

Principles of Galaxy Structure

Balance between gravity and...

Angular momentum (rotation)

Random motions ("dynamical pressure")

Disks and spheroids will typically obey straightforward scaling relations, controlled by fairly simple dynamics

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Principles of Galaxy Structure

Mix of nature vs nurture

Properties of initial overdensity + statistical properties of surrounding density field set mass, angular momentum, time of collapse+accretion, to first order (for a given dark matter model)

Internal evolution (instabilities), specifics of mergers, feedback from SNe+AGN, further shape structure.

x

Principles of Galaxy Structure

- Initial overdensity
- Statistical properties of surrounding density field

- Mass
- Angular momentum
- Timing of collapse & subsequent accretion

Nature

Galactic structure

- Merging history
- Feedback from star formation & AGN
- Internal dynamics (instabilities, scattering, diffusion)

Nurture

2

Today

- Initial overdensity
- Statistical properties of surrounding density field

- Mass
- Angular momentum
- Timing of collapse & subsequent accretion

Nature

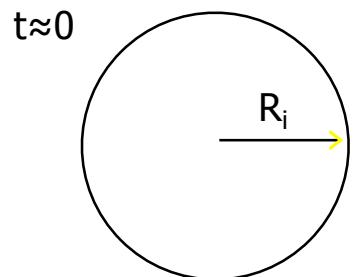
Galactic structure

- Merging history
- Feedback from star formation & AGN
- Internal dynamics (instabilities, scattering, diffusion)

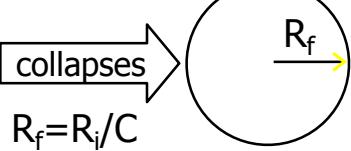
Nurture

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Some simple but useful scalings



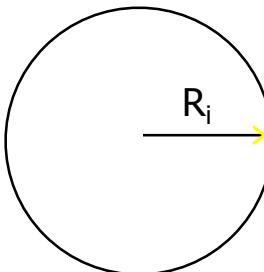
$t = \text{now}$



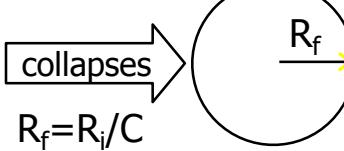
$$\text{Mass } M \sim \rho(t \approx 0) R_i^3$$

Density of the early universe, which can be assumed to be fairly uniform

$t \approx 0$



$t = \text{now}$

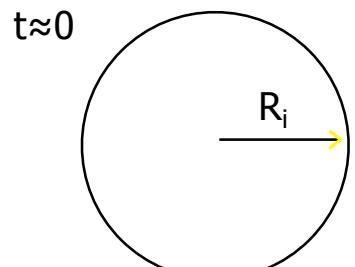


$$\text{Mass } M \sim \rho(t \approx 0) R_i^3$$

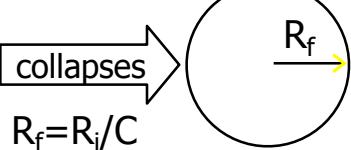
$$\begin{aligned} R_f &\sim R_i/C \\ &\sim (M/\rho)^{1/3} / C \\ &\sim M^{1/3} (C^{-1} \rho^{-1/3}) \end{aligned}$$

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So size increases as $M^{1/3}$



$t = \text{now}$



$$\text{Mass } M \sim \rho(t \approx 0) R_i^3$$

Density of the early universe, which can be assumed to be fairly uniform

$$\begin{aligned} \Sigma &\sim M / R_f^2 \\ &\sim C^2 M / R_i^2 \\ &\sim C^2 M / (M/\rho)^{2/3} \\ &\sim M^{1/3} (C^2 \rho^{2/3}) \end{aligned}$$

So surface density and size both increase as $M^{1/3}$

Broadly:

$$\begin{aligned} R_f &\sim R_i/C \\ &\sim (M/\rho)^{1/3} / C \\ &\sim M^{1/3} (C^{-1} \rho^{-1/3}) \end{aligned}$$

$$\begin{aligned} \Sigma &\sim M / R_f^2 \\ &\sim C^2 M / R_i^2 \\ &\sim C^2 M / (M/\rho)^{2/3} \\ &\sim M^{1/3} (C^2 \rho^{2/3}) \end{aligned}$$

- At same collapse factor C , the radius R and surface density Σ increase like $M^{1/3}$
- Within similar formation pathways, more massive galaxies will tend to be physically larger and higher surface density

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Broadly:

$$R_f \sim R_i/C$$

$$\sim (M/\rho)^{1/3} / C$$

$$\sim M^{1/3} (C^{-1} \rho^{-1/3})$$

$$\Sigma \sim M / R_f^2$$

$$\sim C^2 M / R_i^2$$

$$\sim C^2 M / (M/\rho)^{2/3}$$

$$\sim M^{1/3} (C^2 \rho^{2/3})$$

- At same mass, larger collapse factors lead R to decrease and Σ to increase
- Larger collapse factors result from:
 - Less initial spin, when the collapse is halted by angular momentum
 - More dissipation, when collapse is halted by dynamical pressure (velocity dispersion)

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Broadly:

$$R_f \sim R_i/C$$

$$\sim (M/\rho)^{1/3} / C$$

$$\sim M^{1/3} (C^{-1} \rho^{-1/3})$$

$$\Sigma \sim M / R_f^2$$

$$\sim C^2 M / R_i^2$$

$$\sim C^2 M / (M/\rho)^{2/3}$$

$$\sim M^{1/3} (C^2 \rho^{2/3})$$

- At the same mass and formation pathway, galaxies that collapsed from higher characteristic initial densities will be denser and more compact.
- Initial density dependence can potentially imprint a timing+environmental bias (Larger overdensities collapse faster, starts denser, forms earlier)

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Now look at:

Global Trends in Size, Surface Brightness & Magnitude

Scale Lengths

Surface brightnesses

Size vs Surface Brightness

Basic scaling relations with mass

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1. Faint galaxies are smaller

