

A Travel model notes

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A.1 Traffic model overview

A.1.1 Setup

The traffic model studied in this document was developed by Mahalia Miller during her doctoral work at Stanford. It implements an incremental traffic assignment on a graph of the San Francisco Bay Area road network, which is modeled as including $B = 1743$ bridges owned and managed by the California Department of Transportation (Caltrans). The graph of the road network, denoted G , is configured such that the edge attributes are hourly values – e.g. an edge’s capacity is the number of vehicles that can pass over it in an hour. Thus, any demand assigned to the network should also be in hourly values. The demand already included in the traffic model must be scaled (i.e., multiplied by a factor less than 1) to convert daily demand to hourly demand [87, 56]. The incremental traffic assignment method approximates the user equilibrium (UE) method; some researchers find that it produces a good approximation, while others disagree – see Patriksson for a full discussion [66].

A.1.2 Bugs

I have identified four errors in the original implementation of the traffic assignment algorithm and traffic model – they are described in detail in Section A.4. In brief, they are:

- Inconsistent order of iteration over origins and destinations when assigning traffic, which leads to different network performance results for the same damage maps. For example, the no-damage network performance metrics can vary by at least an order of magnitude depending on the order in which we assign traffic to the road network.
- Incorrect travel time computation – when trips were added to edges in the original implementation, the new travel time over that edge was computed as the travel time due to only the additional trips rather than to all trips on the edge. This would lead to smaller travel times over edges, which could distort the results of the traffic assignment algorithm since shortest paths are found based on edge travel times.
- Incorrect trip assignment – if a trip between a particular origin and destination cannot be made, it’s the result of a zero-capacity edge somewhere in the shortest path between the origin and destination. In the original implementation, the flow between the origin and destination would be assigned to all edges in the shortest path even if the trip between the origin and destination could not be made because of a zero-capacity edge in the shortest path. This increased the total travel time over the network by an order of magnitude.
- Incorrect graph edge weights – in the original graph of the road network, the traversal times t_a of edges with zero capacity were also 0. This meant that these edges were selected as part of shortest paths between origins and destinations but that trips couldn’t actually be assigned to them, resulting in false connectivity losses.

A.2 Needs

My research focuses on developing methods to identify which bridges in the road network to retrofit such that the performance of the network is optimized, in terms of total travel time, trips made, vehicle miles travelled, or some function of those metrics. We retrofit bridges because doing so reduces the probability that they will sustain damage during an earthquake, and because we assume that the road network functions better when bridges are not damaged. Better functionality or performance is defined as smaller travel times, larger numbers of trips made, and fewer vehicle miles travelled. The methods I am developing are built on those assumptions – therefore, the models I use to implement and demonstrate the value of the methods I’m developing should also reflect those assumptions. The traffic model has caused some concern in the past because there have been specific cases in which it appears to violate those assumptions. Even having fixed the bugs identified in Section [A.1.2](#), I find cases in which these assumptions are violated.

- The performance of the network when not damaged should be consistent – that is, the values of the no-damage total travel time, trips made, and vehicle miles travelled should be constant. **Status: Met.**
- When the network is not damaged, the metrics reflecting its performance – travel time, vehicle miles travelled, and the number of trips made – should be no worse than metrics that reflect the performance of a damaged network. Ideally, the metrics reflecting the performance of the undamaged network should indicate better performance than those of a damaged network. **Status: Complicated.** There are cases in which bridges are damaged and one or two of the three network performance metrics improves (e.g. travel time decreases, trips made increases). See the next item for more detailed explanation.

Damaged bridges	Δ Travel time (s)	Δ Vehicle miles	Δ Trips made
<i>none</i>	2.978×10^{13}	3.505×10^7	7.628×10^6
966	-2.294×10^{12}	3.553×10^7	3.022×10^3
917, 972	4.725×10^{12}	3.474×10^7	1.623×10^3

Table 14: Changes in network performance metrics when bridges are damaged. Δ = current condition - no-damage condition. Positive values indicate an increase, while negative values indicate a decrease.

- The network should function no worse with a particular bridge than without it – that is, the network’s performance should not improve when a bridge is damaged relative to when that bridge is undamaged. **Status: Complicated.** There are three metrics that we can track using the travel model: the total travel time, trips made, and vehicle miles travelled. None of these are guaranteed to get worse – that is, reflect network performance worse than the no-damage performance – when bridges are damaged. Consider the cases shown in Table 14, in both cases when bridges are damaged, the number of trips made on the network increases, which taken by itself would suggest improved network performance. When bridge 966 is damaged, more trips are made (an improvement) and the total travel time decreases (an improvement). A cost model that only took into account these two metrics would indicate that damaging bridge 966 improves the performance of the network. However, the vehicle miles travelled more than double when bridge 966 is damaged, indicating that the trips that do get made are more circuitous as a result of the bridge damage, though they are made more quickly. When bridges 917 and 972 are both damaged, the number of trips made increases (an improvement), the travel time increases (a deterioration), and the vehicle miles travelled increase (a deterioration). These sample cases suggest that implementing a cost model to go along with this traffic model must be done with *extreme* care. It is not enough to consider only the number of trips made and the total travel time to get a full picture of the how the network performance changes. Possible solutions include (1) considering all three network performance metrics when computing the cost of the network performance or (2) encoding the assumptions that bridge damage will lead to worse network performance in the cost model itself, e.g. if bridges are damaged, impose a cost per bridge.

