



Modern Physics

AS91172

3 NCEA L2 Credits

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Chapter 1: Atoms and Isotopes

Learning Outcomes

- Define the terms proton, neutron, electron, nucleon, atomic mass, atomic number and isotope.

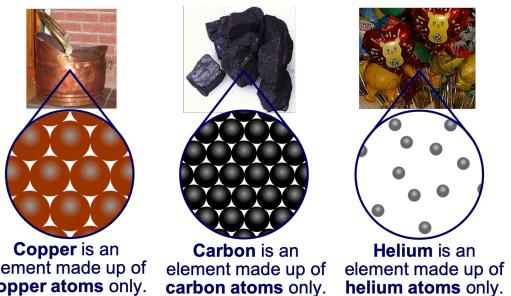
Aristotle and the Greeks in 450BC hypothesised that everything was made of water, earth, air and fire. Some years later, another Greek philosopher Democritus came up with the idea of an indivisible piece of matter - a fundamental building block. He did not know what it was, but theorised that one should exist. He called these pieces of matter *atomos (indivisible)*.



In the modern day we have a different theory that is testable and that allows us to make predictions. Our theory predicts that everything is made up of 119 different elements.

1.1 Atoms and Elements

Pātai: What makes the elements different from each other?

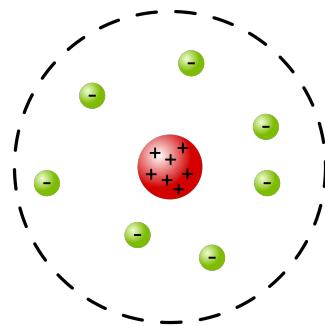


1.1.1 Ngohe: Draw a labelled diagram of a lithium atom

1.1.2 The Rutherford Model

What you have drawn is the Rutherford Model of the atom. This model is the most common one we see in school today because it has very strong predictive powers. It is also very valuable because it allows to easily visualise things like *ions* and *isotopes* and how some chemical bonding works.

The central region is called the _____. It is made of _____ and _____ which are strongly bound together by the _____. Together we call protons and neutrons _____, as they exist in the nucleus.



Electrons are constantly moving around the nucleus in a probabilistic way. This means that they do not have fixed orbits like the planets, but instead exist in a probability cloud. The size of the nucleus compared to the whole atom is very small, but it contains > 99.95% of the mass because electrons are very light.

Protons have a _____ charge, electrons have a _____ charge, and neutrons have _____ charge. Protons and electrons have an equal but opposite sized charge despite their very different masses.

1.2 Atomic and Mass Numbers

The number of protons in an atom (i.e. the atomic number) defines which type of atom it is. For example, an atom that has six protons MUST be a _____ atom, and cannot be any other.

- **Atomic number:**
- **Mass number:**

1.2.1 Ngohe: Reading the Periodic Table

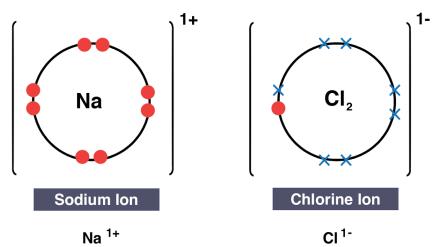
	Protons	Electrons	Neutrons	Nucleons	Atomic #	Mass #
Oxygen	_____	_____	_____	_____	_____	_____
Sodium	_____	_____	_____	_____	_____	_____
Aluminium	_____	_____	_____	_____	_____	_____
Copper	_____	_____	_____	_____	_____	_____

1.3 Ions

An atom is a neutral particle, having equal number of protons and electrons (recall: they have opposite but equal size electric charges). However, an atom may lose or gain one or more electrons during a reaction. This causes them to gain a *net charge*.

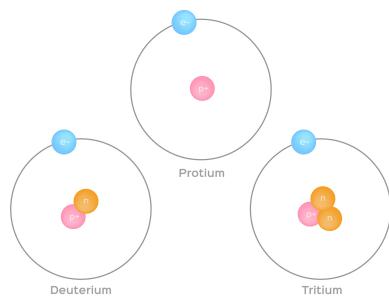
When an atom has a charge it is called an _____.

Positively charged ions are called _____ and negatively charged ions are called _____.



1.4 Isotopes

Hydrogen Isotopes



An isotope is an atom with the same number of protons (same element), but with a different number of neutrons. This means that the *atomic number* is the same, but that the *mass number* is different.

This is why some periodic tables show a mass number with lots of decimal places, it is an average of the different isotopes.

Some isotopes are stable, while others like Carbon-14 is radioactive and will decay over time. Carbon-14 can be used to find the age of organic matter. They do this by looking at the ratio of Carbon-14 compared to the other isotopes.

1.4.1 Ngohe: Carbon Isotopes

For Carbon-12, Carbon-13 and Carbon-14, complete the table below.

	Protons	Electrons	Neutrons	Nucleons	Atomic #	Mass #
Carbon-12						
Carbon-13						
Carbon-14						

1.5 Whakawai: Atomic Structure

Atoms are made of a central dense part called the _____ surrounded by a moving cloud of _____. The particles in the central region are called nucleons and are either protons or _____. The charge on protons is _____.

The nucleons are attracted strongly to each other by a force called the _____ force. The protons however, repel each other, because they have similar charges. This repulsion force between the protons is an _____ force. As a result of these forces in the nucleus, most nuclei are stable. However, if nuclei are disrupted by nuclear reactions enormous amounts of _____ may be released. The reason for this is that the _____ in the nucleus are very strong.

The atomic number is the number of _____ in the nucleus of an atom. The mass number is the number of _____ and _____ in the nucleus of an atom. Isotopes of an element will always have the same _____ number but different _____ numbers.

State the number of protons and neutrons in the following nuclides.

1. $^{222}_{86}Rn$:

2. $^{238}_{92}U$:

3. $^{63}_{29}Cu$:

4. $^{27}_{13}Al$:

Write the following nuclides in their symbol form.

1. A nucleus of carbon with 6 protons and 8 neutrons.

2. A nucleus of sulfur with 16 protons and 17 neutrons.

3. A nucleus of helium with 2 neutrons.

4. A nucleus of hydrogen with no neutrons.

5. A nucleus of nitrogen with a mass number of 16.

6. A nucleus of potassium with 20 neutrons.

7. A nucleus of an atom with 56 protons and 84 neutrons.

Chapter 2: Atomic Structure

Learning Outcomes

- Understand the history and process of how we formulated the current atomic model

Introductory Video: <https://youtu.be/xazQRcSCRaY>

2.1 The Greeks

As mentioned earlier, Aristotle and the Greeks in 450BC thought that everything was made of water, earth, air and fire. Some years later, another Greek philosopher Democritus came up with the idea of some indivisible piece of matter - a fundamental building block. He did not know what it was, but theorised that one should exist. He called these pieces of matter *atomos* (*Latin: indivisible*).

