#### Galaxy Magnitudes & Colors

Magnitude for Extended Objects
Optical & NIR filter systems
Broad properties of galaxy spectra
absorption lines (optical & NIR)
emission lines (overview)
Stellar population synthesis
Age-Sensitive colors
Metallicity-Sensitive colors
Breaking the Age+Metallicity
Degeneracy

More specifically, we define the "Petrosian ratio"  $\mathcal{R}_P$  at a radius r from the center of an object to be the ratio of the local surface brightness averaged over an annulus at r to the mean surface brightness within r:

$$\mathcal{R}_{\rm P}(r) \equiv \frac{\int_{\alpha_{\rm lo} r}^{\alpha_{\rm hi} r} dr' 2\pi r' I(r') / \left[\pi (\alpha_{\rm hi}^2 - \alpha_{\rm lo}^2) r^2\right]}{\int_0^r dr' 2\pi r' I(r') / (\pi r^2)} \,, \tag{1}$$

where I(r) is the azimuthally averaged surface brightness profile and  $\alpha_{lo} < 1$ ,  $\alpha_{hi} > 1$  define the annulus. The SDSS has adopted  $\alpha_{lo} = 0.8$  and  $\alpha_{hi} = 1.25$ .

The Petrosian radius  $r_{\rm P}$  is defined as the radius at which  $\mathcal{R}_{\rm P}(r_{\rm P})$  equals some specified value  $\mathcal{R}_{\rm P,lim}$ . The Petrosian flux in any band is then defined as the flux within a certain number  $N_{\rm P}$  of  $r^*$  Petrosian radii:

$$F_{\rm P} \equiv \int_{0}^{N_{\rm PP}} 2\pi r' \, dr' I(r') \,. \tag{2}$$

Thus, the aperture in all bands is set by the profile of the galaxy in  $r^*$  alone. The SDSS has selected  $\Re_{P,\mathrm{lim}}=0.2$  and  $N_P=2$ . The aperture  $2r_P$  is large enough to contain nearly all of the light for a typical galaxy profile (see below), so even substantial errors in  $r_P$  cause only small errors in the Petrosian flux, but small enough that sky noise in  $F_P$  is small (typical statistical errors near the flux limit of  $r^*=17.65$  are <5%). In practice, there are a number of Based on Petrosian 1976, described in Blanton et al 2001

Petrosian magnitudes partially fix this problem by defining an aperture based on  $\Sigma(r)$  that always captures the same fraction of the flux for a given profile (independent of  $\Sigma_0$  or  $r_{1/2}$ )

#### Standard Photometric Apertures

Within a fixed angular size (3" typical)

but, fraction of detected flux varies with distance

Within a limiting isophotal surface brightness

but, fraction of detected flux varies with surface brightness

Within a multiple of an isophotal surface brightness or 1st moment radius [e.g. "Kron (1980) magnitudes" -- "growing" the aperture]

better, but still surface brightness dependent

Within a "metric" aperture [e.g. a fixed number of scale lengths, Petrosian (1976) magnitudes, etc]

best, but harder to measure

### Magnitudes are defined in "systems" relative to some standard which defines m=0

The apparent magnitude  $m_R$  of the source is related to its spectral density of flux  $f_{\nu}(\nu)$  (energy per unit time per unit area per unit frequency) by

Hogg et al 2002;

$$m_{R} = -2.5 \log_{10} \left[ \frac{\int \frac{\mathrm{d}\nu_{o}}{\nu_{o}} f_{\nu}(\nu_{o}) R(\nu_{o})}{\int \frac{\mathrm{d}\nu_{o}}{\nu_{o}} g_{\nu}^{R}(\nu_{o}) R(\nu_{o})} \right] , \qquad \text{astro-ph/0210394}$$
(4)

where the integrals are over the observed frequencies  $\nu_o$ ;  $g_{\nu}^{R}(\nu)$  is the spectral density of flux for the zero-magnitude or "standard" source, which, for Vega-relative magnitudes, is Vega (or perhaps a weighted sum of a certain set of A0 stars), and, for AB magnitudes (Oke & Gunn 1983), is a hypothetical constant source with  $g_{\nu}^{AB}(\nu)=3631$  Jy (where 1 Jy =  $10^{-26}$  W m<sup>-2</sup> Hz<sup>-1</sup> =  $10^{-23}$  erg cm<sup>-2</sup> s<sup>-1</sup> Hz<sup>-1</sup>) at all frequencies  $\nu$ ; and  $R(\nu)$  describes the bandpass, as follows:

- Canonical standard is Vega, an A-star (m=0,color=0)
- Negative colors = bluer than A-star
- Other standards possible
  - G-stars = typical of galaxy spectra
  - Flat spectrum = "AB Magnitudes"

3

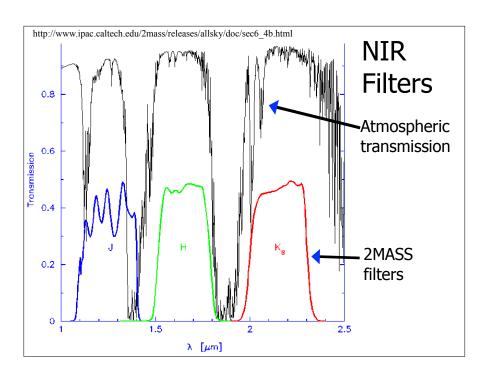
## Definition of AB Magnitudes: Measured relative to a flat-spectrum source with a constant flux at all frequencies

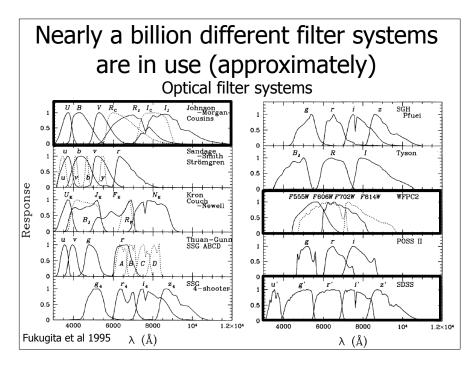
We refer throughout this paper to AB magnitudes, first defined by Oke & Gunn (1983) to measure the ratio of the number of photons included in the signal of the detector relative to that number for a flat spectrum source with  $g(\nu) = 3.631 \times 10^{-20}$  ergs cm<sup>-2</sup> s<sup>-1</sup> Hz<sup>-1</sup>. For a source with a spectrum  $f(\nu)$  the AB magnitude should be (for a perfectly calibrated AB system)

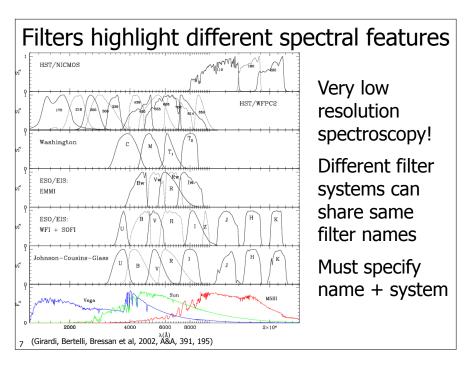
$$m_{AB} = -2.41 - 2.5 \log_{10} \left[ \frac{\int_{0}^{\infty} d\lambda \lambda f(\lambda) R(\lambda)}{\int_{0}^{\infty} d\lambda \lambda^{-1} R(\lambda)} \right]$$

$$= -48.60 - 2.5 \log_{10} \left[ \frac{\int_{0}^{\infty} d\nu \nu^{-1} f(\nu) R(\nu)}{\int_{0}^{\infty} d\nu \nu^{-1} R(\nu)} \right], \qquad (2)$$

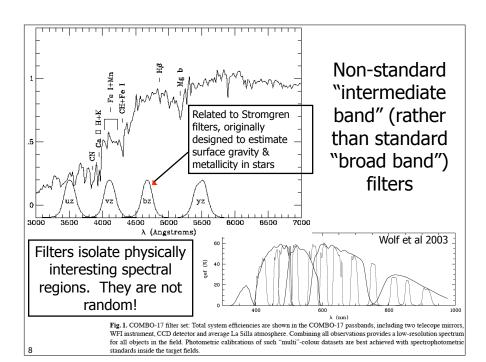
where  $R(\lambda)$  is the fraction of photons entering the Earth's atmosphere which are included in the signal as a function of wavelength (a unitless quantity). Note that  $R(\lambda)$  can be defined even for devices which do not count photons directly (such as bolometers). This equation is written such that  $f(\lambda)$  is in units of ergs cm<sup>-2</sup> s<sup>-1</sup> Å<sup>-1</sup> and  $f(\nu)$  is in units of ergs cm<sup>-2</sup> s<sup>-1</sup> Hz<sup>-1</sup>, while  $\lambda$  is expressed in Å and  $\nu$  is expressed in Hz. The normalizations defined here mean that an object with  $f(\nu) = g(\nu) = 3631$  Jy =  $3.631 \times 10^{-20}$  ergs cm<sup>-2</sup> s<sup>-1</sup> Hz<sup>-1</sup> has all its AB magnitudes equal to zero. The  $\lambda^{-1}$  appears in the integrand of the denominator of the first equation because  $g(\lambda) = c/\lambda^2$  for a "flat spectrum" source with  $g(\nu) = 1$ . The difference in the zeropoints of the two equations simply corresponds to the factor of the speed of light c (expressed in Å s<sup>-1</sup>) in that expression for  $g(\lambda)$ .

