Replication material for the AJAE paper The Informational Content of Geographical Indications

Jean-Sauveur Ay*

Version 2.1: March 24, 2020

Abstract

This file contents the Replication Material (RM) associated to the article named in the title and forthcoming in the *American Journal of Agricultural Economics*. Data, code and prediction materials are under the copyright license GNU GPL V3, which means that license notices must be preserved. Raw data are available from the Inrae dataverse server https://data.inrae.fr. Some R functions are reported in the Appendix to preserve the readability of codes in the main text. The most recent version of this document and a Shiny App about the econometric classification of vineyards in the *Côte d'Or* (Burgundy, France) are available from the remote repository https://github.com/jsay/geoInd.

Contents

1	Desc	criptive Statistics	2	6	Models for GIs of 1936	18
	1.1	Data shaping	2		6.1 Descriptive statistics	18
	1.2	Geology and pedology	3		6.2 Estimation	19
	1.3	Crossing GIs dimensions	4		6.3 Significance	20
					6.4 Goodness of fit	20
2	Mod	dels of GI designation	6		6.5 Marginal effects	21
	2.1	Parametric ordered logit models .	6		6.6 Ordinal superiority measures	22
	2.2	Ordered generalized additive models	7		6.7 Temporal variations	23
					6.8 Decomposition table	24
3	Diag	gnostics	8		1	
	3.1	Significance	8	7	Alternative GI designations	25
	3.2	Goodness of fit	10		7.1 Change latent vineyard quality	25
	3.3	Causal inference	11		7.2 Add a vertical level in GIs	27
					7.3 Decomposition table	28
4	Mar	ginal effects	13		•	
	4.1	Parametric ordered logit	13	A	Session information	30
	4.2	Ordered generalized additive	14			
	4.3	Ordinal superiority figure	15	В	Custom R functions	31
	4.4	Correlation between Communes .	16		B.1 Translation of geology	31
					B.2 Translation of pedology	32
5	Info	rmational content	17		B.3 Surrogate Residuals	33
	5.1	Decomposition tables	17		B.4 Decomposition terms	35

^{*}jean-sauveur.ay@inrae.fr, UMR CESAER, Agrosup, Inrae, Université Bourgogne Franche-Comté, 21000 Dijon (France).

1 Descriptive Statistics

1.1 Data shaping

The data to reproduce the results of the paper are on the dataverse server https://data.inrae.fr/, with the results of the econometric estimations, and the predictions. The R code below allows to download the most recent version of the data with the dataverse package (Leeper, 2017), and to load them in a R session.

```
library(dataverse) ; library(sp)
Sys.setenv("DATAVERSE_SERVER" = "data.inrae.fr")
GeoRasRaw <- get_file("GeoRas.Rda", "https://doi.org/10.15454/ZZWQMN")
writeBin(GeoRasRaw, "Data/GeoRas.Rda")
load("Data/GeoRas.Rda") ; dim(Geo.Ras)</pre>
```

[1] 110350 67

The resulting object Geo.Ras is a SpatialPolygonsDataFrame from the sp package (Bivand et al., 2013). The current version of data counts 110 350 vineyard plots and 67 variables. A detailed dictionary about these variables is available (in French) in the GitHub repo. The additional R code reshapes some variables of particular interest:

- It reorders the commune levels along the North-South gradient
- It standardizes the variable about solar radiation
- It codes the variable about exposition in 8 quadrants
- It projects the geographical coordinates inside the WGS84 system
- It selects the parcels with GIs and drop omitted values

[1] 59113 71

The resulting object is a SpatialPolygonDataFrame that contains 59 113 observations of vineyard plots with 72 variables without omitted values. These data are used in the econometric analysis.

1.2 Geology and pedology

Another pre-regression treatment is the transformation of the geological and pedological variables into dummy variables in order to control sub-soil and soil characteristics of vineyards with fixed effects. A too small number of observation within a given fixed effect can be a problem for the precision and convergence of the estimation, hence we choose to include a fixed effects only for geological and pedological polygons with more than 1 000 vineyard plots.

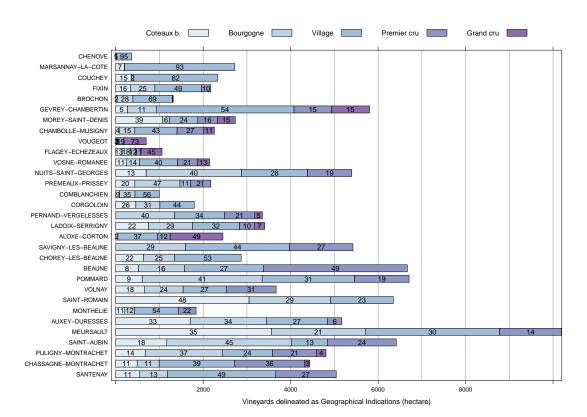
```
Reg.Ras$NOTATION <- factor(Reg.Ras$NOTATION)</pre>
 tmp <- table(Reg.Ras$NOTATION)< 1000</pre>
 Reg.Ras$GEOL <- factor(</pre>
     ifelse(Reg.Ras$NOTATION %in% names(tmp[ tmp]), "OAREF",
             as.character(Reg.Ras$NOTATION)))
 Reg.Ras$NOUC <- factor(Reg.Ras$NOUC)</pre>
 tmp <- table(Reg.Ras$NOUC)< 1000</pre>
 Reg.Ras$PEDO <- factor(</pre>
      ifelse(Reg.Ras$NOUC %in% names(tmp[tmp]), "OAREF",
             as.character(Reg.Ras$NOUC)))
 apply(Reg.Ras@data[, c("GEOL", "PEDO")], 2, table)
$GEOL
OAREF
            C
                    E
                                          Fy
                                                  GP
                                                          j3
                           Fu
                                  Fx
                                                                j3a
                                                                        j3b
                                                                                j4a
 5208 19014
                1997
                        1060
                                2142
                                        1460
                                               8372
                                                       1288
                                                               2570
                                                                       2539
                                                                              1531
  j5a
          j5b
                  j6a
                        p-IV
 3526
         3928
                3087
                        1391
$PEDO
OAREF
                                   28
                                          29
           13
                   14
                           26
                                                  30
                                                          32
                                                                  34
                                                                         35
                                                                                 36
 3310
         1553 17475
                        3718
                                8687
                                        6241
                                               4563
                                                       1802
                                                               1700
                                                                       5255
                                                                              1116
     5
           69
                    8
 1051
        1484
               1158
```

The characteristics of sub-soils and soils are modeled with respectively 14 and 13 fixed effects. In each case, the reference modality coded **QAREF** is equal to 1 for all vineyards plots inside geological and pedological polygons without sufficient observations. Robustness checks have been made with other threshold values than 1 000 without this arbitrary choice changes the results.