2.2 John Dalton (1766 - 1844)

John Dalton was an English chemist who introduced *atomic theory* into chemistry. There is some debate about where he got his theory, but the main points he developed were:

- Elements are made of extremely small particles called atoms
- Atoms of a given element are _____, _____ and other properties
- Atoms cannot be _____
- Atoms of different elements combine in simple whole-number ratios to form chemical compounds. E.g. $MgCl_c$.
- In chemical reactions, atoms are combined, separated or rearranged

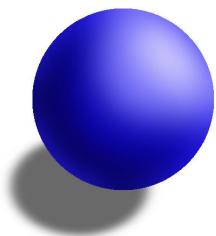


Figure 2.1: Dalton's ball theory of the atom.

He was not able to ascertain the weight of any elements, but did attempt to order them by *relative weight*. It was with John Dalton when *atomos* from the Greeks became *atoms*.

2.3 Joseph Thomson (1856–1940)

Joseph Thomson was a British physicist who did a lot of work with cathode rays (_____) and who was awarded the Nobel Laureate in Physics for discovering the electron. This was the first subatomic particle to be discovered! He is also credited with finding the first scientific evidence of _____.

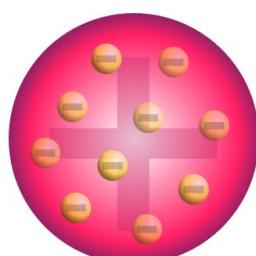


Figure 2.2: Thomson's Plum Pudding theory of the atom.

At the time of his research they were not originally aware that cathode rays were streams of "electrons". He only knew that they were negatively charged and had _____. He hypothesised that the electrons were emitted from the atoms inside the cathode ray tube, and thus concluded _____.

If the electrons were inside the atoms, and an atom was neutral, the electrons would have to be evenly distributed throughout, and the atom itself made of some positive material.

2.4 Ernest Rutherford (1871-1937)

Ernest Rutherford is a New Zealand-born British Physicist credited as the father of nuclear physics. He was the discoverer of the concept of _____, and was awarded the Nobel Prize in Chemistry for his work into the disintegration of the elements (_____).

His work on the atom revolved around something called _____ where he fired alpha particles (_____) at a sheet of thin gold foil. By analysing the scatter pattern of the alpha particles he was able to determine that there is a positive nucleus in the centre of the atom, and that the electrons should orbit around the outside. *Notice that at this point we still have not discovered the neutron.*

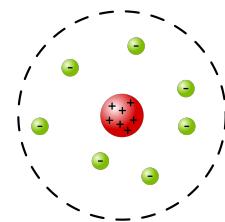
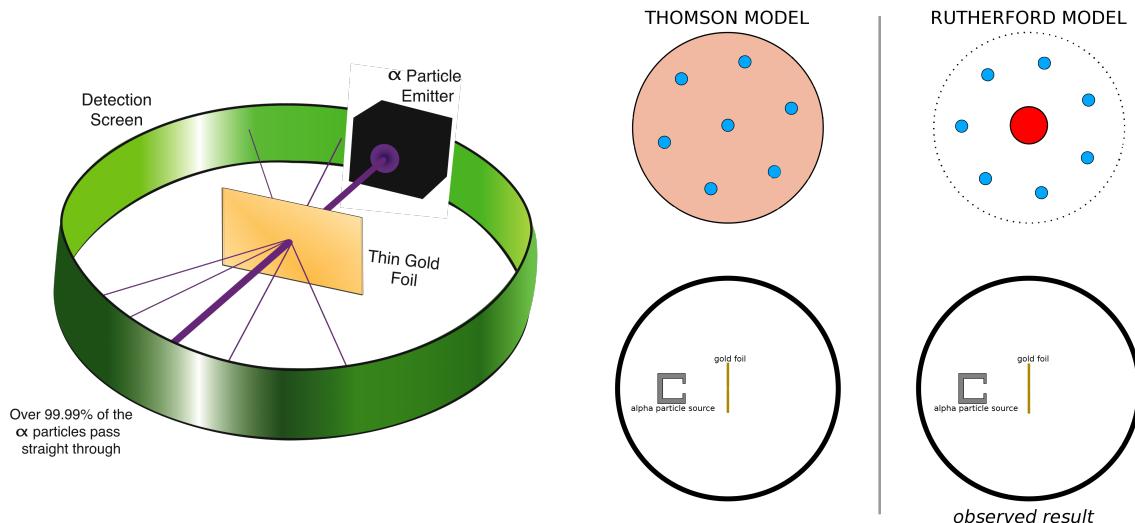


Figure 2.3:
Rutherford's
Model of the
Atom

2.5 The Gold Foil Experiment

Introductory Video: <https://www.youtube.com/watch?v=1EdTw4I6L0U>



- **Observation 1:** Most alpha particles were found to go straight through the foil.

Conclusion:

- **Observation:** Some alpha particles experienced a small angle of deflection.

Conclusion:

- **Observation 3:** Very few alpha particles were deflected.

Conclusion:

- **Observation 4:** Some particles were deflected at a very large angle.

Conclusion:

- Explain why the gold foil experiment had to be carried out in a vacuum.

- Explain why it was necessary for the gold foil to be a few atoms thick.

Chapter 3: Nuclear Decay

Learning Outcomes

- Describe alpha radioactive decay
- Describe beta radioactive decay
- Describe gamma radioactive decay

Introductory Video: <https://youtu.be/UtZw9jfIxXM>

3.1 Pātai: What is a nuclear reaction?

- It is **not** a physical reaction (e.g. changing state)
- It is **not** a chemical reaction (e.g. forming ionic compounds)
- It is a reaction where:

There are three types of nuclear reactions that we are interested in for this topic:

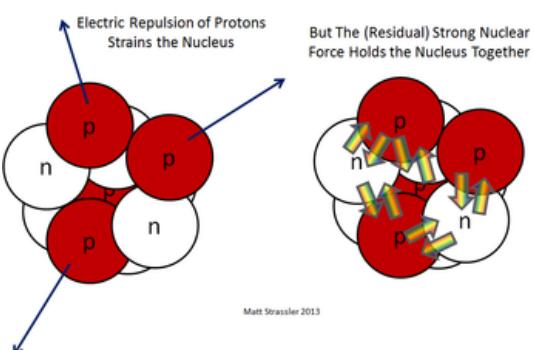
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3.2 Why Nuclear Decay Occurs

Inside the nucleus are the protons and neutrons. The neutrons do not carry an electric charge, so do not interact electrically. The protons, however, carry a positive charge. We know that like charges repel, so *why does the nuclear not fall apart?*

It turns out that when nucleons get close enough another force comes into effect: the _____ . This force glues the nucleons together. Nuclear decay occurs when the nucleus gets very large; either by having a large atomic number, or by being an isotope with a large number of neutrons.