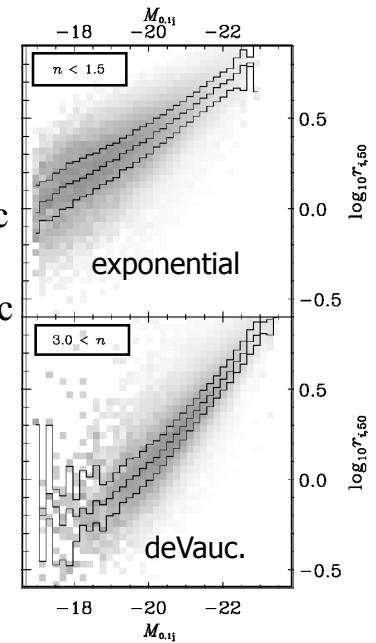
Massive Ellipticals: $r_{50} \sim 10$ kpc

Massive Spirals: $r_{50} \sim 5-8$ kpc

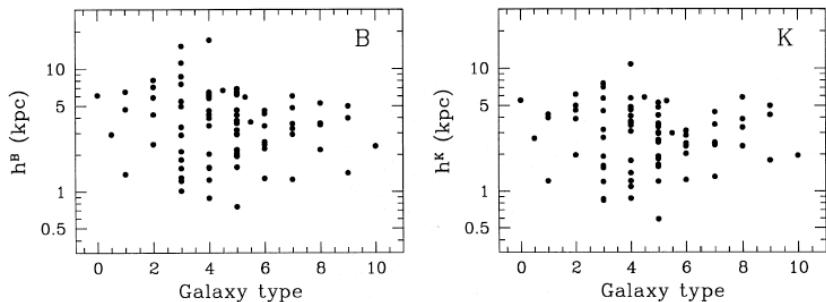
Dwarfs: $r_{50} \sim 1$ kpc

Blanton et al 2003 (r_{50} in h^{-1} kpc)

This analysis corrects for relative numbers. At each absolute magnitude, the vertical grayscale indicates the relative distribution of sizes.



Sizes of Large Spiral Disks



Milky Way has $h_r \sim 2.5\text{-}3.5$ kpc

Note: this is just one particular sample, and is not necessarily representative of the entire disk galaxy population!

(Warning: H_0 varies in older papers!)

de Jong 1996

Sizes of Gas Rich Dwarf Galaxies

Again, not representative of the whole population -- just an indication of the general sizes you'd find.

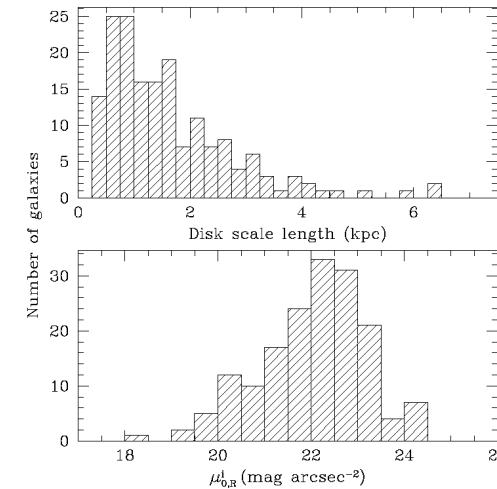


Fig. 15. The distribution of scale lengths (top panel) and of inclination corrected central surface brightnesses for the galaxies in our sample.

Swaters & Balcells 2002

2. Fainter Galaxies have lower surface brightnesses

But, the magnitude-surface brightness relation distribution is wide.

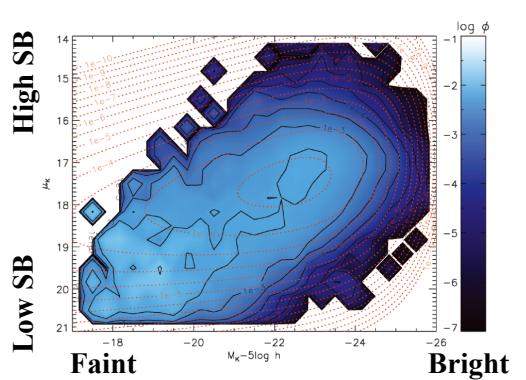


Figure 11. BBD for the full sample in K -band absolute magnitude and absolute effective surface brightness. Shaded regions and solid black contours show the space density, ϕ , as in Fig. 10. The best-fitting Choloniewski function, estimated using $M_K - 5 \log h < -20$ and $\mu_{e,\text{abs}} < 19$, is shown by the red dotted contours. Parameters of the fit are $M^* = 5 \log h = -22.96$ mag, $\alpha = -0.38$, $\phi^* = 0.0201 h^3 \text{Mpc}^{-3}$, $\mu_{e,\text{abs}}^* = 17.36 \text{mag arcsec}^{-2}$, $\sigma_{\mu_{e,\text{abs}}} = 0.672 \text{mag arcsec}^{-2}$ and $\beta = 0.188$.

