## CS221 Fall 2015 Homework [pacman]

## Problem 1: Minimax

1a.

$$V_{opt}(s,d) = \begin{cases} Utility(s) & \text{if } IsEnd(s) \\ Eval(s) & \text{if } d = 0 \\ max_{a \in Actions(s)} V_{opt}(Succ(s,a),d) & \text{if } Player(s) = a_0 \\ min_{a \in Actions(s)} V_{opt}(Succ(s,a),d) & \text{if } Player(s) \in \{a_1,a_2,\dots a_{n-1}\} \\ min_{a \in Actions(s)} V_{opt}(Succ(s,a),d - 1) & \text{if } Player(s) = a_n \end{cases}$$

At state s, call  $V_{opt}(s, d_{max})$  and the order of the turns is  $a_0, a_1, a_2, \dots a_n$ 

## Problem 3: Expectimax

3a.

$$V_{opt,\pi}(s,d) = \begin{cases} Utility(s) & \text{if } IsEnd(s) \\ Eval(s) & \text{if } d = 0 \\ max_{a \in Actions(s)} V_{opt,\pi}(Succ(s,a),d) & \text{if } Player(s) = a_0 \\ \sum_{a \in Actions(s)} V_{opt,\pi}(Succ(s,a),d) * \frac{1}{|Actions(s)|} & \text{if } Player(s) \in [a_1,a_2,...a_{n-1}] \\ \sum_{a \in Actions(s)} V_{opt,\pi}(Succ(s,a),d-1) * \frac{1}{|Actions(s)|} & \text{if } Player(s) = a_n \end{cases}$$
 At state  $s$ , call  $V_{opt,\pi}(s,d_{max})$  and the order of the turns is  $a_0,a_1,a_2,...a_n$ 

At state s, call  $V_{opt,\pi}(s,d_{max})$  and the order of the turns is  $a_0, a_1, a_2, \dots a_n$