Adding nucleons increases the volume of the nucleus, and thereby diluting the strong nuclear force. When the strong nuclear force is diluted such that the electrostatic force is now larger, the nucleus _____. This is called radioactive decay!



Recall the Law of Conservation of Energy. Similar laws apply to nuclear equations and these four properties are also conserved:

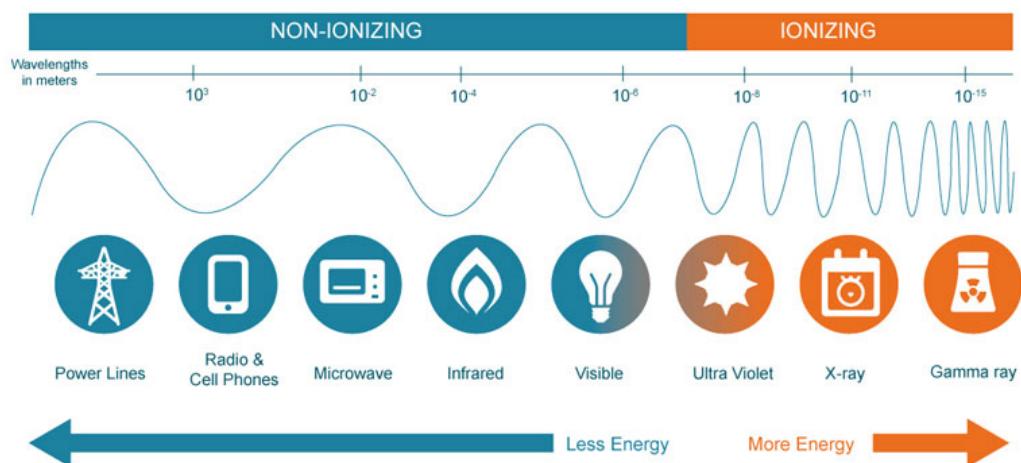
- _____
- _____
- _____
- _____

Video: <https://www.youtube.com/watch?v=TJgc28csgV0>

3.3 Ionizing Radiation

Ionising means to have the ability to strip electrons from an atom/molecule. In some circumstances this can cause bonds to break - this can be bad in regards to cells and DNA. Heavy atoms like α particles may also simply break a molecule on impact (_____).

The ability to ionize is also characterised by having an electric charge. Neutral particles are less ionising. Low energy electromagnetic radiation is also not ionising. This is why your phone or microwave cannot harm you, but repeated x-rays can.



3.4 Alpha Decay

During alpha (α) decay a particle is emitted from the nucleus. This particle is a _____, also known as an alpha particle _____. It is positively charged because it contains just two neutrons and two protons. It is slow moving (up to 10% the speed of light) due to its relatively large mass. Its large mass means it can only move _____ through the atmosphere before being absorbed or *redirected*.

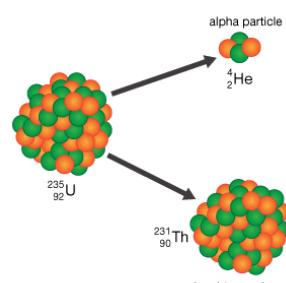


Figure 3.1: Alpha decay of a U-235 nucleus.

It also means that it is _____. Conversely, the large mass (high momentum) means that it will do a lot of damage if it impacts organic matter like DNA. It is said to have _____.

The majority of alpha emitters are the elements with atomic number greater than 83, although some other smaller nuclei also undergoing alpha emission.

3.5 Beta Decay

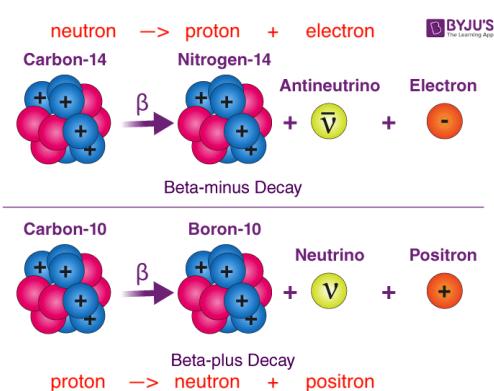


Figure 3.2: The two types of beta decay.

During beta (β^{-1}) decay a neutron inside the nucleus changes (decays) into a proton and a high energy electron is emitted. This changing of a neutron to a proton increases the atomic number of the atom by one, and therefore changes the element!

The emitted high-energy electron can travel up _____ due to its very small mass, and has a medium range in the atmosphere (______). It is able to pass through a sheet of paper but will be stopped by a more dense material e.g. 5mm of aluminium. It is said to have _____ and can disrupt chemical bonding on impact.

Notice how there are two options for beta decay in the diagram to the right. **In both cases electric charge is conserved.**

3.6 Gamma Decay

Gamma (γ) radiation is a form of high-energy electromagnetic radiation, and is not a particle at all. It is instead an electromagnetic wave with an _____. This kind of radiation occurs when a nucleus is left in an *excited state* after undergoing alpha or beta decay. It is a way for the nucleus to release energy.

Due to being electromagnetic radiation, it travels at _____ and will travel through large volumes of atmosphere. It requires several centimetres of dense metal (e.g. lead) to block gamma radiation, and due to its lack of mass, _____.

