Topology Analysis *†‡§

(v2.12.3)

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[‡]Besides, I would like to thank all of the people who have helped me in the development of the program. I am particularly grateful to Prof. Xingtao Huang for his comments on the principles and styles of the program, to Remco de Boer for his suggestions on the tex output and the use of GitHub, and to Xi Chen for his discussions on the core algorithms. I am especially indebted to Prof. Xiqing Hao, Longke Li, Xiaoping Qin, Ilya Komarov, Yubo Li, Guanda Gong, Suxian Li, Junhao Yin, Prof. Xiaolong Wang, Yeqi Chen, Hannah Wakeling, Hongrong Qi, Hui Li, Ning Cao, Sanjeeda Bharati Das, Kazuki Kojima, Tingting Han, Fang Yan, Lin Wang, Meiru An, and Noreen Rauls for their advice in extending and perfecting the program. Also, I thank Xi'an Xiong, Runqiu Ma, Wencheng Yan, Sen Jia, Lu Cao, Dong Liu, Hongpeng Wang, Jiawei Zhang, Jiajun Liu, Maoqiang Jing, Yi Zhang, Wei Shan, and Yadi Wang for their efforts in helping me test the program.

§The paper on the tool has been published by *Computer Physics Communications*. You can find this paper and the preprint corresponding to it in the links Comput. Phys. Commun. 258 (2021) 107540 and arXiv:2001.04016, respectively. If the tool really helps your researches, we would appreciate it very much if you could cite the paper in your publications.

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[†]This package is implemented referring to a program called Topo, which is first developed by Prof. Shuxian Du from Zhengzhou University and later extended and maintained by Prof. Gang Li from Institute of High Energy Physics, Chinese Academy of Sciences. The Topo program has been widely used by colleagues in BESIII collaboration. Several years ago, when I was a Ph.D. student working on the BESIII experiment, I learned the idea of topology analysis and a lot of programming techniques from the Topo program. So, I really appreciate the original works of Prof. Du and Prof. Li very much. To meet my own needs and to practice developing analysis tools with C++, ROOT, and LaTeX, I wrote the package from scratch. At that time, the package functioned well but was relatively simple. At the end of 2017, when I just started my post-doctoral research at Beihang University, my co-supervisor Prof. Chengping Shen reminded me that it could be a useful tool for the Belle II experiment as well. So, I revised and extended it, making it more well-rounded and suitable for the Belle II experiment. Now, it also applies to many other similar high energy physics experiments. Here, I would like to thank Prof. Du and Prof. Li for their original works, and Prof. Shen for his suggestion, guidance, support, and encouragement.

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Table 1: Decay trees and their respective initial-final states.

| rowNo | decay tree (decay initial-final states) | iDcyTr | nEtr | nCEtr |
|-------|---|--------|------|-------|
| 1 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to K^{+}D^{*-}D^{*0}, \bar{B}^{0} \to \rho^{-}D^{+}, D^{*-} \to \pi^{-}\bar{D}^{0}, D^{*0} \to \pi^{0}D^{0}, \rho^{-} \to \pi^{0}\pi^{-}, D^{+} \to \pi^{+}\pi^{+}K^{-}, \bar{D}^{0} \to e^{-}\bar{\nu}_{e}K^{+}, D^{0} \to \pi^{0}\pi^{+}K^{-} $ $(\Upsilon(4S) \dashrightarrow e^{-}\bar{\nu}_{e}\pi^{0}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}K^{+}K^{+}K^{-}K^{-})$ | 2963 | 6 | 6 |
| 2 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^+ D^- D^{*0}, \bar{B}^0 \to \bar{K}^0 K^+ K^-, D^- \to \pi^0 \pi^- K^*, D^{*0} \to \pi^0 D^0, \bar{K}^0 \to K_L^0, K^* \to \pi^0 K^0, D^0 \to K^- a_1^+, K^0 \to K_L^0, a_1^+ \to \pi^0 \rho^+, \rho^+ \to \pi^0 \pi^+ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 K_L^0 K_L^0 \pi^+ \pi^- K^+ K^+ K^- K^-)$ | 160 | 4 | 10 |
| 3 | $ \Upsilon(4S) \to B^0 B^0, B^0 \to K^* \gamma, B^0 \to D^{*-} D_{s1}^+, K^* \to \pi^- K^+, D^{*-} \to \pi^- \bar{D}^0, D_{s1}^+ \to K^+ D^{*0}, \\ \bar{D}^0 \to \pi^0 \phi, D^{*0} \to \pi^0 D^0, \phi \to K^+ K^-, D^0 \to \pi^+ \pi^- \bar{K}^*, \bar{K}^* \to \pi^+ K^- \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^+ K^+ K^- K^- \gamma) $ | 634 | 3 | 13 |
| 4 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \bar{K}^0 K^* \bar{D}^0, \bar{B}^0 \to \pi^0 D^{*0}, \bar{K}^0 \to K_S^0, K^* \to \pi^0 K^0, \bar{D}^0 \to \pi^0 \pi^- K^{*+}, D^{*0} \to \pi^0 D^0, K_S^0 \to \pi^+ \pi^-, K^0 \to K_S^0, K^{*+} \to \pi^0 K^+, D^0 \to \pi^+ K^-, K_S^0 \to \pi^+ \pi^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^-)$ | 854 | 3 | 16 |
| 5 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \pi^- K^+ D^{*+} D^{*-}, \bar{B}^0 \to \rho^- D^{*+}, D^{*+} \to \pi^0 D^+, D^{*-} \to \pi^- \bar{D}^0, \rho^- \to \pi^0 \pi^-, \\ D^{*+} \to \pi^+ D^0, D^+ \to \pi^+ K^+ K^-, \bar{D}^0 \to K^+ a_1^-, D^0 \to \pi^0 \pi^+ K^- \gamma^F, a_1^- \to \pi^0 \rho^-, \rho^- \to \pi^0 \pi^- \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 2558 | 3 | 19 |
| 6 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^+ \eta D^-, \bar{B}^0 \to \pi^+ K_0^{*-}, \rho^+ \to \pi^0 \pi^+, \eta \to \pi^0 \pi^0 \pi^0, D^- \to \pi^0 \pi^+ \pi^- \pi^-, K_0^{*-} \to \pi^0 K^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^-)$ | 2903 | 3 | 22 |
| 7 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \rho^{+}D^{*-}\gamma, \bar{B}^{0} \to \rho^{0}\pi^{-}\eta\omega D^{+}, \rho^{+} \to \pi^{0}\pi^{+}, D^{*-} \to \pi^{-}\bar{D}^{0}, \rho^{0} \to \pi^{+}\pi^{-}, \eta \to \gamma\gamma, \omega \to \pi^{0}\pi^{+}\pi^{-}, D^{+} \to \pi^{0}\pi^{+}\bar{K}^{*}, \bar{D}^{0} \to K^{+}K^{-}, \bar{K}^{*} \to \pi^{+}K^{-} (\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{-}K^{-}\gamma\gamma\gamma)$ | 16 | 2 | 24 |
| 8 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to K^{-}K_{0}^{*+}, \bar{B}^{0} \to \mu^{-}\bar{\nu}_{\mu}D^{*+}, K_{0}^{*+} \to \pi^{0}K^{+}, D^{*+} \to \pi^{+}D^{0}, D^{0} \to \pi^{0}K_{L}^{0}\pi^{+}\pi^{-}, K_{L}^{0} \to e^{+}\nu_{e}\pi^{-} (\Upsilon(4S) \dashrightarrow e^{+}\nu_{e}\mu^{-}\bar{\nu}_{\mu}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{-}\pi^{-}K^{+}K^{-})$ | 52 | 2 | 26 |
| 9 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^+ K^+ K^- K^{*+} K^{*-} D^{*-}, \bar{B}^0 \to \pi^0 D^0, K^{*+} \to \pi^+ K^0, K^{*-} \to \pi^- \bar{K}^0, D^{*-} \to \pi^- \bar{D}^0, \\ D^0 \to \pi^0 \pi^+ K^- \gamma^F, K^0 \to K^0_S, \bar{K}^0 \to K^0_L, \bar{D}^0 \to \pi^0 \pi^- K^+, K^0_S \to \pi^0 \pi^0 \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 K^0_L \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^- K^- \gamma^F) $ | 74 | 2 | 28 |
| 10 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^+ D^-, \bar{B}^0 \to J/\psi \bar{K}_1^0, \rho^+ \to \pi^0 \pi^+, D^- \to \pi^- \rho^- K^+, J/\psi \to \pi^- \bar{K}^0 K^{*+}, \\ \bar{K}_1^0 \to \rho^+ K^-, \rho^- \to \pi^0 \pi^-, \bar{K}^0 \to K_L^0, K^{*+} \to \pi^+ K^0, \rho^+ \to \pi^0 \pi^+, K^0 \to K_L^0 \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 K_L^0 K_L^0 \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^-) $ | 125 | 2 | 30 |
| 11 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^* \eta_c(2S), \bar{B}^0 \to D^+ a_1^-, K^* \to \pi^- K^+, \eta_c(2S) \to \pi^+ K^0 K^-, D^+ \to K_L^0 \pi^+ \pi^+ K^-, a_1^- \to \pi^0 \rho^-, K^0 \to K_L^0, \rho^- \to \pi^0 \pi^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 K_L^0 K_L^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^- K^-)$ | 162 | 2 | 32 |