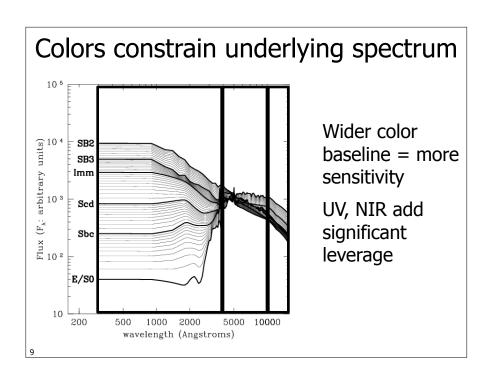


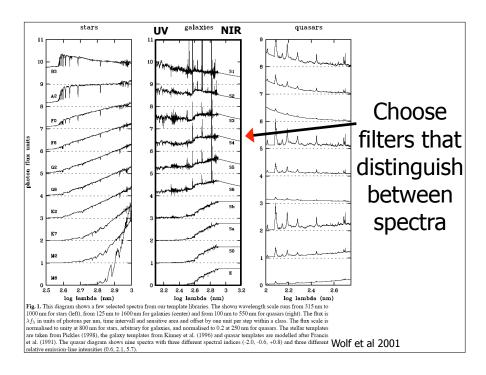


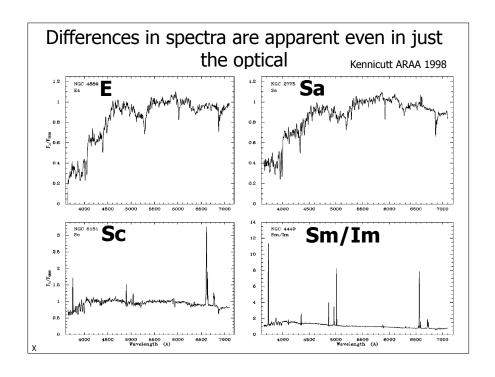


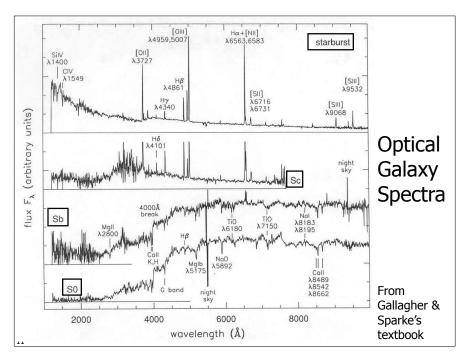
				pe				S	kugita e	et al 199	λ,	<sup>eff</sup> (α L <sub>eff</sub> (α Ly	$yr) = \frac{\int dx}{x}$		$\frac{1}{R},$ $\text{Lyr}(R(\lambda))$ $R(\lambda)$ $\text{Lyr}(R(\lambda))$ $\text{Lyr}(R(\lambda))$	
Lucil C 10-20 (He)	1.89	3.02	2.28	1.89 3.97 3.64 2.90	1.31 4.12 4.15 3.60	1.93 3.82 3.25 2.44	3.95	1.38 3.50 3.89 2.96	3.78 2.92 2.41 2.20	3.74 2.91 2.43 2.19	2.99 2.81 2.56	3.80 2.97 2.28	3.60 3.28 2.82 2.43	3.74 2.90 2.46	1.54 3.93 3.12 2.51 2.19	which are
c(\(\nu_{\text{eff}}^{\text{VegA}}\)^{-1}	4363		6693	3610 4369 5365 6629	3452 4103 4663 5453	3617 4467 5982 7842	4474	3519 3967 4885 6498	5075 6599 7941 9045	5160 6603 7876 9029	6388 6895 7509 8075	4477 6504 8508	5381 5900 6829 7923	5113 6632 7761	3530 4748 6210 7623 9098	Note — a) References are given whenever the response functions are taken from those which are stiffness from the original rough ASSO stands for America's F. Craises 1660, and Maximits for
J. Vega J. eff	6.19	2.15	1.87 0.912	4.30 6.10 3.75 1.96	3.24 7.21 5.68 3.62	4.32 5.54 2.64 1.17	5.73	3.33 6.62 4.84 2.09	4.34 1.99 1.13 0.797	4.14 1.98 1.16 0.798	2.19 1.77 1.36 1.08	5.46 2.08 0.928	3.62 2.73 1.77	1.96	3.67 5.11 2.40 1.28 0.783	ictions are tak
	3709 4393 5439	6410	6688 8571	3710 4407 5368 6628	3496 4119 4666 5455	3737 4537 5978 7838	4515	3542 4013 4888 6496	5083 6600 7942 9071	5166 6602 7876 9054	6384 6899 7508 8077	4562 6503 8532	5387 5901 6826 7906	5121 6632 7756	3594 4765 6205 7617	ponse fur
FWHM	526 1008	1568	2096	595 1028 823 969	363 197 176 244	556 1550 1330 1786	1490	412 469 709 893	913 1028 1604 1472	882 916 1353 984	534 450 608 515	1215 1373 1725	1480 2050 1957 1653	942 1050 1469	556 1297 1358 1547 1530	er the res
1	3652 4448	8060	6930 8785	3647 4466 5423 6712	3465 4109 4668 5459	3656 4625 6168 7953	4604	3536 3992 4927 6538	5147 6659 8056 9141	5238 6677 7973 9133	6401 6904 7526 8087	4614 6585 8668	5536 6102 6979 8092	5154 6696 7837	3585 4858 6290 7706	wheney
ref <sup>®)</sup>	Buser 78 AS69	Bessell 90 Bessell 90			Olson74 Matsu69 Olson74 Olson74	Koo 85										aces are given
band	U3	$R_{\rm C}$	$R_1$	3-0 2 -	# D= #	$_{K_{K}}^{U_{K}}$	$B_{\rm J}$ $R_{\rm F}$	3001	82.22	0, L == N	DCBA	$_{I}^{B_{1}}$	F555W F606W F702W F814W	gross rposs rposs	ז יינ יין נפן נג'	Referen
bandpass system	Johnson-Morgan	Cousins	Johnson	Sandage-Smith	Strömgren	Kron	Couch-Newell	Thuan-Gunn	Schneider et al. (4-shooter)	Schneider et al. (Pfuei)	Schneider et al. (narrow bands)	Tyson (CCD)	WFPC2	POSS II	SDSS	Note — a)

