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Homework Introduction

```
% Geneva Porter, 2019.10.24
% Homework 3, Math 693A
% Professor Uduak George, SDSU

% This assignment minimizes the function:
%
%           f(x) = 10(x2-x1^2)^2 + (1-x1)^2
%
% I use a trust region method, utilizing the Cauchy point algorithm to
% minimize the quadratic model. The trust region radius will vary from zero
% to 2. Results will show the countour lines of the objective function
% juxtaposed against the contour lines of the quadratic model. First, the
% initial point x = (0, -1) will be used, then we will repeat the algorithm
% for x = (0, 0.5).
%
```

Establishing Parameters

```
clear
clc

alpha      = 1.0;
c1         = 1e-4;
tolerance  = 1e-8;

param = [alpha, c1, tolerance];

p1        = [ 0 ; -1];
p2        = [ 0 ; .5];
```

Setting Up Functions

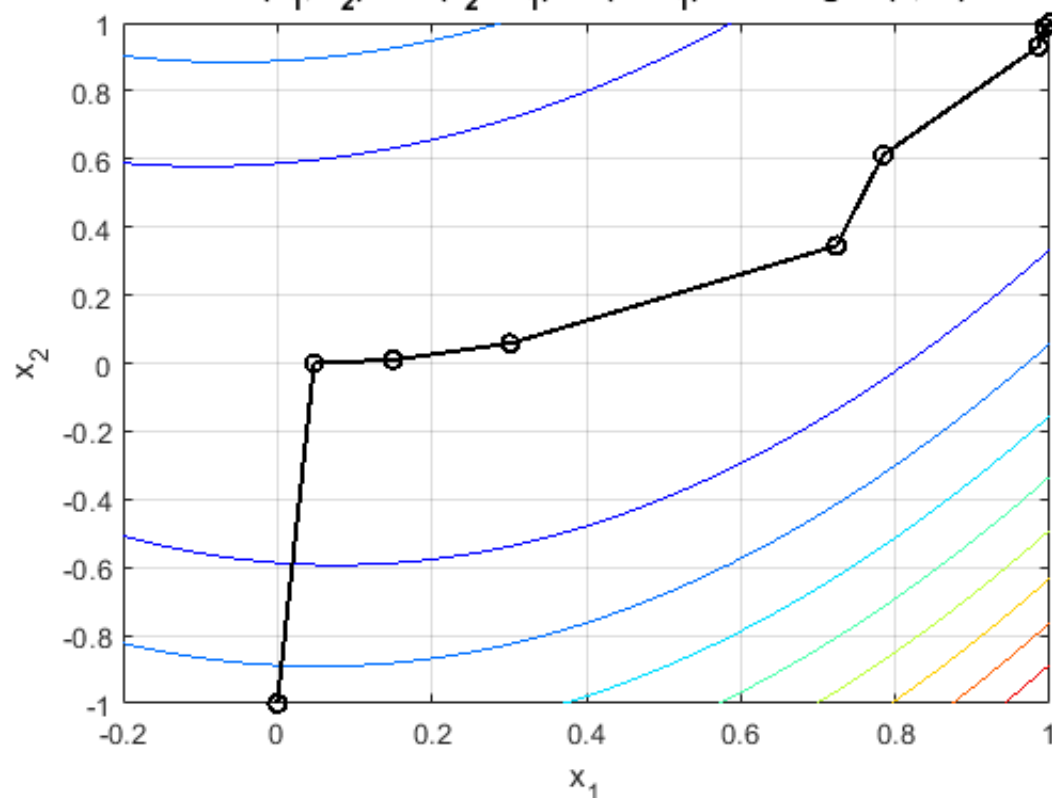
```
x      = sym('x', [2,1]);
p      = sym('p', [2,1]);
f(x)   = 10*(x(2) - x(1).^2).^2 + (1 - x(1)).^2;
f_grad(x) = gradient(f);
f_hess(x) = hessian(f);
m1(x)   = f + p1'*f_grad + 0.5 * p1' * f_hess * p1;
m2(x)   = f + p2'*f_grad + 0.5 * p2' * f_hess * p2;
```

```
NE = "Newton";  
SD = "steepest descent";  
TR = "trust region";
```

