

Identifying Optimal Path

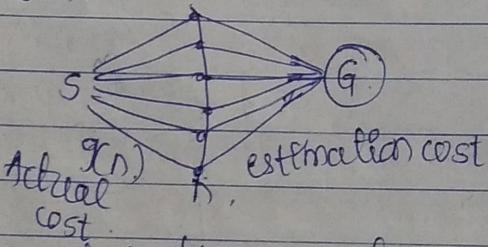
- Optimal path → lowest cost or Travelling the shortest distance
- Method for identifying optimal path → British Museum procedure.
- Techniques of identifying optimal path.
 - * A*
 - * Uniform cost search
 - * Greedy search.

A* Algorithms

A* algorithms operate in the same manner as best first search, but it uses the following function evaluate nodes

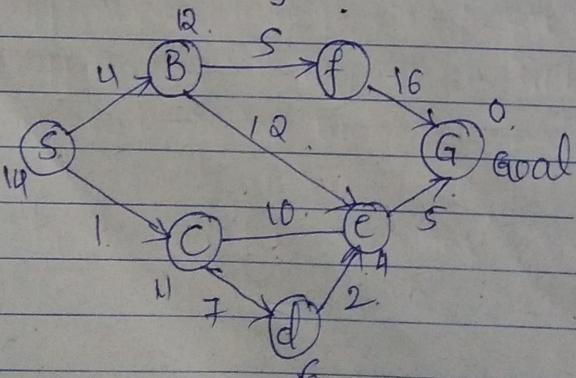
$$f(n) = g(n) + h(n)$$

Actual cost from start node to n.
Estimation cost from n to goal node.



* A* is Admissible algorithm

It guarantees that it will give the optimal solution starts with $f(n) = g(n) + h(n)$



$$f(S) = 0 + 14 = 14$$

$S \rightarrow B$.

$$4 + 12 = 16$$

$S \rightarrow C$.

$$3 + 11 = 14$$

Ass cost path
 $S \rightarrow C$ be 14

$$SC \rightarrow e = 3 + 10 + 4 = 17$$

$$SC \rightarrow d = 3 + 7 + 6 = 16$$

less cost
ie 16

$$scd \rightarrow e = 3 + 7 + 2 + 4 = 16$$

$$scde \rightarrow G = 3 + 7 + 2 + 5 + 0.$$

$Q + SFO = 17$ optimal cost to reach goal

$SB \rightarrow f$

Uniform cost search. {Backtracking is there}

→ Used for traversing

If it is used for traversing weighted ^{tree of} graph, it is used when different cost available in each edge.

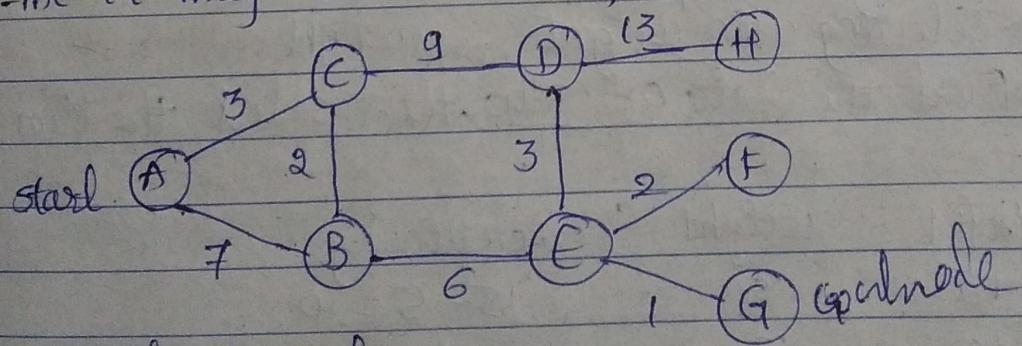
The goal of this is to find a path to the goal node which has lowest cumulative cost.

* It is used in where optimal cost is demand.

* It is implemented by priority queue; it gives maximum priority to lowest cumulative

Advantages → Every state the path with the least cost is chosen {optimal solution}

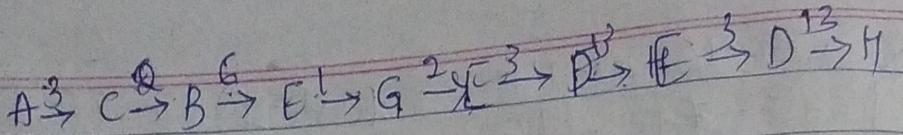
Disadvantage → Does not care about no of steps involved in searching & only concerned about path cost, sometimes it may stuck in infinite.