1.3 Crossing GIs dimensions

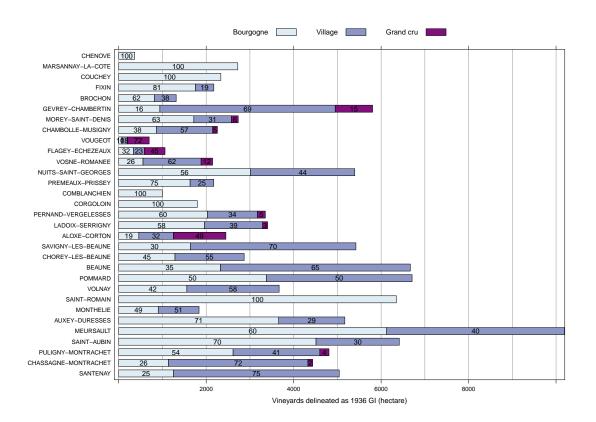
As mentioned in the main paper, the GIs on the area of interest contains both an horizontal level (*commune*) and a vertical level of geographical indication. The balance of the two dimensions can be assessed with the following code that produces Figure OA1 of the Online Supplementary Appendix.

```
library(lattice) ; library(RColorBrewer)
fig.dat <- aggregate(model.matrix(~0+ factor(Reg.Ras$AOC))*</pre>
                     Reg.Ras$AREA/ 1000, by= list(Reg.Ras$LIBCOM), sum)
names(fig.dat) <- c("LIBCOM", "BGOR", "BOUR", "VILL", "PCRU", "GCRU")</pre>
fig.dat$LIBCOM <- factor(fig.dat$LIBCOM, lev= rev(levels(fig.dat$LIBCOM)))</pre>
fig.crd <- t(apply(fig.dat[, -1], 1, function(t) cumsum(t) - t/2))</pre>
fig.lab <- round(t(apply(fig.dat[, -1], 1, function(t) t/ sum(t)))* 100)</pre>
my.pal <- brewer.pal(n= 9, name = "BuPu")[ 2: 8]
barchart(LIBCOM~ BGOR+ BOUR+ VILL+ PCRU+ GCRU, xlim= c(-100, 10200),
         xlab="Vineyards delineated as Geographical Indications (hectare)",
         data= fig.dat, horiz= T, stack= T, col= my.pal, border= "black",
         par.settings= list(superpose.polygon= list(col= my.pal)),
         auto.key= list(space= "top", points= F, rectangles= T, columns= 5,
                         text=c("Coteaux b.", "Bourgogne",
                                "Village", "Premier cru", "Grand cru")),
         panel=function(x, y, ...) {
             panel.grid(h= 0, v = -11, col= "grey60")
             panel.barchart(x, y, ...)
             ltext(fig.crd, y, lab= ifelse(fig.lab> 0, fig.lab, ""))})
```



We also use historical GI designation scheme from 1936, the year of creation of the French national institute in charge of geographical indications (INAO). At his time, the vertical dimension counted only three levels, whereas the horizontal dimension was identical. The balance of the distribution is as follows.

```
library(lattice) ; library(RColorBrewer)
fig.old <- aggregate(model.matrix(~0+ factor(Reg.Ras$AOC36lvl))*</pre>
                      Reg.Ras$AREA/ 1000, by= list(Reg.Ras$LIBCOM), sum)
names(fig.old) <- c("LIBCOM", "BOUR", "VILL", "GCRU")</pre>
fig.old$LIBCOM <- factor(fig.old$LIBCOM, lev= rev(levels(fig.old$LIBCOM)))</pre>
old.crd <- t(apply(fig.old[, -1], 1, function(t) cumsum(t)- t/2))</pre>
old.lab <- round(t(apply(fig.old[, -1], 1, function(t) t/ sum(t)))* 100)</pre>
old.pal \leftarrow brewer.pal(n= 9, name = "BuPu")[ c(2, 5, 8)]
barchart(LIBCOM~ BOUR+ VILL+ GCRU, xlim= c(-100, 10200),
         xlab="Vineyards delineated as 1936 GI (hectare)",
         data= fig.old, horiz= T, stack= T, col= old.pal, border= "black",
         par.settings= list(superpose.polygon= list(col= old.pal)),
         auto.key= list(space= "top", points= F, rectangles= T, columns= 3,
                         text=c("Bourgogne", "Village", "Grand cru")),
         panel=function(x, y, ...) {
             panel.grid(h= 0, v = -11, col= "grey60")
             panel.barchart(x, y, ...)
             ltext(old.crd, y, lab= ifelse(old.lab> 0, old.lab, ""))})
```



2 Models of GI designation

2.1 Parametric ordered logit models

We first estimate the benchmark parametric ordered logistic model polm1 that corresponds to model (0) of Table 1 of the main article. Model polm1a is the auxiliary regression without *commune* fixed effects used to evaluate the causal inference as detailed in the beginning of the online supplementary material. Model polm1b is a secondary auxiliary regression without smoothing of spatial coordinates to compute the Fisher statistics associated to these terms in Table 1. We use the polr function from the MASS package.

Warning messages:

```
    1: In polr(factor(AOC) ~ 0 + LIBCOM + EXPO + GEOL + PEDO + poly(DEM, une coordonnée à l'origine est nécessaire et assumée
    2: In polr(factor(AOC) ~ 0 + LIBCOM + EXPO + GEOL + PEDO + poly(DEM, le plan ne semble pas de rang plein, des coefs seront ignorés
```

The warning messages come from the choice to drop the intercept in order to estimate a coefficient for each *commune* from the variable LIBCOM. This choice is made to compute more easily the ordinal superiority measures from fixed effects. This does not have any effect on the other estimated coefficients.

2.2 Ordered generalized additive models

We estimate here the series of ordered generalized additive models (OGAMs) of GIs designations with a loop. Models (I) to (V) reported in Table 1 of the main are only a subset of all models of the gamod object. Models with high complexities for the spatial effects (more than 600 edf) are long to run. They require about 8 hours each, with the full loop requires about 2 days to run with Intel Core i7-7820HQ CPU 2.90 GHz x 8 and 64 Go of RAM. We advise the reader to not run the full loop, but instead to select values of k in listk and estimate each model separately.

Conversely, the results can be downloaded directly from the dataverse server of Inrae according to the following code. Econometric results cad be assessed directly.

```
library(dataverse)
GamModRaw <- get_file("gamod.Rda", "https://doi.org/10.15454/ZZWQMN")
writeBin(GamModRaw, "Data/gamod.Rda")
load("Data/gamod.Rda") ; names(gamod)</pre>
```

```
[1] "gam50" "gam100" "gam200" "gam300" "gam400" "gam500" "gam600"
```

écoulé

109562

système

384

utilisateur

113038

^{[8] &}quot;gam700" "gam800" "gam900"

3 Diagnostics

3.1 Significance

We first reports the Chi-square statistics for the joint significance of the parametric ordered logit model polm1 that corresponds to model (0) of Table 1 in the main text.

```
library(car)
res1a <- anova(polm1, polm1b)
(res1 <- Anova(polm1))</pre>
```

Le chargement a nécessité le package : carData

Analysis of Deviance Table (Type II tests)

Response: factor(AOC)

```
LR Chisq Df Pr(>Chisq)
LIBCOM
                          9768 31
                                       <2e-16 ***
EXPO
                                       <2e-16 ***
                           743 7
GEOL
                                       <2e-16 ***
                          1716 14
PEDO
                          8811 13
                                       <2e-16 ***
                                       <2e-16 ***
poly(DEM, 2)
                          4030 2
poly(SLOPE, 2)
                           532 2
                                       <2e-16 ***
poly(RAYAT, 2)
                          1885 2
                                       <2e-16 ***
                          1933 3
                                       <2e-16 ***
poly(X, 3)
poly(Y, 3)
                                       <2e-16 ***
                           178 3
poly(X, 3):poly(Y, 3)
                          5257 9
                                       <2e-16 ***
```

--

codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Warning messages:

```
1: glm.fit: fitted probabilities numerically 0 or 1 occurred 2: glm.fit: fitted probabilities numerically 0 or 1 occurred 3: glm.fit: fitted probabilities numerically 0 or 1 occurred 4: glm.fit: fitted probabilities numerically 0 or 1 occurred 5: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

Then, we compute the same Chi-square statistics for all the OGAMs with the function resume. They are reported in the next columns of Table 1 in the main paper.