Broad trend does agree with expected scaling

Surface density and size both increase as $M^{1/3}$

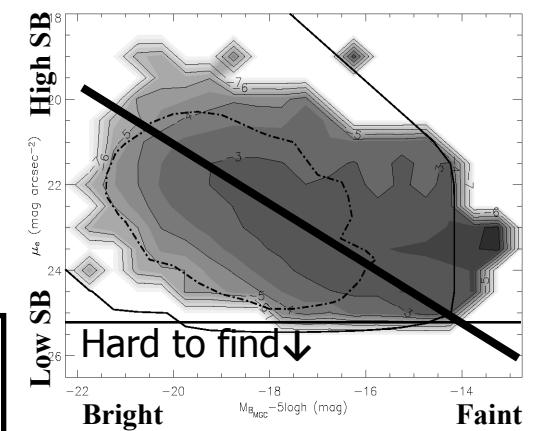
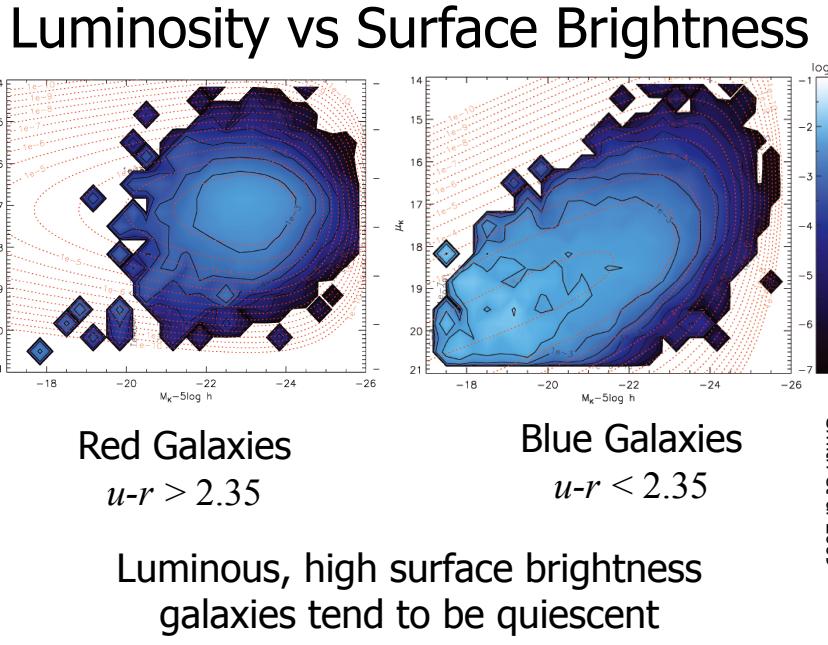


Figure 12. The final space density or bivariate brightness distribution of galaxies shown as both a greyscale image and contours on logarithmic scales in units of $h^3 \text{Mpc}^{-3} \text{mag arcsec}^{-2}$. The contour spacing is 1 dex in ϕ with the greyscale at 0.5 dex intervals. The thick solid line denotes the selection boundary defined as the BBD region where at least 100 galaxies could have been detected and is equivalent to an effective volume limit of $1800 h^{-3} \text{Mpc}^3$. The thick dashed line encompasses the region within which the statistical error is smaller than 25 per cent.

Watch selection effects!

(“BBD”=bivariate brightness distribution)

Smith et al 2009



Fainter
Galaxies have
lower surface
brightnesses

But, the magnitude-surface brightness relation distribution is wide.

Watch selection effects!

(“BBD”=bivariate brightness distribution) Driver et al 2005

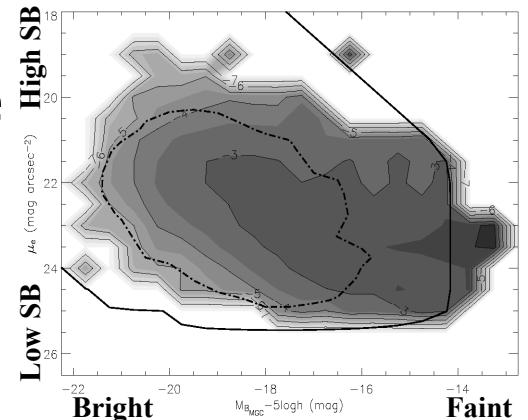
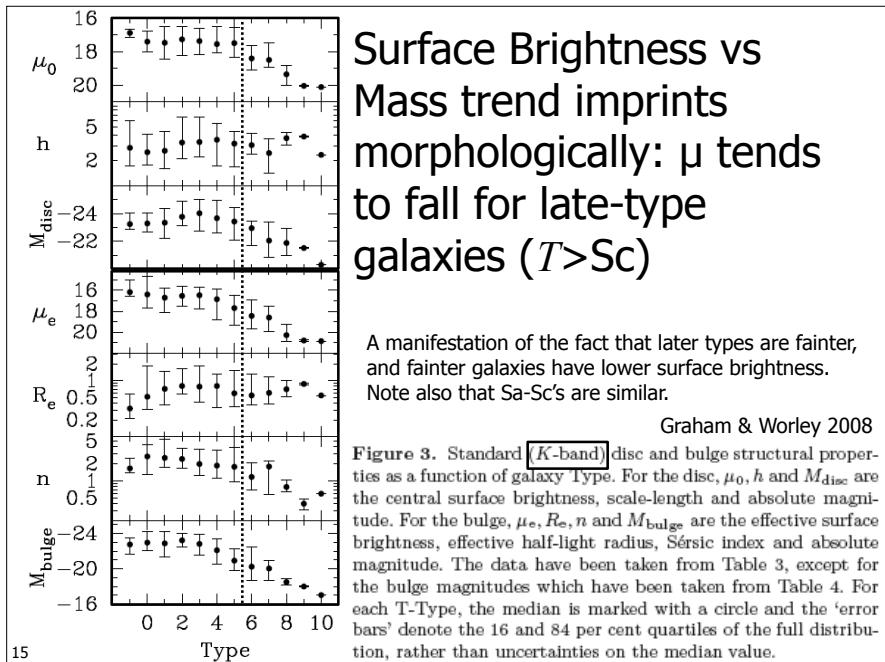


Figure 12. The final space density or bivariate brightness distribution of galaxies shown as both a greyscale image and contours on logarithmic scales in units of $h^3 \text{ Mpc}^{-3} \text{ mag}^{-1}$ (mag arcsec^{-2}) $^{-1}$. The contour spacing is 1 dex in ϕ with the greyscale at 0.5 dex intervals. The thick solid line denotes the selection boundary defined as the BBD region where at least 100 galaxies could have been detected and is equivalent to an effective volume limit of $1800h^{-3}\text{Mpc}^3$. The thick dashed line encompasses the region within which the statistical error is smaller than 25 per cent.