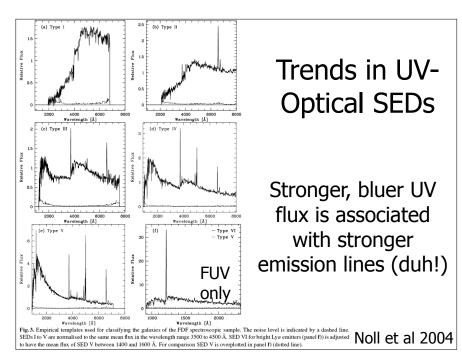


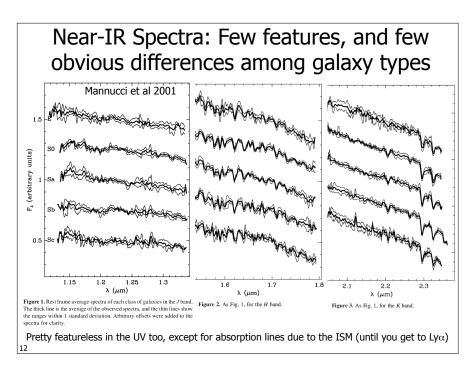






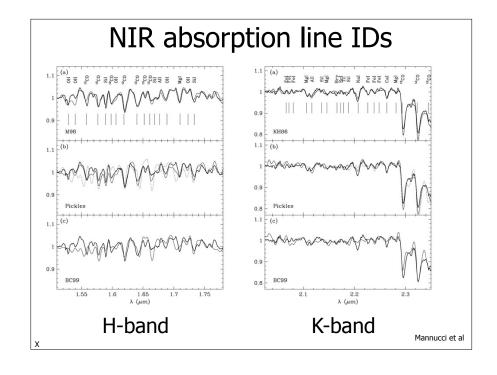


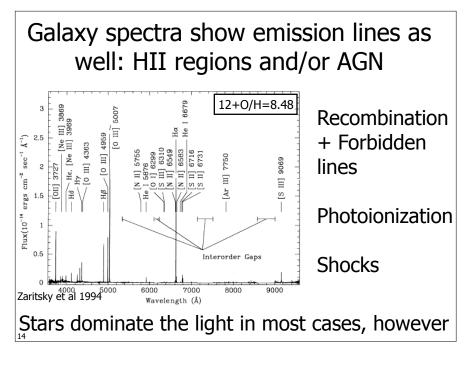




		INDEX DEFINITION:			
Name	Index Bandpass	Pseudocontinua	Units	Measures*	\\\\ : al. T.a.d: a.a.d/.
(2)	(3)	(4)	(5)	(6)	"Lick Indices":
CN <sub>1</sub>	4142.125-4177.125	4080.125-4117.625 4244.125-4284.125	mag	C, N, (O)	
CN <sub>2</sub>	4142.125-4177.125	4083.875-4096.375 4244.125-4284.125	mag	C, N, (O)	Characterize
Ca4227	4222.250-4234.750	4211.000-4219.750 4241.000-4251.000	Å	Ca, (C)	
G4300	4281.375-4316.375	4266.375-4282.625 4318.875-4335.125	Å	C, (O)	strength of optical
Fe4383	4369.125-4420.375	4359.125-4370.375 4442.875-4455.375	Å	Fe, C, (Mg)	
Ca4455	4452.125-4474.625	4445.875-4454.625 4477.125-4492.125	Å	(Fe), (C), Cr	absorption features
Fe4531	4514.250-4559.250	4504.250-4514.250 4560.500-4579.250	Å	Ti, (Si)	•
C <sub>2</sub> 4668	4634.000-4720.250	4611.500-4630.250 4742.750-4756.500	Å	C, (O), (Si)	
Нβ	4847.875-4876.625	4827.875-4847.875 4876.625-4891.625	Å	$H\beta$ , $(Mg)$	
Fe5015	4977.750-5054.000	4946.500-4977.750 5054.000-5065.250	Å	(Mg), Ti, Fe	Age & Metallicity
$Mg_1$	5069.125-5134.125	4895.125-4957.625 5301.125-5366.125	mag	C, Mg, (O), (Fe)	,
$Mg_2$	5154.125-5196.625	4895.125-4957.625 5301.125-5366.125	mag	Mg, C, (Fe), (O)	Sensitive
Mgb	5160.125-5192.625	5142.625-5161.375	Å	Mg, (C), (Cr)	
Fe5270	5245.650-5285.650	5191.375-5206.375 5233.150-5248.150	Å	Fe, C, (Mg)	
Fe5335	5312.125-5352.125	5285.650-5318.150 5304.625-5315.875	Å	Fe, (C), (Mg), Cr	