A.3 Counter-intuitive results

Despite all the bugs fixed, the traffic model still produces counter-intuitive results. I conducted a one-at-a-time analysis of all 1743 bridges included in the model to see in how many cases the road network performance appeared to improve when a single bridge in the network was damaged. This OAT analysis was conducted using the procedure detailed in Section A.3.1. I considered reduced travel time (TT) an improvement. In 138 (8%) of 1743 cases, the travel time on the damaged network was less than that on the undamaged network. A few of these are listed in Table 15.

This raises two questions:

- Why does damage to the network apparently improve its performance?
- Does the improvement in performance happen the same way in each of these counterintuitive cases?

I looked in depth at one of these cases in which bridge 277 was damaged. The decrease in travel time when bridge 277 is damaged relative to the undamaged network is 8.05×10^6 . The largest change occurs on edge (4812, 4884), which experiences a decrease in travel time (edge $t_a \times$ edge flow) of 8.439×10^6 (see Figure 20 for bridge 277 as well as Figures 21, 22). Edge (4812, 4884) is not affected by damage to bridge 277. I got lists of the (O,D) pairs on whose path edge (4812, 4884) appears when bridge 277 is damaged and when it is not damaged. The only difference between these two lists is that when bridge 277 is damaged, edge (4812, 4884) is not on the path from Supernode 13 to Supernode 12 during the first of the four iterations in the traffic assignment algorithm – this results in a decrease in flow and therefore in travel time. This is not an error, however – I verified that the path chosen instead from Supernode 13 to Supernode 12 is indeed the shortest path based on the edge weights of the links included.

In Miller’s original implementation – i.e. without any of the fixes described in this document – this problem occurs too. When I conducted the same OAT analysis on a random set of 712 bridges, counter-intuitive results occurred in 54 (8%) of cases – roughly the same rate at which these results occurred in the OAT analysis with the completely fixed traffic model. This combined with the results of the model with all fixes included leads me to believe that it is the traffic assignment algorithm itself that allows for such counter-intuitive results to occur rather than a simple bug in the code. The size of the road network and the number of origin-destination pairs makes it difficult to demonstrate how these strange results might occur. Therefore, I have included at the end of this section a simple case study (see Figures 23 through 25) in which damage to a network results in improved network performance.

Patriksson notes that the results of traffic assignments made in an incremental fashion, as in this model, are sensitive to:

- order of iteration over origin-destination pairs
- the number of iterations, K
- the choice of increments (e.g., 40%, 30%, 20% and 10%)
- changes in traversal time t_a on an edge, which can lead to large changes in flows and therefore in network performance metrics

Based on this list, I decided to see whether a simple change in the number of iterations or the choice of increments could obviate the counter-intuitive results in Table 15. I tried the following changes to

damaged bridge	TT, $\times 10^8$	trips?	mechanism of change
none	4.2663	576547.674	none
277	4.1859	"	edge (4812, 4884)
107	4.2069	"	edge (4812, 4884)
278	4.1984	"	edge (4812, 4884)
279	4.2053	"	edge (4812, 4884)
93	4.2480	"	three edges
556	4.2635	"	edge (4717, 4627)
1197	4.2641	"	edge (2708, 2710)
686	4.2659	"	five edges
372	4.2440	"	two edges (4717, 4627), (4492, 5028)

Table 15: A selection of counter-intuitive results from the traffic model.

the traffic assignment procedure detailed in Section A.3.1 and checked each of the bridge damage cases listed in Table 15 to see whether the results were still counter-intuitive. These strategies did not resolve the counter-intuitive results in Table 15. Even if they had, there is no guarantee that they would have addressed all possible cases in which counter-intuitive results could occur.

- reversing the order of iteration over origin-destination pairs. (It's not feasible to test all orders of the O-D pairs to find one that gives expected results under all damage conditions, if such an order even exists.)
- Trying the following sets of increments and demand proportions:
 - $K = 4$, 40/30/20/10%
 - $K = 4$, 25/25/25/25%
 - $K = 10$, equal increments of 10%
 - $K = 20$, equal increments of 5%
 - $K = 20$, 5 increments of 8%, 5 of 6%, 5 of 4%, 5 of 2%
- Choosing the shortest path based on $t_a \times$ edge flow rather than just based on t_a .

A.3.1 Modeling Procedure

1. Iterate over origin-destination pairs in a fixed order (i.e., the order of origins and destinations remains the same between iterations and between runs of the traffic assignment algorithm over different graphs).
2. Compute the traversal time t_a of an edge based on its flow-to-capacity ratio (denoted q and c , respectively) using the equation from the Bureau of Public roads with $\alpha = 0.15$ and $\beta = 4$.

$$t_a = t_0(1 + \alpha(\frac{q}{c})^\beta) \quad (57)$$

3. Scale the daily demand to reflect the average demand over a 1-hour period during the morning (6 am to 10 am). This is necessary because edge capacities are hourly.

4. Set the initial conditions of the graph as follows:
 - (a) Use `correct_graph()`, which will make the following adjustments to the graph:
 - if edge capacity is 0, set edge $t_0 = t_a = \infty$
 - if edge length is 0, set edge capacity to 0, set edge $t_0 = t_a = \infty$
 - (b) Use `prune_graph()` as a precaution, which will make the following adjustments to the graph:
 - if edge length is 0, remove edge
 - if edge capacity is 0, remove edge
5. Damaging the links in the graph entails setting the affected edge's capacities to 0, $t_0 = t_a = \infty$, and edge length to 20 times its original value. Then use `prune_graph()` again to remove the affected edges.
6. Assign traffic incrementally over $K = 4$ iterations, in proportions of 40%, 30%, 20% and 10% of the hourly demand between origin and destination. Trips are assigned to the shortest path (based on t_a) between the origin and destination under the following assumptions:
 - All trips from an origin to a destination in a particular increment (i.e., for a particular k) go on the same route.
 - Drivers can check road conditions prior to departure, so that if there is no path between the origin and destination, they will not leave the origin, so no flow is added to the road network when trips can't be made.