Path to goal

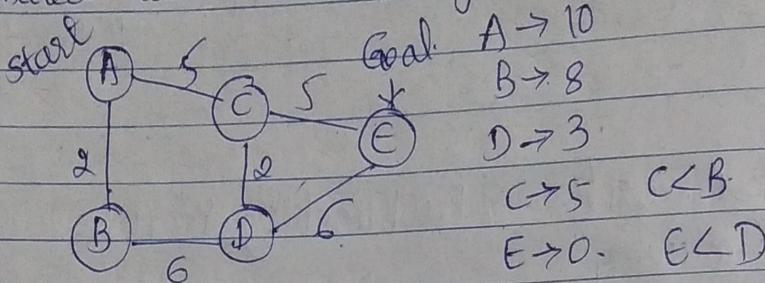
A → B

$$A \xrightarrow{3} C \xrightarrow{2} B \xrightarrow{6} E \xrightarrow{1} G = 12$$



Greedy Search

→ It selects the path that has lowest heuristic value
estimated distance to goal.



$A \rightarrow B \rightarrow E$

$$X = \sum_{i=1}^n w_i x_i$$

$$Y = \begin{cases} +1 & \text{for } x > t \\ 0 & \text{for } x \leq t \end{cases}$$

~~14/05/2022~~ Knapsack Problem

Fractional Knapsack problem.

Object	1	2	3	4	5	6	7	$\frac{3}{4} = \frac{5}{21}$
profit(P)	5	10	15	7	8	9	4	$w = 15$
weight(w)	3	3	5	4	1	3	2	$n = 7$
	5	3.3	3	1.75	8	3	2	max P/w

I approach - selecting max profit

II approach → Selecting min weight $\frac{\text{profit}}{\text{weight}}$

III approach → Find the ratio of p/w , then select the item

I)	Object	profit	weight	Remaining
1	3	15	5	$15 - 5 = 10$
2	2	10	3	7
6	6	9	3	4
5	5	8	1	3
4	4	$\frac{7 \times 3}{4} = 5.25$	3	$3 - 3 = 0$

Approach II. Obj	Profit	Weight	Remain
1	5	1	15 - 1 = 14
5	8	1	13
7	4	2	11
2	10	3	8
6	9	3	5
4.	7	4	1
3	<u>+5</u> 3	1	1 - 1 = 0
	5		

$$\text{II} = 46$$

III	Object	Profit	Weight	Remaining weight
	5	8	1	15 - 1 = 14
	1	5	1	13
	2	10	3	10
	3	15	5	5
	6	9	3	2
	7	<u>4</u>	2	0
		= 51		

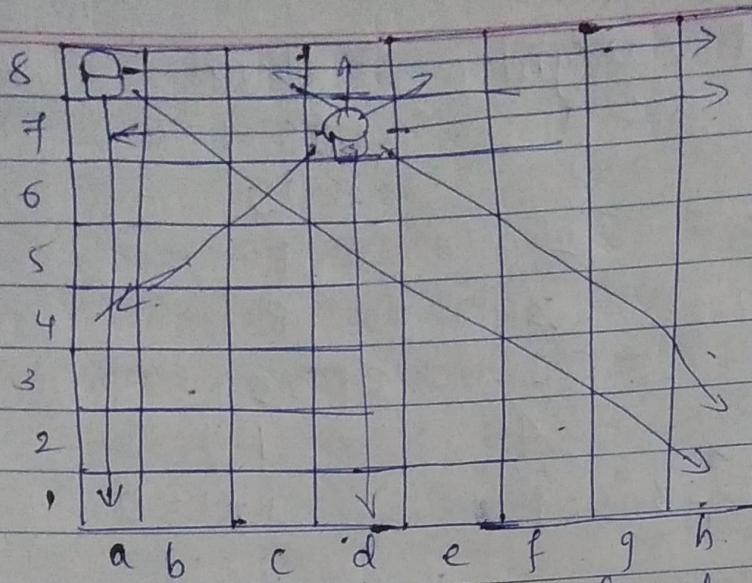
$$P|W = .5 \quad 3.33 \quad 3.175 \quad 8 \quad 3 \quad 2$$

$$\text{profit} = 51$$

Constraint Satisfaction Search

- 8 queens problem → constraint satisfaction problem
- 8 queens must be placed → No 2 queens are on same diagonal row or column
- columns → a to g, rows → 1 to 8
- This is called CSP → solution should satisfy constraints

