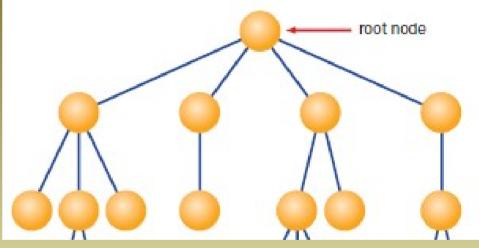




- Generalization of a linked structure
- Has 2 or more links instead of 1 link
 - Binary Tree 2 links
- Operations vary depending on application but usually include:
 - Adding a node to the tree
 - Removing a node from the tree



- Similar to a linked list, contains a reference to the top called the root of the tree
- Recursive structure Tree is either
 - Empty / null
 - Node with N links, all of which are Trees



A visual representation of a tree.

The top node is also called the root node.

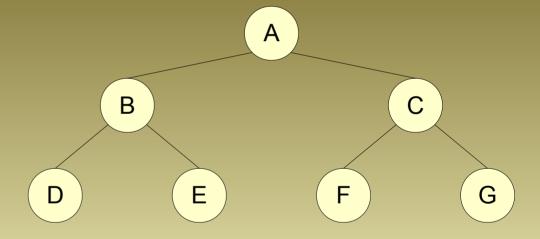
Java Software Solutions



- A binary tree is either:
 - Empty / null
 - Binary tree node with left and right subtrees that are also binary trees
- Any binary tree node has
 - at most 2 children / subtrees
 - At most 1 parent / ancestor



- Root: A
- Parents: A B C
- Children: B C D E F G
- Leaf: DEFG
- Subtrees: (left root right)
 - (DBE)
 - (FCG)

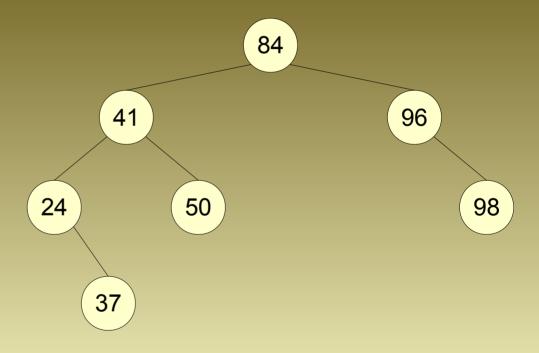




Binary Search Tree

2nd Semester 2008-2009

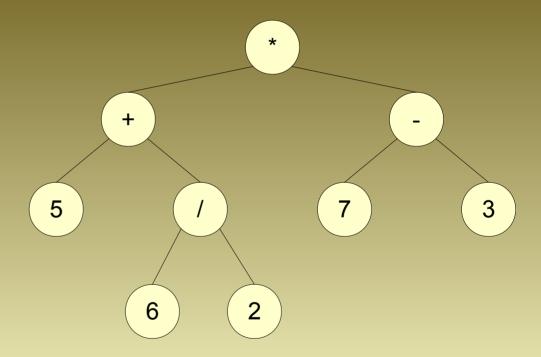
- All items in the left subtree of any node are smaller than the value at that node
- All items in the right subtree of any node are larger than the value at that node





Expression Tree

- Used to evaluate the value of an expression
- Left sub tree and right subtree of a node are operands of the operator at that node





- Implementation
 - Arrays
 - Linked Structures



```
– public class BTNode {
    private BTNode left = null;
    private BTNode right = null;
    private Object data = null;
    public BTNode( Object data ) {
     this.left = null;
     this.right = null;
     this.data = data;
```



```
public BTNode getLeft() {
 return this.left;
public BTNode getRight() {
 return this.right;
public Object getData() {
 return this.data;
public void setLeft( BTNode left ) {
 this.left = left;
```



```
public void setRight( BTNode right ) {
   this.right = right;
}
public void setData( Object data ) {
   this.data = data;
}
```



```
- public class BinaryTree {
    private BTNode root;
    public BinaryTree() {
        this.root = null;
    }
    private BinaryTree( BTNode root ) {
        this.root = root;
    }
```

