

```

EXTENDS  $\sqsubseteq$ Integers,  $\sqsubseteq$ GCD
 $\sqsubseteq$ 
CONSTANT  $\sqsubseteq$ M,  $\sqsubseteq$ N
ASSUME  $\sqsubseteq/\sqsubseteq$ M  $\sqsubseteq$ in  $\sqsubseteq$ Nat  $\sqsubseteq/\sqsubseteq$ {0}
 $\sqsubseteq$ 
ASSUME  $\sqsubseteq/\sqsubseteq$ N  $\sqsubseteq$ in  $\sqsubseteq$ Nat  $\sqsubseteq/\sqsubseteq$ {0}
 $\sqsubseteq$ 
(*****
--algorithm Euclid  $\sqsubseteq$ {
 $\sqsubseteq$ variables  $\sqsubseteq$ x  $\sqsubseteq$ =  $\sqsubseteq$ M,  $\sqsubseteq$ y  $\sqsubseteq$ =  $\sqsubseteq$ N;
 $\sqsubseteq$ { $\sqsubseteq$ while  $\sqsubseteq$ (x  $\sqsubseteq$ #  $\sqsubseteq$ y)  $\sqsubseteq$ {if  $\sqsubseteq$ (x  $\sqsubseteq$ <  $\sqsubseteq$ y)  $\sqsubseteq$ {y  $\sqsubseteq$ :=  $\sqsubseteq$ y -  $\sqsubseteq$ x}
 $\sqsubseteq$ else  $\sqsubseteq$ {x  $\sqsubseteq$ :=  $\sqsubseteq$ x -  $\sqsubseteq$ y}
 $\sqsubseteq$ }
 $\sqsubseteq$ }
}
*****)
PartialCorrectness  $\sqsubseteq$ ==
 $\sqsubseteq$ (pc  $\sqsubseteq$ = "Done")  $\sqsubseteq$ =>  $\sqsubseteq$ (x  $\sqsubseteq$ =  $\sqsubseteq$ y)  $\sqsubseteq$ /  $\sqsubseteq$ (x  $\sqsubseteq$ =  $\sqsubseteq$ GCD(M,  $\sqsubseteq$ N))
 $\sqsubseteq$ 
TypeOK  $\sqsubseteq$ ==  $\sqsubseteq/\sqsubseteq$ x  $\sqsubseteq$ in  $\sqsubseteq$ Nat  $\sqsubseteq/\sqsubseteq$ {0}
 $\sqsubseteq$ /  $\sqsubseteq$ y  $\sqsubseteq$ in  $\sqsubseteq$ Nat  $\sqsubseteq/\sqsubseteq$ {0}
Inv  $\sqsubseteq$ ==  $\sqsubseteq/\sqsubseteq$ TypeOK
 $\sqsubseteq$ /  $\sqsubseteq$ GCD(x,  $\sqsubseteq$ y)  $\sqsubseteq$ =  $\sqsubseteq$ GCD(M,  $\sqsubseteq$ N)
 $\sqsubseteq$ /  $\sqsubseteq$ (pc  $\sqsubseteq$ = "Done")  $\sqsubseteq$ =>  $\sqsubseteq$ (x  $\sqsubseteq$ =  $\sqsubseteq$ y)

```