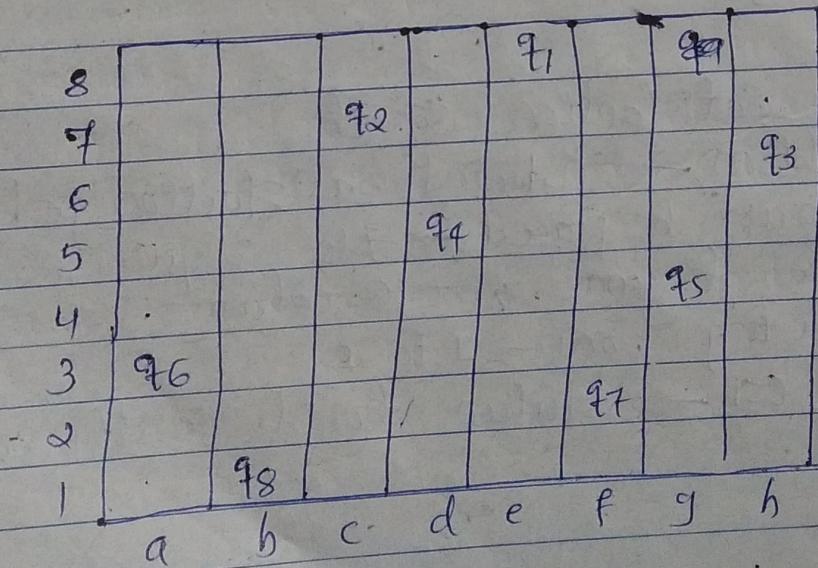
Let x
}



Goal node in the tree should satisfy the constraints that no two node queens are same node & diagonal. Analyze the every possible configuration until one was found that matched the constraint. 8 queen problems would be used to depth first search on a search tree.

The first branch from the root node would represent the 1st choice of square for a queen, the next branch represent choice where to place the second queen.

1st level have branching factor of 64.
next level have lower branching factor



Forward Checking

→ Learning this FCP by map coloring problem.
 Domains {R, G, B}
 variables {WA, NT, SA, QL, NSW, V}

WA	NT	QL
	SA	NSW
	V	

Implicit: $\{(WA \neq NT), (WA \neq SA), (NT \neq SA), (NT \neq QL),$
 $(CSA \neq QL), (QL \neq NSW), (CSA \neq NSW)\}$

Initial domain	WA	NT	SA	QL	NSW	V
	RGB	RGB	RGB	RGB	RGB	RGB
WA = B	B	R.G.	R.G	RGB	RGB	RGB
NT = G	B	G.	R.	RB	RGB	RGB
SA = R	B.	G.	R	B	GB	GB
QL = B	B	G	R	B	GB	GB
NSW = G	B	G	R	B	G	B
V	B	G	R	B	G	B

Forward checking where assigning a variable that removes the conflicting values for all the connected variables with it.

16/05/2022

Sy

3

Object 1 2 3 4 5 6 7

profit(p) 6 12 16 8 10 5 1

w=18

weight(w) 1 2 5 4 2 3 1

Object profit weight p/w Rew

1 6 1 6.1 17

2 12 2 6.2 $17 - 2 = 15$

3 16 5 3.2 15

4 8 4 2

3-5 10 2 5.3

6 5 3 1.6.6

7 1 1 1

object	profit	weight	Remaining weight
1	6	1	$18 - 1 = 17$
2	12	2	$17 - 2 = 15$
3	10	8	$15 - 8 = 7$
4	16	4.5	$7 - 4.5 = 2.5$
5	8	4	$2.5 - 4 = -1.5$
6	5	3	$-1.5 - 3 = -4.5$
7	1	1	$-4.5 - 1 = -5.5$
Profit = 58			

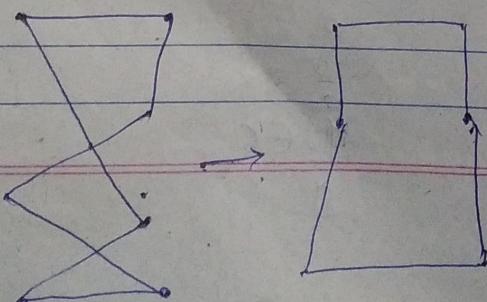
Local Search & metaheuristics

- Starting from some initial configuration (randomly)
- Making changes to the configuration until state is reached
- This is also called metaheuristics with no better state
- Problem of allocating teachers to classrooms randomly & make some changes.

Exchanging heuristics.

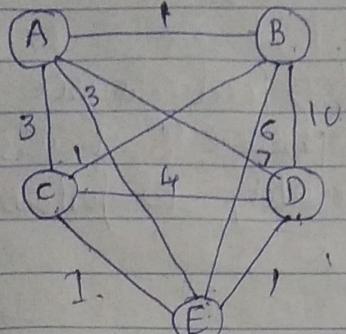
EH moves from one state to another by exchanging one or more variables by giving them different value
 'k' exchange heuristics used to solve the travelling salesman problem. If we use two exchange we remove two edges from the tour and substitute for two other edges.

If this produces a valid tour shorter than previous one then we continue the same or go back to the previous tour.

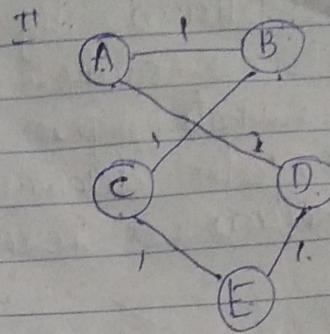


Tabu Search

for TSP



Random Initialization (ACE DBA)
total cost = 16



optimal soln.

