'S-Gravenbrakel", ...: NA ...
$ TYPE_4 : Factor w/ 1 levels "Commune", "Gemeente": 2 2 2 2 2 2 2 2 2 2 2 2 ...
$ ENGTYPE_4 : Factor w/ 1 level "Commune", 1 1 1 1 1 1 1 1 1 ...
$ row : num 0 1 2 3 4 5 6 7 8 9 ...
$ niscode : int 1016 1022 11033 11002 11009 11023 11044 11008 11057 11040 ...
$ twtot : int 4248 5123 4258 265777 7323 7360 3123 12434 7981 11095 ...
$ DENSITEIT: num 381 305 219 2458 307 ...
$ DENSITEIT: num 381 305 219 2458 307 ...
$ DENSITEIT: num -76.5 -71.7 -78.2 -47.1 -73.8 -72.3 -82.7 -66.7 -45.9 -67.1 ...
$ a andeel : num -76.5 -71.7 -78.2 -47.1 -73.8 -72.3 -82.7 -66.7 -45.9 -67.1 ...
$ a andeel : num 23.5 28.3 21.8 52.9 26.2 27.7 17.3 33.3 54.1 32.9 ...
  # turn shapefile into dotmap
dots.pop <- dotsInPolys(belgie,belgie@data$TOTAALBEV/100)</pre>
class(dots.pop)
> class(dots.pop)
```

[1] "SpatialPointsDataFrame" attr(,"package")

[1] "sp"

plot(belgie,lwd=0.05)
plot(dots.pop,add=TRUE,pch=19,cex=0.1,col="#00880030")



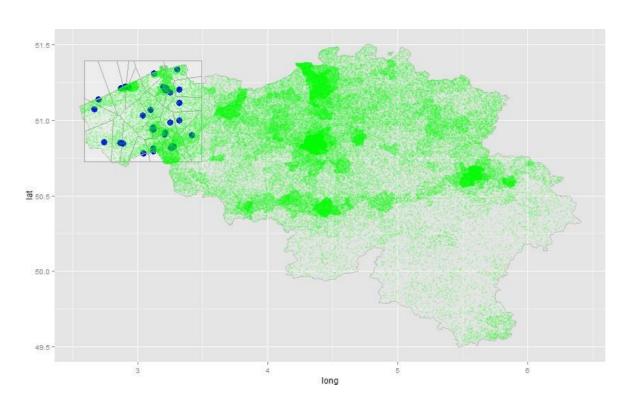
extract dataframe from population dots
pop.df <- data.frame(coordinates(dots.pop[,1:2])
str(pop.df)</pre>

> str(pop.df)

'data.frame': 110063 obs. of 2 variables: \$ x: num 4.49 4.46 4.52 4.5 4.45 ...

\$ x: num 4.49 4.46 4.52 4.5 4.45 ... \$ y: num 51.4 51.4 51.5 51.5 51.5 ...

VorAndDots <- HospAndVor +
geom_point(data=pop.df,aes(x=x,y=y),size=0.5,color="green",alpha=0.15)
VorAndDots</pre>

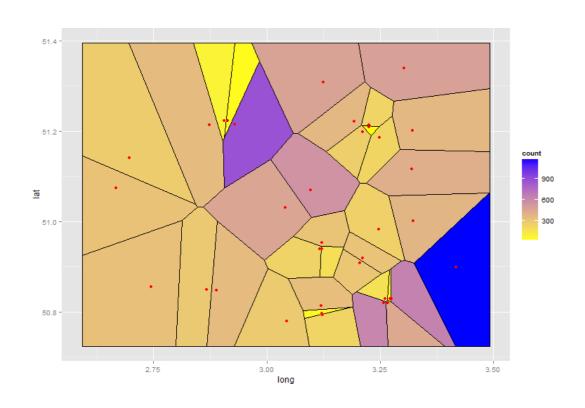


