Metric Learning

Why metric learning

Similarity

Unsupervised Learning

More Classes

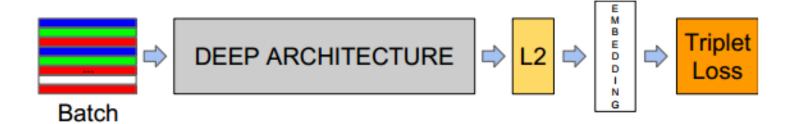
Learning Distance Metrics

$$d(x,y) = d_A(x,y) = ||x-y||_A = \sqrt{(x-y)^T A(x-y)}.$$

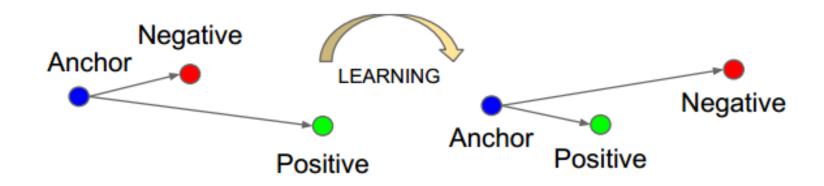
$$\min_{A} \quad \sum_{(x_i, x_j) \in \mathcal{S}} ||x_i - x_j||_A^2$$
s.t.
$$\sum_{(x_i, x_j) \in \mathcal{D}} ||x_i - x_j||_A \ge 1,$$

$$A \succeq 0.$$

FaceNet



Triplet Loss



$$||x_i^a - x_i^p||_2^2 + \alpha < ||x_i^a - x_i^n||_2^2, \forall (x_i^a, x_i^p, x_i^n) \in \mathcal{T}.$$

$$\sum_{i=1}^{N} \left[\|f(x_i^a) - f(x_i^p)\|_2^2 - \|f(x_i^a) - f(x_i^n)\|_2^2 + \alpha \right]_{+}$$



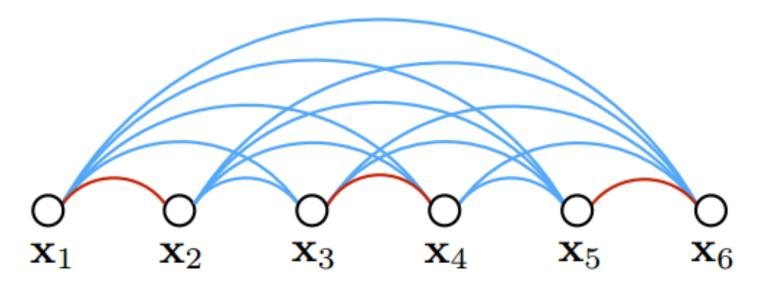
(a) Contrastive embedding

$$J = \frac{1}{m} \sum_{(i,j)}^{m/2} y_{i,j} D_{i,j}^2 + (1 - y_{i,j}) \left[\alpha - D_{i,j} \right]_+^2$$



(b) Triplet embedding

$$J = \frac{3}{2m} \sum_{i=1}^{m/3} \left[D_{ia,ip}^2 - D_{ia,in}^2 + \alpha \right]_{+}$$



(c) Lifted structured embedding

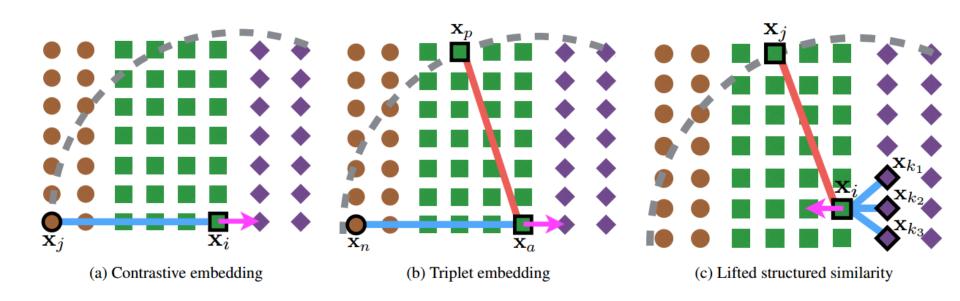
$$\begin{split} J = & \frac{1}{2|\widehat{\mathcal{P}}|} \sum_{(i,j) \in \widehat{\mathcal{P}}} \max\left(0, \ J_{i,j}\right)^2, \\ J_{i,j} = & \max\left(\max_{(i,k) \in \widehat{\mathcal{N}}} \alpha - D_{i,k}, \max_{(j,l) \in \widehat{\mathcal{N}}} \alpha - D_{j,l}\right) + D_{i,j} \end{split}$$

$$J = \frac{1}{2|\widehat{\mathcal{P}}|} \sum_{(i,j)\in\widehat{\mathcal{P}}} \max(0, J_{i,j})^{2},$$

$$J_{i,j} = \max\left(\max_{(i,k)\in\widehat{\mathcal{N}}} \alpha - D_{i,k}, \max_{(j,l)\in\widehat{\mathcal{N}}} \alpha - D_{j,l}\right) + D_{i,j}$$

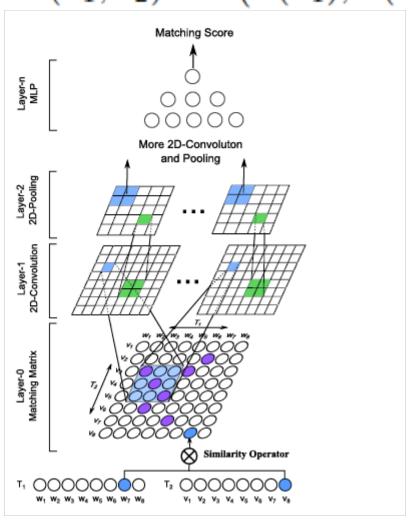
$$\tilde{J}_{i,j} = \log \left(\sum_{(i,k)\in\mathcal{N}} \exp\{\alpha - D_{i,k}\} + \sum_{(j,l)\in\mathcal{N}} \exp\{\alpha - D_{j,l}\} \right) + D_{i,j}$$

$$\tilde{J} = \frac{1}{2|\mathcal{P}|} \sum_{(i,j)\in\mathcal{P}} \max\left(0, \ \tilde{J}_{i,j}\right)^{2}, \tag{4}$$



Text Matching as Image Recognition

$$\operatorname{match}(T_1, T_2) = \operatorname{F}(\Phi(T_1), \Phi(T_2))$$



Text Matching as Image Recognition

$$\mathbf{M}_{ij} = \mathbb{I}_{\{w_i = v_j\}} = \begin{cases} 1, & \text{if } w_i = v_j \\ 0, & \text{otherwise.} \end{cases}$$

$$\mathbf{M}_{ij} = \frac{\vec{\alpha_i}^{\top} \vec{\beta_j}}{\|\vec{\alpha_i}\| \cdot \|\vec{\beta_j}\|}$$

$$\mathbf{M}_{ij} = \vec{\alpha_i}^{\top} \vec{\beta_j}.$$

Summary

Thanks

References:

- [1] Distance Metric Learning, with Application to Clustering with Side-Information
- [2] FaceNet: A Unified Embedding for Face
- **Recognition and Clustering**
- [3] Deep Metric Learning via Lifted Structured
- **Feature Embedding**
- [4] Text Matching as Image Recognition