Private helper constructor.



```
public BinaryTree (BinaryTree leftTree, BinaryTree rightTree,
                   Object data) {
 root = new BTNode( data );
 if( leftTree != null ) {
  root.setLeft( leftTree.root );
 if( rightTree != null ) {
  root.setRight( rightTree.root );
```



```
public boolean isEmpty() {
  return root == null;
}
public BinaryTree getLeftSubtree() {
  if( isEmpty() ) {
    return null;
  }
  return new BinaryTree( root.getLeft() );
}
```



```
public BinaryTree getRightSubtree() {
 if( isEmpty() ) {
  return null;
 return new BinaryTree( root.getRight() );
public Object getData() {
 if( isEmpty() ) {
  return null;
 return root.getData();
```



Preorder

- Visit the root
- Perform preorder traversal of the left subtree
- Perform preorder traversal of the right subtree

Inorder

- Perform inorder traversal of the left subtree
- Visit the root
- Perform inorder traversal of the right subtree

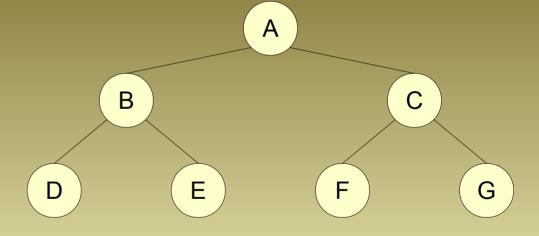


- Postorder
 - Perform postorder traversal of the left subtree
 - Perform postorder traversal of the right subtree
 - Visit the root
- Traversals are recursive!



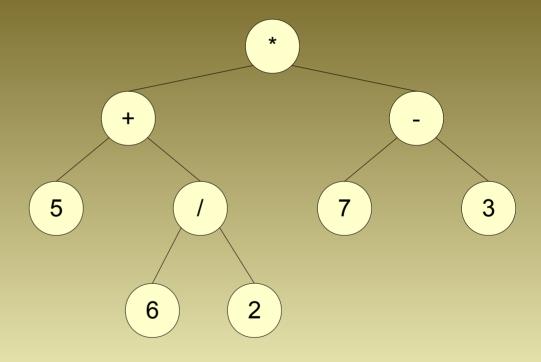
• Example:

- Preorder: ABDECFG
- Inorder: DBEAFCG
- Postorder: D E B F G C A



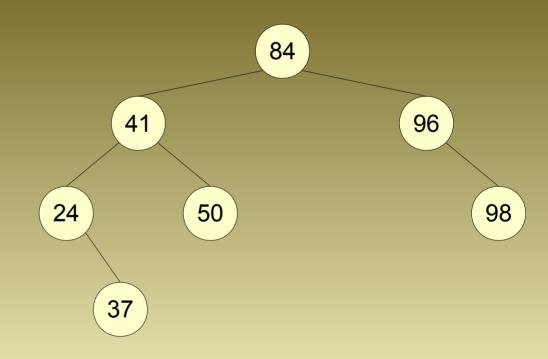


 What does the post order traversal of an expression tree yield?





 What does the inorder traversal of a binary search tree yield?





```
– public String preorder( BinaryTree aTree ) {
    String result = "";
   if( aTree.isEmpty() ) {
    else {
     result = aTree.root.getData().toString();
     result += preorder( aTree.getLeftSubtree() );
     result += preorder( aTree.getRightSubtree() );
    return result;
```

Binary Trees

```
– public String preorder() {
    return preorder(this);
– public String preorder2() {
    if( isEmpty() ) {
     return "";
    else {
     return this.getLeftSubtree().preorder() + this.getData().toString() +
            this.getRightSubtree().preorder();
```