| rowNo | decay tree (decay initial-final states) | iDcyTr | nEtr | nCEtr |
|-------|---|--------|------|-------|
| 12 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^+ D^- D^{*0}, \bar{B}^0 \to \rho^- D^{*+}, D^- \to \pi^- K^- K^{*+}, D^{*0} \to \pi^0 D^0, \rho^- \to \pi^0 \pi^-, \\ D^{*+} \to \pi^+ D^0, K^{*+} \to \pi^0 K^+, D^0 \to \pi^0 \pi^+ K^-, D^0 \to \pi^+ K^- \gamma^F \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^+ K^+ K^- K^- \gamma^F) $ | 166 | 2 | 34 |
| 13 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \rho^+ \omega K^* \bar{K}^* D^{*-}, \bar{B}^0 \to \pi^0 K_2^{*0}, \rho^+ \to \pi^0 \pi^+, \omega \to \pi^0 \pi^+ \pi^-, K^* \to \pi^- K^+, \bar{K}^* \to \pi^+ K^-, D^{*-} \to \pi^- \bar{D}^0, K_2^{*0} \to \pi^+ K^-, \bar{D}^0 \to \pi^0 \rho^- K^+, \rho^- \to \pi^0 \pi^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- K^+ K^+ K^- K^-)$ | 184 | 2 | 36 |
| 14 | $\Upsilon(4S) \to \bar{B}^0 \bar{B}^0, \bar{B}^0 \to K^+ K_0^{*-}, \bar{B}^0 \to \pi^- D^{*+} \gamma^F \gamma^F, K_0^{*-} \to \pi^0 K^-, D^{*+} \to \pi^0 D^+, D^+ \to \mu^+ \nu_\mu \bar{K}^0, \\ \bar{K}^0 \to K_S^0, K_S^0 \to \pi^0 \pi^0 \\ (\Upsilon(4S) \dashrightarrow \mu^+ \nu_\mu \pi^0 \pi^0 \pi^0 \pi^0 \pi^- K^+ K^- \gamma^F \gamma^F)$ | 211 | 2 | 38 |
| 15 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^+ \eta' D^{*-}, \bar{B}^0 \to \pi^+ K_0^{*-}, \eta' \to \pi^0 \pi^0 \eta, D^{*-} \to \pi^0 D^-, K_0^{*-} \to \pi^0 K^-, \eta \to \pi^0 \pi^0 \pi^0, D^- \to \pi^0 \pi^- K_S^0, K_S^0 \to \pi^0 \pi^0 (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 243 | 2 | 40 |
| 16 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^- K_0^{*+}, \bar{B}^0 \to \pi^+ \pi^- K^- D^+ \bar{D}^{*0}, \rho^- \to \pi^0 \pi^-, K_0^{*+} \to \pi^0 K^+, D^+ \to \pi^0 \pi^+ K_S^0, \\ \bar{D}^{*0} \to \bar{D}^0 \gamma, K_S^0 \to \pi^0 \pi^0, \bar{D}^0 \to \pi^0 K_S^0, \pi^0 \to e^+ e^- \gamma^F, K_S^0 \to \pi^0 \pi^0 \\ (\Upsilon(4S) \dashrightarrow e^+ e^- \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^- \gamma^F \gamma) $ | 265 | 2 | 42 |
| 17 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \bar{D}^{*0}, \bar{B}^0 \to \mu^- \bar{\nu}_{\mu} D^{*+}, \bar{D}^{*0} \to \bar{D}^0 \gamma, D^{*+} \to \pi^+ D^0, \bar{D}^0 \to \pi^- K^+, D^0 \to \pi^+ K^- (\Upsilon(4S) \dashrightarrow \mu^- \bar{\nu}_{\mu} \pi^0 \pi^+ \pi^+ \pi^- K^+ K^- \gamma)$ | 293 | 2 | 44 |
| 18 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \pi^{0}\bar{D}^{0}, \bar{B}^{0} \to K^{-}D^{*+}\bar{D}^{*0}, \bar{D}^{0} \to e^{-}\bar{\nu}_{e}K^{+}\gamma^{F}\gamma^{F}, D^{*+} \to \pi^{+}D^{0}, \bar{D}^{*0} \to \pi^{0}\bar{D}^{0},$ $D^{0} \to e^{+}\nu_{e}K^{*-}, \bar{D}^{0} \to \pi^{0}\pi^{-}K^{+}\gamma^{F}, K^{*-} \to \pi^{0}K^{-}$ $(\Upsilon(4S) \dashrightarrow e^{+}e^{-}\nu_{e}\bar{\nu}_{e}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{+}\pi^{-}K^{+}K^{+}K^{-}K^{-}\gamma^{F}\gamma^{F})$ | 314 | 2 | 46 |
| 19 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to D^{*-} D_s^+, \bar{B}^0 \to K^- D^{*+} \gamma^F, D^{*-} \to \pi^0 D^-, D_s^+ \to \pi^+ \eta', D^{*+} \to \pi^+ D^0, D^- \to \pi^0 \pi^- K^*, \eta' \to \rho^0 \gamma, D^0 \to \pi^0 \pi^0 \pi^+ \pi^-, K^* \to \pi^- K^+, \rho^0 \to \pi^+ \pi^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- K^+ K^- \gamma^F \gamma)$ | 378 | 2 | 48 |
| 20 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^+ D^-, \bar{B}^0 \to \pi^0 \pi^+ \pi^- \pi^- \rho^+ \rho^- D^{*+}, \rho^+ \to \pi^0 \pi^+, D^- \to \pi^- \pi^- K^+, \rho^+ \to \pi^0 \pi^+, \rho^- \to \pi^0 \pi^-, D^{*+} \to \pi^0 D^+, D^+ \to \pi^0 \pi^+ \bar{K}^*, \bar{K}^* \to \pi^+ K^- $ $(\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- \pi^- K^+ K^-)$ | 392 | 2 | 50 |
| 21 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^+ D^-, \bar{B}^0 \to \pi^0 \omega \omega K^- D^{*+}, \rho^+ \to \pi^0 \pi^+, D^- \to \pi^- \pi^- K^+ \gamma^F \gamma^F, \omega \to \pi^0 \pi^+ \pi^-, \omega \to \pi^0 \pi^+ \pi^-, D^{*+} \to \pi^+ D^0, D^0 \to \pi^0 \pi^+ K^- \gamma^F (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- K^+ K^- K^- \gamma^F \gamma^F)$ | 417 | 2 | 52 |
| 22 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \pi^- K^+, \bar{B}^0 \to \pi^+ \pi^- D^+ D_s^-, D^+ \to \pi^0 \pi^+ \omega, D_s^- \to \pi^0 \pi^- \omega, \omega \to \pi^0 \pi^+ \pi^-, \omega \to \pi^0 \pi^+ \pi^- \gamma^F $ $(\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- \pi^- K^+ \gamma^F)$ | 418 | 2 | 54 |
| 23 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 f_0(980), \bar{B}^0 \to \mu^- \bar{\nu}_\mu D^{*+}, f_0(980) \to K^+ K^- \gamma^F, D^{*+} \to \pi^+ D^0, D^0 \to \pi^0 \pi^+ K^- (\Upsilon(4S) \to \mu^- \bar{\nu}_\mu \pi^0 \pi^0 \pi^+ \pi^+ K^+ K^- K^- \gamma^F)$ | 420 | 2 | 56 |