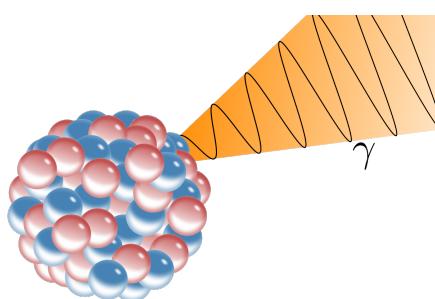
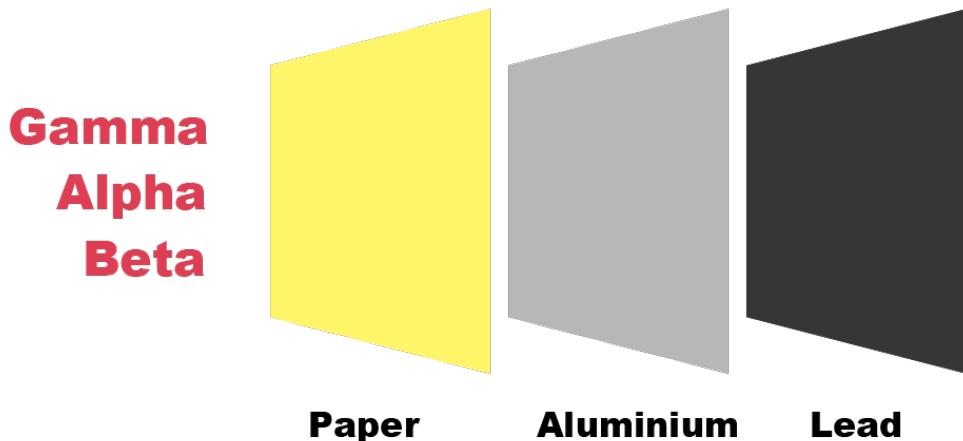


Figure 3.3: Notice that the nucleus stays the same.

3.7 Ngohe: Radiation Protection

Draw an arrow from each type of radiation, stopping the arrow at the material that is capable of blocking it.



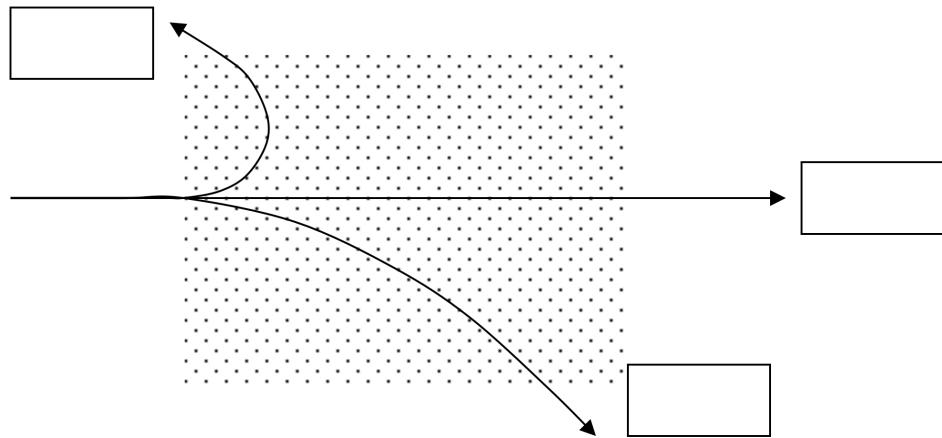
3.8 Whakawai: Types of Radiation

Summarise the types of radiation below.

	Mass	Charge	Speed	Ionising Ability
Alpha Particle				
Beta Particle				
Gamma Ray				

1. State which elements tend to be naturally radioactive and explain why.
2. Identify which of the three types of radiation is being described below.
 - (a) It travels a few cm in air.
 - (b) It will pass through aluminium sheet but is stopped by a few mm of lead.
 - (c) It is stopped by a sheet of paper.
 - (d) It will pass through more than a few mm of lead.

- (e) It is highly ionising.
- (f) It is not deflected by a magnetic field.
3. When the three types of radiation are passed through a magnetic field they separate into three beams as shown. Identify which beam is which.



4. Describe what happens to the atomic number and mass number of a nucleus which emits a beta particle.

Chapter 4: Nuclear Equations

Learning Outcomes

- Balance nuclear equations using the knowledge of the conservation of atomic and mass numbers.

An equation for a nuclear reaction looks a lot like a regular chemical reaction. The reactants go on the left, and the products (daughter products) go on the right. We also use an arrow in the middle. The main change is that we indicate the mass and atomic numbers to the left of each atom. M represents the _____, A represents the _____ and X represents _____.



Pātai: In the space provided write the nuclear symbols for Thorium, Plutonium, Americium and Gold.

4.1 Alpha Decay

In alpha (α) decay a helium nucleus is emitted from the parent atom. This means that the atom loses two protons and two neutrons. This means that the atomic number _____ by _____, and the mass number _____ by _____.

Pātai: Write the nuclear symbol for an alpha particle (two options):

Pātai: Use your knowledge of alpha decay to predict what atom would be produced.

	Before	After
Atom	Thallium-214	
Number of Protons		
Number of Neutrons		
Atomic Number		
Mass Number		

Pātai: Next, we should attempt to write this decay as a nuclear equation where Thallium-214 is the reactant, and the daughter atom and alpha particle are the products.

4.2 Beta Decay

In beta (β^{-1}, e^{-1}) decay a neutron turns into a proton and a _____ is emitted from the nucleus. This means that the atomic number _____ by _____, and the mass number _____.

Pātai: Write the nuclear symbol for a beta particle (two options):

Pātai: Use your knowledge of beta decay to predict what atom would be produced:

	Before	After
Atom	Polonium-218	
Number of Protons		
Number of Neutrons		
Atomic Number		
Mass Number		

Pātai: Next we should attempt to write this decay as a nuclear equation where Polonium-218 is the reactant, and the daughter atom and beta particle are the products.

4.3 Positron Emission

Due to the symmetrical nature of Physics, each particle has an *antiparticle*. In this case, this means that *electrical charge can be conserved* if the opposite of beta decay occurs. This means that a single proton turns into a neutron and emits a positron (think: a positive electron). This means that the atomic number _____ by _____, and the mass number _____.

Pātai: Write the nuclear symbol for a positron (two options):

Pātai: An example atom that undergoes positron decay is Magnesium-23. Use your knowledge of beta decay to predict what atom would be produced:

	Before	After
Atom	Magnesium-23	
Number of Protons		
Number of Neutrons		
Atomic Number		
Mass Number		

Pātai: Next we should attempt to write this decay as a nuclear equation where Magnesium-23 is the reactant, and the daughter atom and positron are the products.

4.4 Gamma Decay

In gamma (γ) decay an excited nucleus emits high-energy electromagnetic waves in the form of gamma radiation. The nucleus does not emit any particles - it only becomes more *relaxed*. This means that the atomic and mass numbers .

Pātai: Write the nuclear symbol for a gamma ray (one option):

Pātai: An example of gamma decay is after Cobolt-60 has decayed to Nickel-60 via beta decay. The Nickel-60 atom is in an excited (high energy state) and needs to emit some energy. Use your knowledge of gamma decay to predict what atom would be produced:

	Before	After
Atom	Nickel-60	
Number of Protons		
Number of Neutrons		
Atomic Number		
Mass Number		

Pātai: Next we should attempt to write this decay as a nuclear equation where Nickel-60 is the reactant, and the daughter atom and gamma ray are the products.