Note that Miller recommends the sizes of the increments and references Wang, Guan, and Wang. In their supplementary information, Wang, Guan, and Wang say that these are "standard values" and reference the user's guide to TransCAD, a proprietary software from Caliper. I have not been able to get a copy of the user's guide and thus haven't been able to verify that reference.

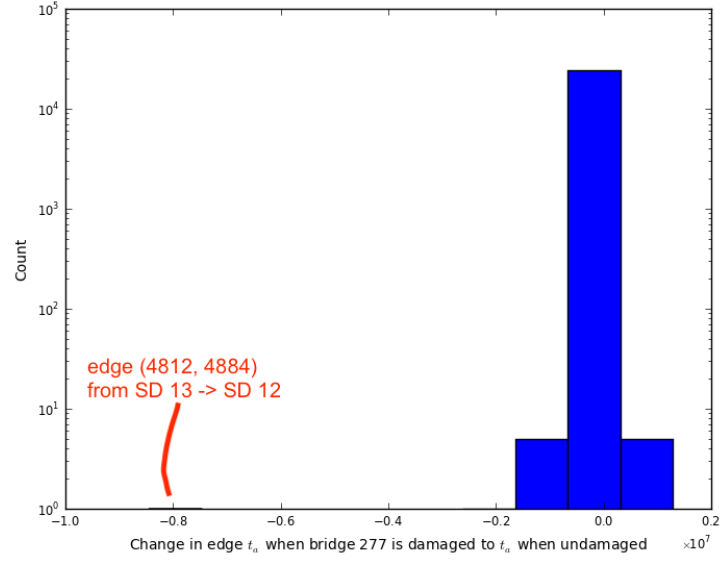


Figure 20: Histogram of changes in travel time ($t_a \times \text{flow}$) for each edge when bridge 277 is damaged vs. when there is no damage.

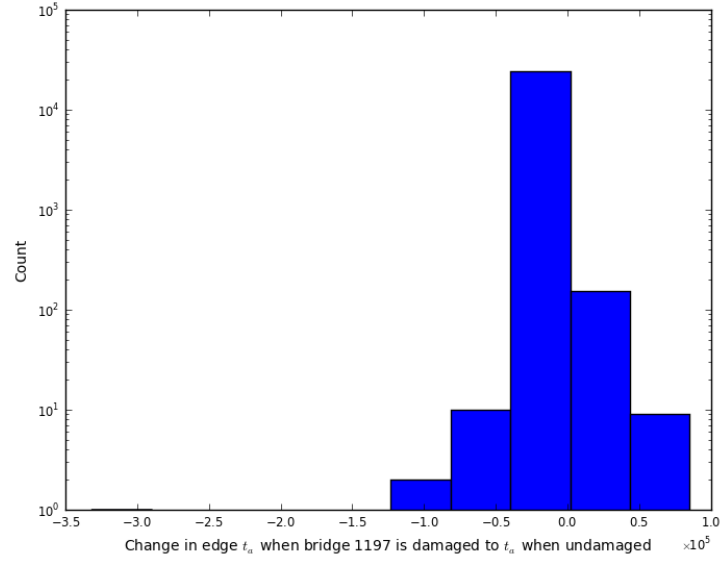


Figure 21: Histogram of changes in travel time ($t_a \times \text{flow}$) for each edge when bridge 1197 is damaged vs. when there is no damage.

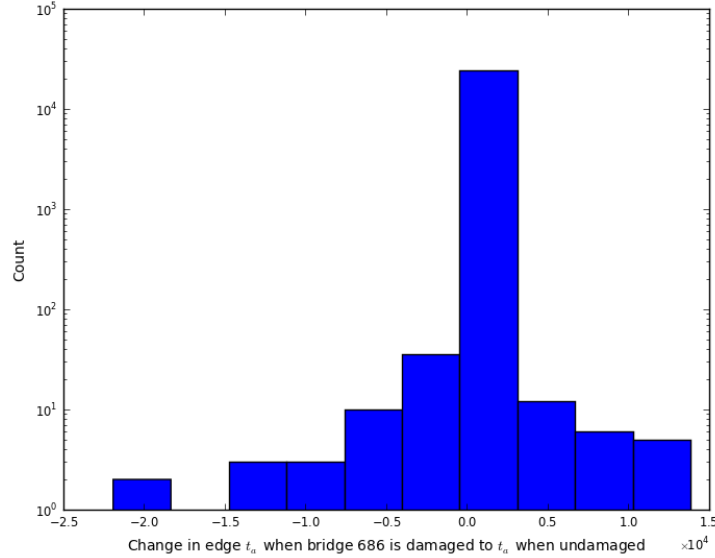


Figure 22: Histogram of changes in travel time ($t_a \times \text{flow}$) for each edge when bridge 686 is damaged vs. when there is no damage.

A.4 Bugs

A.4.1 Order of origin, destination iteration

A dictionary is a particular type in Python. It contains keys that, when looked up, return particular values. Say we have a dictionary `menu`. One key in `menu` is `spaghetti`. The value of `spaghetti` is 7.50. Thus, if we called `menu[spaghetti]`, we would get the price of the spaghetti: 7.50. Say we add the key-value pair (`pizza`, 10.00) to `menu`.