| rowNo | decay tree (decay initial-final states) | iDcyTr | nEtr | nCEtr |
|-------|---|--------|------|-------|
| 24 | $\Upsilon(4S) \to B^0 B^0, B^0 \to K^- K_0^{*+}, B^0 \to \pi^0 \pi^+ \omega D^-, K_0^{*+} \to \pi^0 K^+, \omega \to \pi^0 \pi^+ \pi^-, D^- \to \pi^- \eta K_S^0, \\ \eta \to \pi^0 \pi^+ \pi^-, K_S^0 \to \pi^0 \pi^0 \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^-)$ | 425 | 2 | 58 |
| 25 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \pi^0 \omega \omega \bar{D}^0, \bar{B}^0 \to \bar{K}^0 K^+ K^-, \omega \to \pi^0 \pi^+ \pi^-, \omega \to \pi^0 \pi^+ \pi^-, \bar{D}^0 \to \pi^+ \pi^- K^*, \\ \bar{K}^0 \to K_S^0, K^* \to \pi^0 K^0, K_S^0 \to \pi^0 \pi^0, K^0 \to K_S^0, K_S^0 \to \pi^+ \pi^- \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 433 | 2 | 60 |
| 26 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \bar{D}^0, \bar{B}^0 \to \pi^0 K^0 K^- \phi D^{*+}, \bar{D}^0 \to e^- \bar{\nu}_e K^+ \gamma^F, K^0 \to K_L^0, \phi \to K^+ K^-, D^{*+} \to \pi^+ D^0, D^0 \to K^- a_1^+, a_1^+ \to \pi^0 \rho^+, \rho^+ \to \pi^0 \pi^+ (\Upsilon(4S) \dashrightarrow e^- \bar{\nu}_e \pi^0 \pi^0 \pi^0 K_L^0 \pi^+ \pi^+ K^+ K^- K^- K^- \gamma^F)$ | 464 | 2 | 62 |
| 27 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to D^{*-}D_{s}^{*+}, \bar{B}^{0} \to K_{s}^{0}\eta_{c}(2S), D^{*-} \to \pi^{-}\bar{D}^{0}, D_{s}^{*+} \to D_{s}^{+}\gamma, K_{S}^{0} \to \pi^{0}\pi^{0}, $ $\eta_{c}(2S) \to K^{+}K^{-}, \bar{D}^{0} \to \pi^{0}\pi^{0}\pi^{-}K^{+}, D_{s}^{+} \to \pi^{+}\pi^{+}\pi^{-}\pi^{-}$ $(\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{+}K^{-}\gamma)$ | 465 | 2 | 64 |
| 28 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^+ D^{*-} D^{*0}, \bar{B}^0 \to \pi^0 D^0, D^{*-} \to \pi^- \bar{D}^0, D^{*0} \to \pi^0 D^0, D^0 \to \pi^0 \pi^+ K^-, \\ \bar{D}^0 \to \mu^- \bar{\nu}_\mu K^{*+} \gamma^F, D^0 \to \pi^0 \pi^+ K^-, K^{*+} \to K^+ \gamma \\ (\Upsilon(4S) \dashrightarrow \mu^- \bar{\nu}_\mu \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- K^+ K^+ K^- K^- \gamma^F \gamma) $ | 466 | 2 | 66 |
| 29 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^- K_0^{*+}, \bar{B}^0 \to \pi^0 \pi^- \eta K^+ K^- D^{*+}, \rho^- \to \pi^0 \pi^-, K_0^{*+} \to \pi^0 K^+, \eta \to \pi^0 \pi^+ \pi^-, D^{*+} \to \pi^+ D^0, D^0 \to K^- K^{*+}, K^{*+} \to \pi^+ K^0, K^0 \to K_S^0, K_S^0 \to \pi^0 \pi^0 (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 484 | 2 | 68 |
| 30 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \pi^{-}K^{+}\eta_{c}, \bar{B}^{0} \to \bar{K}^{0}K^{+}K^{-}, \eta_{c} \to K^{-}p\bar{\Lambda}, \bar{K}^{0} \to K_{S}^{0}, \bar{\Lambda} \to \pi^{+}\bar{p}, K_{S}^{0} \to \pi^{0}\pi^{0} $ $(\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{+}\pi^{-}K^{+}K^{+}K^{-}K^{-}p\bar{p})$ | 488 | 2 | 70 |
| 31 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 K^+ K^-, \bar{B}^0 \to \rho^- K^+ K^{*-} D^{*+} \gamma^F, \rho^- \to \pi^0 \pi^-, K^{*-} \to \pi^0 K^-, D^{*+} \to \pi^0 D^+, D^+ \to e^+ \nu_e \bar{K}^0 \gamma^F, \bar{K}^0 \to K_L^0 $ $(\Upsilon(4S) \dashrightarrow e^+ \nu_e \pi^0 \pi^0 \pi^0 \pi^0 K_L^0 \pi^- K^+ K^+ K^- K^- \gamma^F \gamma^F)$ | 535 | 2 | 72 |
| 32 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \rho^{+}D^{-}, \bar{B}^{0} \to D^{*+}D_{s}^{*-}, \rho^{+} \to \pi^{0}\pi^{+}, D^{-} \to \pi^{-}\pi^{-}K^{+}, D^{*+} \to \pi^{+}D^{0},$ $D_{s}^{*-} \to D_{s}^{-}\gamma, D^{0} \to \pi^{+}\pi^{+}\pi^{-}K^{-}, D_{s}^{-} \to \tau^{-}\bar{\nu}_{\tau}, \tau^{-} \to \nu_{\tau}\pi^{0}\pi^{-}$ $(\Upsilon(4S) \dashrightarrow \nu_{\tau}\bar{\nu}_{\tau}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{-}\gamma)$ | 540 | 2 | 74 |
| 33 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \pi^{0}\bar{D}^{0}, \bar{B}^{0} \to \pi^{-}\rho^{+}\rho^{-}D^{*+}, \bar{D}^{0} \to e^{-}\bar{\nu}_{e}K^{+}, \rho^{+} \to \pi^{0}\pi^{+}, \rho^{-} \to \pi^{0}\pi^{-}, D^{*+} \to \pi^{+}D^{0}, D^{0} \to \pi^{0}\pi^{+}K^{-} \to \pi^{0}\pi^{+}K^{-} \to \pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}$ | 612 | 2 | 76 |
| 34 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^0 D_s^- D_s^{*+}, \bar{B}^0 \to \pi^0 \pi^+ K^-, K^0 \to K_S^0, D_s^- \to K^* K^{*-}, D_s^{*+} \to D_s^+ \gamma, K_S^0 \to \pi^+ \pi^-, K^* \to \pi^- K^+, K^{*-} \to \pi^0 K^-, D_s^+ \to \pi^+ K^+ K^- \gamma^F (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^+ K^+ K^- K^- K^- \gamma^F \gamma)$ | 644 | 2 | 78 |
| 35 | $\Upsilon(4S) \to B^0 B^0, B^0 \to K^- K^{*+}, B^0 \to \pi^0 \pi^+ \pi^+ \pi^- D^-, K^{*+} \to \pi^0 K^+, D^- \to \pi^0 K_L^0 \pi^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 K_L^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^-)$ | 715 | 2 | 80 |

| rowNo | decay tree (decay initial-final states) | iDcyTr | nEtr | nCEtr |
|-------|---|--------|------|-------|
| 36 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \bar{D}^{*0}, \bar{B}^0 \to \pi^0 \pi^- \pi^- \rho^+ D^{*+} \gamma^F \gamma^F, \bar{D}^{*0} \to \pi^0 \bar{D}^0, \rho^+ \to \pi^0 \pi^+, D^{*+} \to \pi^+ D^0, \\ \bar{D}^0 \to \mu^- \bar{\nu}_\mu K^+, D^0 \to K^- a_1^+, a_1^+ \to \pi^0 \rho^+, \rho^+ \to \pi^0 \pi^+ \\ (\Upsilon(4S) \dashrightarrow \mu^- \bar{\nu}_\mu \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^+ K^- \gamma^F \gamma^F) $ | 758 | 2 | 82 |
| 37 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \pi^0 \pi^- K^+, \bar{B}^0 \to \pi^0 \pi^+ \pi^- \pi^- K^- K^{*+} D^+, K^{*+} \to \pi^+ K^0, D^+ \to \pi^+ \rho^+ K^-, K^0 \to K_S^0, \\ \rho^+ \to \pi^0 \pi^+, K_S^0 \to \pi^0 \pi^0, \pi^0 \to e^+ e^- \gamma^F \\ (\Upsilon(4S) \dashrightarrow e^+ e^- \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^- K^- \gamma^F)$ | 767 | 2 | 84 |
| 38 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 K^* (1680)^0, \bar{B}^0 \to D^{*+} D_s^-, K^* (1680)^0 \to \pi^- K^+, D^{*+} \to D^+ \gamma, D_s^- \to \pi^- K^+ K^-, D^+ \to K_L^0 a_1^+, a_1^+ \to \pi^0 \rho^+, \rho^+ \to \pi^0 \pi^+ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 K_L^0 \pi^+ \pi^- \pi^- K^+ K^+ K^- \gamma)$ | 779 | 2 | 86 |
| 39 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^+ a_1^-, \bar{B}^0 \to \pi^0 \pi^0 \rho^- \eta D^+, a_1^- \to \pi^0 \rho^-, \rho^- \to \pi^0 \pi^-, \eta \to \gamma \gamma, $ $ D^+ \to \pi^0 \pi^+ \pi^+ \pi^- \eta, \rho^- \to \pi^0 \pi^- \gamma^F, \eta \to \pi^0 \pi^0 \pi^0 $ $ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 786 | 2 | 88 |
| 40 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to D^- D_{s1}^{\prime +}, \bar{B}^0 \to \rho^+ K^{*-}, D^- \to \pi^0 \pi^- K^*, D_{s1}^{\prime +} \to \pi^0 D_s^{*+}, \rho^+ \to \pi^0 \pi^+, K^{*-} \to \pi^0 K^-, K^* \to \pi^- K^+, D_s^{*+} \to D_s^+ \gamma, D_s^+ \to \rho^+ \phi, \rho^+ \to \pi^0 \pi^+, \phi \to K^+ K^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^+ K^- K^- \gamma)$ | 837 | 2 | 90 |
| 41 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to D_2^{*-} D_s^+, \bar{B}^0 \to \pi^0 \rho^+ K^- \gamma^F, D_2^{*-} \to \pi^- \bar{D}^0, D_s^+ \to \pi^0 \pi^+ \omega, \rho^+ \to \pi^0 \pi^+, \\ \bar{D}^0 \to \pi^+ \pi^- K^*, \omega \to \pi^0 \pi^+ \pi^-, K^* \to \pi^0 K^0, K^0 \to K_S^0, K_S^0 \to \pi^0 \pi^0 \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 874 | 2 | 92 |
| 42 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^+ D^-, \bar{B}^0 \to \rho^- D^{*+}, \rho^+ \to \pi^0 \pi^+, D^- \to \pi^0 \pi^- K^*, \rho^- \to \pi^0 \pi^-, D^{*+} \to \pi^+ D^0, K^* \to \pi^- K^+, D^0 \to \pi^+ K^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^-)$ | 896 | 2 | 94 |
| 43 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 K^*, \bar{B}^0 \to K^{*-} D^{*+} \bar{D}^0, K^* \to \pi^- K^+, K^{*-} \to \pi^0 K^- \gamma^F, D^{*+} \to \pi^+ D^0,$ $\bar{D}^0 \to \rho^- K^{*+}, D^0 \to e^+ \nu_e K^{*-}, \rho^- \to \pi^0 \pi^-, K^{*+} \to \pi^0 K^+, K^{*-} \to \pi^0 K^-$ $(\Upsilon(4S) \dashrightarrow e^+ \nu_e \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^- \pi^- K^+ K^- K^- \gamma^F)$ | 905 | 2 | 96 |
| 44 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \pi^{0}\bar{D}^{*0}, \bar{B}^{0} \to \bar{K}^{*}D^{+}D^{*-}, \bar{D}^{*0} \to \pi^{0}\bar{D}^{0}, \bar{K}^{*} \to \pi^{+}K^{-}, D^{+} \to \pi^{+}\pi^{+}K^{-}, D^{*-} \to \pi^{-}\bar{D}^{0}, \bar{D}^{0} \to \pi^{-}K^{+}\gamma^{F}, \bar{D}^{0} \to \pi^{0}\pi^{-}K^{+} $ $(\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{+}K^{-}K^{-}\gamma^{F})$ | 908 | 2 | 98 |
| 45 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \pi^{0}\pi^{+}D^{*-}, \bar{B}^{0} \to \bar{K}^{*}D^{*+}D^{*-}, D^{*-} \to \pi^{-}\bar{D}^{0}, \bar{K}^{*} \to \pi^{+}K^{-}\gamma^{F}, D^{*+} \to \pi^{0}D^{+}, D^{*-} \to \pi^{-}\bar{D}^{0}, \bar{D}^{0} \to \pi^{-}K^{+}, D^{+} \to e^{+}\nu_{e}\bar{K}^{0}, \bar{D}^{0} \to \pi^{0}\pi^{0}K^{+}K^{-}, \bar{K}^{0} \to K^{0}_{S}, K^{0}_{S} \to \pi^{+}\pi^{-} (\Upsilon(4S) \dashrightarrow e^{+}\nu_{e}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{+}K^{-}K^{-}\gamma^{F})$ | 941 | 2 | 100 |
| 46 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^- K^+ \gamma^F, \bar{B}^0 \to \pi^+ K^{*-} D^+ D^{*-}, \rho^- \to \pi^0 \pi^-, K^{*-} \to \pi^0 K^-, D^+ \to K_L^0 a_1^+, D^{*-} \to \pi^- \bar{D}^0, a_1^+ \to \pi^+ f_0(600), \bar{D}^0 \to \pi^0 \pi^- K^{*+}, f_0(600) \to \pi^0 \pi^0, K^{*+} \to \pi^0 K^+ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 1067 | 2 | 102 |
| 47 | $\Upsilon(4S) \to \bar{B}^0 \bar{B}^0, \bar{B}^0 \to \pi^0 f_2', \bar{B}^0 \to \rho^0 \pi^+ \pi^- \pi^- D^{*+}, f_2' \to K^+ K^-, \rho^0 \to \pi^+ \pi^-, D^{*+} \to \pi^+ D^0,$ $D^0 \to \pi^0 \pi^+ K^-$ $(\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^- K^-)$ | 1203 | 2 | 104 |