4.5 Whakawai: Decay Equations

Write the nuclear equations for these reactions. You may choose to write one or two equations in the case of double decays or absorptions.

1. An alpha decay of Polonium-218
2. A beta decay of Hydrogen-3
3. A gamma decay of Carbon-14
4. An absorption of a neutron by Carbon-13
5. A double alpha decay of Uranium-234
6. A double beta decay of Thorium-234

4.6 Whakawai: Types of Radiation

Complete the two nuclear equations below with appropriate symbols and numbers to identify the type of radiation emitted.



3. Uranium-238 decays to thorium (Th) by emitting an alpha particle. Complete the equation for this reaction using appropriate symbols and numbers.



4. What is meant by the term *ionising*?

5. Which type of radiation is most strongly ionising?

6. An electron can be emitted from a radioactive nucleus even though it cannot exist inside the nucleus. Where does that electron come from?

7. As part of an experiment, Rutherford placed an alpha particle emitter into a jar. When the jar was later tested it contained the gas helium that was not previously present. Explain how the helium was formed.

8. The isotope Radon-222 (${}_{86}^{222}Rn$) undergoes two consecutive radioactive decays and turns into the isotope Polonium-218 (${}_{84}^{218}Po$). Write equations to determine the TWO separate emissions. Name the emissions.

Chapter 5: Half-Life

Learning Outcomes

- Be able to make half-life graphs
- Be able to interpret half-life graphs

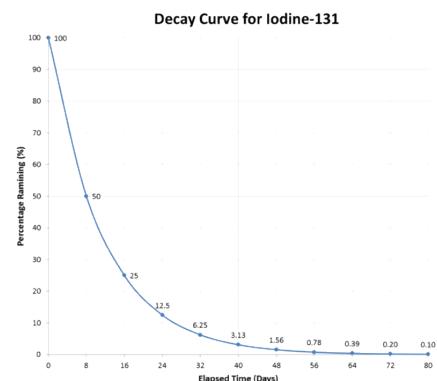
Introductory Video: <https://www.youtube.com/watch?v=zXw2cOSBB8E>

5.1 Whakamātau: Dice

1. In pairs, collect a container of dice from the front.
2. Count and record the total number of dice.
3. Roll all the dice in one go. Discard aside the dice with dots facing up, count the dice without dots and record that value.
4. Roll all the dice in one go that did not land with dots facing up. Discard those with dots facing up, count, record and repeat until no dice remain.
5. Create a line graph showing the number of dice rolled (y-axis) vs the roll number (x-axis).

What you have hopefully discovered is an exponential decay curve! This type of curve can be observed in a multitude of places in nature, but in Nuclear Physics it shows the half-life of a particular radioactive atom.

It is important to note that *for any section of a decay curve, it is steeper on the left and more gentle on the right*. This means that the mass/number of atoms is changing more rapidly on the left.



5.2 What is Half-Life?

Definition: The time taken for half of a radioactive sample to undergo decay.

Many things in the universe are deterministic - calculations can be performed to make accurate and specific predictions, however we are unable to predict when *exactly* a particular radioactive nuclei will decay. It turns out that decay is *probabilistic* and it is impossible to make a prediction for a single nuclei.

It is, however, possible to make predictions about groups of atoms using statistics (exponential decay curves).

We should also note that each different radioactive nuclei has a different half-life. Tellurium-128 is believed to have a half-life of over 128 trillion years, while Hydrogen-7 has a half-life of $23 \times 10^{-24} s$.

Pātai: If there were initially 1200 particles in a sample, fill out the number of particles left *after* each half life has elapsed.

Half-Lives Elapsed	Remaining		
	Fraction	Percentage	Particles
1			
2			
3			
4			
5			
6			
7			

5.3 Half-Life Calculations

Those of who are confident with their math skills will have noticed that you can formulate an equation to help you make precise predictions about the number of particles left for any given time. In Year 12 Physics we do not use a formula, rather we make more approximate predictions by creating and reading graphs. Equation use is something you may see in Year 13 and into tertiary education. We can also perform predictions simply by *dividing by two* (as above) and using this to help us make estimates.

5.3.1 Method 1: Dividing

This method is slightly less accurate in some cases than the graphical method. The half-life of Hydrogen-3 (Tritium) is approximately 12.25 years. If you found a small sample of Tritium containing 5,000,000 un-decayed nuclei.

1. How many nuclei will be left after 12.25 years?
2. How many nuclei will be left after 24.5 years?
3. How many nuclei will be left after 49 years?
4. How many nuclei will be left after 196 years?
5. How long until there is less than 2500 un-decayed nuclei left?

5.3.2 Method 2: Graphs

This method can help us gain a better view when we want to know about non-integer half-lives e.g. the number of particles after 4.5 half-lives.

Pātai: You found a 50g sample of Cobalt-60 which has a half-life of 5 years.

1. Sketch a mass vs. time graph of the Cobalt-60 sample over a 30-year period. Use the graph to answer the following questions:

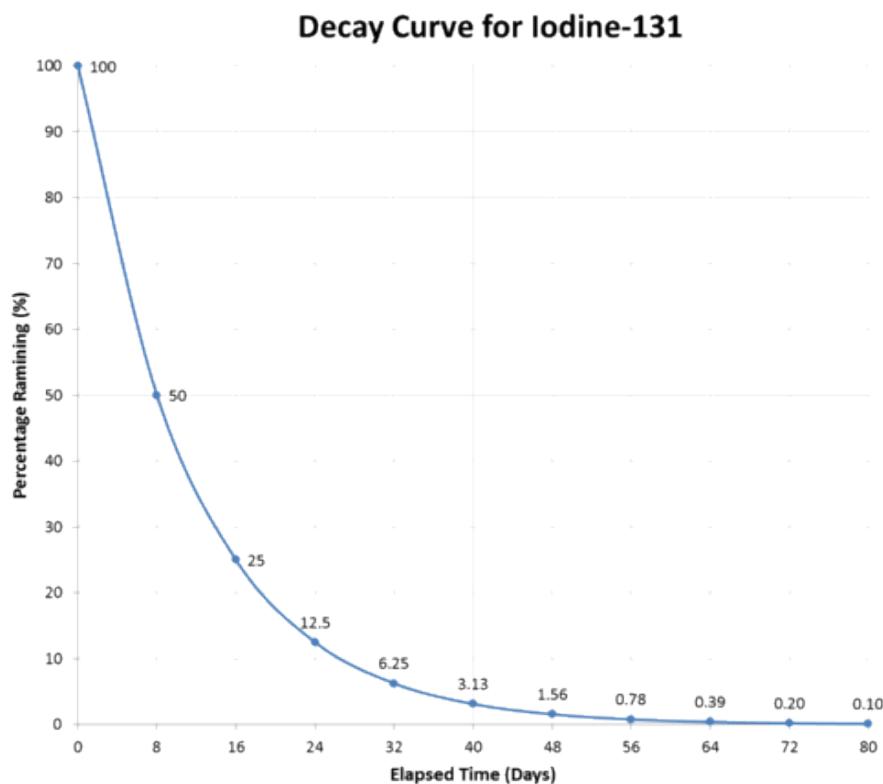
2. How long it would take for the mass of the 50g sample to fall just below 1.17g .