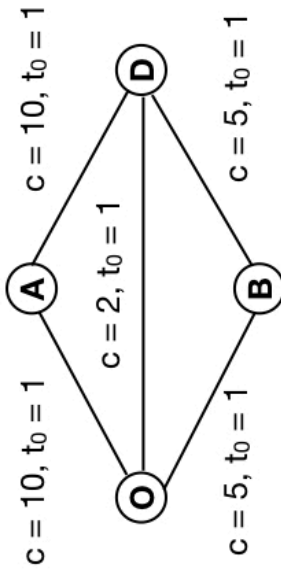
We can look up all the keys in a particular dictionary by calling `menu.keys()`, from which we would expect to get the resulting list: `[spaghetti, pizza]`. We might expect to get that exact list because the keys are listed according to the order in which they were inserted in the dictionary. However, the documentation for Python 2 (in which the traffic model is written) states, “Keys and values are listed in an arbitrary order which is non-random, varies across Python implementations, and depends on the dictionary’s history of insertions and deletions.” Thus, we might get the list of menu items in another order.

In the traffic assignment code `ita.py`, iteration over origins and destinations was originally implemented as follows.

```

1 for origin in self.demand.keys():
2     paths_dict = nx.single_source_dijkstra_path(self.G, origin, cutoff = None, weight =
      ↪ 't_a')
3     for destination in self.demand[origin].keys():

```



This is the undamaged network.

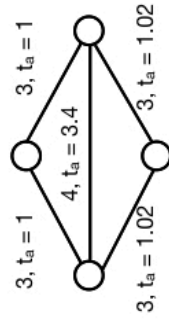
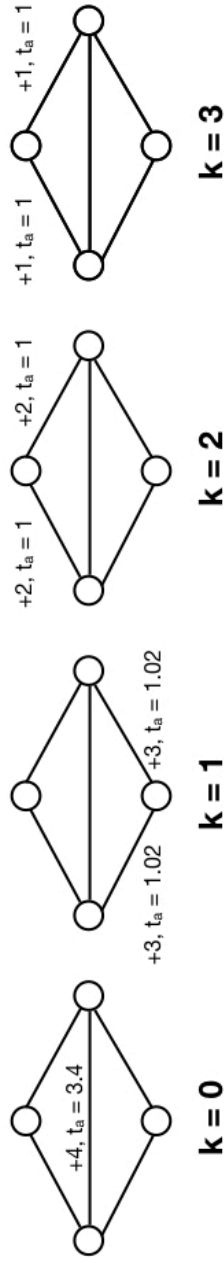
We assign traffic incrementally by finding the shortest path, in terms of traversal time, between O and D.

The settings for the incremental traffic assignment are: $K = 4$ increments, with values of 0.4, 0.3, 0.2, and 0.1 of the total demand between O and D.

The demand between O and D is 10.

We use the Bureau of Public Roads function to compute the traversal time of an edge based on the flow, q , and its capacity, c .

$$t_a = t_0(1 + 0.15(q/c)^4)$$



The total travel time, TT , is 25.7.

$$TT = 3 \times 1 + 3 \times 1 + 4 \times 3.4 + 3 \times 1.02 + 3 \times 1.02$$

$$TT = 25.7$$

end result

Figure 23: Part 1 of 3 in a simple case study in which damage to a network results in improved network performance, a consequence of the iterative traffic assignment algorithm.