```
load("Inter/gamod.Rda")
resume <- function(mod) {
   tmp <- anova(mod)
   res <- c(as.vector(rbind(tmp$s.table[, 3], tmp$s.table[, 1])),
        as.vector(rbind(tmp$pTerms.tab[, 2], tmp$pTerms.tab[, 1])))
   names(res) <- c(as.vector(rbind(rownames(tmp$s.table), rep("", 4))),
        as.vector(rbind(rownames(tmp$pTerms.tab), rep("", 2))))
   round(res, 1)
}
sapply(gamod[ 1: 5* 2], resume)</pre>
```

	gam100	gam300	gam500	gam700	gam900
s(DEM)	4123.2	1793.1	1189.9	1014.1	867.0
	8.9	8.9	8.9	8.8	8.8
s(SLOPE)	922.5	343.6	168.5	155.5	190.1
	8.3	8.2	8.3	8.2	7.7
s(RAYAT)	2091.3	981.6	797.7	646.5	531.0
	8.1	8.1	8.3	8.0	7.3
s(X,Y)	32524.2	59293.9	74154.2	78445.3	86597.1
	98.6	295.0	483.2	666.6	841.4
LIBCOM	3007.9	2295.2	2353.7	1721.6	1363.5
	31.0	31.0	31.0	31.0	31.0
EXP0	61.0	81.3	171.5	159.0	130.5
	7.0	7.0	7.0	7.0	7.0
GEOL	977.4	557.4	500.5	406.4	440.9
	14.0	14.0	14.0	14.0	14.0
PED0	2447.2	713.1	450.4	408.6	387.9
	13.0	13.0	13.0	13.0	13.0

3.2 Goodness of fit

0.37 104.15

We report below the code used to compute the goodness-of-fit measures for model (0) reported in Table 1 of the main paper: Pseudo-R², Akaike information criteria (AIC), and percent of good predictions.

And the same goodness of fit measures for OGAMs.

0.64

```
Le chargement a nécessité le package : nlme
This is mgcv 1.8-28. For overview type 'help("mgcv-package")'.
```

```
gam100 gam300 gam500 gam700 gam900
psR2 0.5323 0.631 0.684 0.7248 0.7565
AIC 77.2170 61.397 53.088 46.7579 41.9259
Pcqp 74.8600 80.387 84.376 87.2566 89.4778
```

3.3 Causal inference

151.3 155.9 160.6

As indicated at the beginning of the online supplementary material, we evaluate the joint significance of *commune* fixed effects on the residuals from auxiliary regressions without such fixed effects. Code below allows to compute the bootstrapped Fisher statistics with 100 replications from parametric ordered logistic model. Note that we use the sure package to compute the surrogate residuals from this parametric model.

```
library(lmtest); library(sandwich); library(sure)
wal1 <- rep(NA, times= nsim <- 100)
for (i in 1: nsim){
    tmp <- surrogate(polm1a) - polm1a$lp
    wal1[i] <- waldtest(lm(tmp~ Reg.Ras$LIBCOM), .~ 1, vcov= vcovHC)$F[2]
}
quantile(wal1, c(.05, .5, .95))</pre>
```

Note that the values obtained are not exactly equal to those reported in the paper because of the bootstrap procedure.

The sure package does not allow to compute surrogate residuals for gam models from the mgcv package. Because this framework is also consistent for OGAMs, we write the function sureOGAM presented and tested in Appendix B.3 to adapt the framework. This function is also available in the file of custom function ./myFcts.R available from the GitHub repo. Hence, we compute the bootstrapped F-statistics for the full set of OGAM belows. The estimation of auxiliary models can be downloaded from https://data.inrae.fr.

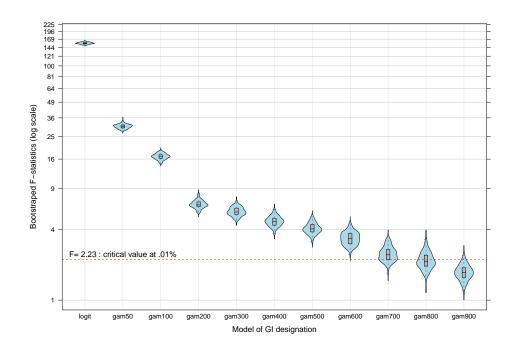
```
load("Inter/gammod.Rda") ; library(ggplot2) ; source("myFcts.R")
omitVar <- function(mod, var, nsim= 100){
    usq <- rep(NA, nsim)
    for(i in 1: nsim) {
        RES <- sureOGAM(mod)
        tmp <- lm(I(RES- mod$linear.pred)~ factor(var))
        usq[ i] <- waldtest(tmp, . ~ 1, vcov= vcovHC)$F[ 2]
    }
    usq
}
wal2 <- sapply(gammod, function(x) omitVar(x, Reg.Ras$LIBCOM, nsim= 100))
apply(wal2[, -1], 2, function(x) quantile(x, c(.05, .5, .95)))</pre>
```

```
gam100 gam200 gam300 gam400 gam500 gam600 gam700 gam800 gam900
5%
                  4.983
                                                     1.699
                                                           1.361
     15.22
           5.724
                         4.033
                                3.522
                                       2.787
                                              2.032
                                4.056 3.373
50%
    16.86 6.504
                  5.658 4.690
                                              2.439
                                                    2.132
                                                            1.722
                                4.916 4.024 3.195 2.827
95%
    18.35 7.429
                  6.536
                        5.487
                                                            2.203
```

Again, the values are not exactly the same. Note that the critical value at 0.01% for the F-distribution in this case is 2.3, as can be assessed from qf(.9999, 31, Inf).

The following plot resumes the specification diagnostics and shows the relevance of OGAMs to control for omitted spatial effects. It corresponds to Figure OA4 of online supplementary appendix.

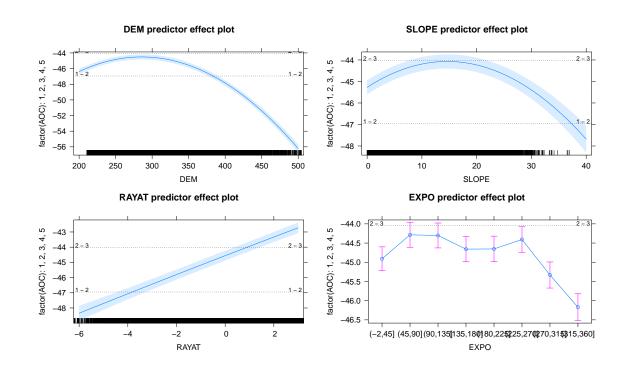
```
library(lattice)
pltdat <- stack(data.frame(logit= wal1, wal2))</pre>
Fstat \leftarrow \text{round}(qf(.9999, 31, Inf), 2)
bwplot(log(values)~ ind, data= pltdat, type=c("1","g"), horizontal= FALSE,
       xlab= 'Model of GI designation',
       ylab= 'Bootstraped F-statistics (log scale)',
       par.settings = list(box.rectangle=list(col='black'),
                           plot.symbol = list(pch='.', cex = 0.1)),
       scales=list(y= list(at= log((1: 15)^2), lab= (1: 15)^2)),
       panel = function(..., box.ratio) {
           panel.grid(h= 0, v = -11)
           panel.abline(h= log((1: 15)^2), col= "grey80")
           panel.violin(..., col = "lightblue",
                         varwidth = FALSE, box.ratio = box.ratio)
           panel.bwplot(..., col='black',
                        cex=0.8, pch='|', fill='gray', box.ratio = .1)
           panel.abline(h= log(Fstat), col= "red", lty= 2, cex= 1.5)
           panel.text(2, log(Fstat)+ .1,
                      paste0("F= ", Fstat, " : critical value at .01%"))})
```



4 Marginal effects

4.1 Parametric ordered logit

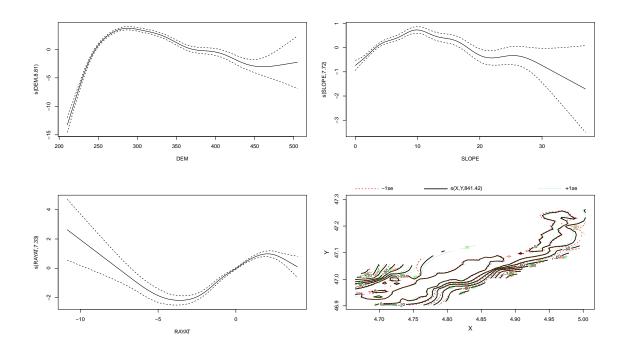
The marginal effects from parametric model polm1 can be directly plotted with the package effect. The following plots corresponds to the dotted lines in Figure OA2 in the online supplementary appendix.



4.2 Ordered generalized additive

The same effect plots can be drawn for the OGAMs models. We report below the effects from the OGAM gam900 which corresponds to a maximum effective degrees of freedom of 900. For all models of gamod, we obtain the gray curves of Figure OA2 in the online supplementary appendix.

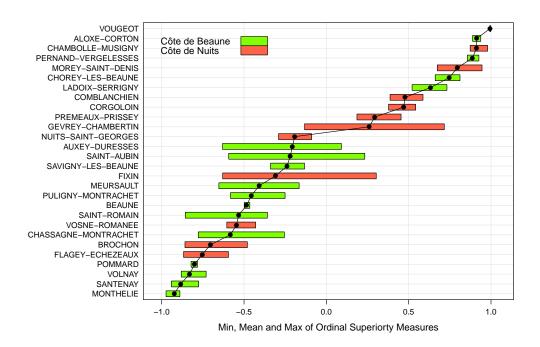
plot(gamod[[10]], pages= 1, scale= 0)



4.3 Ordinal superiority figure

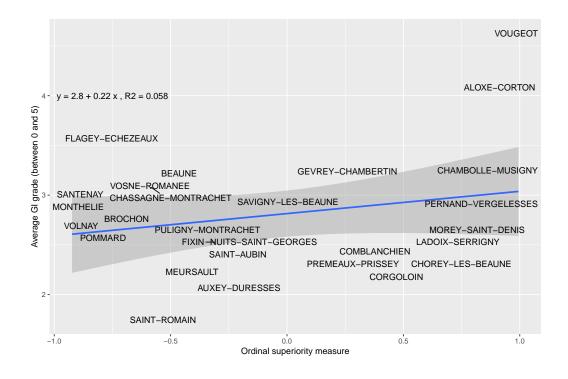
We can now compute ordinal superiority measures for each *communes* relatively to the average. The code below reproduces the Figure 2 of the main paper. Note that we drop the isolated Northern *communes* of *Chenôve*, *Marsannay-la-Côte* and *Couchey* which do not have comparable neighbors. The effect of the proximity to Dijon is too high for these *communes*.