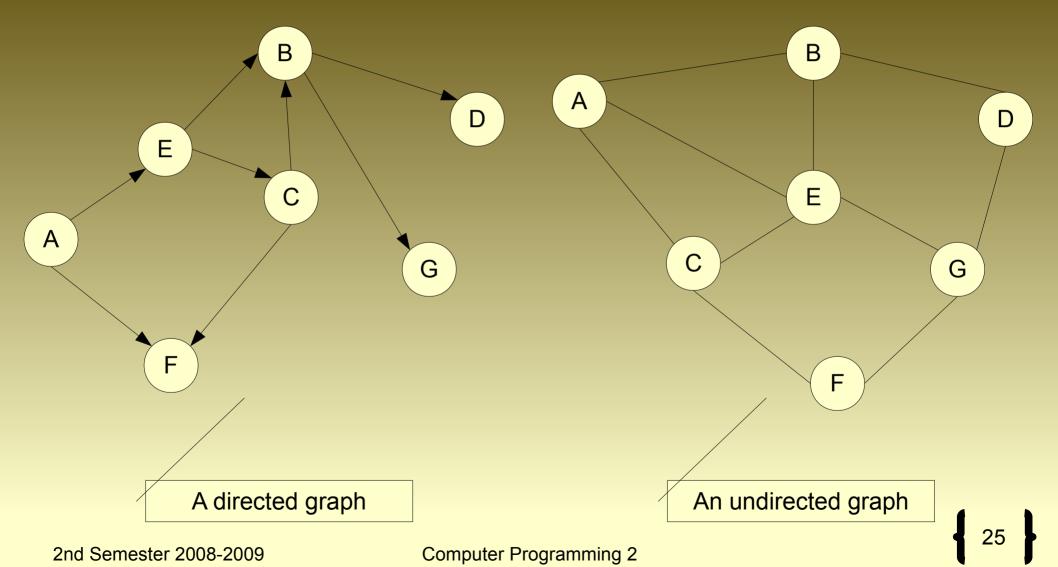


- Like a tree but has no primary entry point / root node
- Composed of:
 - Nodes / Vertices
 - Links / Edges
- Generally no restriction on the number of edges that connect nodes



- 2 types according to connection:
 - Undirected: if Node 1 is connected to Node 2, Node 2 is connected to Node 1
 - Directed: if Node 1 is connected to Node 2, Node 2 is NOT necessarily connected to Node 1
- Applications:
 - Transportation
 - Networks







Implementation

- Arrays: use an adjacency matrix
 - Value at row i and column j indicates connection or cost of connection between node i and column j
 - Usually adjMatrix[i][j] > 0 if node i is connected to node j
 - If undirected adjMatrix[i][j] and adjMatrix[j][i] are equal
- Linked Structures



```
– public class ArrayGraph {
     private int adjMatrix[][];
     public ArrayGraph( int numVertices ) {
      adjMatrix = new int[numVertices][numVertices];
     public int getEdge( int node1, int node2 ) {
      return adjMatrix[node1][node2];
     public void setEdge( int node1, int node2, int value ) {
      adjMatrix[node1][node2] = value;
```



• Problems:

- Path finding
 - Node A and Node B are connected by a path if there exists a set of edges that can be followed from Node A to Node B
- Shortest Path
 - Minimum cost of path from Node A to Node B
- Minimum Spanning Tree
 - Minimum cost/number of edges needed to connect all vertices in a graph. (i.e. all other vertices are reachable from any vertex)



- Class can be declared inside a class
 - Similar to how a loop can be declared inside a loop (nested loop)
- Produces separate bytecode file with the following name: EnclosingClass\$NestedClass.class
- Enclosing class can access attributes
- Used to put implementation classes inside class which use them (encapsulation)



Two types:

- Inner Classes (Non-static)
 - Associated with an instance of the enclosing class
 - No member inside can be declared static (child can only exist if parent exists)
- Static nested classes
 - NOT associated with an instance of the enclosing class
 - Cannot access instance (non-static) attributes and functions



Redefine BinaryTree:

```
– public class BinaryTree {
    private static class BTNode {
     private Object data = null;
     private BTNode left = null;
     private BTNode right = null;
     private BTNode( Object data ) {
      this.left = null;
      this.right = null;
      this.data = data;
```

Use static nested class if enclosing class depends on nested class but not vice versa. BTNode is a SHARED blueprint among BinaryTrees

If class is private, attributes may be declared public without breaking information hiding