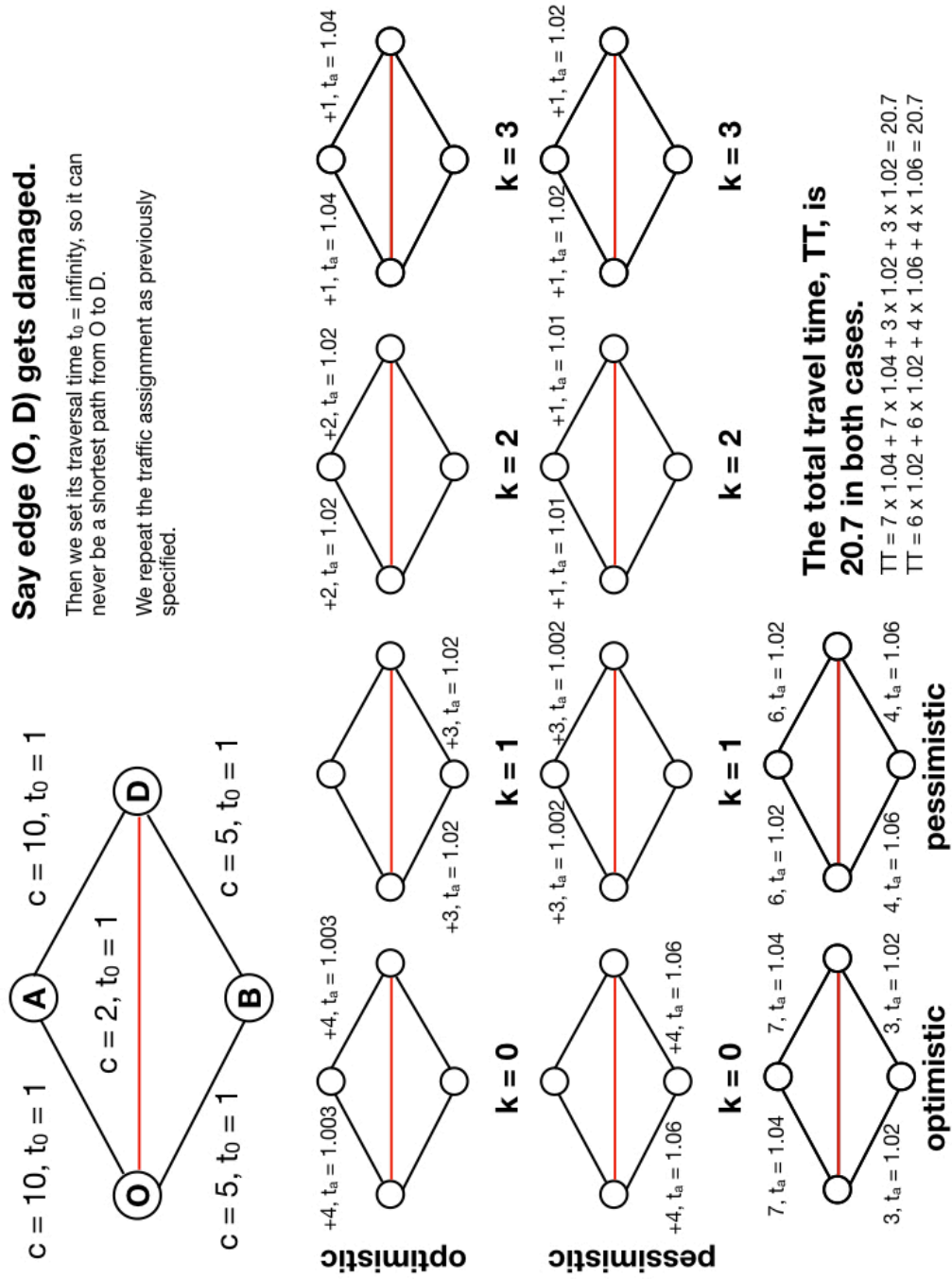


Figure 24: Part 2 of 3 in a simple case study in which damage to a network results in improved network performance, a consequence of the iterative traffic assignment algorithm.

The damaged network appears to perform better than the undamaged network.

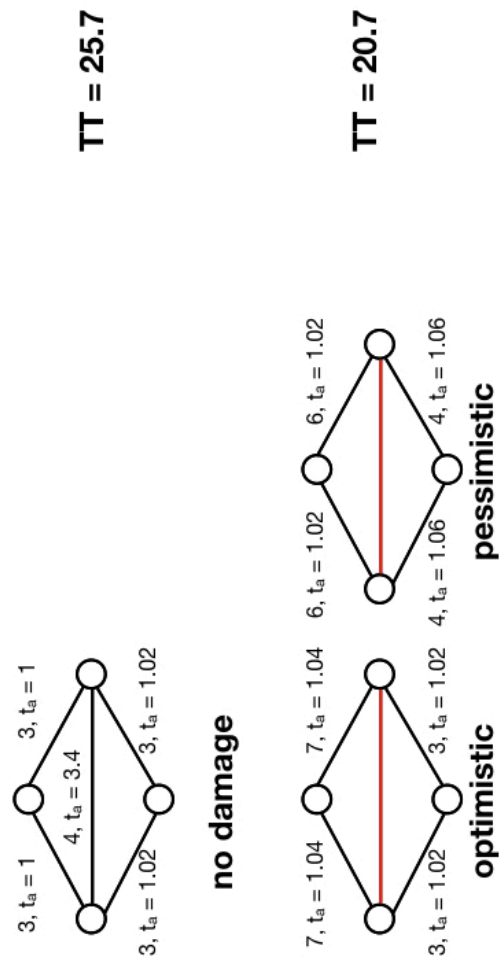


Figure 25: Part 3 of 3 in a simple case study in which damage to a network results in improved network performance, a consequence of the iterative traffic assignment algorithm.

Since the code is written in `Python 2.7`, the results of `self.demand.keys()` and `self.demand[origin].keys()` are not guaranteed to remain the same when called at different times. In fact, we have proof that the lists do not remain the same when called at different times.

Significance The order of the menu items may not matter for a restaurant application. However, consider our fixed-demand travel model. The demand between the origins and destinations that we consider is stored as a nested dictionary called `demand`. The first key of `demand` is an origin, and the second key of `demand` is a destination. Calling `demand[origin][destination]` returns a numerical value. To assign traffic in `ita.py`, we iterate over two lists: first, a list of the origins (which we get by calling `demand.keys()`) and then a list of destinations (which we get by calling `demand[origin].keys()`). The order in which the origins and destinations appear in those lists is not guaranteed to remain the same. In fact, we have demonstrated that when the methods in the traffic model are called in parallel (using the `parallel-python` package), the order of the origins *always* changes from when the methods are not called in parallel. The order in which the traffic assignment algorithm iterates over origins and destinations has a non-negligible impact on the values of the traffic metrics that describe the performance of the road network – the no-damage travel time over the network according to the traffic assignment algorithm is $6.12E12$ seconds for one ordering of the origins and $2.12E14$ seconds for another ordering of the origins. The no-damage travel time can thus vary by at least $5.7E10$ hours depending on the order in which we iterate over the origins. (There are 34 super-nodes, each of which can be both an origin and a destination – I have not tested the no-damage traffic metrics for every ordering of super-nodes in origin and destination lists).

Why is the inconsistency that stems from different orders of origins and destinations a problem? First, because it means that there have been instances in which the performance of the network when damaged has been better than the performance of the undamaged network. This undermines the case for retrofitting bridges – why bother, if the performance of the road network apparently improves when bridges are damaged? Second, if the order in which we iterate over origins and destinations matters so much and also varies, then there may be cases in which a more-damaged network (i.e., one with fewer damaged bridges) seems to perform better than a less-damaged network. Third, the performance of the undamaged network may be inconsistent – in fact, it may vary a great deal. This variation might, unintentionally, do a good job of reflecting the real world – however, in terms of modeling how retrofits affect the road network’s performance, this variation means the goal-posts are constantly shifting. If the goal of retrofitting bridges is to minimize the disruption to the road network, huge variations in the baseline condition of the road network make improvements difficult to discern, to both to human eyes and to agents or analytical tools that assume smaller costs (associated with smaller total travel times) represent improvements in the road network performance rather than essentially meaningless variations in performance due to the order in which traffic was assigned.