```
library(latticeExtra)
plogi \leftarrow function(x) exp(x/ sqrt(2))/ (1+ exp(x/ sqrt(2)))
xx <- data.frame(sapply(gamod, function(x)</pre>
    2* plogi(I(x$coeff[ 4: 31]- mean(x$coeff[ 4: 31])))- 1))
foo_key \leftarrow list(x = .35, y = .95, corner = c(1, 1),
            text = list(c("Côte de Beaune", "Côte de Nuits")),
            rectangle = list(col = c("chartreuse", "tomato")))
ww <- data.frame(xx,</pre>
                 LIBCOM= substr(names(gamod[[1]]$coef[ 4: 31]), 7, 30),
                 REGION= c(rep("tomato", 12), rep("chartreuse", 16)),
                 MIN= apply(xx[ 8: 10], 1, min),
                 MAX= apply(xx[ 8: 10], 1, max),
                 MEAN= apply(xx[ 8: 10], 1, mean))
segplot(reorder(factor(LIBCOM), MEAN)~ MIN+ MAX, length= 5, draw.bands= T,
        data= ww[order(ww$MEAN), ], center= MEAN, type= "o",
        key= foo_key, col= as.character(ww$REGION[order(ww$MEAN)]),
        unit = "mm", axis = axis.grid, col.symbol= "black", cex= 1,
        xlab= "Min, Mean and Max of Ordinal Superiorty Measures")
```



4.4 Correlation between Communes

Below the code to produce the Figure OA5 in online supplementary appendix. It shows the correlation between the average vertical GI score and the mean ordinal superiority measures estimated from OGAMs with highest effective degrees of freedom (gam900).



5 Informational content

5.1 Decomposition tables

We proceed to the decomposition of variance of the latent quality index from the GI designations. The mathematical formula and codes used in the decomposition are presented and tested in Appendix B.4. These functions are also available in the file of custom function ./myFcts.R of the GitHub repo. The following codes perform the decomposition for the subset of models reported in Table 2 of the main paper. The predictions of the latent quality index in the first rows need some time to run.

	gam100	gam300	gam500	gam700	gam900
Total Signal	85.3	94.5	96.0	97.3	97.5
Total Noise	14.7	5.5	4.0	2.7	2.5
Joint Signal	69.7	70.1	76.7	75.2	78.6
Joint Noise	15.6	24.3	19.3	22.2	18.9
Vertical Signal	54.1	48.8	51.7	56.2	65.2
Vertical Residual	15.7	21.4	25.0	18.9	13.4
Vertical Noise	31.3	45.7	44.4	41.1	32.3
Horizontal Signal	18.3	16.6	25.6	22.6	23.8
Horizontal Residual	51.4	53.6	51.1	52.6	54.8
Horizontal Noise	67.0	77.9	70.5	74.7	73.7

6 Models for GIs of 1936

6.1 Descriptive statistics

We turn now to the detail of the analysis with historical GIs of 1936. We make the same econometric analysis than for actual GIs, first with some descriptive statistics.

```
1
            2
                   3
                          4
                                 5
   7124 11452 5111
                               39
                        575
2
      5
           536 15175
                      8101
                              261
3
      0
             1
                  13
                             1604
                          3
```

6.2 Estimation

We estimate both the parametric and generalized additive models we the following codes. Because of the long computation times, the reader would prefer to fit the models individually.

```
library(MASS)
polm2 <- polr(factor(AOCo)~ 0+ LIBCOM+ EXPO+ GEOL+ PEDO</pre>
               + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
               + poly(X, 3)* poly(Y, 3), data= Reg.Old, Hess= T)
polm2a <- polr(factor(AOCo)~ 0+ EXPO+ GEOL+ PEDO</pre>
                + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
                + poly(X, 3)* poly(Y, 3), data= Reg.Old, Hess= T)
polm2b <- polr(factor(AOCo)~ 0+ LIBCOM+ EXPO+ GEOL+ PEDO</pre>
                + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
              , data= Reg.Old, Hess= T)
library(mgcv)
listk <- c(25, 50, 75, 100, 125, 150, 200, 250)
gamold <- vector("list", length(listk))</pre>
system.time(
    for (i in 1: length(listk)){
        gamold[[ i]] <- gam(AOCo~ 0+ LIBCOM+ EXPO+ GEOL+ PEDO</pre>
                             + s(DEM)+ s(SLOPE)+ s(RAYAT)
                             + s(X, Y, k= listk[ i])
                           , data= Reg.Old, family= ocat(R= 3))
    }
)
names(gamold) <- paste0("gam", listk)</pre>
save(gamold, file= "Inter/gamold.Rda")
gammold <- vector("list", length(listk))</pre>
system.time(
for (i in 1: length(listk)){
    gammold[[ i]] <- gam(AOCo~ 0+ EXPO+ GEOL+ PEDO</pre>
                          + s(DEM)+ s(SLOPE)+ s(RAYAT)
                          + s(X, Y, k= listk[ i])
                        , data= Reg.Old, family= ocat(R= 3))
})
names(gammold) <- paste0("gam", listk)</pre>
save(gammold, file= "Inter/gammold.Rda")
```

```
      utilisateur
      système
      écoulé

      20454.2
      309.5
      20766.0

      utilisateur
      système
      écoulé

      28307.5
      462.8
      28772.0
```

6.3 Significance

We first assess the joint significance of variables in all OGAMs of GIs designation. The following results are reported in Table OA2 in the online supplemental appendix.

