

## A RELATION DEFINITIONS

$$\text{Implication} := \{(x, y) \in V \times V \mid l(x) \models l(y)\} \quad (1)$$

$$\text{Alternative} := \{(x, y) \in V \times V \mid l(x) \models \neg l(y)\} \quad (2)$$

$$\begin{aligned} \text{Independent} := \{(x, y) \in V \times V \mid & \text{isSatisfiable}(l(x) \wedge l(y)), \\ & \text{isSatisfiable}(l(x) \wedge \neg l(y)), \\ & \text{isSatisfiable}(\neg l(x) \wedge l(y))\} \end{aligned}$$

## B RELATION COMPLETENESS PROOF & TABLE

PROOF. Formally, "every pair of feature mapping nodes is either in an *Independent*, *Implication*, or *Alternative* relation" translates to the conjunction of the following SAT calls:

$$\begin{aligned} & (\text{SAT}(l(x) \wedge l(y)) \wedge \text{SAT}(l(x) \wedge \neg l(y)) \wedge \text{SAT}(\neg l(x) \wedge l(y)) \\ & \vee \neg \text{SAT}(\neg(\neg l(x) \vee l(y))) \vee \neg \text{SAT}(\neg(\neg l(y) \vee l(x))) \\ & \vee \neg \text{SAT}(\neg(\neg l(x) \vee \neg l(y))) \end{aligned}$$

We apply DeMorgan's law twice:

$$\begin{aligned} & = (\text{SAT}(l(x) \wedge l(y)) \wedge \text{SAT}(l(x) \wedge \neg l(y)) \wedge \text{SAT}(\neg l(x) \wedge l(y)) \\ & \vee \neg \text{SAT}((l(x) \wedge \neg l(y)) \vee \neg \text{SAT}(l(y) \wedge \neg l(x))) \\ & \vee \neg \text{SAT}((l(x) \wedge l(y))) \\ & = (\text{SAT}(l(x) \wedge l(y)) \wedge \text{SAT}(l(x) \wedge \neg l(y)) \wedge \text{SAT}(\neg l(x) \wedge l(y)) \\ & \vee \neg(\text{SAT}(l(x) \wedge l(y)) \wedge \text{SAT}(l(x) \wedge \neg l(y)) \wedge \text{SAT}(\neg l(x) \wedge l(y))) \\ & = \text{true} \end{aligned}$$

Therefore, every pair of feature mappings is guaranteed to be in at least one of the relations *Independent*, *Implication*, and *Alternative*.

**Textual Proof.** We conduct our textual proof by taking a closer look at the check for the *Independent* relation:

$$\begin{aligned} & \text{SAT}(l(x) \wedge l(y)) \\ & \wedge \text{SAT}(l(x) \wedge \neg l(y)) \\ & \wedge \text{SAT}(\neg l(x) \wedge l(y)) \end{aligned}$$

If this formula evaluates to *True*, the two nodes  $x$  and  $y$  are in the *Independent* relation. The two nodes can not be in the *Alternative* relation since  $\text{SAT}(l(x) \wedge l(y)) = \text{True}$ . Additionally, the two nodes can not be in the *Implication* relation, because  $\text{SAT}(l(x) \wedge \neg l(y)) = \text{SAT}(\neg l(x) \wedge l(y)) = \text{True}$ , meaning there are variable assignments that contradict either  $l(x)$  modelling  $l(y)$  or  $l(y)$  modelling  $l(x)$ .

Now, there are several ways the check for *Independent* can evaluate to *False*, namely each or multiple of the SAT calls fail: If  $\text{SAT}(l(x) \wedge l(y))$  succeeds and one or both of the other SAT calls fail, the respective nodes are in an *Implication* relation with each other. Note that the nodes can not be in the *Alternative* relation, since  $\text{SAT}(l(x) \wedge l(y))$  succeeds, i.e., there are variants in which both  $x$  and  $y$  are present. If  $\text{SAT}(l(x) \wedge l(y))$  fails but the two other SAT calls succeed, there are variable assignments that fulfil each formula but none that fulfil both, therefore leaving us with the *Alternative* relation between the two nodes. For  $\text{SAT}(l(x) \wedge l(y))$  failing and exactly one of the two other SAT calls succeeding, one of the respective formulas has to be *False*, giving the node an *Implication* edge, which is analogous to the empty set being a subset of

every other set. If all three SAT calls fail, both  $l(x)$  and  $l(y)$  must be *False*, which would fulfil both *Implication* and *Alternative*. A complete table with all cases any of the SAT calls can fail or succeed for can be found in Table 4. Since we covered every potential case the check for *Independent* can succeed or fail and since for every case at least one relation applies, every pair of feature mapping nodes has a relation from the set  $\{\text{Implication}, \text{Alternative}, \text{Independent}\}$ .  $\square$

## C COMMUTATIVITY OF REDUCE AND PROJECT

LEMMA C.1. For any edge-typed variation diff  $D$  and any time  $t \in \{\text{before}, \text{after}\}$  reduction and projection commute:

$$\text{reduce}_{VT}(\text{project}_{ET}(D, t)) = \text{project}(\text{reduce}_{VD}(D), t).$$

PROOF SKETCH.

$$\begin{aligned} & \text{reduce}_{VT}(\text{project}_{ET}((V, E, r, \tau, l, \Delta, \pi), t)) \\ & = \text{reduce}_{VT}(\{(v \in V \mid \text{exists}(t, \Delta(v))), \\ & \quad \{e \in E \mid \pi(e) = \text{Nesting} \wedge \text{exists}(t, \Delta(e))\} \\ & \quad \cup \{(x, y) \in E \mid \pi(e) \neq \text{Nesting} \\ & \quad \wedge \text{exists}(t, \Delta(x)) \wedge \text{exists}(t, \Delta(y))\}, \\ & \quad r, \tau, l, \pi)) \\ & = (\{v \in V \mid \text{exists}(t, \Delta(v))\}, \\ & \quad \{e \in E \mid \pi(e) = \text{Nesting} \wedge \text{exists}(t, \Delta(e))\} \\ & \quad r, \tau, l)) \\ & = \text{project}((V, \\ & \quad \{e \in E \mid \pi(e) = \text{Nesting}\}, \\ & \quad r, \tau, l, \Delta), t) \\ & = \text{project}(\text{reduce}_{VD}((V, E, r, \tau, l, \Delta, \pi)), t) \end{aligned}$$

$\square$

Evaluation of the SAT calls			Relation type
$SAT(l(x) \wedge l(y))$	$SAT(l(x) \wedge \neg l(y))$	$SAT(\neg l(x) \wedge l(y))$	
1	1	1	<i>Independent</i>
1	1	0	<i>Implication with <math>l(y) \models l(x)</math></i>
1	0	1	<i>Implication with <math>l(x) \models l(y)</math></i>
1	0	0	<i>Implication with <math>l(x)</math> equivalent to <math>l(y)</math></i>
0	1	1	<i>Alternative</i>
0	1	0	<i>Implication where <math>l(y)</math> is False</i>
0	0	1	<i>Implication where <math>l(x)</math> is False</i>
0	0	0	<i>Implication/Alternative where <math>l(x)</math> and <math>l(y)</math> are False</i>

Table 4: All potential cases the *Independent* SAT call can succeed and fail for