| rowNo | decay tree (decay initial-final states) | iDcyTr | nEtr | nCEtr |
|-------|--|--------|------|-------|
| 48 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^0 K^0 D^+ D^-, \bar{B}^0 \to \bar{K}^0 K^+ K^-, \rho^0 \to \pi^+ \pi^-, K^0 \to K_S^0, D^+ \to \mu^+ \nu_\mu \bar{K}^*, D^- \to \pi^- \phi, \bar{K}^0 \to K_S^0, K_S^0 \to \pi^0 \pi^0, \bar{K}^* \to \pi^0 \bar{K}^0, \phi \to K_L^0 K_S^0, K_S^0 \to \pi^0 \pi^0, \bar{K}^0 \to K_L^0, K_S^0 \to \pi^+ \pi^- (\Upsilon(4S) \dashrightarrow \mu^+ \nu_\mu \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 K_L^0 K_L^0 \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^-)$ | 1211 | 2 | 106 |
| 49 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \bar{D}^0, \bar{B}^0 \to \bar{K}^* D^{*+} D^{*-}, \bar{D}^0 \to e^- \bar{\nu}_e K^+, \bar{K}^* \to \pi^+ K^- \gamma^F, D^{*+} \to \pi^+ D^0,$ $D^{*-} \to \pi^- \bar{D}^0, D^0 \to K^- a_1^+, \bar{D}^0 \to \mu^- \bar{\nu}_\mu K^+, a_1^+ \to \rho^0 \pi^+, \rho^0 \to \pi^+ \pi^-$ $(\Upsilon(4S) \dashrightarrow e^- \bar{\nu}_e \mu^- \bar{\nu}_\mu \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^+ K^+ K^- K^- \gamma^F)$ | 1215 | 2 | 108 |
| 50 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \bar{D}^{*0}, \bar{B}^0 \to \pi^0 \bar{D}^{*0}, \bar{B}^0 \to \pi^0 \rho^0 \pi^+ \pi^- \pi^- \eta D^{*+}, \bar{D}^{*0} \to \pi^0 \bar{D}^0, \rho^0 \to \pi^+ \pi^-, \eta \to \pi^0 \pi^+ \pi^-, D^{*+} \to \pi^+ D^0, \bar{D}^0 \to \pi^0 \pi^- K^+, D^0 \to e^+ \nu_e K^{*-}, K^{*-} \to \pi^- \bar{K}^0, \bar{K}^0 \to K_L^0$ $(\Upsilon(4S) \dashrightarrow e^+ \nu_e \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 K_L^0 \pi^+ \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- \pi^- K^+)$ | 1224 | 2 | 110 |
| 51 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^0 K^+ K^-, \bar{B}^0 \to \pi^+ \pi^- \rho^- D^{*+}, K^0 \to K_S^0, \rho^- \to \pi^0 \pi^-, D^{*+} \to \pi^+ D^0, K_S^0 \to \pi^0 \pi^0, D^0 \to \mu^+ \nu_\mu K^- (\Upsilon(4S) \dashrightarrow \mu^+ \nu_\mu \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^- K^-)$ | 1241 | 2 | 112 |
| 52 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \pi^- K^+, \bar{B}^0 \to \pi^0 \pi^+ D^0 D_s^{*-}, D^0 \to \rho^+ K^{*-}, D_s^{*-} \to D_s^- \gamma, \rho^+ \to \pi^0 \pi^+ \gamma^F, K^{*-} \to \pi^0 K^-, D_s^- \to \pi^0 K_L^0 \pi^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 K_L^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^- \gamma^F \gamma)$ | 1334 | 2 | 114 |
| 53 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 K^+ K^-, \bar{B}^0 \to \pi^- \eta \eta K^0 \bar{K}^0 D^{*+}, \eta \to \gamma \gamma, \eta \to \gamma \gamma, K^0 \to K_S^0, \\ \bar{K}^0 \to K_S^0, D^{*+} \to \pi^0 D^+, K_S^0 \to \pi^+ \pi^-, K_S^0 \to \pi^+ \pi^-, D^+ \to K_L^0 K^+ \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 K_L^0 \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^+ K^- \gamma \gamma \gamma \gamma) $ | 1339 | 2 | 116 |
| 54 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \bar{D}^0, \bar{B}^0 \to \bar{K}^* D^{*+} D^{*-}, \bar{D}^0 \to \pi^0 \pi^+ \pi^- K^*, \bar{K}^* \to \pi^+ K^- \gamma^F, D^{*+} \to \pi^+ D^0, \\ D^{*-} \to \pi^0 D^-, K^* \to \pi^- K^+, D^0 \to K^- a_1^+, \pi^0 \to e^+ e^- \gamma^F, D^- \to \pi^- \pi^- K^+ \gamma^F, a_1^+ \to \pi^0 \rho^+, \\ \rho^+ \to \pi^0 \pi^+ \\ (\Upsilon(4S) \dashrightarrow e^+ e^- \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^+ K^- K^- \gamma^F \gamma^F \gamma^F) $ | 1352 | 2 | 118 |
| 55 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^- K_0^{*+}, \bar{B}^0 \to D^+ a_1^-, K_0^{*+} \to \pi^0 K^+, D^+ \to \pi^0 \pi^+ K_S^0, a_1^- \to \pi^0 \rho^-, K_S^0 \to \pi^+ \pi^-, \rho^- \to \pi^0 \pi^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+)$ | 1370 | 2 | 120 |
| 56 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \mu^+ \nu_\mu D^{*-}, \bar{B}^0 \to \rho^- D^+, D^{*-} \to \pi^0 D^-, \rho^- \to \pi^0 \pi^-, D^+ \to \pi^+ \pi^+ K^-,$ $D^- \to \pi^- \pi^- K^+$ $(\Upsilon(4S) \dashrightarrow \mu^+ \nu_\mu \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^-)$ | 1375 | 2 | 122 |
| 57 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^0 \bar{D}^{*0}, \bar{B}^0 \to \pi^+ \eta K^-, \rho^0 \to \pi^+ \pi^-, \bar{D}^{*0} \to \pi^0 \bar{D}^0, \eta \to \pi^0 \pi^0 \pi^0, $ $ \pi^0 \to e^+ e^- \gamma^F, \bar{D}^0 \to K^+ K^{*-}, K^{*-} \to \pi^- \bar{K}^0, \bar{K}^0 \to K^0_S, K^0_S \to \pi^+ \pi^- \gamma^F $ $ (\Upsilon(4S) \dashrightarrow e^+ e^- \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^- \gamma^F \gamma^F) $ | 1384 | 2 | 124 |
| 58 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to D^{*-}D_{s}^{*+}, \bar{B}^{0} \to \bar{K}^{0}K^{+}K^{-}\gamma^{F}, D^{*-} \to \pi^{0}D^{-}, D_{s}^{*+} \to D_{s}^{+}\gamma, \bar{K}^{0} \to K_{S}^{0}, D^{-} \to \pi^{0}K_{L}^{0}\pi^{-}, D_{s}^{+} \to \rho^{+}\eta, K_{S}^{0} \to \pi^{0}\pi^{0}, \rho^{+} \to \pi^{0}\pi^{+}, \eta \to \gamma\gamma$ $(\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}K_{L}^{0}\pi^{+}\pi^{-}K^{+}K^{-}\gamma^{F}\gamma\gamma\gamma)$ | 1429 | 2 | 126 |