3. Disk Scale Length vs Surface Brightness

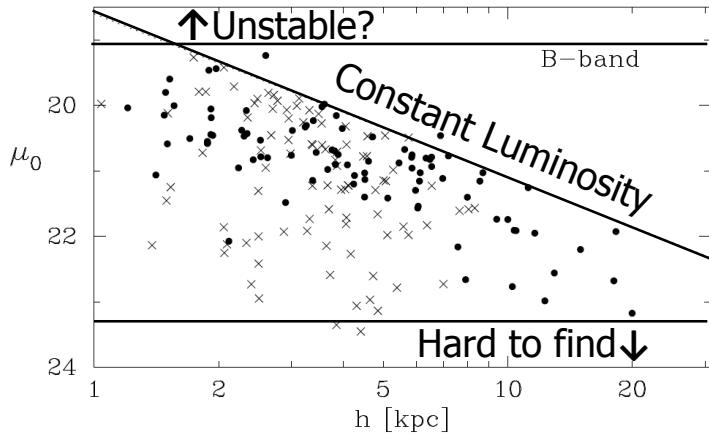
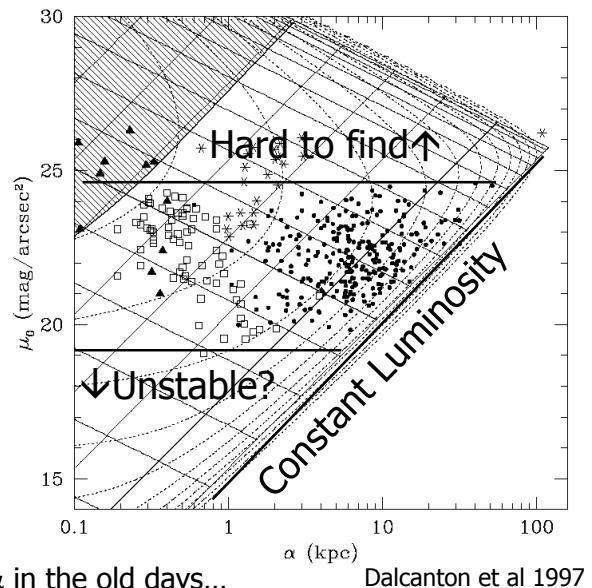


Figure 9. B-band, Central disc surface brightness (corrected using equation 1) versus disc scalelength (corrected using equation 2). Rather than a Freeman (1970) law of constant surface brightness, an outer bright envelope, which has been seen before (Graham 2002, and references therein). The empirically-fitted dotted line in this diagram is such that $\mu_0, \text{bright} = 18.6 + 2.5 \log h$. Galaxy types Sbc ($T = 4$) and earlier are denoted by circles, while later galaxy types are denoted by crosses. The noticeably broader distribution for the late-type disc galaxies has also been noted before (Graham & de Blok 2001).

Revisiting Structural Parameters

Data from a wide variety of sources.
(Don't attach meaning to the relative density of points)

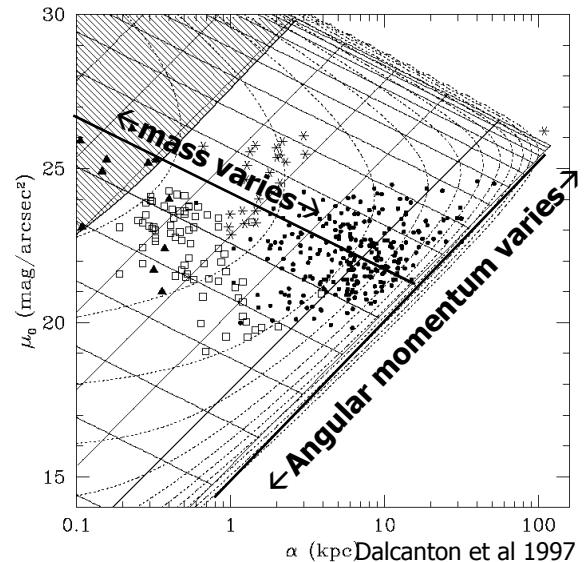
h_r used to be called α in the old days...



Dalcanton et al 1997

Dissipational Collapse, halted by angular momentum

Existence and slope of Luminosity-Surface brightness relationship, and diagonal upper limit in h_r vs μ_0 consistent with dissipational collapse halted by angular momentum



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Broadly:

$$R_f \sim R_i/C$$

$$\sim (M/\rho)^{1/3} / C$$

$$\sim M^{1/3} (C^{-1} \rho^{-1/3})$$

$$\Sigma \sim M / R_f^2$$

$$\sim C^2 M / R_i^2$$

$$\sim C^2 M / (M/\rho)^{2/3}$$

$$\sim M^{1/3} (C^2 \rho^{2/3})$$

But

This is far from the whole picture.
Internal evolution?, Feedback?, etc

These may have their own internal scalings with mass, and some self-regulation that keeps overall scaling intact.

For example,
at high disk
surface
densities, you
make bulges
instead.

Horizontal line is at
same μ_e for $n=1$

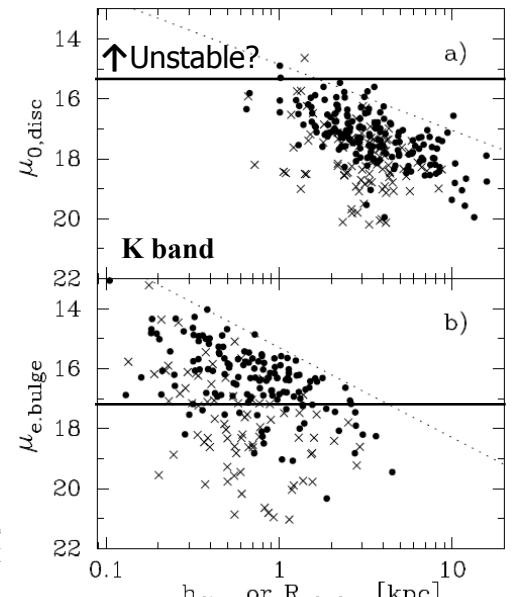


Figure 8. K-band. Top panel: Central disc surface brightness (corrected using equation 1) versus disc scalelength h (corrected using equation 2). Bottom panel: Bulge effective surface brightness (observed) versus the bulge effective radius R_e (observed). The upper bright envelope is traced here with the (empirical) lines $\mu_{0,bright} = 14.85 + 2.2 \log h$ (panel a) and $\mu_{e,bright} = 15.3 + 3.0 \log R_e$ (panel b). Galaxy types Sbc ($T = 4$) and earlier are denoted by the circles, while later galaxy types are denoted by the crosses.

