(1) (a) 
$$\begin{pmatrix} A \\ 0 \\ 1 \\ 1 \end{pmatrix}$$
,  $p_n(\lambda) = det(A-\lambda \bar{1}) = 0$ 

$$\begin{vmatrix} 1-\lambda & 0 & 1 \\ 0 & 1-\lambda & 1 \\ 1 & 1-\lambda \end{vmatrix} = 0 \Rightarrow (1-\lambda)^{\frac{1}{2}}(-\lambda) - ((1-\lambda) + (1-\lambda) = 0$$

$$=) \left(-\lambda\right)\left(\left(1-2\lambda+\lambda^{2}\right)+2\lambda-2=0=\right)-\lambda+2\lambda^{2}-\lambda^{3}+2\lambda-2=0$$

Rascunho

 $\frac{-\lambda^3+2\lambda^2+\lambda-2\left(\lambda-1\right)}{0+\lambda^2+\lambda-2}$ 

 $\frac{-\left(\lambda^{2}-\lambda\right)}{0+2\lambda-2}$ 

$$=)$$
  $-\lambda^3 + 2\lambda^2 + \lambda - 2 = 0$ 

$$(4a \text{ tondo}) \lambda = 1 = ) - 1 + 2 + 1 - 2 = 0$$

$$p(x) = (x-1)(-x^2+x+z) = 0$$

$$-\lambda^2 + \lambda + 2 = 0 = ) \lambda = -1 \pm \sqrt{1 - 4 \cdot (-4) 2} = -2$$

$$=\frac{-1+3}{-2}$$

$$logo, \lambda = 1, \lambda_2 = -1, \lambda_3 = 2$$

## Autoveton de 1=1

$$\begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix} = 0 \Rightarrow \begin{cases} v_3 = 0 \\ v_2 = -v_1 \end{cases} \Rightarrow v = \begin{bmatrix} t \\ -t \\ 0 \end{bmatrix}, t \in \mathbb{N}$$

$$\begin{bmatrix} L & 0 & 17 \\ 0 & L & 17 \\ V_1 & V_3 \end{bmatrix} = 0 = \begin{pmatrix} 2V_1 + V_3 = 0 = \end{pmatrix} V_3 = -2V_2 = \begin{pmatrix} t \\ 2V_2 + V_3 = 0 = \end{pmatrix} V_3 = -2V_2 = \begin{pmatrix} t \\ -2t \end{pmatrix} t \in \mathbb{R}$$

## Aub valor 1/3=2

$$\begin{bmatrix} -1 & 0 & 1 \\ 0 & -1 & L \\ 1 & 1 & -2 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix} = \begin{cases} -\sqrt{1} + \sqrt{1} = 0 = 0 \\ -\sqrt{1} + \sqrt{1} = 0 = 0 \end{cases} \quad \sqrt{1} = V_2 = 0 = 0 \quad \sqrt{1} = V_3 = 0 = 0$$

(b) 
$$A = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
,  $p(A) = det \begin{pmatrix} 1 & \lambda & 0 & 0 \\ 0 & -\lambda & 1 \\ 0 & 1 & -\lambda \end{pmatrix} = det \begin{pmatrix} 1 & \lambda & 0 & 0 \\ 0 & 1 & -\lambda & 1 \\ 0 & 1 & -\lambda & 1 \end{pmatrix}$ 

$$= (1-\lambda)(-\lambda)^2 - (1-\lambda) = 0 \Rightarrow \lambda^3 - \lambda^2 + \lambda - 1 = 0$$

$$\frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda - 1}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{2} + \lambda^{2}}{\lambda^{5} + \lambda^{2}} = \frac{\lambda^{5} \cdot \lambda^{5}}{\lambda^{5} + \lambda^{5}} = \frac{\lambda^{5} \cdot \lambda^{5}}{\lambda^{5} + \lambda^{5}} = \frac{\lambda^{5} \cdot \lambda^{5}}{\lambda^{5}} = \frac{\lambda^{5}}{\lambda^{5}} = \frac{\lambda^{5}}{\lambda^{$$

$$\lambda^2 + 1 = 0 \Rightarrow \lambda^2 = -1 \Rightarrow \lambda^4 = i , \lambda^3 = -i$$

Achando os autoretores:

$$\begin{cases} \int_{-1}^{1-\lambda} \left( \frac{1}{\lambda_{1}} \right) dx = 0 \\ \int_{-1}^{1-\lambda} \left( \frac{1}{\lambda_{2}} \right) dx = 0 \\ \int_{-1}^{1-\lambda} \left( \frac{1}{\lambda_{1}} \right) dx = 0 \\ \int_{-1}^{1-\lambda} \left( \frac{1}{\lambda_{2}} \right) dx = 0 \\ \int_$$

$$\begin{bmatrix}
1-\lambda & 0 & 0 \\
0 & -\lambda & 1 \\
0 & 1 & -\lambda
\end{bmatrix}
V = 0 =$$

$$\begin{bmatrix}
1-i & 1 & 0 & 0 \\
0 & 1 & -i & 1
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V = 0$$

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0 & 1 & -i &$$

$$\begin{bmatrix} 0 & -\lambda & 1 \\ 0 & -\lambda & 1 \end{bmatrix} V = 0 \Rightarrow \begin{bmatrix} 0 & 1 & 1 \\ 0 & 1 & 1 \end{bmatrix} V = 0$$

$$\begin{cases} \sqrt{3^2 + v^3} = 0 \\ \sqrt{3^2 + iv^3} = 0 \end{cases} = \begin{cases} \sqrt{2^2 - iv^3} = 2 \end{cases} = 2 \end{cases} = \begin{cases} \sqrt{2^2 - iv^3} = 2 \end{cases} = 2 \end{cases} = \begin{cases} \sqrt{2^2 - iv^3} = 2 \end{cases} = 2 \end{cases} = \begin{cases} \sqrt{2^2 - iv^3} = 2 \end{cases} = 2 \end{cases} = 2 \end{cases} = \begin{cases} \sqrt{2^2 - iv^3} = 2 \end{cases} = 2 \end{cases}$$

$$\begin{cases}
c(1) & A = \begin{cases}
0 & N & 1 \\
0 & 0 & 0
\end{cases}, & \rho_{A}(\lambda) = det(A - \overline{\lambda}\lambda) = det(\begin{bmatrix} -\lambda & 1 & 1 \\ 0 & -\lambda & 0 \\ 0 & 0 & -\lambda \end{bmatrix})$$

$$\rho(\lambda) = -\lambda^{3} = 0 = \lambda, = \lambda_{1} = \lambda_{2} = 0$$
Achando os autoretores:
$$\underbrace{\lambda = 0}_{0 & 0 - \lambda} \begin{bmatrix} -\lambda & 1 & 1 \\ 0 & 0 & 0 \end{bmatrix} \nabla = 0$$

$$\int \nabla^{2} = -\nabla^{3} = \lambda = \sum_{n=1}^{\infty} \prod_{n=1}^{\infty} \prod_{n=1}^{\infty} \prod_{n=1}^{\infty} e^{-\lambda n} \int_{-\infty}^{\infty} e^{-\lambda n} dn = 0$$

## Reference

Link: MS512 2024S1 Lista de Autopares

Exercise: 1