

Solve each equation below

$$\log_4 \frac{x^2}{4} = \log_x 64$$

$$2\log_4 x - 1 = 3\log_x 4$$

$$2(\log_4 x)^2 - \log_4 x - 3 = 0$$

$$\log_4 x = -1, \text{ or } \frac{3}{2} \quad \therefore x = \frac{1}{4}, \text{ or } 8$$

$$\log_6 6x = \log_x 36$$

$$1 + \log_6 x = 2\log_x 6$$

$$(\log_6 x)^2 + \log_6 x - 2 = 0$$

$$\log_6 x = -2, \text{ or } 1 \quad \therefore x = \frac{1}{36}, \text{ or } 6$$

$$x^{\log_4 x^2} = 4x$$

$$(\log_2 x)^2 = 2 + \log_2 x$$

$$\log_2 x = -1, \text{ or } 2$$

$$\therefore x = \frac{1}{2}, \text{ or } 4$$

$$\log_7 \frac{x^3}{49} = \log_x 7$$

$$3\log_7 x - 2 = \log_x 7$$

$$3(\log_7 x)^2 - 2\log_7 x - 1 = 0$$

$$\log_7 x = 1, \text{ or } -\frac{1}{3} \quad x = 7, \text{ or } \frac{1}{\sqrt[3]{7}}$$

$$x^{\log_2 x} = \frac{4}{x}$$

$$(\log_2 x)^2 = 2 - \log_2 x$$

$$\log_2 x = -2, \text{ or } 1$$

$$x = \frac{1}{4}, \text{ or } 2$$

$$\log_5 \frac{x}{25} = \log_x 125$$

$$2 + \log_5 x = 3 \log_x 5$$

$$\log_5 x = -1, \text{ or } 3$$

$$x = \frac{1}{5}, \text{ or } 125$$

$$\log_3 9x = \log_x 27$$

$$2 + \log_3 x = 3 \log_x 3$$

$$\log_3 x = 1, \text{ or } -3$$

$$x = 3, \text{ or } \frac{1}{27}$$

$$x^{\log_8 x} = \frac{1}{262144x^2} \quad \frac{262144}{x}$$

$$(\log_8 x)^2 = -\log_8 x + 6$$

$$\log_8 x = 2, \text{ or } -3$$

$$\begin{array}{r} 262144 \\ 8 \boxed{32768} \\ 8 \boxed{4096} = 2^{12} \end{array}$$