```
load("Inter/gamold.Rda")
 res2a <- anova(polm2, polm2b)</pre>
 res2 <- Anova(polm2)</pre>
 sapply(gamold[ 1: 7], resume)
           gam25
                   gam50
                           gam100
                                    gam125
                                                      gam200
                                             gam150
                                                               gam250
          1503.8 1196.2
s(DEM)
                            197.7
                                     219.6
                                              144.8
                                                       265.0
                                                                253.0
             8.6
                     8.8
                              7.6
                                       8.4
                                                8.2
                                                          8.7
                                                                   7.4
           534.2
                                                                 169.1
s(SLOPE)
                   478.1
                            466.5
                                     332.8
                                              297.1
                                                       190.4
             8.7
                     8.8
                              8.7
                                       8.8
                                                8.7
                                                          8.8
                                                                   7.5
           339.4
                   208.8
                            139.4
                                     150.2
                                               99.2
                                                         87.7
s(RAYAT)
                                                                 142.8
             8.3
                     8.0
                              1.1
                                       8.0
                                                8.1
                                                          7.4
                                                                   7.4
s(X,Y)
          4789.1 6760.0 14558.9 15981.2 17285.3 18979.3 20905.7
                             98.0
                                     122.4
            23.9
                    48.7
                                              147.1
                                                       194.3
                                                                235.3
          5828.9 3720.9
                           2639.2
                                    2378.3
                                             2177.2
                                                      1831.7
                                                               1264.7
LIBCOM
            25.0
                             25.0
                                      25.0
                    25.0
                                               25.0
                                                        25.0
                                                                  25.0
EXPO
           258.0
                   177.5
                            131.9
                                     101.2
                                               58.5
                                                        43.0
                                                                  64.0
             7.0
                     7.0
                              7.0
                                       7.0
                                                7.0
                                                          7.0
                                                                   7.0
GEOL
          1018.5 1047.0
                            692.1
                                     772.8
                                              710.2
                                                       585.8
                                                                 509.3
            14.0
                    14.0
                             14.0
                                      14.0
                                               14.0
                                                        14.0
                                                                 14.0
PED0
          3335.3 2820.6
                            898.8
                                     660.3
                                              599.4
                                                       537.0
                                                                539.3
            12.0
                    12.0
                             12.0
                                      12.0
                                               12.0
                                                        12.0
                                                                  12.0
```

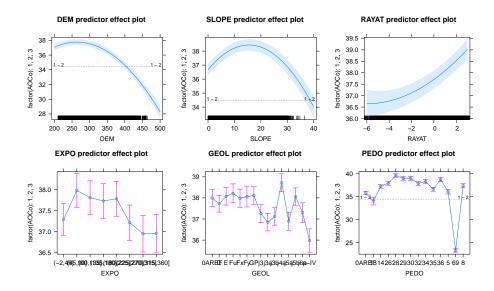
6.4 Goodness of fit

Goodness of fit measures from the same Table OA2 in the online supplementary appendix.

```
round(c(McFaddenR2= psR2(polm2), AIC= AIC(polm2)/ 1000,
        Pcgp= sum(diag(table(predict(polm2), Reg.Old$AOCo)))/ nrow(Reg.Old)), 2)
 rbind(Pcgp= sapply(gamold[1: 7], pcgp),
      AIC= sapply(gamold[1: 7], AIC)/ 1000,
      psR2= sapply(gamold[1: 7 ], psR2))
McFaddenR2
                   AIC
                              Pcgp
      0.45
                 45.22
                              0.82
                gam50 gam100 gam125 gam150 gam200
       gam25
                                                         gam250
Pcgp 82.8820 83.7580 87.8840 88.606 89.8400 91.3480 92.2060
     43.9251 41.2140 31.8196 30.039 28.0878 25.1203 23.1212
psR2 0.4629 0.4968 0.6132 0.636 0.6606 0.6982 0.7236
```

6.5 Marginal effects

Marginal effect can be assessed as for current GIs, the code belows can be used on the models from the gamold object to produce Figure OA6 in the online supplementary appendix.



6.6 Ordinal superiority measures

Ordinal superiority for the GIs of 1936, that corresponds to Figure AO7 in the online supplementary appendix.

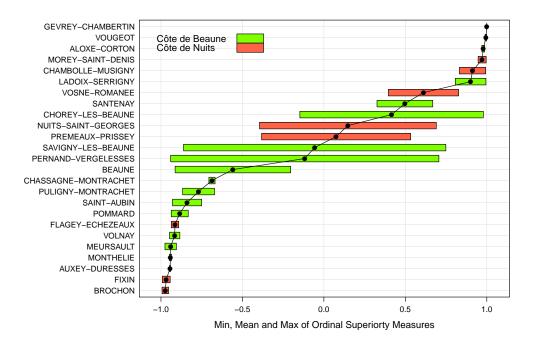
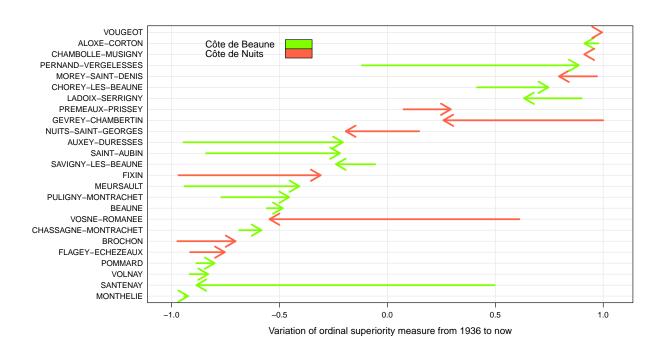


Figure 1: Ordinal superiorty measures for the 1936 GIs

6.7 Temporal variations

The differences between current ordinal superiority measures and those of 1936, this corresponds to the Figure 3 of the main paper.



6.8 Decomposition table

The code below compute the decomposition table for GIs of 1936, unreported.

	gam25	gam50	gam100	gam125	gam150	gam200	gam250
Total Signal	95.9	98.3	97.2	97.4	100.0	99.1	99.6
Total Noise	4.1	1.7	2.8	2.6	0.0	0.9	0.4
Joint Signal	90.8	95.0	72.2	56.1	98.5	59.2	84.4
Joint Noise	5.1	3.4	25.0	41.4	1.5	39.9	15.2
Vertical Signal	2.4	1.3	19.7	16.8	3.1	20.3	13.0
Vertical Residual	88.4	93.7	52.6	39.2	95.4	38.9	71.4
Vertical Noise	93.5	97.1	77.5	80.6	96.9	78.8	86.6
Horizontal Signal	86.0	92.0	54.5	31.7	97.8	39.7	74.8
Horizontal Residual	4.8	3.0	17.7	24.4	0.7	19.5	9.6
Horizontal Noise	9.9	6.4	42.7	65.8	2.1	59.4	24.8

7 Alternative GI designations

7.1 Change latent vineyard quality

We conclude this work with the simulations of alternative GIs designations schemes. Below are scenarios S0 to S3 where the counterfactual GI designations are computed according to (we note $\hat{q}_i^{gam} = B(X_i)^{\mathsf{T}} \hat{\beta}^{gam}$):

$$y_{i}^{S0} = \sum_{j=0}^{5} j \cdot \mathbb{1}[\hat{\alpha}_{j_{i}-1} + \hat{\mu}_{c_{i}} \geq \hat{q}_{i}^{gam} + \hat{\xi}_{i}^{sur} \geq \hat{\alpha}_{j_{i}} + \hat{\mu}_{c_{i}}]$$

$$y_{i}^{S1} = \sum_{j=0}^{5} j \cdot \mathbb{1}[\hat{\alpha}_{j_{i}-1} + \hat{\mu}_{c_{i}} \geq \hat{q}_{i}^{gam} \geq \hat{\alpha}_{j_{i}} + \hat{\mu}_{c_{i}}]$$

$$y_{i}^{S2} = \sum_{j=0}^{5} j \cdot \mathbb{1}[\hat{\alpha}_{j_{i}-1} \geq \hat{q}_{i}^{gam} + \hat{\xi}_{i}^{sur} \geq \hat{\alpha}_{j_{i}}]$$

$$y_{i}^{S3} = \sum_{j=0}^{5} j \cdot \mathbb{1}[\hat{\alpha}_{j_{i}-1} \geq \hat{q}_{i}^{gam} \geq \hat{\alpha}_{j_{i}}]$$

	(-Inf1]	(-1,5.34]	(5.34.14]	(14.217	(21. Infl
1	7847	1510		40	9
2	1688	9476	2126	158	98
3	146	2360		2005	146
4	25	117	2160	5956	421
5	0	1	84	455	1364
	(-Inf,-1]	(-1,5.34]	(5.34,14]	(14,21]	(21, Inf]
1	8592	1021	62	0	0
2	562	11787	1147	50	0
3	7	929	23528	834	11
4	0	9	1089	7446	135
5	0	0	1	363	1540
	(-Inf,-1]	(-1,5.34]	(5.34,14]	(14,21]	(21, Inf]
1	(-Inf,-1] 7580	(-1,5.34] 1770		(14,21] 34	(21, Inf] 11
1 2			280		
_	7580	1770	280 3482	34	11
2	7580 2150	1770 7655	280 3482 16162	34 150 3521	11 109
2	7580 2150 409	1770 7655 5038	280 3482 16162	34 150 3521	11 1 0 9 179
2 3 4	7580 2150 409 28	1770 7655 5038 127	280 3482 16162 2039	34 150 3521 5389	11 109 179 1096
2 3 4	7580 2150 409 28 0	1770 7655 5038 127	280 3482 16162 2039 185	34 150 3521 5389 611	11 109 179 1096 1100
2 3 4	7580 2150 409 28 0	1770 7655 5038 127 8	280 3482 16162 2039 185	34 150 3521 5389 611	11 109 179 1096 1100
2 3 4 5	7580 2150 409 28 0 (-Inf,-1]	1770 7655 5038 127 8 (-1,5.34]	280 3482 16162 2039 185 (5.34,14] 73	34 150 3521 5389 611 (14,21]	11 109 179 1096 1100 (21, Inf]
2 3 4 5	7580 2150 409 28 0 (-Inf,-1] 8197	1770 7655 5038 127 8 (-1,5.34] 1403	280 3482 16162 2039 185 (5.34,14] 73 2875	34 150 3521 5389 611 (14,21] 2	11 109 179 1096 1100 (21, Inf] 0
2 3 4 5	7580 2150 409 28 0 (-Inf,-1] 8197 1624	1770 7655 5038 127 8 (-1,5.34] 1403 8961	280 3482 16162 2039 185 (5.34,14] 73 2875	34 150 3521 5389 611 (14,21] 2 85	11 109 179 1096 1100 (21, Inf] 0 1

7.2 Add a vertical level in GIs

Here we simulate counterfactual GIs designations from scenarios S4, S5, and S6. In each case, we use the GIs from S0 and add a vertical level by computing the mean of the thresholds.

6	5	4	3	2	1	
0	0	0	0	0	9675	1
0	0	0	6146	7400	0	2
0	0	25309	0	0	0	3
0	8679	0	0	0	0	4
1904	0	0	0	0	0	5
6	5	4	3	2	1	
0	0	0	0	0	9675	1
0	0	0	0	13546	0	2
0	0	12517	12792	0	0	3
0	8679	0	0	0	0	4
1904	0	0	0	0	0	5
6	5	4	3	2	1	
0	0	0	0	0	9675	1
0	0	0	0	13546	0	2
0	0	0	25309	0	0	3
0	4607	4072	0	0	0	4
1904	0	0	0	0	0	5

7.3 Decomposition table

And we conclude with the decomposition that are reported Table 3 (p.27) of the Working Paper.