```
# estimate the total population served by each clinic
# pop.df (data frame) and voronoiPolys (SpatialPolygonsDataFrame) must have the
  same CRS
proj4string(voronoiPolys)
> proj4string(voronoiPolys)
[1] "+proj=longlat +datum=WGS84 +no_defs +ellps=WGS84 +towgs84=0,0,0"
coordinates(pop.df) <- ~ x + y</pre>
class(pop.df)
> class(pop.df)
[1] "SpatialPoints"
attr(,"package")
[1] "sp"
proj4string(pop.df) <- proj</pre>
# count the number of dots in each polygon in the voronoi diagram
count <- sapply(over(voronoiPolys, SpatialPoints(pop.df), returnList=TRUE), length)</pre>
count
> count
  1 2
        3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25
26 27 28
372 871 85 175 445 618 36 475 485 227 235 373 356 58 637 178 341 230 238 46 1168 273 251 415 260
291 25 355
 29 30 31 32 33 34 35 36 37
330 303 385 321 283 317 555 310 461
class(voronoiPolys)
> class(voronoiPolys)
[1] "SpatialPolygonsDataFrame"
attr(,"package")
[1] "sp"
class(pop.df)
> class(pop.df)
[1] "SpatialPoints"
attr(,"package")
[1] "sp"
# add the results of the count to the polygons
voronoiPolys <- spCbind(voronoiPolys, as.data.frame(count))</pre>
str(voronoiPolys@data)
> str(voronoiPolys@data)
'data.frame':
                 37 obs. of 3 variables:
       : num 3.32 2.93 2.91 3.26 3.27 ...
       : num 51.2 51.2 51.2 50.8 50.8 ...
$ count: int 372 871 85 175 445 618 36 475 485 227 ...
# convert voronoiPolys (SPDF) into a data frame to plot with ggplot2
voronoiPolys@data$id <- rownames(voronoiPolys@data)</pre>
str(voronoiPolys@data)
```

voronoiPolys.df <- fortify(voronoiPolys,region="id")</pre>

map

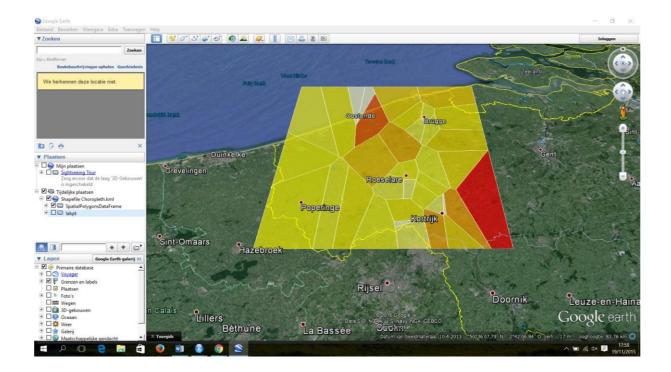
```
str(voronoiPolys.df)
> str(voronoiPolys.df)
'data.frame':
                  239 obs. of 7 variables:
 $ long : num 3.49 3.49 3.29 3.28 3.28 ...
 $ lat : num 51.3 51.2 51.2 51.2 51.3 ...
 $ order: int 1 2 3 4 5 6 7 8 9 10 ...
 $ hole : logi FALSE FALSE FALSE FALSE FALSE FALSE ...
 $ piece: Factor w/ 1 level "1": 1 1 1 1 1 1 1 1 1 1 ...
 \ group: Factor w/ 37 levels "1.1", "10.1", "11.1", ...: 1 1 1 1 1 2 2 2 2 ....
 $ id : chr "1" "1" "1" "1" ...
voronoiPolys.df <- merge(voronoiPolys.df,voronoiPolys@data,by="id")</pre>
str(voronoiPolys.df)
> str(voronoiPolys.df)
'data.frame':
                  239 obs. of 10 variables:
      : chr "1" "1" "1" "1" ...
 $ long: num 3.49 3.49 3.29 3.28 3.28 ...
 $ lat : num 51.3 51.2 51.2 51.2 51.3 ...
 $ order: int 1 2 3 4 5 6 7 8 9 10 ...
 $ hole : logi FALSE FALSE FALSE FALSE FALSE FALSE ...
 $ piece: Factor w/ 1 level "1": 1 1 1 1 1 1 1 1 1 1 ...
 $ group: Factor w/ 37 levels "1.1","10.1","11.1",..: 1 1 1 1 1 1 2 2 2 2 ...
       : num 3.32 3.32 3.32 3.32 ...
       : num 51.2 51.2 51.2 51.2 51.2 ...
 $ count: int 372 372 372 372 372 227 227 227 227 ...
map <- ggplot(voronoiPolys.df,aes(x=long,y=lat)) +</pre>
       geom_polygon(aes(group=group,fill=count),colour="black",size=0.1) +
       scale fill continuous(low="yellow", high="blue") +
       {\tt geom\_point(data=coords,aes(x=long,y=lat),colour="red",size=2) \ +}
       coord equal()
```



plot voronoiPolys (SpatialPolygonsDataFrame) with Google Earth (library plotKML)

library(plotKML)

voronoiPolys <- spTransform(voronoiPolys,CRS("+proj=longlat +datum=WGS84"))
kml(obj=voronoiPolys, folder.name="", file.name="Shapefile Choropleth.kml",
 kmz=FALSE,colour=count,colour_scale=R_pal[["heat_colors"]],alpha=0.75,
 altitude=0,plot.labpt=TRUE,labels=LABEL,LabelScale=0.5)</pre>



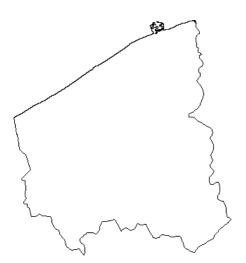
One of the weaknesses of voronoi estimators is their high variability, which makes them very sensitive to noise. We need to clip the voronoi diagram polygons within the geographic borders of the area we want to cover (rather than the arbitrarily large polygons at the edges of the diagram).

To do this, we import a shapefile of Belgian municipalities, select the province of West Flanders and collapse the polygons of that region into a single polygon. Then we repeat the steps of the previous exercise.

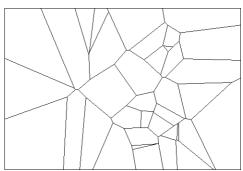
```
belgie <- readOGR(".","BEL_adm4")
wvl <- belgie[belgie@data$NAME_2 == "West-Vlaanderen", ]
plot(wvl)</pre>
```



library(maptools)
regs <- c("West-Vlaanderen")
sp2 <- wvl@data\$NAME_2
sp2[which(!wvl@data\$NAME_2 %in% regs)] <- NA
wvlP <- unionSpatialPolygons(wvl,sp2)
plot(wvlP)</pre>



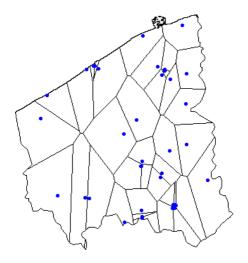
```
# function to clip voronoi polygons to a given extent
voronoipolygons <- function(x, poly) {</pre>
  require (deldir)
  if (.hasSlot(x, 'coords')) {
   crds <- x@coords
  } else crds <- x
  bb = bbox(poly)
  rw = as.numeric(t(bbox(poly)))
  z <- deldir(crds[,1], crds[,2],rw=rw)</pre>
  w <- tile.list(z)
  polys <- vector(mode='list', length=length(w))</pre>
  require(sp)
  for (i in seq(along=polys)) {
    pcrds <- cbind(w[[i]]$x, w[[i]]$y)
    pcrds <- rbind(pcrds, pcrds[1,])</pre>
    polys[[i]] <- Polygons(list(Polygon(pcrds)), ID=as.character(i))</pre>
  SP <- SpatialPolygons(polys)</pre>
  SpatialPolygonsDataFrame (
    SP, data.frame(x=crds[,1], y=crds[,2],
                    row.names=sapply(slot(SP, 'polygons'),
                                       function(x) slot(x, 'ID'))))
V <- voronoipolygons(coords, wvlP)</pre>
class(V)
> class(v)
[1] "SpatialPolygonsDataFrame"
attr(,"package")
[1] "sp"
plot(V)
```



```
proj4string(wvlP)
> proj4string(wvlP)
[1] "+proj=longlat +datum=wGs84 +no_defs +ellps=wGs84 +towgs84=0,0,0"
proj4string(V) <- proj4string(wvlP)

final <- gIntersection(wvlP,V,byid=TRUE)
class(final)
> class(final)
[1] "SpatialPolygons"
attr(,"package")
[1] "sp"
```