A DECBA

Total cost = 16

III A → E → C → D → B → A
total cost = 19

Ant Colony Optimization

- Ant deposit pheromon on ground to mark some path to be followed by other members.
- eg. sugar candy.
- Ants navigate from nest to food source.
- shortest path discovered via pheromon trails.
- more pheromon → Increases probability to follow the path
shortest path

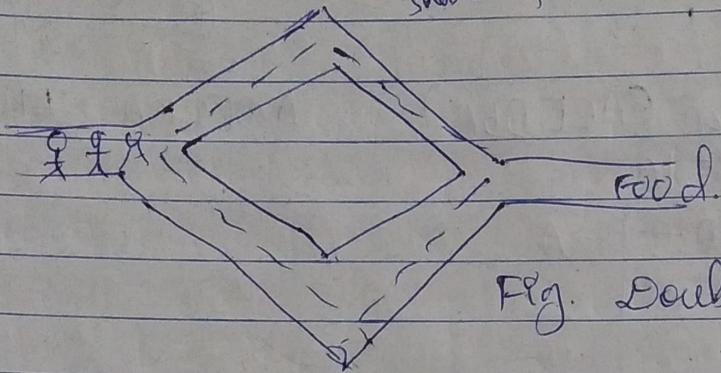


Fig. Double bridge

* simulated Annealing

uses concept

Genetic Algorithm

→ Initialisation

Initialisation

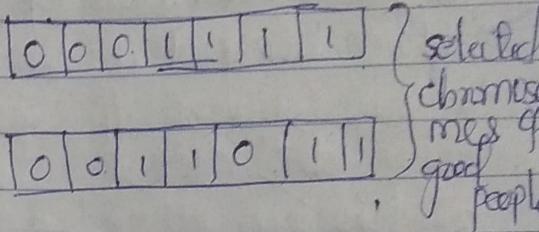
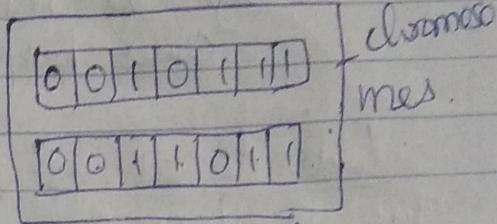
selection

← Fitness Function.

Cross over

Mutation

stop



0011011111

0010111111

} cross over - combining chromosomes & make exchanges

mutation → making random changes to particular genes.

A population of possible solutions is generated & fitness level of value for each chromosome is determined.

This fitness is used to determine the given chromosome will survive to the next generation.

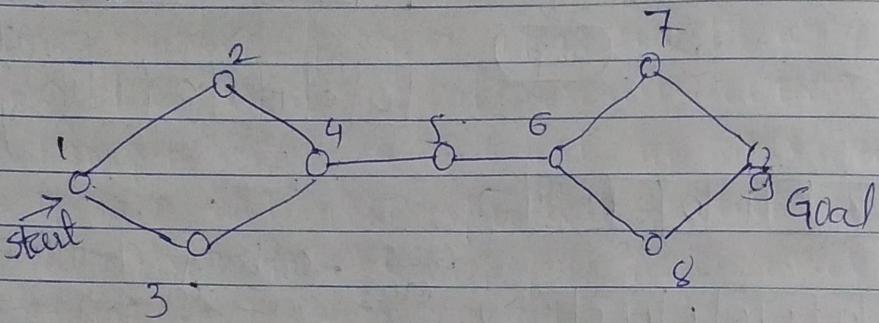
Reproduction is done by applying cross over to two chromosomes, features of each chromosome are combined together & mutation is applied for making random changes to particular genes.

Parallel Search

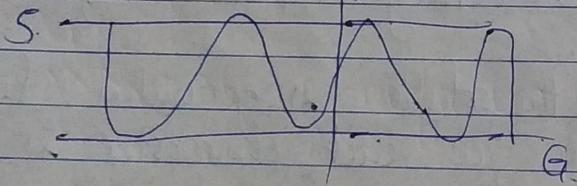
- Task → Broken into no. of subtasks → can run in parallel on separate processor.
- 2 processors → Divide the descendants of root node in half → Assign one half to second.
Assign one half to one processor
other half to second

Bidirectional Search

Two simultaneously search from an initial node to goal & backward from goal to initial stopping when two meet.



If uses breadth first search



Nondeterministic Search

- Running a nondeterministic search → new paths are added to queue at random positions

Function `random()`

{

queue = [];

start = root_node;

while(true)

{

if is_goal(state)

then return Success.

```
else  
add_randomly_to_queue(success(state));  
if queue == []  
    then report failure  
state = queue[0];  
remove_first_item_from(queue);  
}  
}
```