```
decf <- sapply(names(Simv[, 76: 83]), function(x)
    c("Total Signal"= var(Simv[, "ltt"]), "Total Noise"= pi^2/ 3,
        jointSignal(Simv, "ltt", vt= x), jointNoise(Simv, "ltt", vt= x),
        vertiSignal(Simv, "ltt", vt= x), vertiResid(Simv, "ltt", vt= x),
        vertiNoise(Simv, "ltt", vt= x),
        horizSignal(Simv, "ltt", vt= x), horizResid(Simv, "ltt", vt= x),
        horizNoise(Simv, "ltt", vt= x))
round(t(apply(decf, 1, function(x) x/ (pi^2/ 3+ decf[1, ])* 100)), 1)</pre>
```

```
OLD
                          S0
                               SI SII SIII SIV
                                                  SV SVI
Total Signal
                   97.5 97.5 97.5 97.5 97.5 97.5 97.5
Total Noise
                    2.5 2.5 2.5 2.5 2.5 2.5 2.5
Joint Signal
                   48.0 78.2 81.0 79.5 81.5 79.0 79.5 78.9
Joint Noise
                   49.5 19.3 16.5 18.1 16.0 18.5 18.0 18.6
Vertical Signal
                   34.4 64.6 68.2 69.7 72.6 65.6 66.1 65.5
Vertical Residual
                   13.6 13.6 12.8 9.7 8.9 13.4 13.4 13.4
Vertical Noise
                   63.1 32.9 29.3 27.8 24.9 31.9 31.4 32.0
Horizontal Signal
                   23.8 23.8 23.8 23.8 23.8 23.8 23.8 23.8
Horizontal Residual 24.2 54.4 57.2 55.7 57.7 55.2 55.7 55.1
Horizontal Noise
                   73.7 73.7 73.7 73.7 73.7 73.7 73.7
```

References

Bivand, R. S., Pebesma, E. and Gomez-Rubio, V. (2013). *Applied spatial data analysis with R, Second edition*. Springer, NY.

Leeper, T. J. (2017). dataverse: R Client for Dataverse 4. R package version 0.2.0.

A Session information

sessionInfo()

R version 3.6.0 (2019-04-26) Platform: x86_64-pc-linux-gnu (64-bit) Running under: Ubuntu 18.04.2 LTS Matrix products: default BLAS: /usr/lib/x86_64-linux-gnu/blas/libblas.so.3.7.1 LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.7.1 locale: [1] LC_CTYPE=fr_FR.UTF-8 LC_NUMERIC=C [3] LC_TIME=fr_FR.UTF-8 LC_COLLATE=fr_FR.UTF-8 [5] LC_MONETARY=fr_FR.UTF-8 LC_MESSAGES=fr_FR.UTF-8 [7] LC_PAPER=fr_FR.UTF-8 LC_NAME=C [9] LC_ADDRESS=C LC TELEPHONE=C [11] LC_MEASUREMENT=fr_FR.UTF-8 LC_IDENTIFICATION=C attached base packages: [1] stats graphics grDevices utils datasets methods [7] base other attached packages: [1] latticeExtra_0.6-28 effects_4.0-3 gridExtra_2.3 [4] ggplot2_3.1.0 sure_0.2.0 sandwich_2.5-0 [7] lmtest_0.9-36 zoo_1.8-4 mgcv_1.8-28 [10] nlme_3.1-140 car_3.0-2 carData_3.0-1 [13] MASS_7.3-51.1 RColorBrewer_1.1-2 lattice_0.20-38 [16] sp_1.3-1 loaded via a namespace (and not attached): [1] tidyselect_0.2.5 purrr_0.3.2 splines_3.6.0 [4] haven_1.1.2 survival_2.43-3 colorspace_1.3-2 [7] rlang_0.3.4 nloptr_1.0.4 pillar_1.3.0 [10] foreign_0.8-71 glue_1.3.0 withr_2.1.2 [13] readxl_1.1.0 bindrcpp_0.2.2 plyr_1.8.4 [16] bindr_0.1.1 munsell_0.5.0 gtable_0.2.0 [19] cellranger_1.1.0 zip_1.0.0 labeling_0.3 [22] rio_0.5.10 forcats_0.3.0 curl_3.2 [25] Rcpp_1.0.0 scales_1.0.0 $abind_1.4-5$ [28] lme4_1.1-18-1 $hms_0.4.2$ openxlsx_4.1.0 [31] dplyr_0.7.8 survey_3.33-2 grid_3.6.0 [34] rgdal_1.3-6 tools_3.6.0 magrittr_1.5 [37] lazyeval_0.2.1 tibble_1.4.2 crayon_1.3.4 [40] pkgconfig_2.0.2 Matrix_1.2-17 data.table_1.11.4 [43] minqa_1.2.4 assertthat_0.2.1 R6_2.4.0 [46] nnet_7.3-12 compiler_3.6.0

B Custom R functions

B.1 Translation of geology