```
plot(final)
points(coords,pch=20,col="blue")
```



convert voronoiPolys and shapefile Belgium into data frames to plot with ggplot2 $\forall f < -$ fortify(V) class(Vf)

> class(Vf)

[1] "data.frame"

str(Vf)

> str(Vf)

```
'data.frame': 239 obs. of 7 variables:
$ long : num 3.53 3.53 3.29 3.28 3.28 ...
$ lat : num 51.3 51.2 51.2 51.2 51.3 ...
$ order: int 1 2 3 4 5 6 1 2 3 4 ...
$ hole : logi FALSE FALSE FALSE FALSE FALSE FALSE ...
$ piece: Factor w/ 1 level "1": 1 1 1 1 1 1 1 1 1 1 ...
$ group: Factor w/ 37 levels "1.1","2.1","3.1",..: 1 1 1 1 1 1 2 2 2 2 2 ...
$ id : chr "1" "1" "1" "1" ...
wvlf <- fortify(wvlP)
str(wvlf)</pre>
```

> str(wvlf)

```
'data.frame': 3115 obs. of 7 variables:

$ long : num   2.81 2.79 2.78 2.76 ...

$ lat : num   50.7 50.7 50.7 50.8 ...

$ order: int   1 2 3 4 5 6 7 8 9 10 ...

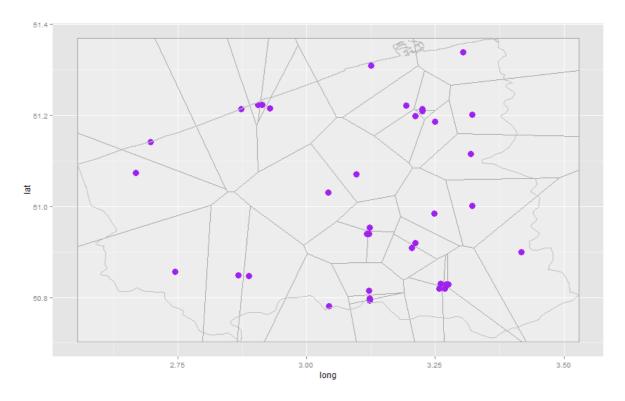
$ hole : logi   FALSE FALSE FALSE FALSE FALSE FALSE ...

$ piece: Factor w/ 2 levels "1","2": 1 1 1 1 1 1 1 1 1 1 1 1 1 1 ...

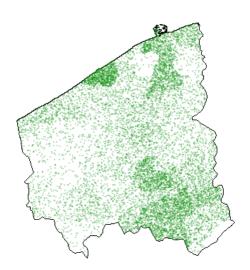
$ group: Factor w/ 2 levels "West-Vlaanderen.1",..: 1 1 1 1 1 1 1 1 1 ...

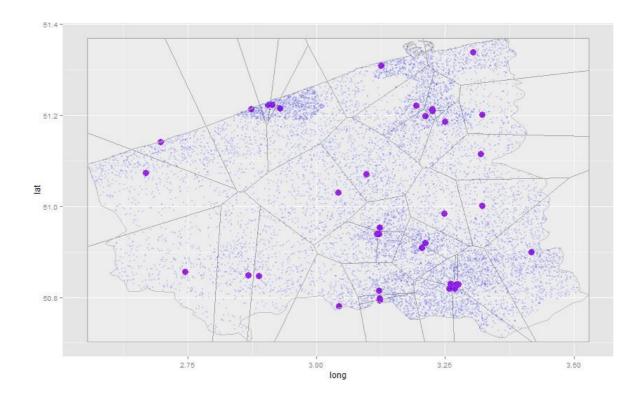
$ id : chr   "West-Vlaanderen" "West-Vlaanderen" "West-Vlaanderen" ...
```

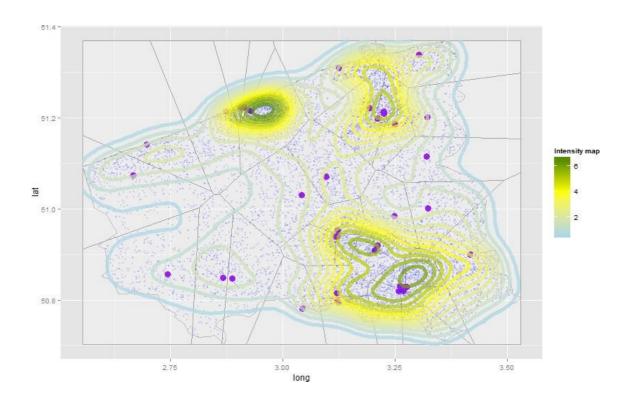
```
# plot voronoi polygons (Vf) and hospitals (coords)
HospAndVor <- ggplot(data=Vf,aes(x=long,y=lat)) +
  geom_polygon(aes(group=group),colour="grey65",size=0.4,fill="white",alpha=0.3) +
  geom_point(data=coords,aes(x=long,y=lat),colour="purple",size=4) +
  geom_polygon(data=wvlf,aes(x=long,y=lat,group=group),color="grey",fill="NA")
HospAndVor</pre>
```



```
Next, we create a dot density map of the population in West Flanders.
belgie <- readOGR(".","newbelgie")
wvl_pop <- belgie[belgie@data$NAME_2=="West-Vlaanderen", ]
# turn shapefile into dotmap
dots.popWVL <- dotsInPolys(wvl_pop,wvl_pop@data$TOTAALBEV/100)
plot(wvlP,lwd=0.05)
plot(dots.popWVL,add=TRUE,pch=19,cex=0.1,col="#00880030")</pre>
```









plotting contour map on a Google maps background
centroids <- coordinates(wvlP)
centroids</pre>

> centroids

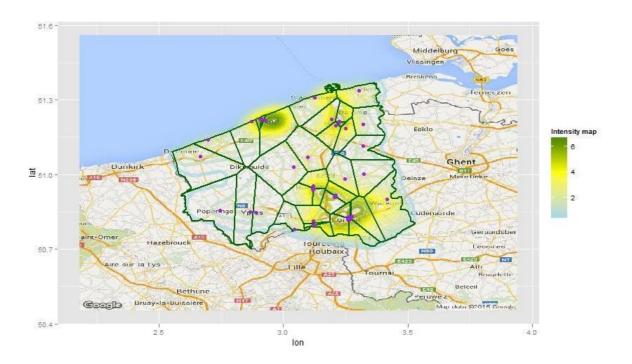
[,1] [,2] West-Vlaanderen 3.062247 51.01051

library(RgoogleMaps)