Fe5406	5387.500-5415.000	5353.375-5363.375 5376.250-5387.500	Å	Fe	Note that the name
Fe5709	5696.625-5720.375	5415.000-5425.000 5672.875-5696.625	Å	(C), Fe	
Fe5782	5776.625-5796.625	5722.875-5736.625 5765.375-5775.375	Å	Cr	sometimes has no
Na D	5876.875-5909.375	5797.875-5811.625 5860.625-5875.625	Å	Na, C, (Mg)	
TiO,	5936.625-5994.125	5922.125-5948.125 5816.625-5849.125	mag	C	connection to what
•		6038.625-6103.625			
TiO <sub>2</sub>	6189.625-6272.125	6066.625-6141.625 6372.625-6415.125	mag	C, V, Sc	elements are et al 199

λ (μm)	Main contribution	Other species	NIR absorption line IDs
1.529	OH	CN,TiI	
1.540	OH	Siı	•
1.558	<sup>12</sup> CO	OH	
1.577	<sup>12</sup> CO	Mg I,Fe I	
1.589	Siı	OH	
1.598	<sup>12</sup> CO	Si 1, <sup>13</sup> CO	
1.606	OH	011.0	
1.619	<sup>12</sup> CO <sup>12</sup> CO	OH,Ca1	
1.640	13CO	Si I,[Fe II]	
1.652	12CO	OH OH	
1.661	Sit	OH OH	Spectrum dominated by
1.672	Alı	H1. <sup>12</sup> CO	Spectrum dominated by
1.677	Ali	nı, co	• •
1.689	OH	HLCO	cool stars
1.710	MgI	CO.OH	COOI StarS
1.723	OH	Sit	
1.733	Sit	Hi	
2.067	Fei	***	
2.072	Fei		
2.081	Fei	Siı	
2.107	MgI	H <sub>2</sub> O,Si I	Dominated by Molecules
2.117	Alı	H <sub>2</sub> ,Mg I,Fe I	Dominated by Molecules
2.136	Siı	2. 0.	· · · · · · · · · · · · · · · · · · ·
2.146	MgI	Na I,Si I,Ca II	and Low Ionization
2.166	Bry	VI	aliu LOW IUIIZaliuli
2.173	ScI	Fei	
2.179	TiI	Si 1,Fe 1	Chasica
2.189	Siı	TiI,Fe 1	Species
2.208	Naı	ScI,TiI,VI,Fe 1,Si 1	-p
2.226	Fe I	ScI,TiI	
2.239	Fei	ScI	
2.248	Fei	VI,TiI	
2.263	Cai	ScI,TiI,Fe1,S1	
2.281 2.294	MgI <sup>12</sup> CO	Caı,Feı,Sı,HF Til	
2.294	12CO	111	
2.345	13CO		