```
trans_geol <- data.frame(</pre>
    GEOL= Reg.Ras$GEOL[!duplicated(Reg.Ras$GEOL)],
        "Calcaires massifs de \"Comblanchien\" (Bathonien sup.)",
        "Marnes et calcaires divers (Callovien inférieur)",
        "Marnes et calcaires argileux (Oxfordien moyen)",
        "Eboulis ordonnés cryoclastiques et colluvions diverses",
        "Oolithe ferrugineuse (Oxfordien moyen-sup)",
        "Calcaires hydrauliques de Molesmes et Noiron (Oxfordien sup.)",
        "Colluvions diverses",
        "Dépôts argilo-limoneux, sables et graviers du Villafranchien",
        "Calcaires de Tonnerre, Oisellemont et calcaires á Astartes",
        "Eboulis et glissements de terrains",
        "Calcaires grenus bicolores (Bathonien terminal)",
        "Terrasse argilo-limoneuse de Saint-Usage",
        "Formation de Saint-Cosme (marnes fluvio-lacustres varvées)",
        "Alluvions anciennes indifférenciées, argilo-limoneuses",
        "Calcaires bioclastiques, graveleux, á oolithes (Bathonien inf.)"
    ),
    GEOe= c(
        "Massive limestones from \"Comblanchien\" (upper Bathonian)",
        "Various marls and limestones (lower Callovian)",
        "Marls and argillaceous limestones (middle Oxfordian)",
        "Ordered cryoclastic scree and various colluviums",
        "Ferruginous Oolite (middle-upper Oxfordian)",
        "Hydraulic limestones of Molesmes and Noiron (upper Oxfordian)",
        "Various colluviums",
        "Clay-silt deposits, sand and gravel from Villafranchien",
        "Limestones of Thunder, Oisellemont and limestones in Astartes",
        "Screes and landslides",
        "Two-tone gray limestones (terminal Bathonian)",
        "Clay-silty terrace of Saint-Usage",
        "Formation of Saint-Cosme (varnished fluvio-lacustrine marls)",
        "Undifferentiated ancient alluvium, clay-silty",
        "Bioclastic limestones, gravelly, with oolites (lower Bathonian)")
)
```

B.2 Translation of pedology

```
trans_pedo <- data.frame(</pre>
    PEDO= Reg.Ras$PEDO[!duplicated(Reg.Ras$PEDO)],
        "Vignoble de la Côte de de Beaune",
        "Cônes de déjection du pied de Côte",
        "Côteaux viticoles des Hautes Côtes de Nuits",
        "Courtes pentes marneuses des plateaux plio-pléistocène",
        "Piedmont de la côte viticole",
        "Versants pentus des Hautes Côtes de Beaune",
        "Sommets des collines des Hautes Côtes de Beaune",
        "Alluvions récentes calcaires des vallées (Ouche, Tille, Meuzin)",
        "Pentes liasiques du Haut-Auxois",
        "Basses terrasses gravelo-caillouteuses des plaines alluviales",
        "Basses terrasses argileuses des plaines alluviales",
        "Terrasse argilo-limoneuse de Saint-Usage",
        "Vignoble de la Côte de Nuits",
        "Rebord oriental des plateaux calcaires dominant la Côte viticole"
    ),
    PEDe= c(
        "Vineyard of the Côte de Beaune",
        "Coot footing cones",
        "Wine hills of Hautes Côtes de Nuits",
        "Oxfordian limestone-marly trays of the Hautes Côtes",
        "Short marly slopes of Plio-Pleistocene plateaus",
        "Piedmont of the vineyard of the Côte",
        "Sloping slopes of the Hautes Côtes de Beaune".
        "Summits of the hills of the Hautes Côtes de Beaune",
        "Recent alluvial limestone valleys (Ouche, Tille, Meuzin)",
        "Liastic slopes of Haut-Auxois",
        "Gravelo-stony low terraces of alluvial plains",
        "Low clay terraces of alluvial plains",
        "Vineyard of the Côte de Nuits".
        "Eastern edge of the limestone plateaus overlooking the Côte"
    )
)
```

B.3 Surrogate Residuals

The R package sure allows to simulate the surrogate residuals from a large panel of ordered parametric models https://koalaverse.github.io/sure/index.html. Actually, it is not possible to compute the residuals for semiparametric ordered generalized additive model fitted with the package mgcv. Here, we first define the truncLogis function for the simulation of random draws from a truncated logistic distribution with a vector of inputs (locations and thresholds) as the package truncdist is only designed for a given value of location and thresholds. Then, we code the function surePOLR inspired from the sure package which simulate surrogate residuals from polr models from the MASS package. This will be used to check the validity of used functions.

```
truncLogis <- function(n, spec, a = -Inf, b = Inf, ...) {
    require(truncdist)
    p \leftarrow runif(n, min = 0, max = 1)
    G <- get(paste("p", spec, sep = ""), mode = "function")</pre>
    Gin <- get(paste("q", spec, sep = ""), mode = "function")</pre>
    G.a \leftarrow G(a, ...)
    G.b \leftarrow G(b, \ldots)
    pmin(pmax(a, Gin(G(a, ...) + p * (G(b, ...) - G(a, ...)), ...)), b)
}
surePOLR <- function(mod, newd= NULL){</pre>
    if (mod$method!= "logistic") stop("Logistic required")
    gg <- as.numeric(mod$zeta)</pre>
    if (is.null(newd)){
        g1 <- as.integer(model.response(model.frame(mod)))</pre>
        g6 \leftarrow mod p
    } else {
        g1 <- as.integer(newd[, "AOCc"])</pre>
        g6 <- gg[ 1]-qlogis(predict(mod, newdata= newd, type= 'probs')[, 1])</pre>
    }
    nn <- length(g1)</pre>
    suls <- sapply(g1, switch,</pre>
                     "1"= c(-Inf , gg[ 1]), "2"= c(gg[ 1], gg[ 2]),
                     "3"= c(gg[ 2], gg[ 3]), "4"= c(gg[ 3], gg[ 4]),
                     "5"= c(gg[ 4], Inf
                                           ))
    sls <- data.frame(unlist(t(suls)))</pre>
    truncLogis(nn, spec= "logis", a= sls[, 1], b= sls[, 2],
                location= g6, scale= 1)
}
```

```
sure1 <- surrogate(polm1)+ polm1$zeta[ 1]
sure2 <- resids(polm1)
polr1 <- surePOLR(polm1) ; polr2 <- surePOLR(polm1)- polm1$lp</pre>
```

The custom function surePOLR allows to compute the same surrogate value and surrogate residuals than the functions surrogate and resids from the sure package.

Now we use the same structure to simulate the surrogate residuals for the OGAM through the function sureOGAM. Again, the function is tested for a random OGAM.

```
sureOGAM <- function(mod, newd= NULL){</pre>
```

```
if (is.null(newd)){
    g1 <- as.integer(mod$y)
    g6 <- mod$linear.predictors
} else {
    g1 <- as.integer(newd[, names(mod$model[ 1])])
    g6 <- predict(mod, newdata= newd)
}
nn <- length(g1)
gt <- data.frame(rep(NA, nn), rep(NA, nn))
gg <- c(mod$family$getTheta(TRUE), Inf)
kk <- c(- Inf, gg[ 1])
for (j in 2: length(unique(g1))) kk <- rbind(kk, c(gg[ j- 1], gg[ j]))
gt <- data.frame(t(sapply(g1, function(x) kk[x, ])))
truncLogis(nn, spec= "logis", a= gt[, 1], b= gt[, 2], location= g6)
}</pre>
```