```
library(plyr)
library(jpeg)
LOCATION
                       <- 'west-vlaanderen'
                       <- c(lat = 51.01051, lon = 3.062247)
CoordinateCenter
COLOR TYPE
                       <- c('color','bw')[1]
RGBCoefficients
                       <- c(0, 1, 0)
ZOOM LEVEL
                       <- 9
MAP_TYPE
                      <- 'osm'
                      <- 'GoogleMap.jpg'
GOOGLE MAP
NUMBER OF PIXELS
                      <- 640
```

Voronoi Diagrams

```
GetMap(center
                               = CoordinateCenter[c('lat','lon')],
                               = c(NUMBER OF PIXELS, NUMBER OF PIXELS),
              size
                              = ZOOM LEVEL,
              zoom
              format = 'jpg',
             maptype = MAP TYPE,
              destfile = "test.jpg")
# load map
map <- readJPEG("test.jpg")</pre>
GoogleMapColorMatrix <- readJPEG("test.jpg")</pre>
{\tt GoogleMapColorMatrix} \leftarrow {\tt apply} ({\tt GoogleMapColorMatrix}, 1:2, {\tt function}({\tt v}) {\tt rgb}({\tt v[1]}, {\tt rgb}({\tt 
v[2], v[3]))
GoogleMapInformationList <- list(lat= CoordinateCenter['lat'],</pre>
                                                                  lon= CoordinateCenter['lon'],
                                                                  zoom = ZOOM LEVEL,
                                                                  GoogleMapColorMatrix)
str(GoogleMapInformationList)
class(GoogleMapInformationList)
CoordinateIndex <- (-NUMBER OF PIXELS/2) : (NUMBER OF PIXELS/2 - 1)
CreateLatitudeValuesFromIndex <- function(x) XY2LatLon(GoogleMapInformationList, -
NUMBER OF PIXELS/2, x) [1]
CreateLongitudeValuesFromIndex <- function(y) XY2LatLon(GoogleMapInformationList,</pre>
y, -NUMBER_OF_PIXELS/2)[2]
Latitudes <- apply(data.frame(CoordinateIndex), 1, CreateLatitudeValuesFromIndex)
Longitudes <- apply(data.frame(CoordinateIndex), 1, CreateLongitudeValuesFromIndex)</pre>
Latitudes <- seq(range(Latitudes)[1], range(Latitudes)[2],
length.out=length(Latitudes))
Longitudes <- seq(range(Longitudes)[1], range(Longitudes)[2],
length.out=length(Longitudes))
library(reshape)
GoogleMapColorDataFrame
                                                            <- melt(GoogleMapColorMatrix)</pre>
names(GoogleMapColorDataFrame) <- c('x','y','fill')</pre>
GoogleMapColorDataFrame <- within(GoogleMapColorDataFrame,{</pre>
   x <- x - NUMBER_OF_PIXELS/2 - 1
y <- y - NUMBER_OF_PIXELS/2 - 1
})
XYCoordinates
                                                           <- expand.grid(x = CoordinateIndex, y =
CoordinateIndex)
LatitudesAndLongitudes
                                                          <- expand.grid(lat = rev(Latitudes), lon =
Longitudes)
PlotData.Map <- data.frame(XYCoordinates, LatitudesAndLongitudes)
PlotData.Map <- suppressMessages(join(PlotData.Map, GoogleMapColorDataFrame, type
= 'right'))
PlotData.Map
                                           <- PlotData.Map[,c('lon','lat','fill')]
LatitudeRange
                                           <- range(PlotData.Map$lat)
                                            <- range(PlotData.Map$lon)
LongitudeRange
str(PlotData.Map)
theme_nothing <- function (base_size = 12){</pre>
    structure(list(axis.line
                                                                           = theme blank(),
                                  axis.text.x
                                                                         = theme_blank(), axis.text.y = theme_blank(),
                                  axis.ticks
                                                                           = theme_blank(),
                                  axis.title.x
                                                                           = theme_blank(), axis.title.y =
theme blank(),
                                                                           = unit(0, "lines"), axis.ticks.margin =
                                 axis.ticks.length
unit(0, "lines"),
                                                                        = "none",
                                  legend.position
                                  panel.background
                                                                           = theme_rect(fill = 'white'),
                                                                           = theme blank(),
                                  panel.border
                                                                           = theme_blank(), panel.grid.minor =
                                 panel.grid.major
theme blank(),
                                                                            = unit(0, "lines"),
                                  panel.margin
                                                                           = theme rect(colour = 'white'),
                                  plot.background
                                                                           = theme text(size = base size * 1.2),
                                  plot.title
                                                                           = unit(\overline{c}(-1, -1, -1.5, -\overline{1.5}), "lines")),
                                 plot.margin
                        class = "options")
vplayout <- function(x, y) {</pre>
```





```
final <- spTransform(final,osm())
class(final)

> class(final)
[1] "spatialPolygons"
attr(,"package")
[1] "sp"

#alpha definition
add.alpha <- function(col, alpha=1) {
   if (missing(col))
      stop("Please provide a vector of colours.")
   apply(sapply(col, col2rgb)/255, 2,
      function(x)
      rgb(x[1], x[2], x[3], alpha=alpha))
}
mycol=add.alpha("#507415",alpha=.4)
plot(final,add=T,col=mycol)</pre>
```



```
# add the points (hospital locations to the map)
class(points)
```

> class(points)

[1] "SpatialPoints"
attr(,"package")

[1] "sp"

proj4string(points)

> proj4string(points)

[1] NA