For reference:
Average galaxy colors measured for different Hubble types

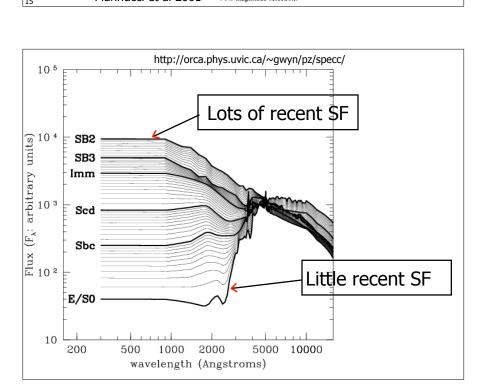
**Table 2.** Average effective colours of galaxies with  $M_V < -21$ . For each colour the standard deviation and the number of used objects are also reported.

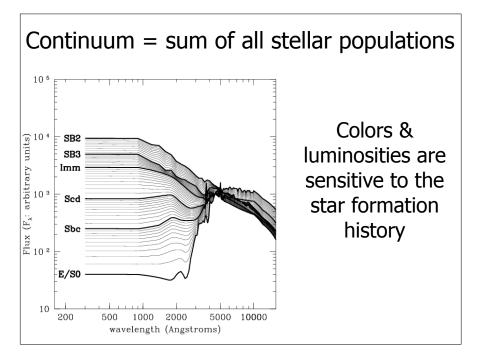
	U-B	B-V	V-R	V-I	V - K	$J-H^a$	$H-K^{c}$
E	0.50	0.99	0.59	1.22	3.30	0.66	0.21
	(0.08)	(0.05)	(0.05)	(0.07)	(0.09)	(0.05)	(0.02)
	323	418	314	221	32	225	225
SO.	0.47	0.97	0.58	1.20	3.25	0.66	0.22
	(0.11)	(0.08)	(0.05)	(0.08)	(0.14)	(0.05)	(0.02)
	287	344	227	158	13	235	235
Sa	0.36	0.90	0.58	1.17	3.24	0.67	0.25
	(0.19)	(0.11)	(0.08)	(0.11)	(0.18)	(0.06)	(0.03)
	138	185	73	82	17	105	105
Sb	0.22	0.82	0.57	1.16	3.21	0.66	0.25
	(0.20)	(0.12)	(0.09)	(0.11)	(0.28)	(0.06)	(0.03)
	321	541	156	315	16	93	93
Sc	0.06	0.70	0.52	1.15	3.03	0.66	0.25
	(0.18)	(0.13)	(0.10)	(0.15)	(0.24)	(0.07)	(0.04)
	294	536	133	287	23	46	46
$\mathrm{Sd}^b$	-0.12	0.62	0.47	1.09	2.95	0.65	0.23
	(0.16)	(0.18)	(0.13)	(0.19)	(0.32)	(0.08)	(0.05)
	53	99	25	58	12	26	24
[c	-0.15	0.51	0.40	1.08	2.35	0.51	0.21
	(0.20)	(0.17)	(0.20)	(0.30)	(0.35)	(0.10)	(0.06)
	102	117	28	35	5	22	20

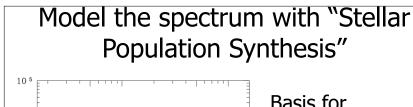
 $<sup>^</sup>a$ : The J-H and H-K colours are based also on the results in Fioc & Rocca-Volmerange (1999), where only average quantities are given. In these cases the scatter is not measured but estimated.