```
library(mgcv)
fit.ogam <- gam(AOC~ poly(DEM, 2)+ poly(SLOPE, 2)</pre>
                + poly(RAYAT, 2)+ poly(ASPECT, 2)+ poly(PERMEA, 2)
              , family= ocat(R= 5), data= Reg.Ras)
ogam1 <- sureOGAM(fit.ogam)</pre>
ogam2 <- sureOGAM(fit.ogam) - fit.ogam$linear.pred
par(mfrow= c(3, 2))
plot(sure1, polr1)
abline(h= fit.polr$zeta, v= fit.polr$zeta, lty= 2, col= "blue")
abline(0, 1, col= "orange")
plot(sure2, polr2)
abline(0, 1, col= "orange")
plot(polr1, ogam1- mean(ogam1))
abline(h= fit.ogam$family$getTheta(TRUE) - mean(ogam1),
       v= fit.polr$zeta, lty= 2, col= "blue")
abline(0, 1, col= "orange")
plot(polr2, ogam2)
abline(0, 1, col= "orange")
plot(sure1, ogam1- mean(ogam1))
abline(h= fit.ogam$family$getTheta(TRUE) - mean(ogam1),
       v= fit.polr$zeta, lty= 2, col= "blue")
abline(0, 1, col= "orange")
plot(sure2, ogam2)
abline(0, 1, col= "orange")
```

B.4 Decomposition terms

For each terms of the decomposition presented in the main text, we code a different function as reported below. First note the vector of predicted latent quality index $\hat{q}_i = B(X_i)^{\mathsf{T}}\hat{\beta}$. With N_y , N_c and $N_{y,c}$ the numbers of vineyard plots respectively in rank y, in *commune* c and both in rank y and *commune* c, we define:

$$\overline{q}_{y_i} = \frac{1}{N_{y_i}} \sum_{\ell=1}^{N} \mathbb{1}[y_{\ell} = y_i] \cdot \hat{q}_{\ell}
\overline{q}_{c_i} = \frac{1}{N_{c_i}} \sum_{\ell=1}^{N} \mathbb{1}[c_{\ell} = c_i] \cdot \hat{q}_{\ell}
\overline{q}_{y_i,c_i} = \frac{1}{N_{y_i,c_i}} \sum_{\ell=1}^{N} \mathbb{1}[(y_{\ell}, c_{\ell}) = (y_i, c_i)] \cdot \hat{q}_{\ell}$$

The **joint signal** terms is the variance of the expected quality conditionally on vertical and horizontal dummies:

$$\mathbb{V}\{\mathbb{E}[q(X^*) \mid y, c]\} = \frac{1}{N} \sum_{i=1}^{N} \left[\overline{q}_{y_i, c_i} - \overline{q} \right]^2$$
 (1)

```
jointSignal <- function(dat, lt, vt= "AOC", hz= "LIBCOM"){
    jS <- rep(0, nrow(dat))
    for (i in unique(dat[, vt])){
        for (j in unique(dat[, hz])){
            tmp <- dat[, vt]== i & dat[, hz]== j
            jS[ tmp] <- mean(dat[tmp, lt])
        }
    }
    c("Joint Signal"= var(jS))
}</pre>
```

The **joint noise** terms is the expectation of the variance quality conditionally on vertical and horizontal dummies:

$$\mathbb{E}\{\mathbb{V}[q(X^*) \mid y, c]\} = \sum_{y=1}^{J} \sum_{c=1}^{C} \left[\frac{N_{y,c}}{N} \sum_{i=1}^{N} \mathbb{1}[(y_i, c_i) = (y, c)] \cdot (\hat{q}_i - \overline{q}_{y_i, c_i})^2 \right]$$
(2)

```
jointNoise <- function(dat, lt, vt= "AOC", hz= "LIBCOM"){
    jN <- 0
    for (i in unique(dat[, vt])){
        for (j in unique(dat[, hz])){
            tmp <- dat[, vt]== i & dat[, hz]== j
            if (sum(tmp)> 1) jN <- jN+ var(dat[ tmp, lt])* mean(tmp)
        }
    }
    c("Joint Noise"= jN)
}</pre>
```

The **vertical signal** terms is the variance of the expectation quality conditionally on vertical GI dummies:

$$\mathbb{V}\{\mathbb{E}[q(X^*) \mid y]\} = \frac{1}{N} \sum_{i=1}^{N} [\overline{q}_{y_i} - \overline{q}]^2$$
 (3)

```
vertiSignal <- function(dat, lt, vt= "AOC", hz= "LIBCOM"){
    vS <- rep(0, nrow(dat))
    for (i in unique(dat[, vt])){
        vS[ dat[, vt]== i] <- mean(dat[dat[, vt]== i, lt])
    }
    c("Vertical Signal"= var(vS))
}</pre>
```

The **vertical residual** terms is the expectation of the conditional on horizontal variance of the expectation quality conditionally on vertical GI dummies:

$$\mathbb{E}\{\mathbb{V}[\mathbb{E}(q(X^*) \mid y, c) \mid c]\} = \sum_{y=1}^{J} \left[\frac{N_y}{N} \sum_{i=1}^{N} (\overline{q}_{y_i} - \overline{q})^2 \right]$$
(4)

The **vertical Noise** terms is the expectation of the variance of the quality conditionally on vertical GI dummies:

$$\mathbb{E}\{\mathbb{V}[q(X^*) \mid y]\} = \sum_{y=1}^{J} \left[\frac{N_y}{N} \sum_{i=1}^{N} \mathbb{1}[y_i = y] \cdot (\hat{q}_i - \overline{q}_{y_i})^2 \right]$$
 (5)

```
vertiNoise <- function(dat, lt, vt= "AOC", hz= "LIBCOM"){
    vN <- 0
    for (i in unique(dat[, vt])){
        vN <- vN+ var(dat[dat[, vt]== i, lt])* mean(dat[, vt]== i)
    }
    c("Vertical Noise"= vN)
}</pre>
```

The **horizontal signal** terms is the variance of the expectation quality conditionally on horizontal GI dummies:

$$\mathbb{V}\{\mathbb{E}[q(X^*) \mid c]\} = \frac{1}{N} \sum_{i=1}^{N} \left[\overline{q}_{c_i} - \overline{q} \right]^2$$
 (6)

```
horizSignal <- function(dat, lt, vt= "AOC", hz= "LIBCOM"){
   hS <- rep(0, nrow(dat))
   for (j in unique(dat[, hz])){
      hS[ dat[, hz]== j] <- mean(dat[dat[, hz]== j, lt])
   }
   c("Horizontal Signal"= var(hS))
}</pre>
```

The **horizontal residual** terms is the expectation of the conditional on vertical variance of the expectation quality conditionally on horizontal GI dummies:

$$\mathbb{E}\{\mathbb{V}[\mathbb{E}(q(X^*) \mid y, c) \mid y]\} = \sum_{c=1}^{C} \left[\frac{N_c}{N} \sum_{i=1}^{N} (\overline{q}_{c_i} - \overline{q})^2 \right]$$
 (7)

```
horizResid <- function(dat, lt, vt= "AOC", hz= "LIBCOM"){
    sig <- rep(0, nrow(dat)) ; hR <- 0
    for (i in unique(dat[, vt])){
        for (j in unique(dat[, hz])){
            tmp <- dat[, vt]== i & dat[, hz]== j
            sig[ tmp] <- mean(dat[ tmp, lt])
        }
    }
    for (j in unique(dat[, hz])){
        hR <- hR+ var(sig[dat[, hz]== j])* mean(dat[, hz]== j)
    }
    c("Horizontal Residual"= hR)
}</pre>
```

The **horizontal Noise** terms is the expectation of the variance of the quality conditionally on horizontal GI dummies:

$$\mathbb{E}\{\mathbb{V}[q(X^*) \mid c]\} = \sum_{c=1}^{C} \left[\frac{N_c}{N} \sum_{i=1}^{N} \mathbb{1}[c_i = c] \cdot (\hat{q}_i - \overline{q}_{c_i})^2 \right]$$
(8)

```
horizNoise <- function(dat, lt, vt= "AOC", hz= "LIBCOM"){
   hN <- 0
   for (j in unique(dat[, hz])){
      hN <- hN+ (var(dat[dat[, hz]== j, lt])* mean(dat[, hz]== j))
   }
   c("Horizontal Noise"= hN)
}</pre>
```