Graham & Worley 2008

What controls vertical surface brightness distributions?



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Vertical Structure of Disks

Exponential at large scale heights

Different possible structures at midplane

Profile set by balance of gravity and dynamical pressure

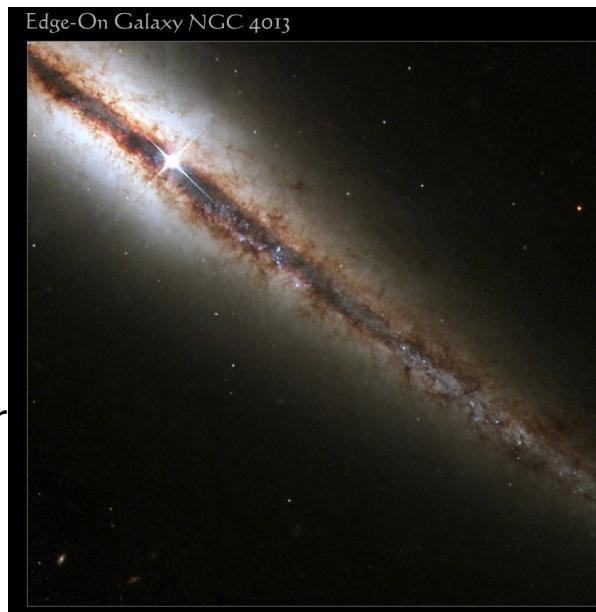
Dynamical pressure set by "vertical heating"

Depends on galaxy mass and/or T-type

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Obviously, dust is a problem

- Near-IR ideal
- R or I-band sometimes used for better FOV and/or sensitivity

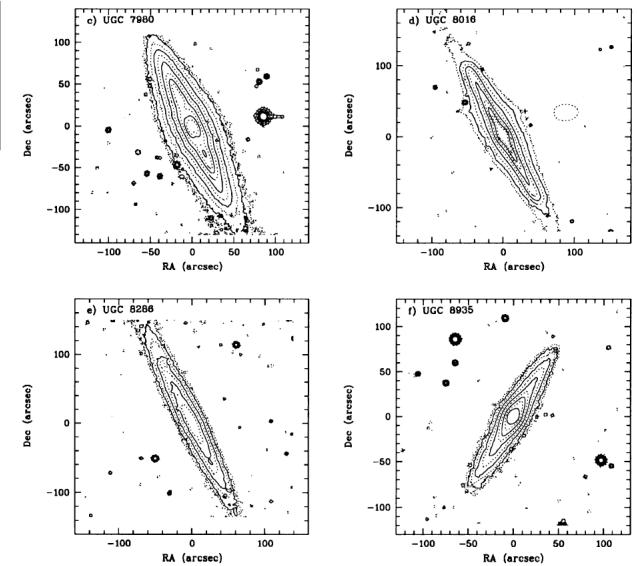


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Vertical light distributions of disks:

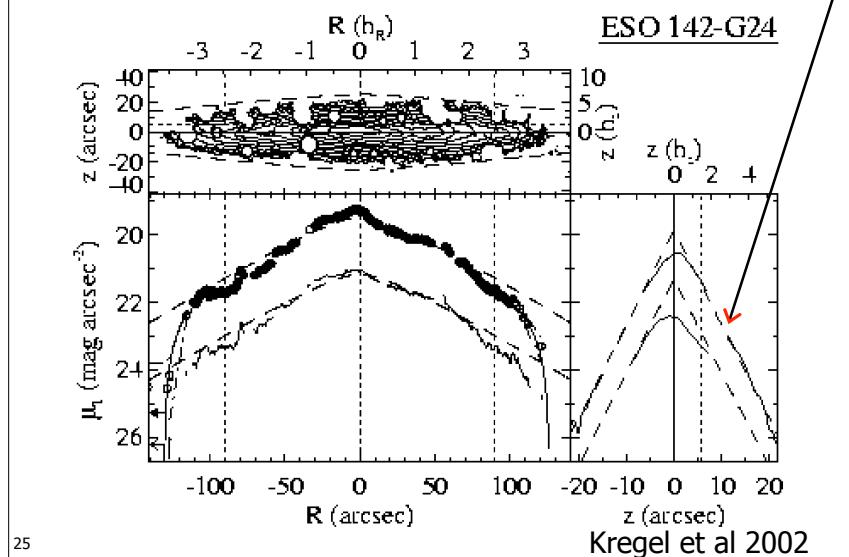
Edge-on
galaxies in
the I-band.

Generally
rounder at
low light
levels,
probably due
to analogs of
MW thick
disks.



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Falls off with z as straight line in μ



Fitting formula for vertical surface brightness

Isothermal, self-gravitating sheet (Spitzer 1942)