Nested Classes

```
private BTNode root;
public BinaryTree() {
  root = null;
}
private BinaryTree( BTNode root ) {
  this.root = root;
}
```

End of BTNode class definition. No need for getters and setters since enclosing class can access the attributes directly.



public BinaryTree (BinaryTree leftTree, BinaryTree rightTree,

```
Object data ) {
root = new BTNode( data );
if( leftTree != null ) {
  root.left = leftTree.root;
}
if( rightTree != null ) {
  root.right = rightTree.right;
}
```

If BTNode were declared not as a nested class, root.left and root.right wouldn't be accessible unless they were declared public

Nested Classes

```
public boolean isEmpty() {
  return root == null;
}

public BinaryTree getRightSubtree() {
  if( isEmpty() ) {
    return null;
  }

return new BinaryTree( root.right );
}
```

Nested Classes

```
private BinaryTree getLeftSubtree() {
 if( isEmpty() ) {
  return null;
 return new BinaryTree( root.left );
public Object getData() {
 if( isEmpty() ) {
  return null;
 return root.data;
```



- Allow writing safe and easy code without Objects and casts
 - Problems with using Object
 - Need typecast
 - Allow adding any type. No automatic checking
- Write classes that are type customizable
- Particularly useful for abstract data types / collections
- Way to implement/use homogeneous collections



Without generics:

- ArrayList names = new ArrayList();
- names.add("Rose");
- names.add("Enzo");
- String aName1 = (String) names.get(0);
- names.add(new Integer(1234567890));
- String aName2 = (String) names.get(2);

Need to typecast objects retrieved since their type is Object.

Causes a
ClassCastException.
Since ArrayList uses
Object, all types may
be added and
sometimes they are
not the expected type.



With generics:

- ArrayList<String> names = new ArrayList<String>();
- names.add("Enzo");
- names.add("Rose");
- String aName = names.get(0);
- names.add(new Integer(1234567890));

A homogenous ArrayList. Can only work on Strings.

No need for a typecast.

Causes a compiler error. Neat.



- Defining a generic class:
 - Append type variable(s) to class name
 class. Type names can be any valid name but typically use only 1 letter.
 - ClassName<type1,type2,...,typeN>
 - Use the type to define:
 - Type of attributes/variables
 - Type of method parameters
 - Method return type
- Object allocation
 2nd Semester 2008-2009



Example:

```
- public class Pair<T> {
    private T first;
                                                       T used to define type
                                                            of attributes.
    private T second;
    public Pair( T first, T second ) {
     setFirst( first )
     setSecond( second );
                                                       T used to define return
                                                          type of method.
    public T getFirst() {
     return this.first;
```



```
public T getSecond() {
 return this.second;
public void setFirst( T first ) {
 this.first = first;
public void setSecond( T second ) {
 this.second = second;
```

T used to define type of method parameters.



Redefining BinaryTree again:

```
– public class BinaryTree<E> {
    private class BTNode<E> {
     private E data = null;
     private BTNode<E> left = null;
     private BTNode<E> right = null;
     private BTNode(E data) {
      this.data = data;
```



```
private BTNode<E> root;
public BinaryTree() {
  root = null;
}
private BinaryTree( BTNode<E> root ) {
  this.root = root;
}
```



```
public BinaryTree( BinaryTree<E> leftTree,
                   BinaryTree<E> rightTree<E>, E data ) {
 root = new BTNode<E>(data);
 if( leftTree != null ) {
  root.left = leftTree.root;
 if( rightTree != null ) {
  root.right = rightTree.root;
```



```
public boolean isEmpty() {
  return root == null;
}
public BinaryTree<E> getRightSubtree() {
  if( isEmpty() ) {
    return null;
  }
  return new BinaryTree<E>(root.right);
}
```



```
public BinaryTree<E> getLeftSubtree() {
 if( isEmpty() ) {
  return null;
 return new BinaryTree<E>(root.left);
public E getData() {
 if( isEmpty() ) {
  return null;
  return root.data;
```



```
– public class GenericTreeTest {
    public static void main( String args[] ) {
     BinaryTree<Integer> left = new BinaryTree<Integer>(null,null,2);
     BinaryTree<Integer> right = new BinaryTree<Integer>(null,null,3);
     BinaryTree<Integer> aTree = new BinaryTree<Integer>(left,right,1);
     System.out.println(aTree.getData());
     System.out.println(aTree.getLeftSubtree().getData());
     System.out.println(aTree.getRightSubtree().getData());
```



 In general, GenericClass<A> cannot be assigned to GenericClass even if B is a subclass of A (B extends A).