$$\therefore 2^{18} = 8^6$$

$$x = 64, \text{ or } \frac{1}{512}$$

$$\log_2 \frac{x^2}{2} = \log_x 2$$

$$2 \log_2 x - 1 = \log_x 2$$

$$\log_2 x = 1, \text{ or } -\frac{1}{2}$$

$$x = 2, \text{ or } \frac{\sqrt{2}}{2}$$

$$x^{\log_7 x^3} = \frac{49}{x}$$

$$3(\log_7 x)^2 = 2 - \log_7 x$$

$$\log_7 x = -1, \text{ or } \frac{2}{3}$$

$$x = \frac{1}{7}, \text{ or } \sqrt[3]{49}$$

$$x^{\log_4 x^2} = \cancel{4} \frac{x^3}{4}$$

$$(\log_2 x)^2 = 3 \log_2 x - 2$$

$$\log_2 x = 1, \text{ or } 2$$

$$x = 2, \text{ or } 4$$

$$x^{\log_5 x} = 25x$$

$$(\log_5 x)^2 = 2 + \log_5 x$$

$$\log_5 x = 2 \text{ or } -1$$

$$x = 25, \text{ or } \frac{1}{5}$$

$$x^{\log_9 x} = \frac{1}{81x^3}$$

$$(\log_9 x)^2 = -2 - 3\log_9 x$$

$$\log_9 x = -1, \text{ or } -2$$

$$x = \frac{1}{9} \text{ or } \frac{1}{81}$$

$$\log_5 25x^3 = \log_x 5$$

$$2 + 3\log_5 x = \log_x 5$$

$$\log_5 x = -1, \text{ or } -\frac{1}{3}$$

$$x = \frac{1}{5}, \sqrt[3]{5}$$

$$\log_4 4x^2 = \log_x 64$$

$$1 + 2\log_4 x = 3\log_x 4$$

$$\log_4 x = 1, \text{ or } -\frac{3}{2}$$

$$x = 4, \text{ or } \frac{1}{8}$$

$$\log_9 \frac{x}{729} = \log_{x^2} 9 \quad \log_x \frac{1}{81}$$

$$\log_9 x - 3 = -2\log_x 9$$

$$\log_9 x = 1, \text{ or } 2$$

$$x = 9, \text{ or } 81$$

$$x^{\log_5 x} = \frac{1}{25x^3}$$

$$(\log_5 x)^2 = -2 - 3\log_5 x$$

$$\log_5 x = -1, \text{ or } -2$$

$$x = \frac{1}{5}, \text{ or } \frac{1}{25}$$

$$\log_3 27x = \log_{x^3} \log_x \frac{1}{9}$$

$$3 + \log_3 x = -2 \log_x 3$$

$$\log_3 x = -1, \text{ or } -2$$

$$x = \frac{1}{3}, \text{ or } \frac{1}{9}$$

$$x^{\log_4 x^3} = \frac{x^2}{4} 4x^2$$

$$3(\log_4 x)^2 = 2\log_4 x + 1$$

$$\log_4 x = 1, \text{ or } -\frac{1}{3}$$

$$x = 4, \text{ or } \frac{1}{\sqrt[3]{4}}$$

$$x^{\log_2 x^3} = \frac{x^2}{4} 4x$$

$$3(\log_2 x)^2 = \log_2 x + 2$$

$$\log_2 x = 1, \text{ or } -\frac{2}{3}$$

$$x = 2, \text{ or } \frac{1}{\sqrt[3]{4}}$$

$$x^{\log_2 x^2} = 2x^2$$

$$3(\log_2 x)^2 = 1 + 2\log_2 x$$

$$\log_2 x = 1, \text{ or } -\frac{1}{3}$$

$$x = 2, \text{ or } \frac{1}{\sqrt[3]{2}}$$

$$x^{\log_5 x^2} = 5x$$

$$2(\log_5 x)^2 = 1 + \log_5 x$$

$$\log_5 x = 1, \text{ or } -\frac{1}{2}$$

$$x = 5, \text{ or } \frac{\sqrt{5}}{5}$$

$$\log_3 3x^3 = \log_x 9$$

$$1 + 3\log_3 x = 2\log_x 3$$

$$\log_3 x = -1, \text{ or } \frac{2}{3}$$

$$x = \frac{1}{3}, \text{ or } \sqrt[3]{9}$$

$$\log_6 6x^2 = \log_x 6$$

$$1 + 2\log_6 x = \log_x 6$$

$$\log_6 x = -1, \text{ or } \frac{1}{2}$$

$$x = \frac{1}{6} \text{ or } \sqrt{6}$$

$$\log_9 729x = \log_x \frac{1}{81}$$

$$3 + \log_9 x = -2 \log_x 9$$

$$\log_9 x = -1, \text{ or } -2$$

$$x = \frac{1}{9}, \text{ or } \frac{1}{81}$$

$$\log_8 \frac{x}{512} = \log_x \frac{1}{64}$$

$$\log_8 x - 3 = -2 \log_x 8$$

$$\log_8 x = 1, \text{ or } 2$$

$$x = 8, \text{ or } 64$$

$$x^{\log_8 x} = \cancel{512} 512 x^2$$

$$(\log_8 x)^2 = 2 \log_8 x + 3$$

$$\log_8 x = -1, \text{ or } 3$$

$$\therefore x = \frac{1}{8}, \text{ or } 512$$

$$x^{\log_4 x^2} = \frac{1}{4x^3}$$

$$(\log_2 x)^2 = -3 \log_2 x - 2$$

$$\log_2 x = -1, \text{ or } -2$$

$$x = \frac{1}{2}, \text{ or } \frac{1}{4}$$

$$\log_7 \frac{x}{7} = \log_x 49$$

$$\log_7 x - 1 = 2 \log_x 7$$

$$\log_7 x = -1, \text{ or } 2$$

$$x = \frac{1}{7}, \text{ or } 49$$

$$\log_8 \frac{x^3}{8} = \log_x 64$$

$$3 \log_8 x - 1 = 2 \log_x 8$$

$$\log_8 x = 1, \text{ or } -\frac{2}{3}$$

$$x^{\log_6 x^2} = \frac{216}{x}$$

$$2(\log_6 x)^2 = 3 - \log_6 x$$

$$\log_6 x = 1, \text{ or } -\frac{3}{2}$$

$$x = 6, \text{ or } \frac{\sqrt{6}}{36}$$

$$x^{\log_5 x^2} = \frac{5}{x}$$

$$2(\log_5 x)^2 = 1 - \log_5 x$$

$$\log_5 x = -1, \text{ or } \frac{1}{2}$$

$$x = \frac{1}{5}, \text{ or } \sqrt{5}$$