```
\label{eq:proj4string} $$ proj4string(points) <- CRS("+proj=longlat +ellps=WGS84") $$ points <- spTransform(points,CRS("+proj=merc +a=6378137 +b=6378137 +lat_ts=0.0 +lon_0=0.0 +x_0=0.0 +y_0=0 +k=1.0 +units= m +nadgrids=@null +no_defs")) $$
```

proj4string(points)

> proj4string(points)

[1] "+proj=merc +a=6378137 +b=6378137 +lat_ts=0.0 +lon_0=0.0 +x_0=0.0 +y_0=0 +k=1.0 +units=m + nadgrids=@null +no_defs"

proj4string(final)

> proj4string(final)

[1] "+proj=merc +a=6378137 +b=6378137 +lat_ts=0.0 +lon_0=0.0 +x_0=0.0 +y_0=0 +k=1.0 +units=m + nadgrids=@null +no_defs"

points(points@coords,col="darkblue",pch=19,cex=0.7)



```
# aggregate dot density data
# count the number of dots within each of the voronoi polygons for West Flanders
pop.wf <- data.frame(coordinates(dots.popWVL)[,1:2])</pre>
str(pop.wf)
> str(pop.wf)
'data.frame':
                   11560 obs. of 2 variables:
 $ x: num 3.29 3.3 3.37 3.37 3.34 ...
 $ y: num 51.3 51.3 51.3 51.3 51.3 ...
coordinates(pop.wf) <- ~ x + y</pre>
class(pop.wf)
> class(pop.wf)
[1] "SpatialPoints"
attr(,"package")
[1] "sp"
proj4string(pop.wf) <- proj</pre>
proj4string(pop.wf)
> proj4string(pop.wf)
[1] "+proj=longlat +datum=WGS84 +no_defs +ellps=WGS84 +towgs84=0,0,0"
proj4string(V) <- proj</pre>
proj4string(V)
> proj4string(V)
[1] "+proj=longlat +datum=WGS84 +no_defs +ellps=WGS84 +towgs84=0,0,0"
# count the number of dots in each polygon in the voronoi diagram
count <- sapply(over(V,pop.wf,returnList=TRUE),length)</pre>
count.
> count
  1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27
28 29 30 31
197 859 79 167 287 360 32 477 454 230 264 384 369 63 624 188 370 199 251 49 899 268 246 224 267 295 21
294 322 315 370
32 33 34 35 36 37
367 177 303 546 272 471
# add the results of the count to the voronoi polygons
V <- spCbind(V, as.data.frame(count))</pre>
str(V@data)
> str(v@data)
                    37 obs. of 3 variables:
'data.frame':
 $ x : num 3.32 2.93 2.91 3.26 3.27 ...
 $ y : num 51.2 51.2 51.2 50.8 50.8 ...
 $ count: int 155 885 65 173 262 383 27 481 450 240 ...
V@data$count <- V@data$count * 100
# convert V (SPDF) into a data frame to plot with ggplot2
V@data$id <- rownames(V@data)</pre>
str(V@data)
> str(v@data)
'data.frame':
'data.frame': 37 obs. of 4 variables:

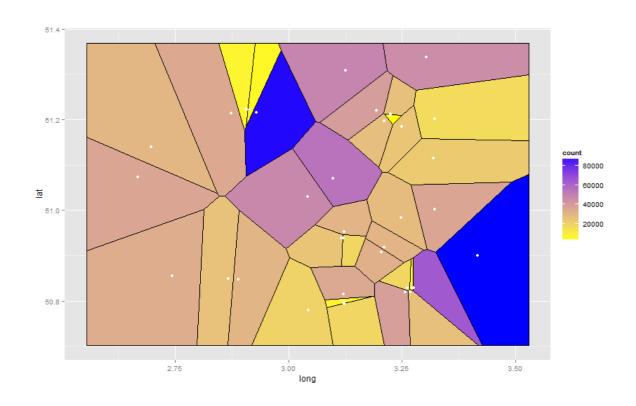
$ x : num 3.32 2.93 2.91 3.26 3.27 ...

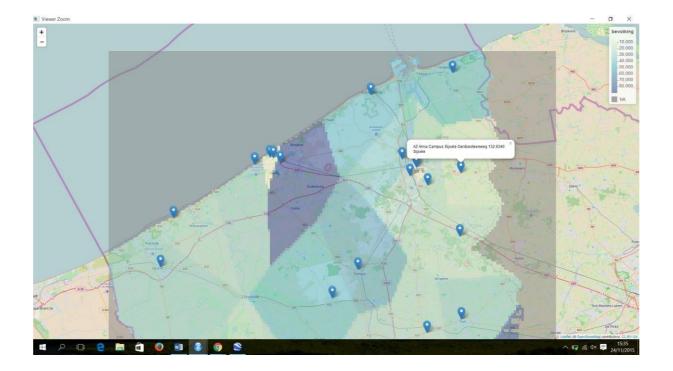
$ y : num 51.2 51.2 51.2 50.8 50.8 ...

$ count: num 15500 88500 6500 17300 26200 38300 2700 48100 45000 24000 ...

$ id : chr "1" "2" "3" "4" ...
```

```
V.df <- fortify(V,region="id")</pre>
str(V.df)
> str(V.df)
                  239 obs. of 7 variables:
'data.frame':
 $ long : num 3.53 3.53 3.29 3.28 3.28 ...
 $ lat : num 51.3 51.2 51.2 51.2 51.3 ...
 $ order: int 1 2 3 4 5 6 7 8 9 10 ...
 $ hole : logi FALSE FALSE FALSE FALSE FALSE FALSE ...
 $ piece: Factor w/ 1 level "1": 1 1 1 1 1 1 1 1 1 1 ...
 \ group: Factor w/ 37 levels "1.1","10.1","11.1",...: 1 1 1 1 1 1 2 2 2 2 ....
 $ id : chr "1" "1" "1" "1" ...
V.df <- merge(V.df, V@data, by="id")</pre>
str(V.df)
> str(V.df)
'data.frame':
                  239 obs. of 10 variables:
 $ id : chr "1" "1" "1" "1" ...
 $ long : num 3.53 3.53 3.29 3.28 3.28 ...
 $ lat : num 51.3 51.2 51.2 51.2 51.3 ...
 $ order: int 1 2 3 4 5 6 7 8 9 10 ...
 $ hole : logi FALSE FALSE FALSE FALSE FALSE FALSE ...
 $ piece: Factor w/ 1 level "1": 1 1 1 1 1 1 1 1 1 1 ...
 $ group: Factor w/ 37 levels "1.1","10.1","11.1",..: 1 1 1 1 1 1 2 2 2 2 ...
       : num 3.32 3.32 3.32 3.32 ...
        : num 51.2 51.2 51.2 51.2 51.2 ...
 $ count: num 15500 15500 15500 15500 15500 24000 24000 24000 24000 ...
map <- ggplot(V.df,aes(x=long,y=lat)) +</pre>
  geom polygon(aes(group=group,fill=count),colour="black",size=0.1) +
  scale fill continuous(low="yellow", high="blue") +
  {\tt geom\_point(data=coords,aes(x=long,y=lat),colour="white",size=2) \ +}
  coord equal()
map
```





(3) Voronoi intensity mapping