3. Estimate the mass of Cobalt-60 left after 12.5 years.

4. Estimate the number of Cobalt-60 particles after 20 years.

5.3.3 Whakawai: Iodine-131

Predict the amount of time until there is 37.5% of the original sample of Iodine-131 left.



5.3.4 Whakawai: Carbon-Dating

Radio-carbon dating is used to estimate the age of objects that were once living. All living things contain a small amount of radioactive Carbon-14 (^{14}C). Radioactive C-14 is created through the impact of cosmic rays with carbon in the atmosphere. This carbon is then used by plants in photosynthesis, and these plants eaten by animals.

Organisms have a relatively constant ratio of C-14 in them over their lifetime due to them continually consuming it through food. Once they die they are no longer acquiring C-14 and it starts to decay away.

Carbon-14, which has a half-life of 5700 years, decays to Carbon-12. By measuring the activity of a sample of dead tissue, its approximate age can be determined. Activity is measured in counts per minute ($\frac{\text{counts}}{\text{min}}$ or $\frac{\text{decays}}{\text{minute}}$).

1. Calculate the number of neutrons present in a carbon 14 nucleus.
 2. State what is meant by the term *half-life*.
 3. A sample of living wood has an activity of $16\text{counts}/\text{min}$ per gram. Calculate the activity of a 20g sample of living wood.
 4. Hence calculate the activity of a 20g sample of wood from a tree that died 17,100 years ago. State the correct unit for your answer.
 5. A 5.0g sample of wood from an archaeological site has an activity of $20\text{counts}/\text{min}$. Calculate the activity of the sample when the wood was living, and hence calculate how long ago the tree died.

Chapter 6: Fission and Fusion

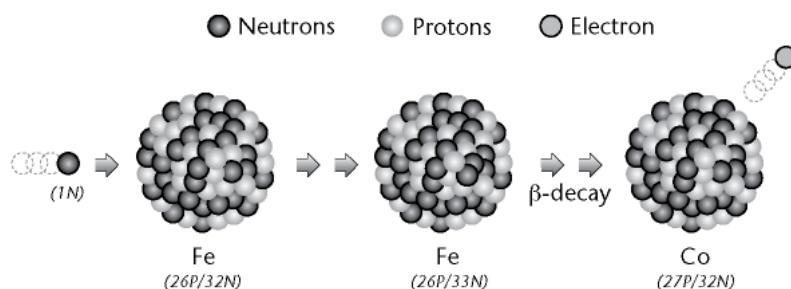
Learning Outcomes

- Understand the difference between nuclear fission and fusion
- Use $E = mc^2$
- Use $P = \frac{E}{t}$

Introductory Video: <https://www.youtube.com/watch?v=rcOFV4y5z8c>

6.1 Nuclear Fission

Recall from earlier that nuclei are generally stable because the _____ is greater than the _____. This means that even though the protons repel each other, the nucleus does not break apart. Also recall that atoms with a nucleus that is too large in volume can be unstable (radioactive). This is because the electrostatic force is greater than the strong nuclear force, and the atom can then break down (decay) via alpha or beta/positron emission.



By colliding high-speed neutrons with an already large nucleus, the neutron can sometimes be incorporated into the nucleus via the _____. This in turn causes the electrostatic force to now become larger than the strong nuclear force and **the nuclei to break apart in nuclear fission**. This is the process through which nuclear reactors produce energy here on Earth.

6.1.1 Pātai: Fission of Uranium

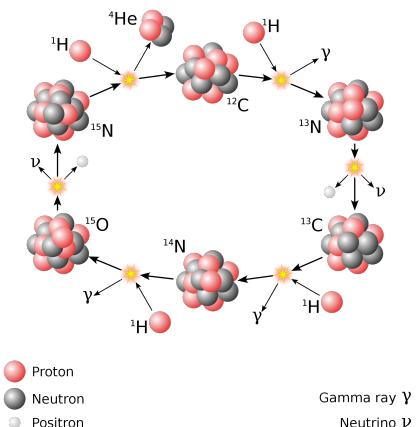
Uranium-235 is bombarded with a high speed neutron. The resulting nucleus becomes radioactive and decays into two daughter nuclei: Krypton-92 and Barium-141.

1. Write a nuclear equation describing the bombardment and fission of U-235
2. What is the third product? How did you determine it - what was conserved?

6.2 Nuclear Fusion

Unlike Nuclear Fission, with fusion we can add whole nuclei together! This is the process through which stars produce energy. Fusion typically requires very high temperatures and pressures in order to get the nuclei close enough to combine. It is for this reason that we struggle to create self-sustaining fusion reactions here on Earth - it is hard to create and maintain these conditions.

However, it is important to note that fusing nuclei smaller than iron produces energy, while trying to fuse nuclei larger than iron requires more energy than is produced. We will see this concept again later!



6.2.1 Pātai: Fusion of Hydrogen

In the Sun deuterium (H-2) and tritium (H-3) are fused together to create helium (He-4) and one other product.

1. Write a nuclear equation describing the fusion of H-2 and H-3
2. What is the second product? How did you determine it - what was conserved?

6.3 Mass-Energy Equivalence

You probably know Einstein's most famous formula where E is energy, m is mass and c is the speed of light:

$$E = mc^2$$

Because the speed of light is so large, this implies that a small amount of mass can be converted into a large amount of energy.

