

**C3.**  $\mathcal{CW} = \{c \in \mathcal{Cand} : \forall d \in \mathcal{Cand} : c \succeq^+ d\}$

1.  $\mathcal{CW} \subseteq \{c \in \mathcal{Cand} : \forall d \in \mathcal{Cand} : c \succeq^+ d\}$

PROOF: This follows from property C2 by the argument in the preceding paragraph.

2.  $\{c \in \mathcal{Cand} : \forall d \in \mathcal{Cand} : c \succeq^+ d\} \subseteq \mathcal{CW}$

2.1. It suffices to assume  $c \in \mathcal{Cand}$  and  $\forall d \in \mathcal{Cand} : c \succeq^+ d$ , and to prove  $c \in \mathcal{CW}$ .

PROOF: Obvious

2.2. Let  $d$  be an element of  $\mathcal{CW}$ .

PROOF: By definition,  $\mathcal{CW}$  is nonempty.

2.3.  $c \succeq^+ d$

PROOF: By 2.2 and the assumption of 2.1.

2.4. Q.E.D.

PROOF: By 2.2 and 2.3, since as we observed above, a simple induction argument shows that  $d \in \mathcal{CW}$  and  $c \succeq^+ d$  implies  $c \in \mathcal{CW}$ .

3. Q.E.D.

PROOF: By steps 1 and 2.