A Code Search Engine for Go

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"All programming language proofs are by induction"

- 1 Background
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- 3 Type2Metric

3.1 Levenshtein Combinator

The Levenshtein edit distance is a commonly used metric for strings. It gives the number of substitutions, deletions, or additions to edit one string into another string [1]. It is well known that the normal Levenshtein distance on strings satisfies the properties of a metric. There are a couple of assumptions that the Levenshtein metric makes: that all substitutions are of the same cost, that deletions and additions are of the same cost and the same cost as a substitution. While this is a safe assumption for strings of characters, it is not genereral, as there might be better substitutions than others. For example, it is clear that in a real sense [1,2,3] is closer to [2,2,3] than it is to [10,2,3], as a 1 is closer to a 2 than a 10; however, the Levenshtein edit distance would be the same from the first string to the second string (1). To that end we define the Levenshtein Combinator.

Definition 1 (Levenshtein Combinator). Assume that $d: (T \times T) \to \mathbb{R}^{\geq 0}$ is a metric. Suppose further that κ is any positive real. Then we say the Levenshtein Combinator of d is Lev $_d: (List\ T \times List\ T) \to \mathbb{R}^{\geq 0}$. Such that it is defined on lists of T. We define the combinator as:

$$Lev_d(a,b) = \begin{cases} \kappa |a[1:]| & |b| = 0\\ \kappa |b[1:]| & |a| = 0 \end{cases}$$

$$Lev_d(a,b[1:]) + \kappa$$

$$Lev_d(a,b[1:]) + \kappa$$

$$Lev_d(a[1:],b[1:]) + d(a[0],b[0])$$
otherwise.

The Levenshtein Combinator runs almost the same as the traditional Levenshtein edit distance. The only differences are the generalizations of the κ from 1, and the addition of the metric between elements of the list. In fact, the original Levenshtein distance can be recovered by substituting 1 for κ , and the characteristic function $1_{a\neq b}$ as the d metric. We will now show that the Levenshtein combinator of a metric is itself a metric.

Identity of indiscernibles and symmetry are pretty obvious, and so are omitted. The triangle inequality also follows in a similar manner as the proof of traditional levenshtein [2]. Suppose we are considering a transformation between lists X and Z, that is a series of insertion, deletions, and substitutions. A transformation from X to some Y followed by a transformation from X to some Z is a transformation from X to Z. As the transformation from X to Z is the minimal transformation, it follows $d(X,Z) \leq d(X,Y) + d(Y,Z)$.

3.2 Linear Combinator

We will now briefly show that the linear combination of metrics is a metric. Suppose we have a metric $d(a,b) = \sum c_i d_i(a,b)$, where c_i is a positive real number, and d_i is a metric. Symmetry follows clearly.

Identity of indescernables follows as each term goes to zero, leaving the sum at zero. The triangle inequality follows $d(a,b) = \sum c_i d_i(a,b) \le \sum c_i d_i(a,c) + c_i d_i(a,b) = d(a,c) + d(b,c)$.

3.3 Alteration

Suppose that we have a tuple (n, v), where n is some natural number less than some N, and a mapping $f: n \to (v \times v \to \mathbb{R})$. Then we can define the alteration combinator on these tuples.

Definition 2 (Alteration Combinator). Let $T = E \times V$, such that E is some finite set of objects, and V is any other set of objects. Let $f: E \to (V \times V \to \mathbb{R})$ be a relation, such that for all e in E, we have (fe) restricted to $\{(d,v) \in T: d=e\}$ is a metric on that restriction. Furthermore, let $\kappa \in \mathbb{R}^+$. Then we define the alteration combinator $Alt: f \to T \times T \to \mathbb{R}^{\geq 0}$

$$Alt(f, ((e_1, v_1), (e_2, v_2))) = \begin{cases} \min([fe_1](v_1, v_2), \kappa) & e_1 = e_2 \\ \kappa & otherwise. \end{cases}$$

Symmetry, and identity of indiscernables is pretty straightforward. The triangle inequality for Alt(f), is a little trickier. We consider four cases. Let A, B, and C all be in E. We can consider the triangle inequality as triple of three of these types, and ask where it will hold. If all three are of the same type (A, A, A), then the inequality is inherited by that of (fA). Consider (A, A, B), then the inequality can be seen $(fA)(A, A) \le \kappa \le (fA)(A, A) + \kappa \le (fA)(A, A) + Alt(f)(A, B)$ Consider (A, B, B), then the inequality can be seen $(fA)(A, B) = \kappa \le \kappa + (fB)(B, B)$. Consider (A, B, C), then the inequality obviously holds.

3.4 From Types To Metrics

$$\frac{x: \text{List } T \quad y: \text{List } T}{\text{Lev}_T(x,y)} \text{ Lists} \qquad \frac{x: (T_1, T_2, \dots, T_n) \quad y: (T_1, T_2, \dots, T_n)}{\sum_{i=0}^n c_i d_{T_i}(x_i, y_i)} \text{ Products}$$

$$\frac{x:T_1|T_2|\dots|T_n}{1_{\text{type}(x)=\text{type}(y)}\min(\kappa,d_{\text{type}(x)}(x,y))+1_{\text{type}(x)\neq\text{type}(y)}\kappa}\text{ Sums }\frac{x:\text{Map }T_1\quad T_2}{\dots}\text{ Map }x:T_1\qquad y:\text{Number }x:T_1\qquad y:\text{Number }x:T_1$$

4 Example: Go Code Look Up

4.1 Generics

5 Metric Trees

Metric trees are an efficient way to search for object based on some metric.

- 6 Implementation
- 7 Related Work
- 8 Future Work
- 8.1 Best Approximation
- 9 Conclusion

References

[1] Wikipedia contributors. levenshtein distance, 2020. [Online; accessed 19-April-2020].

 $[2]\,$ Jeremy Kun. Metrics on words, May 2014.