6.3.1 Pātai: Antimatter

Let's pretend $2g$ of material is converted directly into energy (this would be a matter-antimatter collision). Calculate the amount of energy generated by this reaction, given

$$c \approx 3 \times 10^8 \text{ m s}^{-1}.$$

Knowns:

Unknowns:

Formula:

Substitute:

Solve + Unit:

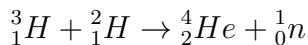
Introductory Video: <https://www.youtube.com/watch?v=HEYbgyL5n1g>

6.4 How Fission and Fusion Produce Energy

It turns out that if you measure the mass of the reactants and products of a nuclear reaction, mass is not (exactly) conserved. Instead, the products have slightly less total mass than the reactants. This means that some mass was lost. Where did it go? It turned into energy via mass-energy equivalence.

6.4.1 Pātai: Fusion of Deuterium

Introductory Video: <https://www.youtube.com/watch?v=mZsaaturR6E>



- Tritium (3_1H) = $5.00641 \times 10^{-27} \text{ kg}$
- Deuterium (2_1H) = $3.3436 \times 10^{-27} \text{ kg}$
- Helium (4_2He) = $6.64466 \times 10^{-27} \text{ kg}$
- Neutron (1_0n) = $1.67493 \times 10^{-27} \text{ kg}$

Use these data to answer the following questions.

1. Calculate the total mass of the reactants.
2. Calculate the total mass of the products.
3. Calculate the amount of mass lost during the reaction.

- Calculate the energy produced during this reaction.
- Calculate the power output of this reaction if it took 0.0001s to occur ($P = \frac{E}{t}$).

6.4.2 Pātai: Fission of U235

A nuclear power plant in the US can produce 1GW of power through neutron bombardment of U-235 and consequently, its fission. This fission produces Ba-141, Kr-92 and three neutrons.

- $U - 235 = 390.2480 \times 10^{-27}\text{kg}$
- $Ba - 141 = 233.9616 \times 10^{-27}\text{kg}$
- $Kr - 92 = 152.5794 \times 10^{-27}\text{kg}$
- $\text{Neutron} = 1.67493 \times 10^{-27}\text{kg}$

Use these data to answer the following questions.

- Write an equation describing this nuclear reaction.
- Calculate the total mass of the reactants.
- Calculate the total mass of the products.
- Calculate the amount of mass lost during the reaction.
- Calculate the energy produced during this reaction.

6. If the plant is running for one year, calculate the mass of U-235 required. Start by calculating the amount of mass needed to produce $1GW$ of power, and then scale that up to the length of one year.