$$L(z) = L_0 \operatorname{sech}^2(z/z_0)$$

Exponential

$$L(z) = L_0 \exp(-z/h_z)$$

Generalized (van der Kruit 1988) $[z_0 \approx 2h_z]$

$$L(z) = 2^{-2/n} L_0 \operatorname{sech}^{2/n}(nz/2z_0)$$

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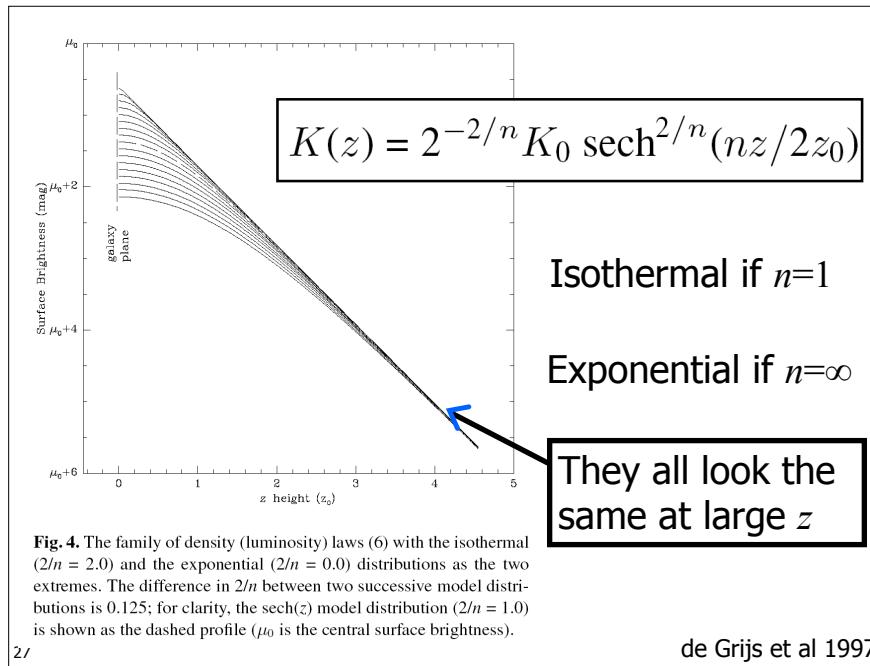


Fig. 4. The family of density (luminosity) laws (6) with the isothermal ($2/n = 2.0$) and the exponential ($2/n = 0.0$) distributions as the two extremes. The difference in $2/n$ between two successive model distributions is 0.125; for clarity, the $\operatorname{sech}(z)$ model distribution ($2/n = 1.0$) is shown as the dashed profile (μ_0 is the central surface brightness).

The exponential distribution is typically adopted however, since differences are only pronounced near the midplane:

Luminosity density in space:

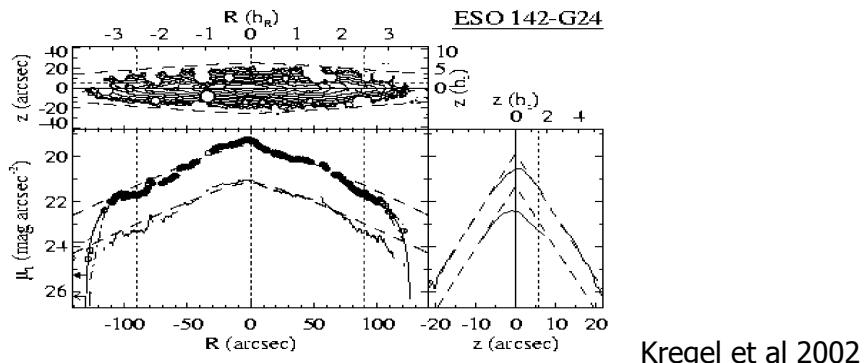
$$L(R, z) = L_0 e^{-R/h_R} e^{-z/h_z}$$

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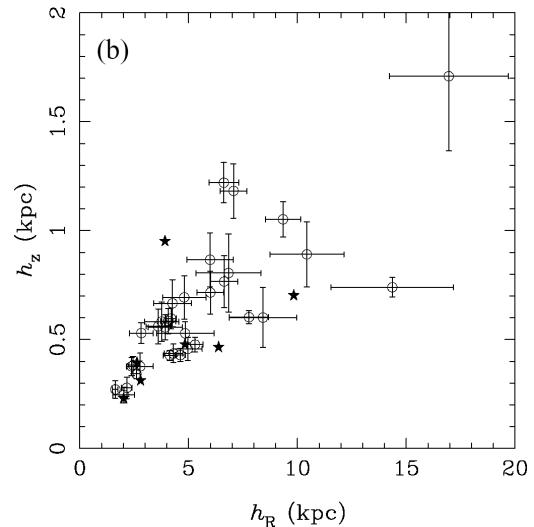
Projected surface brightness, seen edge-on:

$$\Sigma_{\text{disc}}(R', z) = \Sigma_0 (R'/h_R) K_1(R'/h_R) e^{-z/h_z} \quad (2)$$

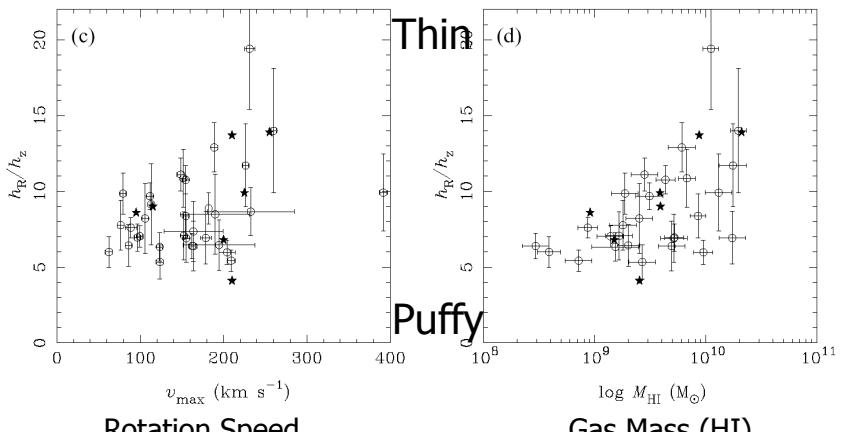
where R' is the projected radius along the major axis, $\Sigma_0 = 2h_R L_0$ is the projected *edge-on* central surface brightness and K_1 is the modified Bessel function of the first order.
(assumes optically thin disk!) Van der Kruit & Searle 1981



Scale heights tend to be < 1 kpc



Lower mass, fainter galaxies tend to be puffier



Contradicts...

Bulge fitting
problems, I
think...