| rowNo | decay tree (decay initial-final states) | iDcyTr | nEtr | nCEtr |
|-------|---|--------|------|-------|
| 59 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to X_{sd} \gamma, \bar{B}^0 \to D^{*+} D_s^- \gamma, X_{sd} \to \pi^- K^+, D^{*+} \to \pi^+ D^0, D_s^- \to K^* K^{*-}, D^0 \to \pi^0 \bar{K}_1^0, K^* \to \pi^- K^+, K^{*-} \to \pi^0 K^-, \bar{K}_1^0 \to \rho^+ K^-, \rho^+ \to \pi^0 \pi^+ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^+ K^- K^- \gamma \gamma)$ | 1432 | 2 | 128 |
| 60 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \pi^{-}K_{1}^{+}, \bar{B}^{0} \to D^{*+}\bar{\Lambda}\Xi^{-}, K_{1}^{+} \to \pi^{0}K^{*+}, D^{*+} \to D^{+}\gamma, \bar{\Lambda} \to \pi^{+}\bar{p},$ $\Xi^{-} \to \pi^{-}\Lambda, K^{*+} \to \pi^{0}K^{+}, D^{+} \to \pi^{0}\pi^{+}\pi^{+}\pi^{-}, \Lambda \to \pi^{0}n$ $(\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}K^{+}n\bar{p}\gamma)$ | 1494 | 2 | 130 |
| 61 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^- K^+ D^0 \bar{D}^{*0}, \bar{B}^0 \to \pi^0 D^0, D^0 \to \pi^+ K^-, \bar{D}^{*0} \to \bar{D}^0 \gamma, D^0 \to \pi^0 \pi^+ K^-, \bar{D}^{*0} \to K^+ a_1^-, a_1^- \to \pi^0 \rho^-, \rho^- \to \pi^0 \pi^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^+ K^- K^- \gamma) $ | 1517 | 2 | 132 |
| 62 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to D^- a_1^+, \bar{B}^0 \to K^{*-} D^+ \bar{D}^0, D^- \to \pi^- \pi^- K^+, a_1^+ \to \pi^0 \rho^+, K^{*-} \to \pi^0 K^-, D^+ \to \pi^+ \pi^+ K^-, \bar{D}^0 \to \pi^0 \pi^- K^+, \rho^+ \to \pi^0 \pi^+ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^+ K^- K^-)$ | 1581 | 2 | 134 |
| 63 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \rho^{0}\pi^{+}\pi^{-}\rho^{+}D^{-}, \bar{B}^{0} \to \bar{X}_{sd}\gamma, \rho^{0} \to \pi^{+}\pi^{-}, \rho^{+} \to \pi^{0}\pi^{+}, D^{-} \to e^{-}\bar{\nu}_{e}K^{*}, \\ \bar{X}_{sd} \to \pi^{+}K^{-}, K^{*} \to \pi^{-}K^{+} \\ (\Upsilon(4S) \dashrightarrow e^{-}\bar{\nu}_{e}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{-}\gamma)$ | 1596 | 2 | 136 |
| 64 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to D^{*-} a_1^+, \bar{B}^0 \to \pi^0 D^0, D^{*-} \to \pi^0 D^-, a_1^+ \to \pi^+ \pi^+ \pi^- \gamma^F, D^0 \to \pi^0 K^+ K^-, \\ D^- \to \mu^- \bar{\nu}_\mu K^0, K^0 \to K_L^0 \\ (\Upsilon(4S) \dashrightarrow \mu^- \bar{\nu}_\mu \pi^0 \pi^0 \pi^0 K_L^0 \pi^+ \pi^+ \pi^- K^+ K^- \gamma^F) \\ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 K^+ K^+ K^- K^- K^{*+} D^{*-}, \bar{B}^0 \to \rho^+ K^-, K^{*+} \to \pi^+ K^0, D^{*-} \to \pi^- \bar{D}^0, \rho^+ \to \pi^0 \pi^+ \gamma^F, $ | 1645 | 2 | 138 |
| 65 | $K^{0} \to K_{S}^{0}, \bar{D}^{0} \to \pi^{0}\pi^{0}\pi^{-}K^{+}, K_{S}^{0} \to \pi^{+}\pi^{-}$ $(\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{+}K^{-}K^{-}K^{-}\gamma^{F})$ | 1680 | 2 | 140 |
| 66 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^{*+} D^{*-} D^0, \bar{B}^0 \to \pi^0 D^0, K^{*+} \to \pi^0 K^+, D^{*-} \to \pi^0 D^-, D^0 \to \pi^0 \bar{K}^0, \\ D^0 \to \pi^0 \pi^+ K^-, D^- \to \pi^0 \pi^+ \pi^- K^-, \bar{K}^0_1 \to \pi^0 \bar{K}^*, \pi^0 \to e^+ e^- \gamma^F, \bar{K}^* \to \pi^+ K^- \\ (\Upsilon(4S) \dashrightarrow e^+ e^- \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- K^+ K^- K^- K^- \gamma^F) $ | 1718 | 2 | 142 |
| 67 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 K_2^{*0}, \bar{B}^0 \to D^{*+} \Delta^0 \bar{\Delta}^-, K_2^{*0} \to \pi^- K^+, D^{*+} \to \pi^0 D^+, \Delta^0 \to \pi^0 n, $ $ \bar{\Delta}^- \to \pi^0 \bar{p}, D^+ \to \pi^+ \pi^+ K^- $ $ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- K^+ K^- n \bar{p}) $ | 1723 | 2 | 144 |
| 68 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 K^* (1410)^0, \bar{B}^0 \to K^0 K^{*-} \phi D^{*+}, K^* (1410)^0 \to \pi^0 K^*, K^0 \to K_S^0, K^{*-} \to \pi^0 K^-, \\ \phi \to K^+ K^-, D^{*+} \to \pi^+ D^0, K^* \to \pi^- K^+, K_S^0 \to \pi^+ \pi^-, D^0 \to \rho^+ K^{*-}, \rho^+ \to \pi^0 \pi^+, \\ K^{*-} \to \pi^0 K^- \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^+ K^+ K^- K^-)$ | 1729 | 2 | 146 |
| 69 | $\Upsilon(4S) \to B^{0} \bar{B}^{0}, B^{0} \to \rho^{+} \rho^{+} \rho^{-} \eta D^{-}, \bar{B}^{0} \to \pi^{0} D^{0}, \rho^{+} \to \pi^{0} \pi^{+}, \rho^{+} \to \pi^{0} \pi^{+}, \rho^{-} \to \pi^{0} \pi^{-} \gamma^{F},$ $\eta \to \gamma \gamma, D^{-} \to \rho^{-} K^{*}, D^{0} \to \pi^{+} K^{-}, \rho^{-} \to \pi^{0} \pi^{-}, K^{*} \to \pi^{0} K^{0}, K^{0} \to K_{S}^{0},$ $K_{S}^{0} \to \pi^{+} \pi^{-}$ $(\Upsilon(4S) \dashrightarrow \pi^{0} \pi$ | 1764 | 2 | 148 |

| rowNo | decay tree (decay initial-final states) | iDcyTr | nEtr | nCEtr |
|-------|--|--------|------|-------|
| 70 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^0 \pi^+ \rho^- \bar{K}^0 K^+ D^{*-}, \bar{B}^0 \to \pi^0 D^0, \rho^0 \to \pi^+ \pi^-, \rho^- \to \pi^0 \pi^-, \bar{K}^0 \to K_L^0,$ $D^{*-} \to D^- \gamma, D^0 \to \pi^0 \pi^+ K^-, D^- \to \pi^0 \pi^- K^*, K^* \to \pi^- K^+$ $(\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 K_L^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- K^+ K^+ K^- \gamma)$ | 1825 | 2 | 150 |
| 71 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \rho^- K^+, \bar{B}^0 \to \rho^- D^{*+}, \rho^- \to \pi^0 \pi^-, \rho^- \to \pi^0 \pi^-, D^{*+} \to \pi^+ D^0, $ $ \pi^0 \to e^+ e^- \gamma^F, D^0 \to \pi^0 \pi^0 K_L^0 \pi^+ \pi^- $ $ (\Upsilon(4S) \dashrightarrow e^+ e^- \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 K_L^0 \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ \gamma^F) $ $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to D^{*-} \bar{\Delta}^- \Delta^{++}, \bar{B}^0 \to \rho^- D^{*+}, D^{*-} \to \pi^- \bar{D}^0, \bar{\Delta}^- \to \pi^0 \bar{p}, \Delta^{++} \to \pi^+ p, $ | 1850 | 2 | 152 |
| 72 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to D^{*-} \bar{\Delta}^- \Delta^{++}, \bar{B}^0 \to \rho^- D^{*+}, D^{*-} \to \pi^- \bar{D}^0, \bar{\Delta}^- \to \pi^0 \bar{p}, \Delta^{++} \to \pi^+ p,$ $\rho^- \to \pi^0 \pi^-, D^{*+} \to \pi^+ D^0, \bar{D}^0 \to K^+ a_1^-, D^0 \to \pi^+ K^-, a_1^- \to \pi^0 \rho^-, \rho^- \to \pi^0 \pi^-$ $(\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^- p \bar{p})$ | 1858 | 2 | 154 |
| 73 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \bar{D}^0, \bar{B}^0 \to \pi^- \eta K^* \bar{K}^* D^{*+}, \bar{D}^0 \to \pi^0 \pi^- K^+, \eta \to \pi^+ \pi^- \gamma^F, K^* \to \pi^0 K^0, \\ \bar{K}^* \to \pi^+ K^-, D^{*+} \to \pi^+ D^0, K^0 \to K^0_L, D^0 \to \pi^0 \pi^+ K^- \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 K^0_L \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^- K^- \gamma^F) $ | 1863 | 2 | 156 |
| 74 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \pi^{0}\bar{D}^{0}, \bar{B}^{0} \to \bar{K}^{0}\bar{K}^{0}D^{-}D_{s}^{*+}, \bar{D}^{0} \to \pi^{0}\pi^{-}K^{+}, \bar{K}^{0} \to K_{L}^{0}, \bar{K}^{0} \to K_{L}^{0}, K_{L}^{0} \to \pi^{0}\pi^{-}K_{S}^{0}, D_{s}^{*+} \to D_{s}^{+}\gamma, K_{L}^{0} \to \pi^{0}\pi^{0}\pi^{0}, K_{S}^{0} \to \pi^{+}\pi^{-}, D_{s}^{+} \to \bar{K}^{*}K^{*+}, \bar{K}^{*} \to \pi^{+}K^{-}, K^{*+} \to \pi^{+}K^{0}, K^{0} \to K_{L}^{0}$ $(\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}K_{L}^{0}K_{L}^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{-}\gamma)$ | 1875 | 2 | 158 |
| 75 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to K^{+}D^{*-}D^{*0}, \bar{B}^{0} \to \pi^{0}\bar{K}_{0}^{*0}, D^{*-} \to \pi^{0}D^{-}, D^{*0} \to D^{0}\gamma, \bar{K}_{0}^{*0} \to \pi^{+}K^{-}, D^{-} \to \pi^{-}\pi^{-}K^{+}, D^{0} \to \rho^{+}K^{*-}, \rho^{+} \to \pi^{0}\pi^{+}, K^{*-} \to \pi^{-}\bar{K}^{0}, \bar{K}^{0} \to K_{S}^{0}, K_{S}^{0} \to \pi^{+}\pi^{-}\gamma^{F}$ $(\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{+}K^{-}\gamma^{F}\gamma)$ | 1945 | 2 | 160 |
| 76 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \pi^0 \rho^0 \rho^+ \eta D^{*-}, \bar{B}^0 \to \rho^- D^{*+}, \rho^0 \to \pi^+ \pi^-, \rho^+ \to \pi^0 \pi^+, \eta \to \pi^0 \pi^+ \pi^-, \rho^{*-} \to \pi^- \bar{D}^0, \rho^- \to \pi^0 \pi^-, D^{*+} \to \pi^0 D^+, \bar{D}^0 \to \pi^0 \pi^- K^+, D^+ \to e^+ \nu_e \pi^+ K^- (\Upsilon(4S) \dashrightarrow e^+ \nu_e \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 1954 | 2 | 162 |
| 77 | $\Upsilon(4S) \to B^{0}B^{0}, B^{0} \to K^{+}D_{s}^{*-}, B^{0} \to K^{0}K^{0}\bar{K}^{0}D^{+}D^{-}, D_{s}^{*-} \to D_{s}^{-}\gamma, K^{0} \to K_{L}^{0}, K^{0} \to K_{S}^{0}, \bar{K}^{0} \to K_{L}^{0}, D^{+} \to e^{+}\nu_{e}\bar{K}^{0}, D^{-} \to \pi^{0}K_{L}^{0}\pi^{-}, D_{s}^{-} \to K_{S}^{0}K^{-}\gamma^{F}, K_{S}^{0} \to \pi^{+}\pi^{-}, K_{L}^{0} \to \mu^{+}\nu_{\mu}\pi^{-}\gamma^{F}, \bar{K}^{0} \to K_{S}^{0}, K_{S}^{0} \to \pi^{+}\pi^{-}, K_{S}^{0} \to \pi^{0}\pi^{0}$ $(\Upsilon(4S) \dashrightarrow e^{+}\nu_{e}\mu^{+}\nu_{\mu}\pi^{0}\pi^{0}\pi^{0}K_{L}^{0}K_{L}^{0}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{-}\gamma^{F}\gamma^{F}\gamma)$ | 1961 | 2 | 164 |
| 78 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \eta K_2^{*0}, \bar{B}^0 \to D_s^{*-} D_1^+, \eta \to \gamma \gamma, K_2^{*0} \to \pi^0 K^*, D_s^{*-} \to D_s^- \gamma, $ $D_1^+ \to \pi^+ D^{*0}, K^* \to \pi^- K^+, D_s^- \to \pi^- K^+ K^-, D^{*0} \to \pi^0 D^0, D^0 \to \rho^0 \bar{K}^*, \rho^0 \to \pi^+ \pi^-, $ $\bar{K}^* \to \pi^+ K^- $ $(\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^+ K^- K^- \gamma \gamma \gamma)$ | 1984 | 2 | 166 |
| 79 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^- K^* (1680)^+, \bar{B}^0 \to K^- D^+ \bar{D}^{*0}, K^* (1680)^+ \to \pi^0 K^+, D^+ \to K_L^0 K^{*+}, \bar{D}^{*0} \to \bar{D}^0 \gamma, K^{*+} \to \pi^+ K^0, \bar{D}^0 \to K^+ a_1^-, K^0 \to K_S^0, a_1^- \to \pi^+ \pi^- \pi^- \gamma^F, K_S^0 \to \pi^+ \pi^- (\Upsilon(4S) \dashrightarrow \pi^0 K_L^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^+ K^- K^- \gamma^F \gamma)$ | 2013 | 2 | 168 |
| 80 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^0 K^+ K^-, \bar{B}^0 \to \pi^0 \rho^0 \pi^- D^+, K^0 \to K_S^0, \rho^0 \to \pi^+ \pi^- \gamma^F, D^+ \to \pi^0 K_L^0 \pi^+, K_S^0 \to \pi^0 \pi^0 $ $(\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 K_L^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^- \gamma^F)$ | 2016 | 2 | 170 |