For example, I am using global variance-based sensitivity analysis to measure how changes in the fragilities of highway bridges affect the expected performance of the road network. This analytical setup assumes that changes in the performance of the road network are explained by which bridges are damaged (a function of the hazard and the bridges’ fragility). However, if the largest variations in the travel time stem from changes in the order over which origins and destinations are iterated, the results of any variance-based sensitivity analysis using code as written *must* be assumed to be flawed unless the number of samples used to conduct the sensitivity analysis is sufficiently large to cover all the orderings of origins and destinations that might occur. In practice, it does not seem that the origins and destinations are

returned in random and different orders each time they are called – however, there is no guarantee against such a situation.

Solutions

A.4.1.1 Sort lists by integer values

The simplest fix I can think of is to ensure that origins and destinations are iterated over in a fixed order. To implement this, I have made the following change to `ita.py`. Ordering the destinations in this fashion is necessary because each origin has a different set of associated destinations.

```
1 origins = [int(i) for i in self.demand.keys()] # get SD node IDs as integers
2 origins.sort() # sort them
3 origins = [str(i) for i in origins] # make them strings again
4 for origin in origins:
5     paths_dict = nx.single_source_dijkstra_path(self.G, origin, cutoff = None, weight =
6         ↪ 't_a')
7     destinations = [int(i) for i in self.demand[origins].keys()]
8     destinations.sort()
9     destinations = [str(i) for i in destinations]
10    for destination in destinations:
```

A.4.1.2 Create an origin-destination defaultdict

Another potential fix is to create an additional dictionary – let’s call it `origins_destinations` – in which the keys are origins and the values are lists of destinations. Because the order of elements in a list is guaranteed to be persistent in Python, this would eliminate the need to sort the list of destinations for every origin, as is done in the snippet code above. That is, we could rewrite the code above as:

```
1 origins = [int(i) for i in self.demand.keys()] # get SD node IDs as integers
2 origins.sort() # sort them
3 origins = [str(i) for i in origins] # make them strings again
4
5 origins_destinations = build_od() # returns a defaultdict with keys of origin IDs and
6     ↪ values of lists of destination IDs
7
8 for origin in origins:
9     paths_dict = nx.single_source_dijkstra_path(self.G, origin, cutoff = None, weight =
10        ↪ 't_a')
11     destinations = origins_destinations[origin] # this is a list of destination node
12        ↪ IDs
13     for destination in destinations:
```

To make the above piece of code feasible, we would have to create the dictionary `origins_destinations` as an instance of the class `defaultdict` (the regular dictionary class does not allow key-value pairs in which the value is a list, while the `defaultdict` class does). However, we need to ensure that the order of destinations remains the same not only between calls to the iterative traffic assignment code but also between runs of a larger piece of code – therefore, we would have to sort the lists of destinations when

creating the `origins_destinations` in the first place.

Why not simply change `demand` from a regular dictionary to an instance of the class `defaultdict` and then call `origins` as `demand.keys()`? As before, the order of the elements in the resulting list would not be guaranteed.

I implemented the following method (`build_od`) in `bd.py`.

```
1 def build_od(demand_dict):
2
3     od_dict = defaultdict() # keys are origins, values are lists of destinations
4
5     for origin in demand_dict.keys():
6         temp_destinations = []
7         for d in demand_dict[origin].keys():
8             temp_destinations.append(d)
9
10        destinations = [int(i) for i in temp_destinations]
11        destinations.sort()
12        destinations_sorted = [str(i) for i in destinations]
13
14        od_dict[origin] = destinations_sorted
15
16    return od_dict
```

Additional notes In doing some bare-bones testing, it seems that the type of the keys in a dictionary has an effect on the order in which they are returned. I created two dictionaries, `test_dict.a` and `test_dict.b`.

```
1 test_dict_a = {}
2 test_dict_a['04'] = 4
3 test_dict_a['01'] = 1
4 test_dict_a['02'] = 2
5 test_dict_a['03'] = 3
6
7 test_dict_b = {}
8 test_dict_b['spaghetti'] = 7.50
9 test_dict_b['pizza'] = 10.00
```

By Python convention, the `test_dict_a.keys()` ought to return the keys in order of insertion (though again, this is not guaranteed), i.e. `['04', '01', '02', '03']`. Instead, it returns `['02', '03', '01', '04']`. This remains true when the keys are accessed in parallel using `parallel python`. However, `test_dict_b.keys()` produces the expected (though not guaranteed) result – `[spaghetti, pizza]` – both in a standard call and in multiple calls made in parallel using `parallel python`. The origins and destinations in the `demand` dictionary are numbered in much the same way that the keys of `test_dict_a` are – that is, with numbers stored as strings.

A.4.2 Travel time computation

This bug was identified and shared by Jorge M. Lozano.

Significance In the original traffic assignment code (see Listing 1), the travel time along an edge is computed as the travel time induced by the additional flow rather than the total flow along the edge. This is obviously problematic and would result in underestimates of the total travel time across the network.

Solution The solution, as shown in line 33 of Listing 2, is to compute the travel time along an edge using the total flow assigned to that edge.

A.4.3 Trip assignment

Significance To track connectivity losses due to bridge damage, I implemented a counter for the number of trips made on the road network to `ita.py`. In doing so, I found that not all trips demanded of the road network are made when there is no damage.