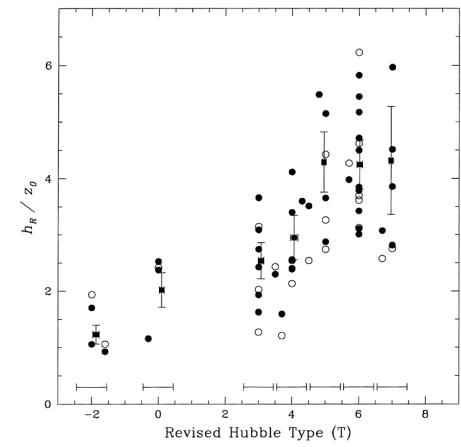


Figure 6. Dependence of the h_R/z_0 ratio on galaxy type for both *I*-band data (filled dots) and *K*-band observations (open circles). The filled squares show the *I*-band ratios averaged over the type bins indicated by the horizontal bars; the errors indicate the standard deviations of the distribution.

de Grijs 1998

Disk flares for early types, but not late-types

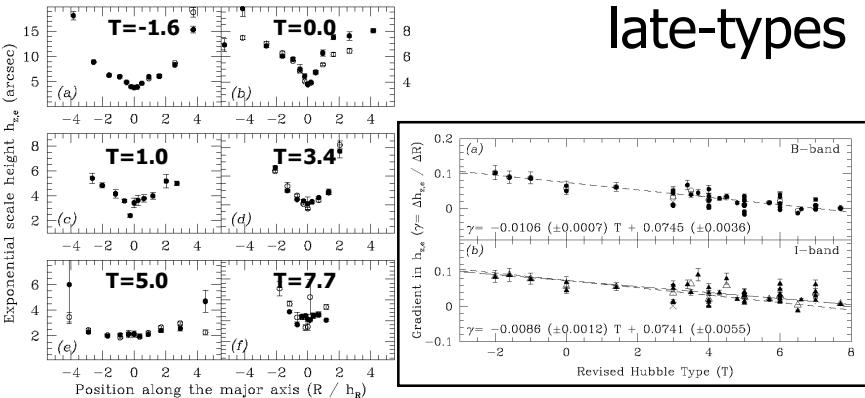


Fig. 1. Examples of the I -band scale height behaviour as a function of galactocentric distance for (a) ESO 358G-29 ($T = -1.6$), (b) ESO 311G-12 ($T = 0.0$), (c) ESO 315G-20 ($T = 1.0$), (d) ESO 322G-87 ($T = 3.4$), (e) ESO 435G-50 ($T = 5.0$), and (f) ESO 505G-03 ($T = 7.7$). Open and closed symbols represent data taken on both sides of the galaxy planes.

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de Grijs & Peletier 1997

Why you expect the observed vertical structure:

A slab of stars, with total surface density Σ and vertical density profile $\rho(z)$.

$$\downarrow F_z = mg_z$$

Assume that the slab is “self-gravitating”

A particle of mass m at z feels a downward force $F_z = mg_z$, where g_z is the gravitational acceleration (or force field).

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Via Gauss's Law:

$$\vec{g} = -\nabla \phi$$

$$\downarrow F_z = mg_z$$

$$\nabla \cdot \vec{g} = \nabla^2 \phi = -4\pi G \rho$$

So ignoring horizontal forces (that in a real disk would be due to $\Sigma(r)$)

$$\nabla \cdot \vec{g} \approx \frac{dg_z}{dz} = -4\pi G \rho$$

This is an equation which can be solved!

Via Gauss's Law:

$$\frac{dg_z}{dz} = -4\pi G \rho$$

$$\downarrow F_z = mg_z$$

Since forces=0 at the midplane:

$$g_z = -4\pi G \int_0^z \rho(z') dz'$$

If the disk is in equilibrium, then something must be balancing the the gravitational pull.

Dynamical Pressure: $P_z = \sigma_z^2 \rho$

(assuming “isothermal” -- i.e. σ_z constant)

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Similar to stellar structure eqn's:

$$AP_z(z+dz) \quad \downarrow dz$$

Consider one layer
of the slab, with
thickness dz , area
 A , and mass ρAdz

$$F_z = mg_z \quad \downarrow \quad \uparrow AP_z(z)$$

Pressure = Force / Area

$$[P_z(z + dz) - P_z(z)]A = (\rho Adz)g_z$$

Yielding:

$$\frac{dP_z}{dz} = \rho g_z$$

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Substituting dynamical pressure:

$$\frac{dP_z}{dz} = \rho g_z \longrightarrow \frac{d(\sigma_z^2 \rho)}{dz} = \rho g_z$$

$$\sigma_z^2 \frac{1}{\rho} \frac{d\rho}{dz} = g_z + g_z = -4\pi G \int_0^z \rho(z') dz'$$

A tasty differential equation:

$$\frac{d \ln \rho}{dz} = -\frac{4\pi G}{\sigma_z^2} \int_0^z \rho(z') dz'$$

Substituting dynamical pressure:

$$\frac{dP_z}{dz} = \rho g_z \longrightarrow \frac{d(\sigma_z^2 \rho)}{dz} = \rho g_z$$

↓ Rearranging...

$$\sigma_z^2 \frac{1}{\rho} \frac{d\rho}{dz} = g_z$$

Note that this step only worked because the velocity dispersion was constant (I.e. "isothermal"). However, you can model the pressure of more complex distributions as being the sum of the pressure from several populations with different velocity dispersions.