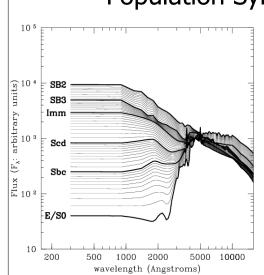
Mannucci et al 2001  $\stackrel{b: M_V}{\sim} No ma$ 

001 °: No magnitude selection



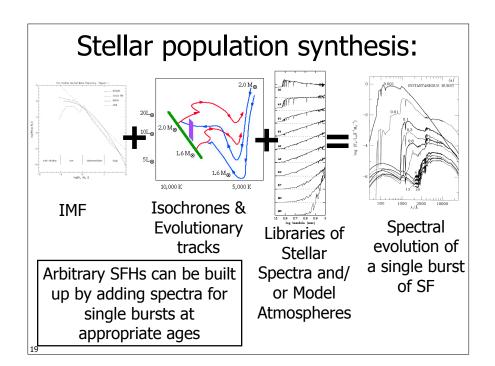




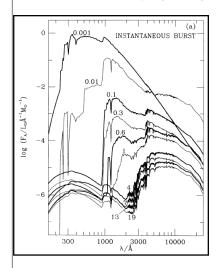


Basis for essentially <u>all</u> estimates of extragalactic physical quantities

(e.g., stellar mass, age, metallicity, extinction, SFRs)



#### Instantaneous burst



Luminous at early times

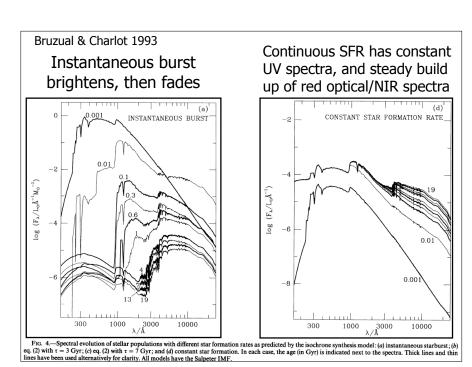
Fades and reddens at late times

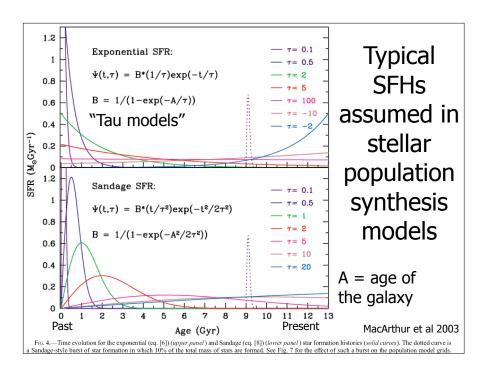
Little spectral evolution after t>4 Gyr

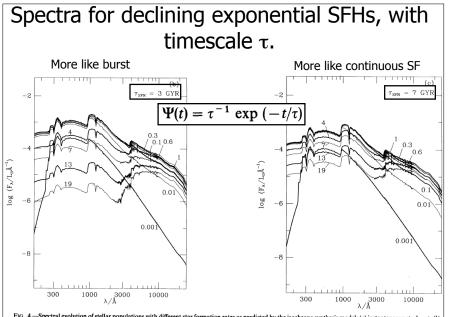
Young burst can swamp light from old stars

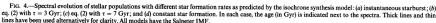
#### Bruzual & Charlot 1993

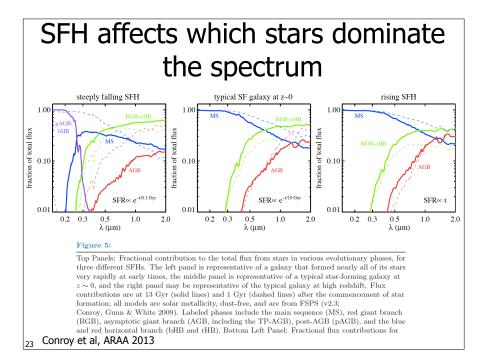
Fig. 4.—Spectral evolution of stellar populations with different star formation rates as predicted by the isochrone synthesis model; (a) instantaneous starburst; (be eq. (2) with  $\tau = 7$  Gyr; and (d) constant star formation. In each case, the age (in Gyr) is indicated next to the spectra. Thick lines and thin lines have been used alternatively for clairly in the Salpeter IMF.