There are 11,179,420 trips demanded of the road network. Under no-damage conditions, I would expect almost (if not) all trips to be assigned to the road network. However, only 7.7 million trips are made on the undamaged road network when the order in which we iterate over origins and destinations is held constant as described in Section A.4.1. When the order of origins and destinations is not fixed, about 7.9 million trips are assigned, suggesting this problem is not an unintended result of fixing the order in which we iterate over origins/destinations.

Solution The original mechanism by which trips were or were not made between origin-destination pairs is depicted schematically in Figure 27 and was carried out as follows. Say we have an origin \mathcal{O} and a destination \mathcal{D} . The number of trips demanded between \mathcal{O} and \mathcal{D} is T . The shortest path between \mathcal{O} and \mathcal{D} is returned as a list of nodes, L , as shown in Figure 26. We keep track of whether the trips between \mathcal{O} and \mathcal{D} are made using a boolean, `od_made`. We initially assume that all the trips can be made and so set `od_made = True`. We then have to check this assertion by iterating, in order, over the nodes in L and adding the trips T to the flow on the series of edges defined therein. Each edge – defined by a pair of nodes – has a capacity. If an edge’s capacity is greater than 0, we add the flow (T) to that edge. If the edge’s capacity is not greater than 0, we do not assign T , and we change `od_made` to `False`, since the path between \mathcal{O} and \mathcal{D} has been interrupted.

Note that in the above description, if the path between \mathcal{O} and \mathcal{D} was interrupted and the trip was not made, we would *still* assign the trips demanded to subsequent edges that have non-zero capacities, as shown in Figure 27. This didn’t make sense to me. Therefore, I modified the code in `ita.py` such that if we encounter a zero-capacity edge while traversing the shortest path from \mathcal{O} to \mathcal{D} , we will now not iterate over the subsequent edges, regardless of their capacity, since they must not be reachable from \mathcal{O} . (This is accomplished by adding the `break` in Line 36 of Listing 2). Thus, the flow assigned to edges downstream of the zero-capacity edge will be 0, as shown in Figure 28. If we adhered to the original implementation and did iterate over the subsequent edges, the total travel time and the vehicle miles travelled would be artificially inflated, though the number of trips made (the counter I implemented) would not be.

Despite all the changes described above, not all trips demanded are assigned to the undamaged road network. This is most likely because even in the undamaged network, more than 25% of all edges (representing roads) have capacities of zero. Trips cannot be assigned to zero-capacity edges.

Code version	Total travel time	Total flow	Total vehicle miles travelled
original	2.23×10^{14} s	7.69×10^6 trips	1.12×10^8 miles
updated	2.98×10^{13} s	7.63×10^6 trips	3.51×10^7 miles

Table 16: Traffic metrics on the undamaged road network.

For complete transparency, I have included the original traffic assignment code from `ita.py` in Listing [1](#) and the code with my modifications in Listing [2](#). Note that Listing [2](#) includes all other modifications listed in this document (i.e. ordered iteration over origins and destinations, correct time computation).

A.4.4 Graph edge weights

Significance Trips between point A and point B are assigned by first identifying the shortest path between A and B in the graph of the road network. The shortest path is the path with the smallest sum of the traversal times t_a of each edge in the path. For each edge in the path, we check that its capacity is greater than 0 before adding flow to it.

However, the graph of the road network includes edges with zero capacity (i.e. that cannot be assigned any traffic) but finite traversal times. Therefore, an edge with 0 capacity and a finite traversal time could be identified as being on the shortest path between point A and point B – but in the next step, we would not be able to assign any flow to that edge, and the trip would not be made. This results in the false loss of more than 3 million trips when the network is undamaged.

Solution The solution is to correct the graph of the road network before assigning any traffic to its edges. The correction is simple – any edge with zero capacity should have a traversal time $t_a = \infty$. The implementation of this correction is shown in Listing [3](#). It need only be carried out once and the resulting graph saved as a `gpickle`. The correction affects more than 25% of edges in the graph.

The result of this correction is that on the undamaged road network, 10.8 million trips (97%) of the 11.1 million trips demanded can be made. The remaining 0.3 million trips cannot be completed because there is no shortest path between their origin that does not include edges with infinite traversal times t_a .

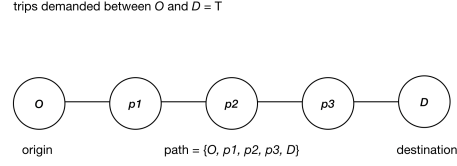


Figure 26: Schematic of shortest path between an origin and destination node.

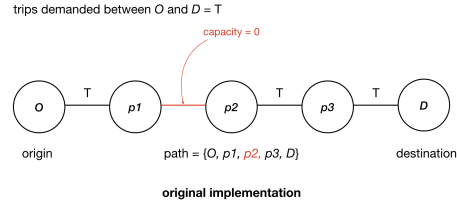


Figure 27: Schematic of original method assigning flow to the edges along the shortest path between an origin and destination node. Even if flow can't be assigned to the edge between $p1$ and $p2$, it will be assigned to subsequent edges along the path. Thus, while the trip from the origin to the destination couldn't be made along the shortest path, the travel time and vehicle miles travelled would be calculated as though the trip were made except for a skipped edge. This method of flow assignment would presumably lead to artificially high total travel times and vehicle miles travelled.