```
Source: "Voronoi intensity mapping with R and d3: Part 1",
             (http://www.jonzelner.net/2015/02/26/voronoi)
R script: "c:/R/Rdata/voronoi.R"
In the case of the visualization of crime, for example, we can rely on markers to
highlight the location of crime types. This can lead to overplotting in areas that
have experienced more than their fair share of crime. A Voronoi intensity map
might be the right way to do justice to these data. The basic idea behind a
Voronoi diagram is that it is a set of polygons representing the set of points
closest to a set of pre-defined points. Applied to crime, each Voronoi cell
represents the set of points closer to one of the crimes in the data set than any
other. The intuition behind Voronoi intensity mapping is that the closer points
are together in a given area, the smaller the Voronoi cells in that area will be.
For this exercise, we use a dataset of the location of homicides in Philadelphia,
US.
setwd("c:/R/Rdata")
data <- read.csv("PPD Crime Incidents 2012-2014.csv", header=T, sep=",")
str(data)
                        569426 obs. of 8 variables:

: int 23 19 16 6 24 18 26 22 25 3 ...

: Factor w/ 6 levels "1","2","3","4",...: 2 2 1 1 2 1 6 2 2 2 ...

: Factor w/ 446678 levels "01/01/2012 01:03:00 AM",..: 41045 11217 179381 40897 124388 59363 411631
 $ ï..District
$ PSA
$ PSA
$ Dispatch.Date.Time
51509 35601 51513 ...
$ DC.Number : $ Location.Block : 376 12209 9614 15974 16709
                        : num 2.01e+11 2.01e+11 2.01e+11 2.01e+11 2.01e+11 ...
: Factor w/ 55578 levels "/C BAGGAGE"," 59TH ST / CATHARINE ST",..: 13219 3728 20498 10718 12778 37
376 12209 9614 15974 16709 ...
$ UCR. Code : int 1800 1800 2600 600 1800 800 200 1700 200 200 ...
$ General.Crime.Category: Factor w/ 33 levels "Aggravated Assault Firearm", ..: 18 18 3 30 18 20 24 21 24 24 ...
$ Coordinates : Factor w/ 235950 levels "","(0, 0)","(39.8741308038022, -75.2179316185477)", ..: 88478 79215 68389 45503 109872 41876 98752 101461 117221 1648 ...
data$Coordinates <- as.character(data$Coordinates)</pre>
data$X <- sapply(strsplit(as.character(data$Coordinates), ","), "[", 2)</pre>
\label{eq:datasy} $$ $\operatorname{datasy}, \ \operatorname{split}'(', \ \operatorname{fixed=TRUE}), \ \operatorname{function}(x) \ (x[2])$ )
data$X <- sapply(strsplit(data$X, split=')', fixed=TRUE), function(x) (x[1]))</pre>
data$Y <- as.numeric(data$Y)</pre>
data$X <- as.numeric(data$X)</pre>
data$datetime <- as.POSIXct(data$Dispatch.Date.Time, format="%m/%d/%Y %I:%M:%S %p")
library(lubridate)
data$year <- year(data$datetime)</pre>
data <- data[(data$General.Crime.Category == "Homicide - Criminal" |</pre>
                    data$General.Crime.Category == "Homicide - Gross Negligence" |
                    data$General.Crime.Category == "Homicide - Justifiable"), ]
str(data)
> str(data)
'data.frame': 8'
$ i.District : $PSA : Dispatch.Date.Time : 309077 363245 413184 ...
$ DC.Number : $Location.Block : 928 13204 16104 9573 11643
                        871 obs. of 12 variables:

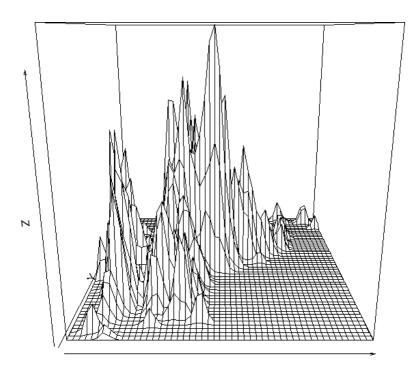
: int 1 1 1 1 1 1 1 1 1 1 1 1 ...

: Factor w/ 6 levels "1","2","3","4",...: 1 1 1 1 2 1 1 1 1 1 ...