| rowNo | decay tree (decay initial-final states) | iDcyTr | nEtr | nCEtr |
|-------|---|--------|------|-------|
| 81 | $\Upsilon(4S) \to B^0 B^0, B^0 \to K^* \bar{K}^*, B^0 \to K^0 D^- D^{*+}, K^* \to \pi^- K^+, \bar{K}^* \to \pi^+ K^-, K^0 \to K_S^0, D^- \to \pi^0 \pi^+ \pi^- \pi^-, D^{*+} \to \pi^0 D^+, K_S^0 \to \pi^0 \pi^0, D^+ \to \pi^0 \pi^+ K_S^0, K_S^0 \to \pi^+ \pi^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- K^+ K^-)$ | 2023 | 2 | 172 |
| 82 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \rho^{0}\pi^{+}\pi^{+}\pi^{-}D^{*-}\gamma^{F}, \bar{B}^{0} \to \rho^{-}D^{+}, \rho^{0} \to \pi^{+}\pi^{-}\gamma^{F}, D^{*-} \to \pi^{-}\bar{D}^{0}, \rho^{-} \to \pi^{0}\pi^{-}, D^{+} \to \pi^{+}\pi^{+}K^{*-}, \bar{D}^{0} \to K^{+}a_{1}^{-}, K^{*-} \to \pi^{0}K^{-}, a_{1}^{-} \to \pi^{-}f_{0}(600), f_{0}(600) \to \pi^{+}\pi^{-} (\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{-}\gamma^{F}\gamma^{F})$ | 2027 | 2 | 174 |
| 83 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^0 K^+ K^-, \bar{B}^0 \to \pi^0 \rho^0 \pi^+ \pi^- \rho^- D^{*+}, K^0 \to K_S^0, \rho^0 \to \pi^+ \pi^- \gamma^F, \rho^- \to \pi^0 \pi^-, D^{*+} \to \pi^+ D^0, K_S^0 \to \pi^0 \pi^0, D^0 \to \pi^0 \pi^+ K^- (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^- K^- \gamma^F)$ | 2092 | 2 | 176 |
| 84 | $ \begin{array}{c} (\Upsilon(4S) - \to \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^- K^- \gamma^F) \\ \Upsilon(4S) B^0 \bar{B}^0, B^0 D^{*-} D^{*+}_{s0}, \bar{B}^0 \rho^- D^{*+}, D^{*-} \pi^- \bar{D}^0, D^{*+}_{s0} \pi^0 D^+_s, \rho^- \pi^0 \pi^-, \\ D^{*+} \pi^0 D^+, \bar{D}^0 \pi^0 \rho^- K^+, D^+_s e^+ \nu_e \eta \gamma^F, D^+ \pi^+ \pi^+ K^- \gamma^F, \rho^- \pi^0 \pi^-, \eta \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 2154 | 2 | 178 |
| 85 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \pi^0 \pi^0 \rho^+ \eta \bar{K}^0 K^* D^{*-}, \bar{B}^0 \to \pi^0 D^{*0}, \rho^+ \to \pi^0 \pi^+, \eta \to \pi^0 \pi^0, \bar{K}^0 \to K_S^0, K^* \to \pi^- K^+ \gamma^F, D^{*-} \to \pi^0 D^-, D^{*0} \to \pi^0 D^0, K_S^0 \to \pi^0 \pi^0, D^- \to \pi^- \pi^- K^+, D^0 \to \mu^+ \nu_\mu K^- (\Upsilon(4S) \dashrightarrow \mu^+ \nu_\mu \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 2177 | 2 | 180 |
| 86 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^0 K^+ K^- \gamma^F, \bar{B}^0 \to \pi^0 \pi^+ \pi^- \pi^- D^{*+}, K^0 \to K_S^0, D^{*+} \to \pi^+ D^0, K_S^0 \to \pi^+ \pi^-, D^0 \to \pi^0 \pi^0 K_S^0, K_S^0 \to \pi^0 \pi^0 (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- K^+ K^- \gamma^F)$ | 2180 | 2 | 182 |
| 87 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to K^{+}D^{*-}, \bar{B}^{0} \to \rho^{0}\pi^{-}\omega D^{+}n\bar{n}, D^{*-} \to \pi^{0}D^{-}, \rho^{0} \to \pi^{+}\pi^{-}, \omega \to \pi^{0}\pi^{+}\pi^{-}, D^{+} \to \pi^{0}\pi^{+}K_{S}^{0}, D^{-} \to \pi^{-}K_{S}^{0}, K_{S}^{0} \to \pi^{0}\pi^{0}, K_{S}^{0} \to \pi^{+}\pi^{-} $ $(\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}\pi^{-}K^{+}n\bar{n})$ $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \pi^{0}\pi^{-}\rho^{+}K^{0}\bar{K}^{0}K^{+}K^{-}, \bar{B}^{0} \to \pi^{-}D^{*+}, \rho^{+} \to \pi^{0}\pi^{+}, K^{0} \to K_{L}^{0}, \bar{K}^{0} \to K_{S}^{0},$ | 2187 | 2 | 184 |
| 88 | $D^{*+} \to \pi^{0}D^{+}, K_{S}^{0} \to \pi^{+}\pi^{-}, D^{+} \to \pi^{0}\pi^{+}K_{S}^{0}, K_{S}^{0} \to \pi^{+}\pi^{-} $ $(\Upsilon(4S) \dashrightarrow \pi^{0}\pi^{0}\pi^{0}\pi^{0}K_{L}^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{-})$ | 2205 | 2 | 186 |
| 89 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^* D_s^+ D_s^{*-}, \bar{B}^0 \to \pi^+ K^{*-}, K^* \to \pi^- K^+, D_s^+ \to K_S^0 K^+, D_s^{*-} \to D_s^- \gamma, K^{*-} \to \pi^0 K^-, K_S^0 \to \pi^+ \pi^-, D_s^- \to \rho^- \eta', \rho^- \to \pi^0 \pi^-, \eta' \to \pi^+ \pi^- \eta, \eta \to \pi^0 \pi^0 \pi^0 (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 2264 | 2 | 188 |
| 90 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^- K^{*+} \gamma \gamma, \bar{B}^0 \to K^- D^{*+} \bar{D}^{*0}, \rho^- \to \pi^0 \pi^-, K^{*+} \to \pi^0 K^+, D^{*+} \to \pi^+ D^0, \\ \bar{D}^{*0} \to \pi^0 \bar{D}^0, D^0 \to \pi^0 \pi^0 K^0_S, \bar{D}^0 \to K^+ K^{*-}, K^0_S \to \pi^+ \pi^-, K^{*-} \to \pi^0 K^- \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^+ K^- K^- \gamma \gamma)$ | 2290 | 2 | 190 |
| 91 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to D^{*-} D_{s1}^{\prime+}, \bar{B}^0 \to \pi^- D^+ \gamma^F, D^{*-} \to \pi^- \bar{D}^0, D_{s1}^{\prime+} \to \pi^0 D_s^{*+}, D^+ \to \pi^0 \pi^0 \pi^+, \\ \bar{D}^0 \to \pi^0 \pi^0 K_S^0, D_s^{*+} \to D_s^+ \gamma, K_S^0 \to \pi^0 \pi^0, D_s^+ \to \bar{K}^0 K^{*+}, \bar{K}^0 \to K_L^0, K^{*+} \to \pi^0 K^+, \\ K_L^0 \to \pi^0 \pi^0 \pi^0 \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0$ | 2328 | 2 | 192 |