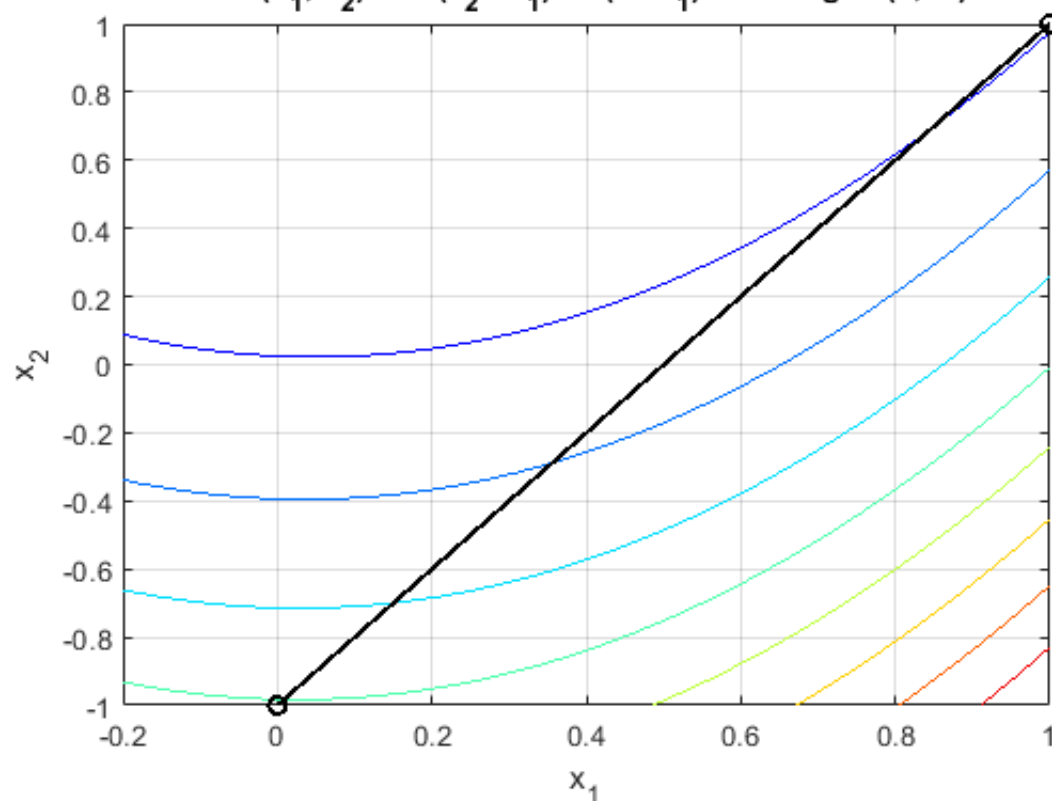
Iterating Methods and Printing Results:

```
figure(1)  
clf  
hold on  
  
SD_point1 = line_search3(NE, f, p1, param);  
plot_trust(SD_point1, NE, f);  
  
figure(2)  
clf  
hold on  
  
TR_point1 = line_search3(TR, f, p1, param);  
plot_trust(TR_point1, TR, m1);  
  
figure(3)  
clf  
hold on  
  
SD_point2 = line_search3(NE, f, p2, param);  
plot_trust(SD_point2, NE, f);  
  
figure(4)  
clf  
hold on  
  
TR_point2 = line_search3(TR, f, p2, param);  
plot_trust(TR_point2, TR, m2);
```

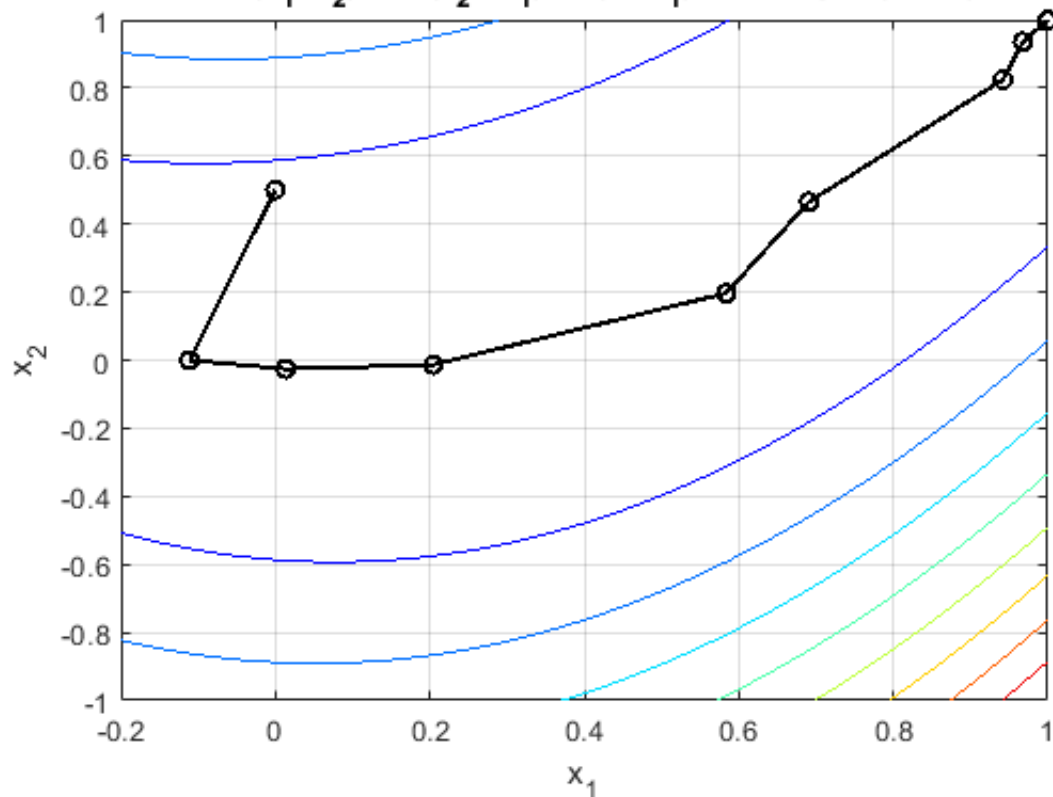
Backtracking line search using Newton method
 for $f(x_1, x_2) = 10(x_2 - x_1^2)^2 + (1 - x_1)^2$ starting at $(0, -1)$



Backtracking line search using trust region method
 for $f(x_1, x_2) = 10(x_2 - x_1^2)^2 + (1 - x_1)^2$ starting at $(0, -1)$



Backtracking line search using Newton method
 for $f(x_1, x_2) = 10(x_2 - x_1^2)^2 + (1 - x_1)^2$ starting at $(0, 0.5)$



Backtracking line search using trust region method
 for $f(x_1, x_2) = 10(x_2 - x_1^2)^2 + (1 - x_1)^2$ starting at $(0, 0.5)$