: Factor w/ 446678 levels "01/01/2012 01:03:00 AM",...: 9804 87561 172960 184898 240742 260831 288019
                          num 2.01e+11 2.01e+11 2.01e+11 2.01e+11 2.01e+11 ...
Factor w/ 55578 levels "/C BAGGAGE","` 59TH ST / CATHARINE ST",..: 50703 8930 13172 15011 20201 50
$ datetime
21:00" ...
 $ year
                        : num 2012 2012 2012 2012 2012 ...
```

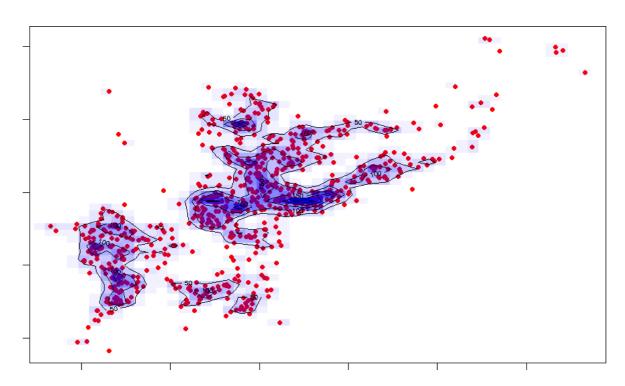
```
data <- subset(data, select=c(X,Y))</pre>
data <- na.omit(data)</pre>
names(data) <- c("lon", "lat")</pre>
str(data)
> str(data)
                  869 obs. of 2 variables:
'data.frame':
 $ lon: num -75.2 -75.2 -75.2 -75.2 ...
 $ lat: num 39.9 39.9 39.9 39.9 39.9 ...
 - attr(*, "na.action")=Class 'omit' Named int [1:2] 38 389
  ....- attr(*, "names")= chr [1:2] "35715" "273937"
head(data, 20)
> head(data,20)
            lon
     -75.17871 39.92806
919 -75.18199 39.92928
1782 -75.18428 39.92383
1896 -75.19430 39.92173
2527 -75.19158 39.90670
2706 -75.18388 39.92872
2968 -75.18341 39.92611
3167 -75.19167 39.92361
3677 -75.17777 39.92798
4115 -75.18310 39.92696
4331 -75.18672 39.91879
6515 -75.10037 40.04559
7573 -75.08769 40.04680
9863 -75.11230 40.04186
10376 -75.08505 40.04370
11513 -75.07637 40.04328
13413 -75.10086 40.03982
15299 -75.07881 40.05525
15688 -75.16724 39.93156
15690 -75.16724 39.93156
# density estimation with package KernSmooth
library(KernSmooth)
# compute density with cross-validation techniques to get optimal bandwidths
kde2d <- bkde2D(data, bandwidth=c(bw.ucv(data[,1]),bw.ucv(data[,2])))</pre>
class(kde2d)
> class(kde2d)
[1] "list"
str(kde2d)
> str(kde2d)
List of 3
$ x1 : num [1:51] -75.3 -75.3 -75.3 -75.3 -75.2 ...
 $ x2 : num [1:51] 39.9 39.9 39.9 39.9 39.9 ...
 $ fhat: num [1:51, 1:51] 0 0.000117 0.003742 0.013732 0.083049 ...
```

z <- kde2d\$fhat
persp(z)</pre>

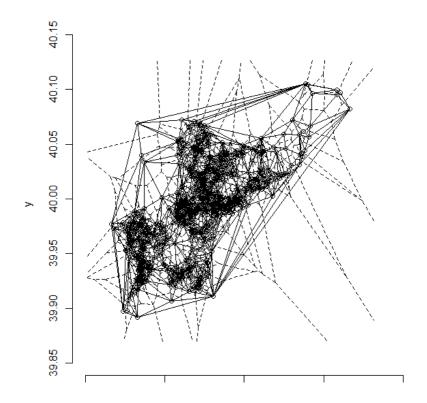


clrs <- colorRampPalette(c(rgb(0,0,1,0),rgb(0,0,1,1)),alpha=TRUE)(20)

plot(data,col="red",pch=19)
image(x=kde2d\$x1,y=kde2d\$x2,z=kde2d\$fhat,col=clrs,add=TRUE)
contour(x=kde2d\$x1,y=kde2d\$x2,z=kde2d\$fhat,add=TRUE)



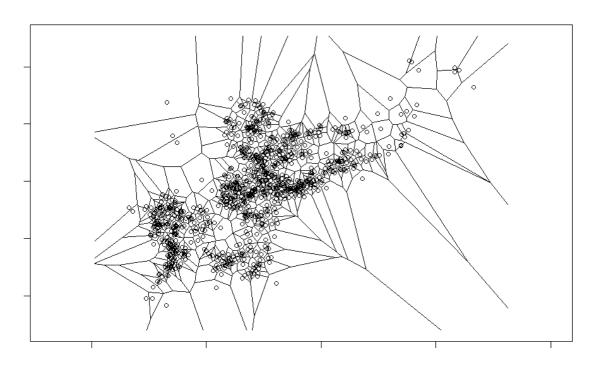
library(deldir)
voronoi <- deldir(data\$lon,data\$lat)
plot(voronoi,xlim=c(-75.3,-74.9),ylim=c(39.85,40.14))</pre>



vtiles <- tile.list(voronoi)
class(vtiles)</pre>

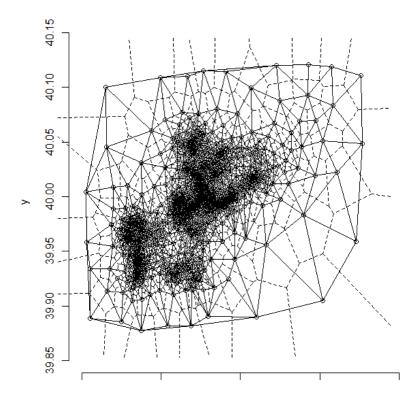
> class(vtiles) [1] "tile.list"

plot(vtiles)

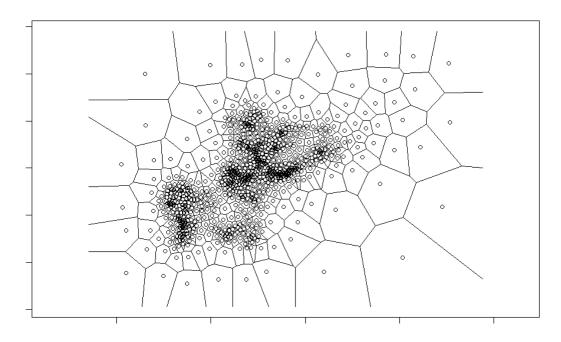


There are some very small polygons in the highest density areas and very irregular ones in the low-density areas. One way to deal with this is to do a little bit of regularization using centroidal voronoi estimation in which we take the output of a single iteration of the voronoi tessalation and make the centroids of the voronoi cells the input sites to the next iteration.