| rowNo | decay tree (decay initial-final states) | iDcyTr | nEtr | nCEtr |
|-------|---|--------|------|-------|
| 92 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^+ D^-, \bar{B}^0 \to D^{*+} D'_{s1}^-, \rho^+ \to \pi^0 \pi^+, D^- \to \pi^- \pi^- K^+, D^{*+} \to \pi^+ D^0,$ $D'_{s1}^- \to D_s^- \gamma, D^0 \to K^* \bar{K}^*, D_s^- \to \pi^- \eta', K^* \to \pi^- K^+, \bar{K}^* \to \pi^+ K^-, \eta' \to \pi^+ \pi^- \eta,$ $\eta \to \pi^0 \pi^+ \pi^-$ $(\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- \pi^- \pi^- K^+ K^+ K^- \gamma)$ | 2329 | 2 | 194 |
| 93 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to K^0 K^+ K_0^{*-}, \bar{B}^0 \to \rho^- D_1'^+, K^0 \to K_S^0, K_0^{*-} \to \pi^0 K^-, \rho^- \to \pi^0 \pi^-, D_1'^+ \to \pi^+ D^{*0}, K_S^0 \to \pi^+ \pi^-, D^{*0} \to \pi^0 D^0, D^0 \to \pi^+ \eta K^-, \eta \to \gamma \gamma$ $(\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^+ K^- K^- \gamma \gamma)$ | 2361 | 2 | 196 |
| 94 | $ \Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \rho^0 \pi^+ \eta K^+ K^- D^-, \bar{B}^0 \to \pi^0 D^{*0}, \rho^0 \to \pi^+ \pi^- \gamma^F, \eta \to \gamma \gamma, D^- \to \pi^- K_S^0, \\ D^{*0} \to \pi^0 D^0, K_S^0 \to \pi^0 \pi^0, D^0 \to \pi^+ K^- \\ (\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^+ K^- K^- \gamma^F \gamma \gamma) $ | 2372 | 2 | 198 |
| 95 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^+ D^-, \bar{B}^0 \to \bar{K}^* D^- D^{*+}, \rho^+ \to \pi^0 \pi^+, D^- \to \pi^- \pi^- K^+, \bar{K}^* \to \pi^+ K^-, D^- \to e^- \bar{\nu}_e K^0, D^{*+} \to \pi^+ D^0, K^0 \to K^0_L, D^0 \to \pi^0 \pi^+ K^- (\Upsilon(4S) \dashrightarrow e^- \bar{\nu}_e \pi^0 \pi^0 K^0_L \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^+ K^- K^-)$ | 2374 | 2 | 200 |
| 96 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \pi^0 \bar{D}^0, \bar{B}^0 \to K^- D^{*+} \bar{D}^{*0}, \bar{D}^0 \to \pi^+ \pi^- \pi^- K^+, D^{*+} \to \pi^+ D^0, \bar{D}^{*0} \to \bar{D}^0 \gamma,$ $D^0 \to \pi^+ K^-, \bar{D}^0 \to \omega K^*, \omega \to \pi^0 \pi^+ \pi^-, K^* \to \pi^- K^+$ $(\Upsilon(4S) \dashrightarrow \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- K^+ K^+ K^- K^- \gamma)$ | 2381 | 2 | 202 |
| 97 | $\Upsilon(4S) \to B^{0} \bar{B}^{0}, B^{0} \to \rho^{0} \rho^{0} \pi^{+} \omega D^{-}, \bar{B}^{0} \to \rho^{-} D^{*+} \gamma, \rho^{0} \to \pi^{+} \pi^{-}, \rho^{0} \to \pi^{+} \pi^{-}, \omega \to \pi^{0} \pi^{0}, \omega \to \pi^{0$ | 2428 | 2 | 204 |
| 98 | $\Upsilon(4S) \to B^0 \bar{B}^0, B^0 \to \rho^+ D^{*-}, \bar{B}^0 \to e^- \bar{\nu}_e D^{*+}, \rho^+ \to \pi^0 \pi^+, D^{*-} \to \pi^- \bar{D}^0, D^{*+} \to \pi^+ D^0,$ $\bar{D}^0 \to \pi^- K^+, D^0 \to \pi^0 \pi^+ K^-$ $(\Upsilon(4S) \dashrightarrow e^- \bar{\nu}_e \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^+ K^-)$ | 2439 | 2 | 206 |
| 99 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \pi^{0}\rho^{+}\eta D^{-}, \bar{B}^{0} \to \pi^{0}D^{0}, \rho^{+} \to \pi^{0}\pi^{+}, \eta \to \pi^{0}\pi^{0}\pi^{0}, D^{-} \to \pi^{-}\pi^{-}K_{S}^{0}K^{+}, D^{0} \to e^{+}\nu_{e}K^{-}\gamma^{F}\gamma^{F}, K_{S}^{0} \to \pi^{0}\pi^{0} (\Upsilon(4S) \dashrightarrow e^{+}\nu_{e}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0}\pi^{0$ | 2465 | 2 | 208 |
| 100 | $\Upsilon(4S) \to B^{0}\bar{B}^{0}, B^{0} \to \rho^{+}\eta D^{*-}, \bar{B}^{0} \to K^{-}D^{+}, \rho^{+} \to \pi^{0}\pi^{+}, \eta \to \gamma\gamma, D^{*-} \to \pi^{-}\bar{D}^{0},$ $D^{+} \to \pi^{0}K_{L}^{0}\pi^{+}, \bar{D}^{0} \to \pi^{-}K^{+}\eta', K_{L}^{0} \to e^{-}\nu_{e}\pi^{+}\gamma^{F}\gamma^{F}, \eta' \to \pi^{+}\pi^{-}\eta, \eta \to \gamma\gamma$ $(\Upsilon(4S) \dashrightarrow e^{-}\nu_{e}\pi^{0}\pi^{0}\pi^{+}\pi^{+}\pi^{+}\pi^{+}\pi^{-}\pi^{-}\pi^{-}K^{+}K^{-}\gamma^{F}\gamma^{F}\gamma\gamma\gamma\gamma)$ | 2489 | 2 | 210 |
| rest | $\Upsilon(4S) \to \text{others (3413 in total)}$ ($\Upsilon(4S) \dashrightarrow \text{corresponding to others)}$ | | 3443 | 3653 |

Table 2: Decay branches of B^0 .

| rowNo | decay branch of ${\cal B}^0$ | iDcyBrP | nCase | nCCase |
|-------|--|---------|-------|--------|
| 1 | $B^0 \to \pi^0 \bar{D}^0$ | 3 | 238 | 238 |
| 2 | $B^0 \to \rho^+ D^-$ | 26 | 220 | 458 |
| 3 | $B^0 \to \rho^+ D^{*-}$ | 15 | 196 | 654 |
| 4 | $B^0 \to \pi^0 \bar{D}^{*0}$ | 11 | 154 | 808 |
| 5 | $B^0 \to K^0 K^+ K^-$ | 2 | 96 | 904 |
| 6 | $B^0 \to \pi^0 K^+ K^-$ | 25 | 87 | 991 |
| 7 | $B^0 \to K^- K_0^{*+}$ | 40 | 61 | 1052 |
| 8 | $B^0 \to \pi^0 \pi^+ D^{*-}$ | 5 | 59 | 1111 |
| 9 | $B^0 \to K^+ D^{*-} D^{*0}$ | 20 | 45 | 1156 |
| 10 | $B^0 \to K^- K^{*+}$ | 77 | 44 | 1200 |
| 11 | $B^0 \to D^{*-}D_{s0}^{*+}$ | 7 | 42 | 1242 |
| 12 | $B^0 \to D^{*-}D_s^{*+}$ | 8 | 40 | 1282 |
| 13 | $B^0 \to K^+ D^-$ | 107 | 40 | 1322 |
| 14 | $B^0 \to \pi^0 K^* (1410)^0$ | 31 | 32 | 1354 |
| 15 | $B^0 \to \pi^- K_0^{*+}$ | 48 | 28 | 1382 |
| 16 | $B^0 \to D^{*-} D_{s1}^{\prime+}$ | 1 | 28 | 1410 |
| 17 | $B^0 \to X_{sd} \gamma$ | 65 | 26 | 1436 |
| 18 | $B^0 \to \pi^0 \pi^+ \pi^+ \pi^- D^{*-}$ | 124 | 26 | 1462 |
| 19 | $B^0 \to \mu^+ \nu_\mu D^{*-}$ | 69 | 24 | 1486 |
| 20 | $B^0 \to \rho^- K^+$ | 101 | 24 | 1510 |
| 21 | $B^0 \to K^+ D^- D^{*0}$ | 103 | 24 | 1534 |
| 22 | $B^0 \to K^+ D^{*-}$ | 184 | 24 | 1558 |
| 23 | $B^0 \to D^{*-} a_1^+$ | 49 | 23 | 1581 |
| 24 | $B^0 \to \tau^+ \nu_\tau D^{*-}$ | 83 | 23 | 1604 |
| 25 | $B^0 \to e^+ \nu_e D^{*-}$ | 30 | 22 | 1626 |
| 26 | $B^0 \to D^- D_s^+$ | 113 | 22 | 1648 |
| 27 | $B^0 	o \pi^+ D^-$ | 18 | 19 | 1667 |
| 28 | $B^0 \to \pi^0 f_0(980)$ | 84 | 19 | 1686 |
| 29 | $B^0 \to K^+ a_1^-$ | 292 | 19 | 1705 |
| 30 | $B^0 \to \pi^0 K^+ K^- \gamma^F$ | 95 | 18 | 1723 |
| 31 | $B^0 \to \rho^+ D^- \gamma$ | 157 | 17 | 1740 |
| 32 | $B^0 \to K^0 D^{*+} D^{*-}$ | 32 | 16 | 1756 |
| 33 | $B^0 \to D^- D_s^{*+}$ | 23 | 15 | 1771 |