Non chronological Backtracking

→ It is alternative to chronological backtracking

→ chronological Backtracking

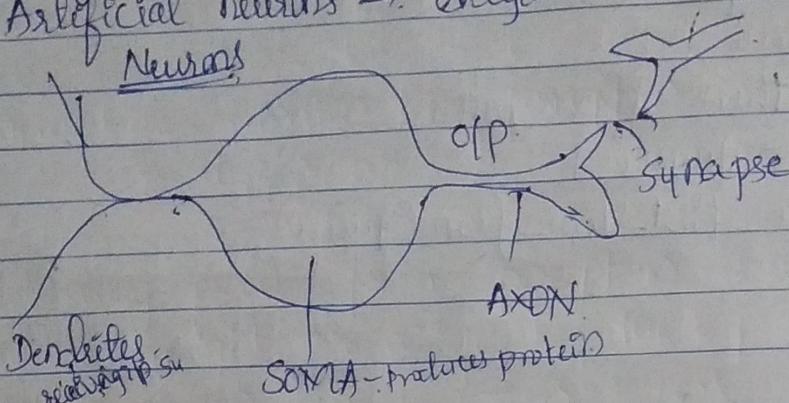
When dead end in a tree is found move back up the search tree to the last point in a tree where decision has to be made. and choose the next option at this junction.

It is useful in solving constraint satisfaction problem where backtracking can be applied by going back to the previous choice that caused contradiction to fail.

Unit-3

Neural Networks

- Biological neurons → human brain
- Artificial neurons → Artificial neural networks



→ human brain - Ten billion neurons → Each connected to other neurons - synapses

→ Neuron receives IP from other neurons using dendrite when this input signal exceeds certain threshold the neuron fires, a chemical reaction occurs, it is known as action potential which is send to the Axon toward synapse that connect the neuron to dendrite of other neurons.

→ Artificial neurons

→ ANN → No. of artificial neurons

→ Neurons in ANN have fewer connections than biological neurons

→ Each neuron in neural network receives no. of inputs

→ Activation function applied to these input values → Results in activation level of neuron

- Step function
- Sigmoid function
- Linear function

Behaviour of neuron

$$x_i = \sum_{j=1}^n w_{ij} x_j$$

$$y = \begin{cases} 1 & \text{for } x > t \\ 0 & \text{for } x \leq t \end{cases}$$

Activation level.

Wp - weight

Most commonly used function is the I/P to the neurons are summed (multiplied by a weight) the sum is compared with threshold 't'. If sum is greater than threshold then the neuron fires & has activation level of +1. Otherwise it is inactive & has activation level of 0.

X - weighted sum of n input to neuron

x_1 to $x_n \rightarrow$ Each I/P multiplied by corresponding weight w_i

$$w_1 = 0.8$$

$$w_2 = 0.4$$

the I/P x_1 & x_2 neuron $x_1 = 0.7$ & $x_2 = 0.9$

Calculate the sum weight

$$x = w_1 x_1 + w_2 x_2$$

$$0.8 \times 0.7 + 0.4 \times 0.9$$

$$0.56 + 0.36$$

$$x = 0.92$$

Perception

→ Perception → can have many no of inputs

→ can be used for image classification or recognition tasks

→ Perception uses step function returns +1 if weighted sum of input (x) $>$ threshold (t) & 0 if x less than or equal to t .

$$x = \sum_{i=1}^n w_i x_i$$

$$y = \begin{cases} +1 & \text{if } x > t \\ 0 & \text{if } x \leq t \end{cases}$$

step(x) :

$$\text{step}(x) = \begin{cases} +1 & \text{for } x > t \\ 0 & \text{for } x \leq t \end{cases}$$

activation function for perception.

$$Y = \text{step}\left(\sum_{i=0}^n w_i x_i\right)$$

Learning process for a perceptron is as follows
random weights are assigned to the inputs. Weights
will be chosen between -0.5 & +0.5.

An item of training data is presented to perception
& its output classifi. Once if the op
is wrong the weights are adjusted.

If the perceptron incorrectly classifies a +ve piece
of training data is -ve then the weights need
to modify to increase the op from set of ip.

$$w_i \leftarrow w_i + (a \times x_i \times e)$$

where e is error.

a - Learning rate

epoch

logical OR function for 2 inputs, threshold ($t=0$)
& learning rate of 0.2

Epoch	x_1	x_2	Expected Y	Actual Y	Error	w_1	w_2
1	0	0	0	0	0	-0.2	0.4
1	0	1	1	1	0	-0.2	0.4
1	1	0	1	0	1	0	0.4
1	1	1	1	1	0	0	0.4
2	0	0	0	0	0	0	0.4
2	0	1	1	1	0	0	0.4
2	1	0	1	0	1	0.2	0.4
2	1	1	1	1	0	0.2	0.4
3	0	0	0	0	0	0.2	0.4
3	0	1	1	0	1	0.2	0.4
3	1	0	1	0	1	0.2	0.4
3	1	1	1	1	0	0.2	0.4

$$w_0 = 0.2$$

$$w_1 = 0.4$$

Training data $x_1 = 0 \quad x_2 = 0$.

our expected output $x_1 \vee x_2 = 0$.

apply our formula

$$Y = \text{step} \left(\sum_{i=0}^1 w_i x_i \right)$$

$$= \text{step}(0 \cdot x_0 \cdot 2) + (0 \cdot x_0 \cdot 4)$$
$$= 0$$

Q1P y is expected error & it is 0, so weights don't change.