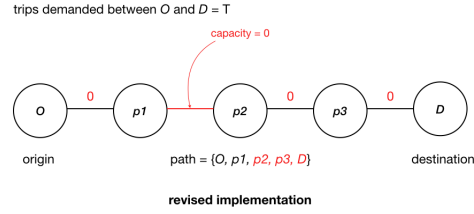


Figure 28: Schematic of revised method of assigning flow to the edges along the shortest path between an origin and destination node. Now, if flow can't be assigned to a particular edge, then the trip cannot be made and the trips demanded will not be assigned to subsequent edges along the path between an origin and a destination.

Listing 1: The original implementation of traffic assignment in ita.py, written by Mahalia Miller. Some comments have been omitted for brevity.

```

1  def assign(self):
2      for i in range(4): #do 4 iterations
3          for origin in self.demand.keys():
4              paths_dict = nx.single_source_dijkstra_path(self.G, origin, cutoff = None,
5                  ↪ weight = 't_a')
6              for destination in self.demand[origin].keys():
7                  od_flow = iteration_vals[i] * self.demand[origin][destination]*0.053
8                  path_list = paths_dict[destination] #list of nodes
9
10                 for index in range(0, len(path_list) - 1):
11                     u = path_list[index]
12                     v = path_list[index + 1]
13
14                     if self.G.is_multigraph():
15                         num_multi_edges = len(self.G[u][v])
16                         if num_multi_edges > 1: #multi-edge
17                             best = 0
18                             best_t_a = float('inf')
19                             for multi_edge in self.G[u][v].keys():
20                                 new_t_a = self.G[u][v][multi_edge]['t_a'] #causes problems
21                                 if (new_t_a < best_t_a) and (self.G[u][v][multi_edge]['capacity'] > 0):
22                                     best = multi_edge
23                                     best_t_a = new_t_a
24                             else:
25                                 best = 0
26                         if (self.G[u][v][best]['capacity'] > 0):
27                             self.G[u][v][best]['flow'] += od_flow
28                             t = util.TravelTime(self.G[u][v][best]['t_0'], self.G[u][v][best]['
29                                 ↪ capacity'])
30                             travel_time = t.get_new_travel_time(od_flow)

```

```

29         self.G[u][v][best]['t_a'] = travel_time
30     else:
31         try:
32             if (self.G[u][v]['capacity']>0):
33                 self.G[u][v]['flow'] += od_flow
34                 t = util.TravelTime(self.G[u][v]['t_0'], self.G[u][v]['capacity'])
35                 travel_time= t.get_new_travel_time(od_flow)
36                 self.G[u][v]['t_a'] = travel_time #in seconds
37         except KeyError as e:
38             print 'found_key_error:', e
39             pdb.set_trace()
40
41     return self.G

```

Listing 2: The modified implementation of traffic assignment in ita.py, with fixes for the order of iteration over origins and destinations, the computation of travel time, and the assignment of trips.

```

1  def assign(self):
2
3  total_flow = 0 # GB ADDITION -- tracker for number of trips made on the whole
   ↪ network
4
5  # GB ADDITION -- adding sorting
6  origins = [int(i) for i in self.demand.keys()] # get SD node IDs as integers
7  origins.sort() # sort them
8  origins = [str(i) for i in origins] # make them strings again
9
10 od_dict = bd_test.build_od(self.demand)
11
12 for i in range(4): #do 4 iterations
13     for origin in origins:
14
15         paths_dict = nx.single_source_dijkstra_path(self.G, origin, cutoff = None,
   ↪ weight = 't_a')
16
17         for destination in od_dict[origin]:
18
19             od_flow = iteration_vals[i] * self.demand[origin][destination]
20
21             path_list = paths_dict[destination] #list of nodes
22
23             od_made = True
24
25             for index in range(0, len(path_list) - 1):
26                 u = path_list[index]
27                 v = path_list[index + 1]
28
29                 try:
30                     if (self.G[u][v]['capacity']>0):
31                         self.G[u][v]['flow'] += od_flow
32                         t = util.TravelTime(self.G[u][v]['t_0'], self.G[u][v]['capacity'])
33                         travel_time= t.get_new_travel_time(self.G[u][v]['flow']) # GB
   ↪ MODIFICATION
34                         self.G[u][v]['t_a'] = travel_time #in seconds
35
36                 else:
37                     od_made = False
38                     break # GB ADDITION -- we should not continue assigning traffic to edges
   ↪ between origin and destination if destination is not reachable
   ↪ from origin!
39

```

```

40         except KeyError as e:
41             print('found_key_error:', e)
42             pdb.set_trace()
43
44         total_flow += od_made*od_flow
45
46     return self.G, total_flow

```

Listing 3: A method to correct the original road network graph prior to any traffic assignment by ensuring that zero-capacity edges have infinite traversal times.

```

1
2     def correct_graph(G):
3         count = 0
4         count0 = 0
5         count1 = 0
6         for edge in G.edges():
7             if G[edge[0]][edge[1]]['capacity'] == 0:
8                 if G[edge[0]][edge[1]]['t_a'] != float('inf'):
9                     G[edge[0]][edge[1]]['t_a'] = float('inf')
10                    count += 1
11                    if G[edge[0]][edge[1]]['t_0'] != float('inf'):
12                        G[edge[0]][edge[1]]['t_0'] = float('inf')
13                        count0 += 1
14                    if G[edge[0]][edge[1]]['distance_0'] == 0:
15                        G[edge[0]][edge[1]]['capacity'] = 0
16                        G[edge[0]][edge[1]]['t_0'] = float('inf')
17                        G[edge[0]][edge[1]]['t_a'] = float('inf')
18                        G[edge[0]][edge[1]]['distance'] = 0
19
20                    count1 += 1
21
22         print 'corrected', count, 'zero-capacity and', count1, 'zero-length edges in
23             ↪ graph'
24
25     return G

```