| rowNo | decay branch of B^0 | iDcyBrP | nCase | nCCase |
|-------|--|---------|-------|--------|
| 34 | $B^0 \to \pi^0 \pi^- K^+$ | 52 | 15 | 1786 |
| 35 | $B^0 \to D^- D_{s0}^{*+}$ | 41 | 15 | 1801 |
| 36 | $B^0 \to \rho^+ D^{*-} \gamma$ | 17 | 15 | 1816 |
| 37 | $B^0 \to K^0 K^+ K^- \gamma^F$ | 126 | 15 | 1831 |
| 38 | $B^0 \to \pi^+ D^{*-}$ | 127 | 15 | 1846 |
| 39 | $B^0 \to D^{*-}D_s^+$ | 44 | 14 | 1860 |
| 40 | $B^0 \to \pi^0 \rho^- K^+$ | 66 | 13 | 1873 |
| 41 | $B^0 \to f_2(1270)K^*$ | 46 | 12 | 1885 |
| 42 | $B^0 \to K^{*+}D^{*-}D^{*0}$ | 144 | 12 | 1897 |
| 43 | $B^0 \to K^0 D^- D^{*+}$ | 346 | 12 | 1909 |
| 44 | $B^0 \to K^* \gamma$ | 35 | 11 | 1920 |
| 45 | $B^0 \to K^{*+} D^{*-} D^0$ | 99 | 11 | 1931 |
| 46 | $B^0 \to \rho^- K_0^{*+}$ | 154 | 11 | 1942 |
| 47 | $B^0 \to \pi^0 \pi^0 \bar{D}^0$ | 457 | 11 | 1953 |
| 48 | $B^0 \to D_2^{*-} D_s^{*+}$ | 511 | 11 | 1964 |
| 49 | $B^0 \to \pi^+ \pi^+ \pi^+ \pi^- \pi^- D^{*-}$ | 42 | 10 | 1974 |
| 50 | $B^0 \to D^- a_1^+$ | 116 | 10 | 1984 |
| 51 | $B^0 \to \pi^0 K^*$ | 130 | 10 | 1994 |
| 52 | $B^0 \to K^+ D_s^-$ | 138 | 10 | 2004 |
| 53 | $B^0 \to D_2^{*-} D_s^+$ | 226 | 10 | 2014 |
| 54 | $B^0 \to e^+ \nu_e D^{*-} \gamma^F$ | 304 | 10 | 2024 |
| 55 | $B^0 \to K^* D^{*+} D^{*-}$ | 96 | 9 | 2033 |
| 56 | $B^0	o\pi^0a_0^0$ | 64 | 9 | 2042 |
| 57 | $B^0 \to \pi^- \bar{D}^0 D_s^{*+}$ | 219 | 9 | 2051 |
| 58 | $B^0 	o \mu^+ \nu_\mu D^-$ | 297 | 9 | 2060 |
| 59 | $B^0 \to D^- D_{s1}^{\prime +}$ | 355 | 9 | 2069 |
| 60 | $B^0 \to \rho^- K^{*+}$ | 461 | 9 | 2078 |
| 61 | $B^0 \to \bar{K}^0 K^+ D^-$ | 108 | 8 | 2086 |
| 62 | $B^0 \to \rho^+ D_2^{*-}$ | 181 | 8 | 2094 |
| 63 | $B^0 \to K^- K^* (1680)^+$ | 267 | 8 | 2102 |
| 64 | $B^0 \to K^- K_0^{*+} \gamma^F$ | 269 | 8 | 2110 |
| 65 | $B^0 \to e^+ \nu_e D^-$ | 311 | 8 | 2118 |
| 66 | $B^0 \to K^*K^+K^-$ | 333 | 8 | 2126 |
| 67 | $B^0 \to \pi^0 \phi$ | 51 | 7 | 2133 |
| 68 | $B^0 \to \pi^- K_0^{*+} \gamma^F$ | 27 | 7 | 2140 |

| rowNo | decay branch of B^0 | iDcyBrP | nCase | nCCase |
|-------|---|---------|-------|--------|
| 69 | $B^0 \to \bar{K}^0 K^+ D^{*-}$ | 178 | 7 | 2147 |
| 70 | $B^0 \to \pi^0 \pi^0 \pi^- K^+$ | 229 | 7 | 2154 |
| 71 | $B^0 \to \pi^0 K_2^{*0}$ | 281 | 7 | 2161 |
| 72 | $B^0 \to K^* D^+ D^{*-}$ | 91 | 6 | 2167 |
| 73 | $B^0 \to \pi^- K^{*+}$ | 94 | 6 | 2173 |
| 74 | $B^0 \to \pi^0 \pi^0 K^+ K^-$ | 67 | 6 | 2179 |
| 75 | $B^0 \to \pi^+ \pi^- \rho^+ D^{*-}$ | 73 | 6 | 2185 |
| 76 | $B^0 \to \pi^- K^* (1410)^+$ | 75 | 6 | 2191 |
| 77 | $B^0 	o K^* \eta_c(2S)$ | 105 | 6 | 2197 |
| 78 | $B^0 	o \pi^0 \pi^0 ar{D}^{*0}$ | 160 | 6 | 2203 |
| 79 | $B^0 \to K^* f_0(980)$ | 167 | 6 | 2209 |
| 80 | $B^0 	o ho^- K^+ \gamma^F$ | 228 | 6 | 2215 |
| 81 | $B^0 \to e^+ \nu_e D_1^{\prime -}$ | 409 | 6 | 2221 |
| 82 | $B^0 \to \mu^+ \nu_\mu D^- \gamma^F$ | 92 | 5 | 2226 |
| 83 | $B^0 \to K^0 D^{*0} \bar{D}^{*0}$ | 81 | 5 | 2231 |
| 84 | $B^0 \to \rho^+ \eta D^{*-}$ | 55 | 5 | 2236 |
| 85 | $B^0 \to \mu^+ \nu_\mu D_1^-$ | 14 | 5 | 2241 |
| 86 | $B^0 \to e^+ \nu_e D_0^{*-} \gamma^F$ | 24 | 5 | 2246 |
| 87 | $B^0 	o 	au^+ u_	au D^-$ | 119 | 5 | 2251 |
| 88 | $B^0 \to \pi^0 \pi^- \bar{D}^0 D_s^{*+}$ | 129 | 5 | 2256 |
| 89 | $B^0 \to \pi^0 \pi^+ \eta D^{*-}$ | 188 | 5 | 2261 |
| 90 | $B^0 \to \pi^0 \rho^+ \eta D^-$ | 189 | 5 | 2266 |
| 91 | $B^0 	o \pi^0 \pi^+ \omega D^-$ | 220 | 5 | 2271 |
| 92 | $B^0 \to \pi^0 \pi^+ D^{*-} \gamma^F$ | 223 | 5 | 2276 |
| 93 | $B^0 \to \pi^- \bar{D}^0 D_s^+$ | 231 | 5 | 2281 |
| 94 | $B^0 \to \tau^+ \nu_\tau D_2^{*-}$ | 265 | 5 | 2286 |
| 95 | $B^0 \to D^{*-} D_{s1}^+$ | 291 | 5 | 2291 |
| 96 | $B^0 	o \pi^+ \omega D^-$ | 378 | 5 | 2296 |
| 97 | $B^0 \to \pi^0 \pi^+ \pi^- \rho^+ D^{*-}$ | 384 | 5 | 2301 |
| 98 | $B^0 \to D_s^{*+} D_1^{\prime-}$ | 394 | 5 | 2306 |
| 99 | $B^0 	o ho^+ \eta D^-$ | 406 | 5 | 2311 |
| 100 | $B^0 \to K^* D^+ D^-$ | 431 | 5 | 2316 |
| rest | $B^0 \to \text{others (938 in total)}$ | | 1317 | 3633 |

Table 3: Cascade decay branches of B^0 (only the first ten hierarchies are involved).

| rowNo | cascade decay branch of ${\cal B}^0$ | iCascDcyBrP | nCase | nCCase |
|-----------------------|--|-------------|-------|--------|
| 1 | $B^0 \to \rho^+ D^-, \rho^+ \to \pi^0 \pi^+, D^- \to \pi^- \pi^- K^+$ | 27 | 105 | 105 |
| 2 | $B^0 	o \pi^0 K^+ K^-$ | 26 | 87 | 192 |
| 3 | $B^0 \to \pi^0 \bar{D}^0, \bar{D}^0 \to \pi^0 \pi^- K^+$ | 3 | 84 | 276 |
| 4 | $B^0 \to \rho^+ D^{*-}, \rho^+ \to \pi^0 \pi^+, D^{*-} \to \pi^- \bar{D}^0, \bar{D}^0 \to \pi^- K^+$ | 15 | 78 | 354 |
| 5 | $B^0 \to K^0 K^+ K^-, K^0 \to K^0_S, K^0_S \to \pi^0 \pi^0$ | 35 | 64 | 418 |
| 6 | $B^0 \to K^- K_0^{*+}, K_0^{*+} \to \pi^0 K^+$ | 46 | 57 | 475 |
| 7 | $B^0 \to K^- K^{*+}, K^{*+} \to \pi^0 K^+$ | 100 | 43 | 518 |
| 8 | $B^0 \to \pi^0 \bar{D}^0, \bar{D}^0 \to \pi^- K^+$ | 135 | 41 | 559 |
| 9 | $B^0 \to \rho^+ D^{*-}, \rho^+ \to \pi^0 \pi^+, D^{*-} \to \pi^- \bar{D}^0, \bar{D}^0 \to \pi^0 \pi^- K^+$ | 101 | 30 | 589 |
| 10 | $B^0 \to \pi^- K_0^{*+}, K_0^{*+} \to \pi^0 K^+$ | 58 | 28 | 617 |
| rest | $B^0 \to \text{others (2163 in total)}$ | _ | 3016 | 3633 |