PERIODIC TABLE OF THE ELEMENTS

1		Group (IUPAC)		Group (CAS)		Atomic Number		Oxidation States		Electron Shells		Energy Level		Shell Name		Max. Electrons		Periodic Table		VIIA		VIA		VA		IVA		IIIA		IIIB		VIIIB		VIB		IVIB		IIIB		IIIA		IIA		IA																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																								
1	H	2		3	+1	Hydrogen	1.008	1	+1	1	L	M	N	O	P	Q	R	1	2	3	4	5	6	7	8	5	6	7	8	13	14	15	16	17	VIIA	18	He	0	Helium	4.003	2																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																											
3	Li	4	Be	2	+2	Lithium	6.941	2.1	+1	9.012	2.2	S	2	2	2	2	2	2	2	8	18	32	18	8	2	5	B	C	4	Gd	Tb	6	7	8	15	16	VIA	17	F	-1	Fluorine	18.998	27																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																									
2		11	+1	Na	12	+2	Sodium	22.990	2.1	Magnesium	24.305	2.82	p	6	6	6	6	6	6	d	10	10	10	10	10	10	5	Boron	Carbon	12.011	2.3	Nitrogen	14.007	25	Oxygen	15.999	26	VIIA	16	O	-2	Neon	20.180	28																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																								
3		19	+1	K	Ca	20	+2	Sc	21	+3	Ti	22	+4	V	23	+5	Cr	24	+6	Mn	25	+7	Fe	26	+8	Co	27	+9	Cu	28	+10	Ni	29	+11	Zn	30	+12	Ga	31	+13	Ge	32	+14	As	33	+15	Se	34	+16	Br	35	+17	Cl	36	+18	Ar	37	+19	He	0	Helium	4.003	2																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																					
4		37	+1	Rb	Sr	38	+2	Y	39	+3	Zr	40	+4	Mo	41	+5	Nb	42	+6	Ru	43	+7	Tc	44	+8	Rh	45	+9	Pd	46	+10	Ag	47	+11	Cd	48	+12	In	49	+13	Sn	50	+14	Sh	51	+15	Te	52	+16	I	53	+17	Xe	54	+18	Rn	55	+19	Au	56	+20	Kr	57	+21	Gd	58	+22	Lu	59	+23	Xe	60	+24	He	0	Helium	4.003	2																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																						
5		87	+1	Fr	Ra	88	+2	Cs	89	+3	Ba	90	+4	Ra	91	+5	Th	92	+6	Hf	93	+7	Ta	94	+8	W	95	+9	Re	96	+10	Os	97	+11	Ir	98	+12	Pt	99	+13	Hg	100	+14	Au	101	+15	Pb	102	+16	Bi	103	+17	At	104	+18	Rn	105	+19	Fr	106	+20	Fr	107	+21	Fr	108	+22	Fr	109	+23	Fr	110	+24	Fr	111	+25	Fr	112	+26	Fr	113	+27	Fr	114	+28	Fr	115	+29	Fr	116	+30	Fr	117	+31	Fr	118	+32	Fr	119	+33	Fr	120	+34	Fr	121	+35	Fr	122	+36	Fr	123	+37	Fr	124	+38	Fr	125	+39	Fr	126	+40	Fr	127	+41	Fr	128	+42	Fr	129	+43	Fr	130	+44	Fr	131	+45	Fr	132	+46	Fr	133	+47	Fr	134	+48	Fr	135	+49	Fr	136	+50	Fr	137	+51	Fr	138	+52	Fr	139	+53	Fr	140	+54	Fr	141	+55	Fr	142	+56	Fr	143	+57	Fr	144	+58	Fr	145	+59	Fr	146	+60	Fr	147	+61	Fr	148	+62	Fr	149	+63	Fr	150	+64	Fr	151	+65	Fr	152	+66	Fr	153	+67	Fr	154	+68	Fr	155	+69	Fr	156	+70	Fr	157	+71	Fr	158	+72	Fr	159	+73	Fr	160	+74	Fr	161	+75	Fr	162	+76	Fr	163	+77	Fr	164	+78	Fr	165	+79	Fr	166	+80	Fr	167	+81	Fr	168	+82	Fr	169	+83	Fr	170	+84	Fr	171	+85	Fr	172	+86	Fr	173	+87	Fr	174	+88	Fr	175	+89	Fr	176	+90	Fr	177	+91	Fr	178	+92	Fr	179	+93	Fr	180	+94	Fr	181	+95	Fr	182	+96	Fr	183	+97	Fr	184	+98	Fr	185	+99	Fr	186	+100	Fr	187	+101	Fr	188	+102	Fr	189	+103	Fr	190	+104	Fr	191	+105	Fr	192	+106	Fr	193	+107	Fr	194	+108	Fr	195	+109	Fr	196	+110	Fr	197	+111	Fr	198	+112	Fr	199	+113	Fr	200	+114	Fr	201	+115	Fr	202	+116	Fr	203	+117	Fr	204	+118	Fr	205	+119	Fr	206	+120	Fr	207	+121	Fr	208	+122	Fr	209	+123	Fr	210	+124	Fr	211	+125	Fr	212	+126	Fr	213	+127	Fr	214	+128	Fr	215	+129	Fr	216	+130	Fr	217	+131	Fr	218	+132	Fr	219	+133	Fr	220	+134	Fr	221	+135	Fr	222	+136	Fr	223	+137	Fr	224	+138	Fr	225	+139	Fr	226	+140	Fr	227	+141	Fr	228	+142	Fr	229	+143	Fr	230	+144	Fr	231	+145	Fr	232	+146	Fr	233	+147	Fr	234	+148	Fr	235	+149	Fr	236	+150	Fr	237	+151	Fr	238	+152	Fr	239	+153	Fr	240	+154	Fr	241	+155	Fr	242	+156	Fr	243	+157	Fr	244	+158	Fr	245	+159	Fr	246	+160	Fr	247	+161	Fr	248	+162	Fr	249	+163	Fr	250	+164	Fr	251	+165	Fr	252	+166	Fr	253	+167	Fr	254	+168	Fr	255	+169	Fr	256	+170	Fr	257	+171	Fr	258	+172	Fr	259	+173	Fr	260	+174	Fr	261	+175	Fr	262	+176	Fr	263	+177	Fr	264	+178	Fr	265	+179	Fr	266	+180	Fr	267	+181	Fr	268	+182	Fr	269	+183	Fr	270	+184	Fr	271	+185	Fr	272	+186	Fr	273	+187	Fr	274	+188	Fr	275	+189	Fr	276	+190	Fr	277	+191	Fr	278	+192	Fr	279	+193	Fr	280	+194	Fr	281	+195	Fr	282	+196	Fr	283	+197	Fr	284	+198	Fr	285	+199	Fr	286	+200	Fr	287	+201	Fr	288	+202	Fr	289	+203	Fr	290	+204	Fr	291	+205	Fr	292	+206	Fr	293	+207	Fr	294	+208	Fr	295	+209	Fr	296	+210	Fr	297	+211	Fr	298	+212	Fr	299	+213	Fr	300	+214	Fr	301	+215	Fr	302	+216	Fr	303	+217	Fr	304	+218	Fr	305	+219	Fr	306	+220	Fr	307	+221	Fr	308	+222	Fr	309	+223	Fr	310	+224	Fr	311	+225	Fr	312	+226	Fr	313	+227	Fr	314	+228	Fr	315	+229	Fr	316	+230	Fr	317	+231	Fr	318	+232	Fr	319	+233	Fr	320	+234	Fr	321	+235	Fr	322	+236	Fr	323	+237	Fr	324	+238	Fr	325	+239	Fr	326	+240	Fr	327	+241	Fr	328	+242	Fr	329	+243	Fr	330	+244	Fr	331	+245	Fr	332	+246	Fr	333	+247	Fr	334	+248	Fr	335	+249	Fr	336	+250	Fr	337	+251	Fr	338	+252	Fr	339	+253	Fr	340	+254	Fr	341	+255	Fr	342	+256	Fr	343	+257	Fr	344	+258	Fr	345	+259	Fr	346	+260	Fr	347	+261	Fr	348	+262	Fr	349	+263	Fr	350	+264	Fr	351	+265	Fr	352	+266	Fr	353	+267	Fr	354	+268	Fr	355	+269	Fr	356	+270	Fr	357	+271	Fr	358	+272	Fr	359	+273	Fr	360	+274	Fr	361	+275	Fr	362	+276	Fr	363	+277	Fr	364	+278	Fr	365	+279	Fr	366	+280	Fr	367	+281	Fr	368	+282	Fr	369	+283	Fr	370	+284	Fr	371	+285	Fr	372	+286	Fr	373	+287	Fr	374	+288	Fr	375	+289	Fr	376	+290	Fr	377	+291	Fr	378	+292	Fr	379	+293	Fr	380	+294	Fr	381	+295	Fr	382	+296	Fr	383	+297	Fr	384	+298	Fr	385	+299	Fr	386	+300	Fr	387	+301	Fr	388	+302	Fr	389	+303	Fr	390	+304	Fr	391	+305	Fr	392	+306	Fr	393	+307	Fr	394	+308	Fr	395	+309	Fr	396	+310	Fr	397	+311	Fr	398	+312	Fr	399	+313	Fr	400	+314	Fr	401	+315	Fr	402	+316	Fr	403	+317	Fr	404	+318	Fr	405	+319	Fr	406	+320	Fr	407	+321	Fr	408	+322	Fr	409	+323	Fr	410	+324	Fr	411	+325	Fr	412	+326	Fr	413	+327	Fr	414	+328	Fr	415	+329	Fr	416	+330	Fr	417	+331	Fr	418	+332	Fr	419	+333	Fr	420	+334	Fr	421	+335	Fr	422	+336	Fr	423	+337	Fr	424	+338	Fr	425	+339	Fr	426	+340	Fr	427	+341	Fr	428	+342	Fr	429	+343	Fr	430	+344	Fr	431	+345	Fr	432	+346	Fr	433	+347	Fr	434	+348	Fr	435	+349	Fr	436	+350	Fr	437	+351	Fr	438	+352	Fr	439	+353	Fr	440	+354	Fr	441	+355	Fr	442	+356	Fr	443	+357	Fr	444	+358	Fr	445	+359	Fr	446	+360	Fr	447	+361	Fr	448	+362	Fr	449	+363	Fr	450	+364	Fr	451	+365	Fr	452	+366	Fr	453	+367	Fr	454	+368	Fr	455	+369	Fr	456	+370	Fr	457	+371	Fr	458	+372	Fr	459	+373	Fr	460	+374	Fr	461	+375	Fr	462	+376	Fr	463	+377	Fr	464	+378	Fr	465	+379	Fr	46