Example:

- ArrayList<String> stringList = new ArrayList<String>();
- ArrayList<Object> objList = stringList; Compiler will be upset.
- Also, parametized type cannot be a primitive.
 - ArrayList<int> intList = new ArrayList<int>();



- Proof: (Assume class Charizard extends Pokemon)
 - ArrayList<Charizard> cList = new ArrayList<Charizard>();
 - ArrayList<Pokemon> pList = cList;
 - pList.add(new Pokemon());
 - Charizard aCharzard = cList.get(0);

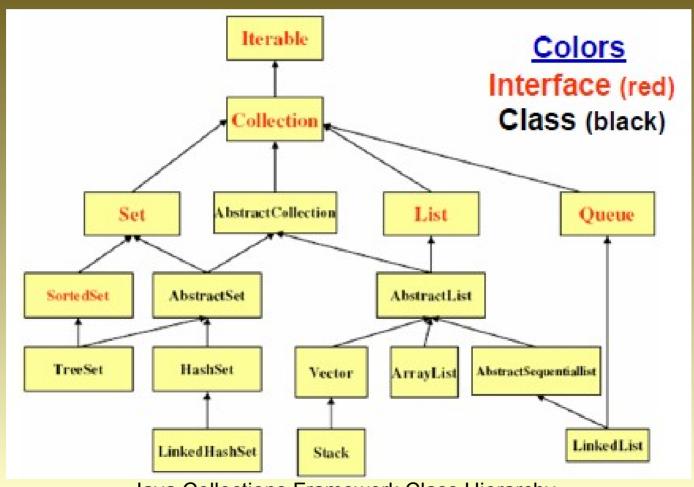
Pokemon will be added to the list of Charizards.

Error! A Pokemon will be retrieved and assigned to a Charizard object but not all Pokemon's are Charizards.



- Generic capable collections
- Consists of:
 - Interfaces/Abstract Classes
 - Define behaviors of a collection
 - Implementation
 - Concrete classes that extend/implement the interfaces
 - Algorithms
 - Generic operations that can be performed on collections

Java Collections



Java Collections Framework Class Hierarchy.
University of Maryland
Computer Programming 2



- Separating interface from implementation
 - Use concrete class only when constructing the object. Use interface class to hold the object reference
 - List<Integer> aList1 = new LinkedList<Integer>();
 - List<Double> aList2 = new ArrayList<Double>();
 - Queue<String> aQueue = new LinkedList<String>();



 All collections have an iterator. Use iterator interface to traverse a whole Collection. It has three methods:

```
public interface Iterator<E> {
    E next();
    boolean hasNext();
    void remove();
}
```

An iterator can process an element only after "skipping" (see example)

Java Collections

Example (traversing a collection):

```
Collection<String> aCollection = new LinkedList<String>();
Iterator<String> anIter = aCollection.iterator();
while(anIter.hasNext()) {
   String curString = anIter.next();
   //do something with curString
   System.out.println( curString );
}
```



Example (traversing a collection using a for each loop):

```
for( String curString: aCollection ) {
  //do something with curString
  System.out.println( curString );
}
```

Read as, for each string in aCollection. Call the current element as curString.



```
Example (removing an element):
```

```
anlter.next();
```

anlter.remove();

Example (removing two elements):

```
anlter.next();
```

anlter.remove();

anlter.next();

anlter.remove();

Can't call remove immediately. Must "skip" before removing.



Collection vs Collections

- Collection
 - Parent/root interface of collection classes
 - Methods: add, contains, remove, size
- Collections
 - Class which contains static methods that operate on collections
 - Methods: binarySearch, copy, fill, max, min, sort, shuffle