This differential equation:

$$\frac{d \ln \rho}{dz} = -\frac{4\pi G}{\sigma_z^2} \int_0^z \rho(z') dz'$$

Has solutions of the form:

$$\rho(z) = \rho_0 \operatorname{sech}^2\left(\frac{z}{2z_0}\right)$$

Where z_0 is some combination of G , σ_z , & ρ_0

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$$\frac{d \ln \rho}{dz} = -\frac{4\pi G}{\sigma_z^2} \int_0^z \rho(z') dz'$$

At large distances above the plane:

$$\int_0^{z \rightarrow \infty} \rho(z') dz' \rightarrow \frac{\Sigma}{2} \longrightarrow \frac{d \ln \rho}{dz} = -\frac{2\pi G \Sigma}{\sigma_z^2}$$

Which has exponential solutions:

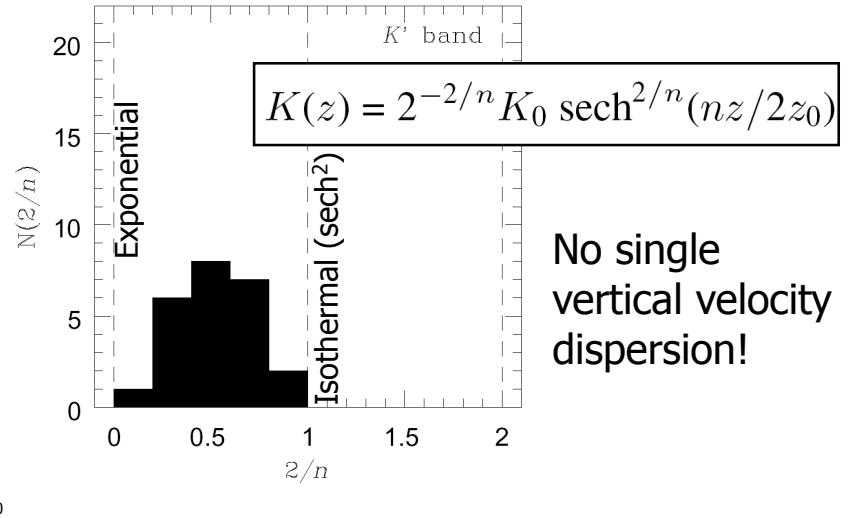
$$\rho(z) = \rho_0 e^{-z/z_0}$$

Where:

$$z_0 = \frac{\sigma_z^2}{2\pi G \Sigma}$$

³⁹ (z_0 is set by the battle between random motions σ_z and self gravity Σ)

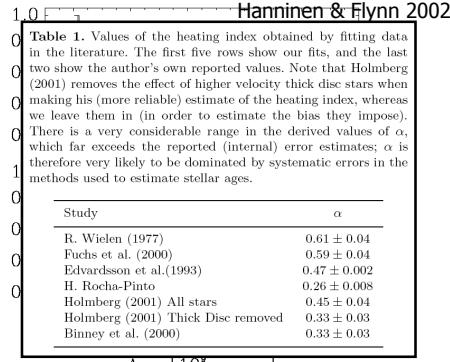
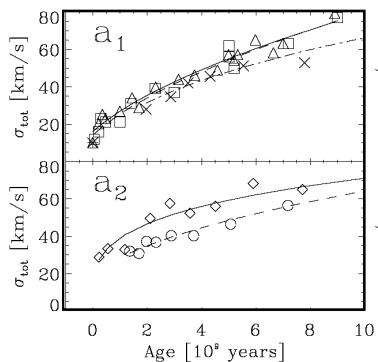
Real disks are somewhere between an isothermal and an exponential



Why not isothermal?

$$\sigma(t) = \sigma_\circ (1 + \frac{t}{\tau})^\alpha$$

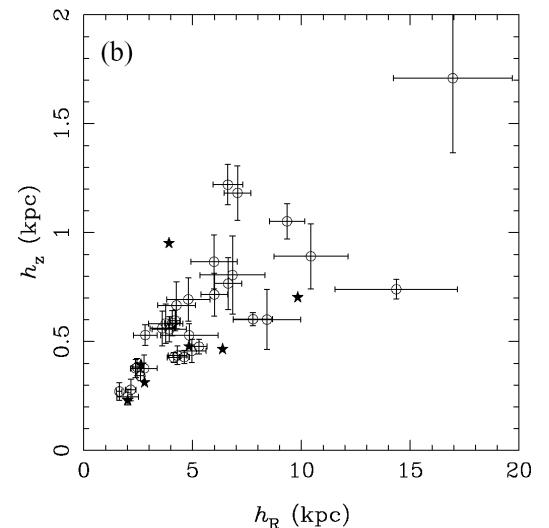
Scattering off GMCs & Spiral Arms, and/or accretion



What might be reasons for the dispersion?

$$\rho(z) = \rho_0 e^{-z/z_0}$$

$$z_0 = \frac{\sigma_z^2}{2\pi G \Sigma}$$



Kregel et al 2002

What might be reasons for flaring?

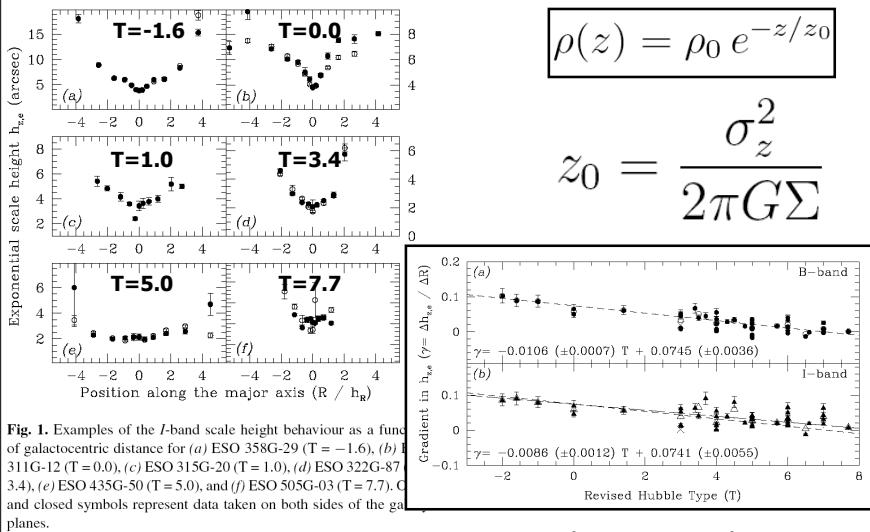


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$$\rho(z) = \rho_0 e^{-z/z_0}$$

$$z_0 = \frac{\sigma_z^2}{2\pi G \Sigma}$$

de Grijs & Peletier 1997