$$x_1 = 0 \quad x_2 = 1 \quad w_0 = -0.2$$

$$0 \cdot x_1 - 0.2 + 0 \cdot x_2 \cdot 4$$
$$= 0.4$$

$$\text{step}(0.4) = 1 > 0$$

For $x_1 = 1 \quad x_2 = 0$.

$$Y = \text{step}(1 \cdot x_1) + (0 \cdot x_2 \cdot 4)$$
$$= \text{step}(1)$$
$$= 1$$

This is incorrect value; weights are adjusted

$$w_0 \leftarrow w_0 + (1 \cdot x_1 \cdot x_2)$$

$$w_0 = -0.2 + (0.2 \cdot 1 \cdot 1)$$

$$= 0.2$$

$$w_1 = 0.4 + (0.2 \cdot 0 \cdot 1)$$

$$= 0.4$$

$$x_1 = 1 \quad x_2 = 1$$

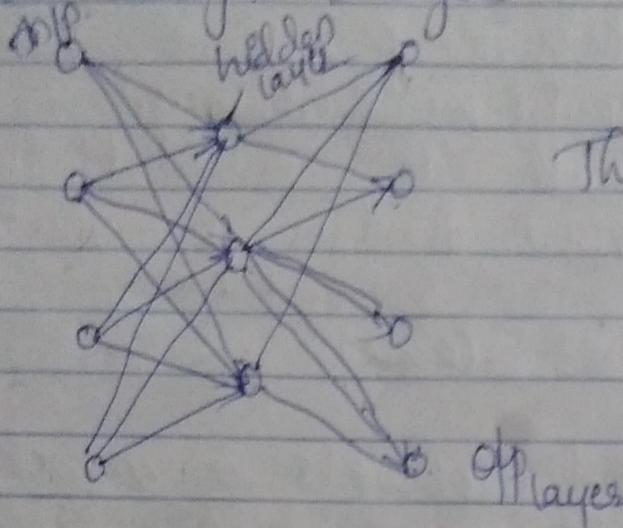
$$0 + 0.4 \cdot 1$$

$$0 + 0.4$$

$$0.4 = 1$$

Multilayer Neural Networks

- Neural networks consist of no of neurons connected together arranged in layers



Three layers feed forward neural network

Back propagation

Each neuron has weights associated with its inputs & greater numbers of weights to be adjusted when an error is made with piece of training data. So how to assign credit to various weights used in back propagation

Multilayer back propagation.
uses sigmoid function.

$$\text{It is defined as } \sigma(x) = \frac{1}{1+e^{-x}}$$

Recurrent Networks

- Feed forward → Data passes from I/p to O/p & not vice versa
- It does not have memory
- Recurrent networks have connections that go backward from O/p node to I/p nodes.
- Has memory
- Used in stock market, weather prediction.

Unsupervised learning networks

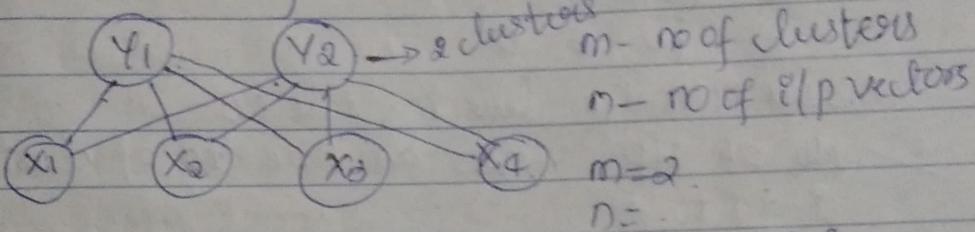
- Kohonen maps
- Called as self organising feature map.
- Trained using unsupervised learning.
- + Used for clustering data.

Algorithm

Step 0: Initialize weights w_{ij} , random values may be assigned, initialize the learning rate

Step 1: Complete the square of Euclidean distance for each $j = 1 \text{ to } m$.

$$D_j = \sum_{i=1}^n \sum_{j=1}^m (x_i - w_{ij})^2$$



Step 2: Find the winning index j so that D_j is minimum.

Step 3: For all units j and for all i calculate new weights

$$w_{ij}^{\text{new}} = w_{ij}^{\text{old}} + \alpha (x_i - w_{ij}^{\text{old}})$$

new old learning I/p vector old.