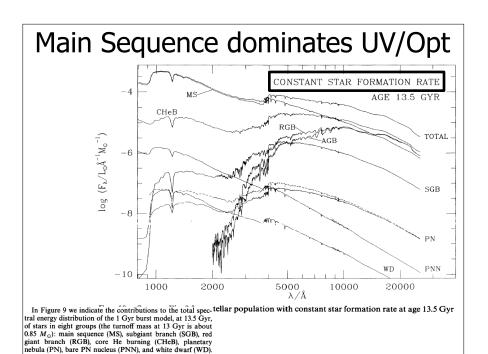


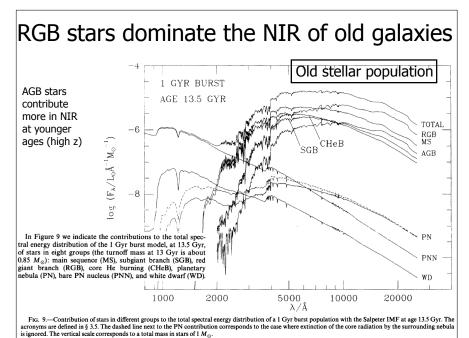










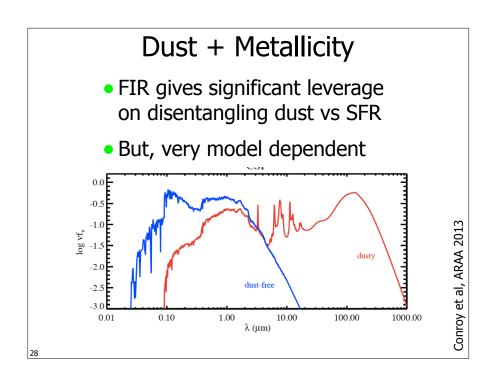


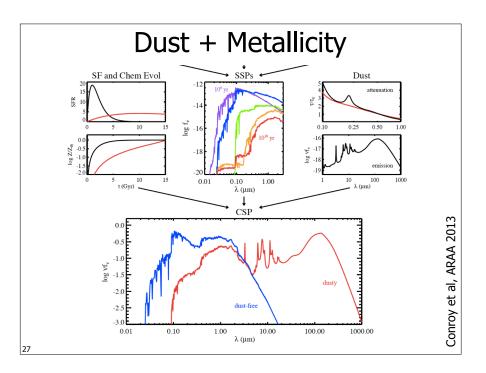
#### Stellar population synthesis (SPS):

Compilation: http://www.sedfitting.org/SED08/Models.html

- Many different publicly available codes:
  - FSPS (Conroy)
  - GISSEL (Bruzual & Charlot)
  - PEGASE (Rocca-Volmerange)
  - STARBURST99 (Leitherer)
- Various features can be added on:
  - Metallicity evolution
  - Dust
  - Emission lines







#### Stellar population synthesis:

- Limitations:
  - Quality of spectral libraries (not so good in NIR or extreme metallicities)
  - Late-stage (post-main sequence) stellar evolution
  - Cool stars

# Uncertainties in Ingredients: Various libraries, Z. = Z., 13 Cyr Various libraries, Z. = Z., 13 Cyr

Fig. 1 Evolutionary tracks of solar composition low mass stars (0.9 - 10  $M_{\odot}$ ) demonstrating the differences between four different models (as labelled): MPA08 (Weiss and Schlattl 2008), BaSTI04 (with/without overshoot; Pietrinferni et al. 2009), and Padova08 (Marigo and Girardi 2007; Marigo et al. 2008) [Courtesy S. Charlott.]

3.8

 $log (T_{eff}/K)$ 

3.6

See Conroy et al 2009, Conroy & Gunn 32010 for assessment of uncertainties

Fig. 2 Optical spectra from both theoretical and empirical stellar libraries (as labelled) demonstrating the improvement of spectral resolution over time with the associated improvement in library size [Courtesy S. Charlot].

Nice Review of Synthesis Modeling: Walcher et al 2010

#### Two basic roles for SPS models

- Predict observable properties given star formation history, metallicity, etc.
- Infer fundamental properties (SFR, stellar mass, etc) from observed spectrum.

#### The latter can be highly degenerate

However, in the age of widespread spectra+ multiwavelength data, using SPS for inference is unavoidable

(and better than most alternatives)

#### Degeneracies in SPS models

Spectra are "light weighted", favoring young ages

Old SSPs are faint and hard to detect

Complex SFH's bias inference

Higher SNR spectra, wide wavelength coverage all help

Relative measures always better than absolute

Summary: Be cautious if you need a factor of 2 rather than a factor of 10 level of accuracy!