```
for (i in 1:2) {
  voronoi <- deldir(tile.centroids(vtiles))
  vtiles <- tile.list(voronoi)
}
plot(voronoi,xlim=c(-75.3,-74.9),ylim=c(39.85,40.14))</pre>
```



plot(vtiles)



This gives us little less of the extreme variability in polygon size, while still maintaining the large differences in density across space.

What we further need to do is to clip the polygons tot he borders of the city. This will ensure that the areas of the polygons in our intensity map match the portions of the city that they're meant to cover, rather than the arbitrarily large polygons at the edges of the diagram.

We can enclose the voronoi polygons within the geographic borders of Philadelphia with the help of the $gIntersection\ function\ (package\ rgeos)$.

To use this function we need to have both the voronoi polygons and the geographic borders as SpatialPolyDataFrame objects.

First, we convert the neighborhoods of the Philadelphia shapefile into a single polygon.

```
library(rgdal)
library(maptools)
phila <- readOGR(".", "Neighborhoods")
class(phila)</pre>
```

> class(phila)

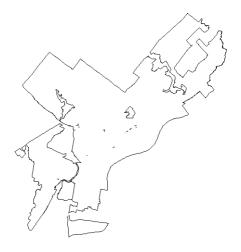
[1] "SpatialPolygonsDataFrame"
attr(,"package")

[1] "sp"

plot(phila)



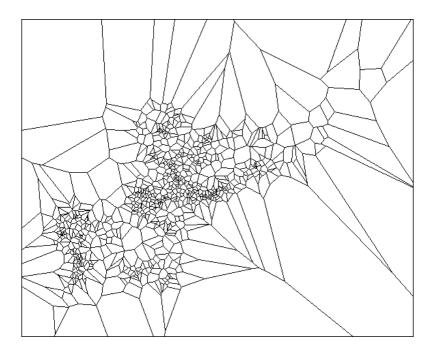
```
regs <- c("Philadelphia")
phila@data$NAME_2 <- "Philadelphia"
sp2 <- phila@data$NAME_2
sp2[which(!phila@data$NAME_2 %in% regs)] <- NA
PH <- unionSpatialPolygons(phila,sp2)
plot(PH)</pre>
```



To convert the deldir object to a SpatialPolgygonsDataFrame we use the following function :

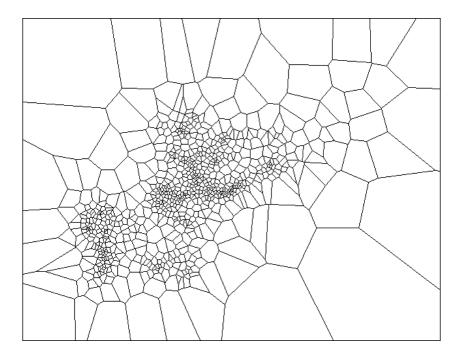
```
voronoipolygons <- function(x, poly) {</pre>
  require(deldir)
  if (.hasSlot(x, 'coords')) {
    crds <- x@coords
  } else crds <- x
  bb = bbox(poly)
  rw = as.numeric(t(bbox(poly)))
  z <- deldir(crds[,1], crds[,2],rw=rw)</pre>
  w <- tile.list(z)</pre>
  polys <- vector(mode='list', length=length(w))</pre>
  require(sp)
  for (i in seq(along=polys)) {
    pcrds <- cbind(w[[i]]$x, w[[i]]$y)</pre>
    pcrds <- rbind(pcrds, pcrds[1,])</pre>
    polys[[i]] <- Polygons(list(Polygon(pcrds)), ID=as.character(i))</pre>
  SP <- SpatialPolygons(polys)</pre>
  SpatialPolygonsDataFrame(
    SP, data.frame(x=crds[,1], y=crds[,2],
                     row.names=sapply(slot(SP, 'polygons'),
                                        function(x) slot(x, 'ID')))
}
q <- voronoipolygons(data,PH)</pre>
Error in data.frame(x = crds[, 1], y = crds[, 2], row.names = sapply(slot(SP, : row names))
supplied are of the wrong length
This is error is due to duplicate coordinates in the data frame, so we need to
deduplicate :
data <- data[!duplicated(data$lat), ]</pre>
data <- data[!duplicated(data$lon), ]</pre>
```

```
q \leftarrow voronoipolygons(data, PH) plot(q)
```



```
\# adjusted function to perform centroidal voronoi estimatrion
voronoipolygons2 <- function(x, poly) {</pre>
  require(deldir)
  if (.hasSlot(x, 'coords')) {
    crds <- x@coords
  } else crds <- x
 bb = bbox(poly)
  rw = as.numeric(t(bbox(poly)))
  z <- deldir(crds[,1], crds[,2],rw=rw)</pre>
  w <- tile.list(z)</pre>
    for (i in 1 : 2) {
    voronoi <- deldir(tile.centroids(w))</pre>
    vtiles <- tile.list(voronoi)</pre>
  polys <- vector(mode='list', length=length(vtiles))</pre>
  require(sp)
  for (i in seq(along=polys))
   pcrds <- cbind(vtiles[[i]]$x, vtiles[[i]]$y)</pre>
    pcrds <- rbind(pcrds, pcrds[1,])</pre>
    polys[[i]] <- Polygons(list(Polygon(pcrds)), ID=as.character(i))</pre>
  SP <- SpatialPolygons(polys)</pre>
  SpatialPolygonsDataFrame(
    SP, data.frame(x=crds[,1], y=crds[,2],
                    row.names=sapply(slot(SP, 'polygons'),
                                        function(x) slot(x, 'ID'))))
}
```

q2 <- voronoipolygons2(data,PH)
plot(q2)</pre>



```
proj4string(PH)

> proj4string(PH)
[1] "+proj=longlat +datum=WGS84 +no_defs +ellps=WGS84 +towgs84=0,0,0"

proj4string(q2)

> proj4string(q2)
[1] NA

proj4string(q2) <-proj4string(PH)

library(rgeos)
final <- gIntersection(PH, q2, byid=TRUE)
class(final)

> class(final)
[1] "SpatialPolygons"
attr(,"package")
[1] "sp"
```

plot(final)
image(x=kde2d\$x1,y=kde2d\$x2,z=kde2d\$fhat,col=clrs,add=TRUE)