Step 4: Update the learning rate α using the formula

$$\alpha(t+1) \quad - t = \text{iteration}$$

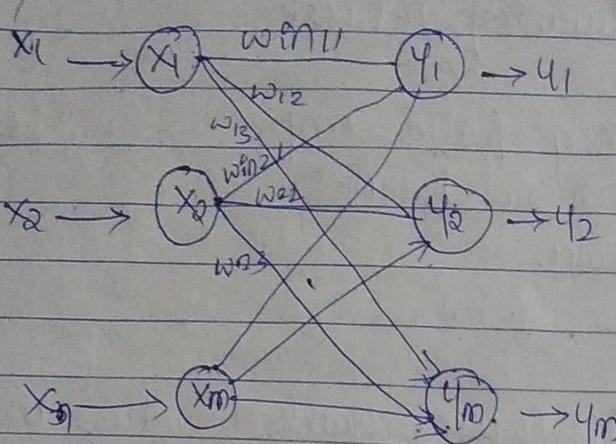
Step 5: After number of epochs test for stopping condition of the network.

$$w_{01} = 0.1234$$

$$w_{02} = 0.1234$$

$$w_{03} = 0.1233$$

$$w_{04} = 0.1235$$

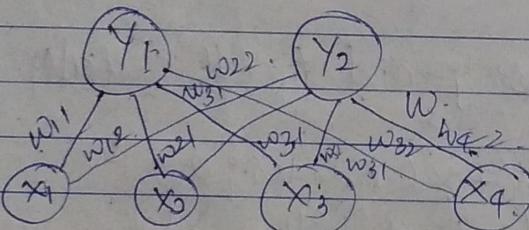


Construct (EASE) on to cluster for 4 given vectors

- x 1) $\begin{bmatrix} 0 & 0 & 1 & 1 \end{bmatrix}$ 4 no of clusters are formed
 2) $\begin{bmatrix} 1 & 0 & 0 & 0 \end{bmatrix}$ at 2.
 3) $\begin{bmatrix} 0 & 1 & 1 & 0 \end{bmatrix}$
 4) $\begin{bmatrix} 0 & 0 & 0 & 1 \end{bmatrix}$

Assume initial learning rate 0.5

No of ip vectors are n=4 no of clusters n=2
 $i = 1$ to 4.
 $j = 1$ to 2.



Here we have 4 values top clusters y_1 & y_2 and we calculate distance whichever is minimum for that update the weights & repeat the process.

$$w_{ij} = \begin{pmatrix} 0.2 & 0.9 \\ 0.4 & 0.7 \\ 0.6 & 0.5 \\ 0.8 & 0.3 \end{pmatrix}$$

w_{i1}
weights going for
cluster

w_{i2}
weight

0.0
0.8
0.2
0.5
0.0

First if $x = [0 \ 0 \ 1 \ 1]$

$$D_1 = \sum_{i=1}^m \sum_{j=1}^n (x_i - w_{ij})^2$$

$$D_1 = (x_1 - w_{11})^2 + (x_2 - w_{21})^2 + (x_3 - w_{31})^2 + (x_4 - w_{41})^2$$

$$= (0 - 0.2)^2 + (0 - 0.4)^2 + (1 - 0.6)^2 + (1 - 0.8)^2$$

$$= 0.4 + 0.16 + 0.4$$

$$D_2 = (x_1 - w_{12})^2 + (x_2 - w_{22})^2 + (x_3 - w_{32})^2 + (x_4 - w_{42})^2$$

$$= (0 - 0.9)^2 + (0 - 0.7)^2 + (1 - 0.5)^2 + (1 - 0.3)^2$$

$$= 2.04$$

$D_1 < D_2$ winning cluster is $j=1$ i.e. $y=1$

Update weights of winning clusters

$$j=1, y=1$$

$$w_{11}^* = w_{11} + \alpha (x_1 - w_{11})$$

$$w_{21}^* = w_{21} + \alpha (x_2 - w_{21})$$

$$w_{31}^* = w_{31} + \alpha (x_3 - w_{31})$$

$$= 0.2 + 0.5(0 - 0.2)$$

$$= 0.1 \quad (x_1 \rightarrow y_1)$$

$$w_{41}^* = w_{41} + \alpha (x_4 - w_{41})$$

$$= 0.4 + 0.5(0 - 0.4)$$

$$= 0.2$$

$$w_{31}^* = w_{31} + \alpha (x_3 - w_{31})$$

$$= 0.6 + 0.5(1 - 0.6)$$

$$= 0.8$$

$$w_{41}^* = w_{41} + \alpha (x_4 - w_{41})$$

$$= 0.8 + 0.5(1 - 0.8)$$

$$= 0.9$$

So, now updated weight

$$w_{ij}^* = \begin{bmatrix} 0.1 \\ 0.2 \\ 0.8 \\ 0.9 \end{bmatrix} \begin{bmatrix} 0.9 \\ 0.7 \\ 0.5 \\ 0.3 \end{bmatrix}$$

Second i/p vect

$$D(1) = \sqrt{(x_1 - w_{11})^2 + (x_2 - w_{21})^2 + (x_3 - w_{31})^2 + (x_4 - w_{41})^2}$$

$$= \sqrt{(1 - 0.1)^2 + (0 - 0.2)^2 + (0 - 0.8)^2 + (0 - 0.9)^2}$$

$$= 2.3$$

$$D(2) = \sqrt{(x_1 - w_{12})^2 + (x_2 - w_{22})^2 + (x_3 - w_{32})^2 + (x_4 - w_{42})^2}$$

$$= \sqrt{(1 - 0.9)^2 + (0 - 0.7)^2 + (0 - 0.5)^2 + (0 - 0.3)^2}$$

$$= 0.84$$

$$D(2) < D(1)$$

$$j=2 \quad y=2$$

update the weights of existing cluster

$$w_{1j}^e = w_{1j}^e + \alpha (x_p - w_{1j}^e)$$

$$w_{12}^e = w_{12}^e + \alpha (x_p - w_{12}^e)$$

$$w_{12} = w_{12} + 0.5(x_1 - w_{12})$$

$$= 0.9 + 0.5(1 - 0.9)$$

$$= 0.95$$

$$w_{2j}^e = w_{22} + 0.5(x_2 - w_{22})$$

$$= 0.7 + 0.5(0 - 0.7)$$

$$= 0.35$$

$$w_{3j}^e = w_{32} + 0.5(x_3 - w_{32})$$

$$= 0.5 + 0.5(0 - 0.5)$$

$$= 0.25$$

$$w_{4j}^e = w_{42} + 0.5(x_4 - w_{42})$$

$$= 0.3 + 0.5(0 - 0.3)$$

$$= 0.15$$

so now updated weights are

$$w_j^e = \begin{bmatrix} 0.1 \\ 0.2 \\ 0.8 \\ 0.9 \end{bmatrix} \begin{bmatrix} 0.95 \\ 0.35 \\ 0.25 \\ 0.15 \end{bmatrix}$$

3rd i/p ($x = [0.0 \ 1]$)

$$D_1 = \sqrt{(x_1 - w_{11})^2 + (x_2 - w_{21})^2 + (x_3 - w_{31})^2 + (x_4 - w_{41})^2}$$

$$= \sqrt{(0 - 0.1)^2 + (0 - 0.2)^2 + (0 - 0.8)^2 + (1 - 0.9)^2}$$

$$D_1 = 1.5$$

$$D_2 = (x_1 - w_{12})^2 + (x_2 - w_{22})^2 + (x_3 - w_{32})^2 + (x_4 - w_{42})^2$$

$$= 1.91$$

$$D(1) < D(2) \quad j=1 \quad y=1$$

update the weights of winning cluster

$$w_{11} = 0.05 \quad D(1)$$

$$w_{ij}^{\text{new}} = w_{ij}^{\text{old}} + \alpha (x_i^{\text{old}} - w_{ij}^{\text{old}})$$

$$w_{11}^{\text{old}} = w_{11} + \alpha (x_1^{\text{old}} - w_{11}^{\text{old}})$$

$$w_{11} = w_{11} + 0.5 (x_1 - w_{11})$$

$$= 0.1 + 0.5 (0 - 0.1)$$

$$= 0.05$$

$$w_{21}$$

$$= 0.6$$

$$w_{31}$$

$$= 0.9$$

$$w_{41} = 0.45$$

$$w_{ij} = \begin{bmatrix} 0.05 & 0.95 \\ 0.6 & 0.35 \\ 0.9 & 0.25 \\ 0.45 & 0.15 \end{bmatrix}$$

$$4^{\text{th}} \text{ I/P} \quad 0 \ 0 \ 0 \ 1$$

$$D(1) =$$

$$= 1.0475$$

$$D(2) = 2.065$$

$$D(2) = 1.081$$

$$D(1) < D(2) \quad j=1, \quad y=1$$

update weights

 $w_{11} = 0.025 \quad w_{21} = 0.3 \quad w_{31} = 0.45 \quad w_{41} = 0.7$

α

1st

$$\alpha(t+1) = 0.5 \times \alpha(t)$$

$$\alpha(0+1) = 0.5 \times \alpha(0.05)$$

$$= 0.25$$

Hopfield Networks ^{feedback}

→ Form of Recurrent networks.

→ Uses sign activation function

$$\text{sign}(x) = \begin{cases} +1 & \text{for } x > 0 \\ -1 & \text{for } x < 0 \end{cases}$$

weight of network represented by matrix, w

$$w = \sum_{i=1}^N x_i^t x_i^t - NI$$

$$x_1 = \begin{bmatrix} 2 \\ -1 \\ 1 \end{bmatrix}, x_1^t = [1 \ -1 \ 1], J = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Eg: 5 nodes & 3 training input

$$x_1 = \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}, x_2 = \begin{bmatrix} -1 \\ -1 \\ -1 \\ -1 \end{bmatrix}, x_3 = \begin{bmatrix} 1 \\ 1 \\ -1 \end{bmatrix}$$

x_1, x_2, x_3 are training p/p

$$w = \sum_{i=3}^3 x_i^t x_i^t - 3J$$

$$= x_1 x_1^t - 3J$$

$$\begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 & 1 \end{bmatrix} - 3 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$