

# The informational content of geographical indications

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## Abstract

This file contains the R codes associated with the paper "The informational content of geographical indications" AAWE Working Paper No XXX. Data, code and results are under the copyleft licence GNU GPL V3 (licence notices must be preserved). Data are available from the INRA dataverse website: <https://data.inra.fr/geoInd>. Some R functions are reported in the Appendix to preserve the visibility of codes. The most recent version of this document and a Shiny application are available from the online repository: <https://github.com/jsay/geoInd>.

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# 1 Descriptive Statistics

## 1.1 Data shaping

The details of data construction are presented (in French) in the data paper: <https://github.com/jsay/geoInd/blob/master/DataPaper.pdf> which also contains the details of the variables used here. The file that results from these preliminary treatments can be downloaded from the INRA dataverse server: <https://data.inra.fr/geoInd/GeoRas.Rda>. The following code allows to load this file once downloaded and located in the /Inter/ folder at the root of the working directory of the R session (CHANGE). It loads a `SpatialPolygonDataFrame` object from the `sp` package that contains the characteristics of the vineyard plots under consideration (session information used for this article is reported at Section XX).

The following code also reshapes some variables of particular interest:

- It reorders the *commune* levels along the North-South gradient
- It standardizes the variable about solar radiation
- It recodes the variable about exposition in 8 quadrants
- It projects the geographical coordinates inside the WGS84 system
- It selects the parcels with GIs and drop omitted values

---

```
library(sp) ; load("Inter/GeoRas.Rda")
Geo.Ras$LIBCOM <- factor(Geo.Ras$LIBCOM, levels=
  unique(Geo.Ras$LIBCOM[order(Geo.Ras$YCHF, decreasing= T)]))
Geo.Ras$RAYAT <- as.numeric(scale(Geo.Ras$SOLAR))
Geo.Ras$EXPO <- cut(Geo.Ras$ASPECT, breaks= c(-2, 1: 8* 45))
GR84 <- spTransform(Geo.Ras, CRS("+proj=longlat +ellps=WGS84"))
dd <- coordinates(GR84) ; Geo.Ras$X= dd[, 1] ; Geo.Ras$Y= dd[, 2]
dim(Reg.Ras <- subset(Geo.Ras, !is.na(AOC1b) & !is.na(DEM) & !is.na(DESCR)
  & !is.na(RUD) & !is.na(AOC36lab) & !is.na(REGION)))
```

---

[1] 59113      72

The resulting object is a `SpatialPolygonDataFrame` that contains 59 113 observations of vineyard plots with 72 variables without omitted values for each.

## 1.2 Geology and pedology

Another preamble treatment is about the geological and pedological variables to be included in regressions. We control sub-soil and soil characteristics with fixed effects, which is the more general way knowing the raw spatial resolution of these data and the numerous correlated variables that are available. A too small number of observation can nevertheless be a problem for the convergence of the estimation, hence we choose to include a fixed effects only for geological and pedological polygons with more than 1 000 vineyard plots. The details of this choice is presented in the data paper mentioned above.

---

```
Reg.Ras$NOTATION <- factor(Reg.Ras$NOTATION)
tmp <- table(Reg.Ras$NOTATION)< 1000
Reg.Ras$GEOL <- factor(
  ifelse(Reg.Ras$NOTATION %in% names(tmp[ tmp]), "0AREF",
        as.character(Reg.Ras$NOTATION)))
Reg.Ras$NOUC <- factor(Reg.Ras$NOUC)
tmp <- table(Reg.Ras$NOUC)< 1000
Reg.Ras$PEDO <- factor(
  ifelse(Reg.Ras$NOUC %in% names(tmp[tmp]), "0AREF",
        as.character(Reg.Ras$NOUC)))
apply(Reg.Ras@data[, c("GEOL", "PEDO")], 2, table)
```

---

\$GEOL

0AREF	C	E	Fu	Fx	Fy	GP	j3	j3a	j3b	j4a
5208	19014	1997	1060	2142	1460	8372	1288	2570	2539	1531
j5a	j5b	j6a	p-IV							
3526	3928	3087	1391							

\$PEDO

0AREF	13	14	26	28	29	30	32	34	35	36
3310	1553	17475	3718	8687	6241	4563	1802	1700	5255	1116
5	69	8								
1051	1484	1158								

The characteristics of sub-soils and soils are controlled with respectively 14 and 13 fixed effects. In each case, the reference modality coded 0AREF contains all the vineyards plots from geological and pedological polygons without sufficient observations. Robustness checks have been made with other threshold values without that changes the results.

### 1.3 Crossing GIs dimensions

The data are now ready for the analysis. The GIs on the area of interest contains both an horizontal (*communes*) and a vertical (*ranking*) dimension. The balance of the distribution can be assessed with the following Figure, which corresponds to Figure 3 (p.36) in the working paper.

```
library(lattice) ; library(RColorBrewer)
fig.dat <- aggregate(model.matrix(~0+ factor(Reg.Ras$AOC))*
  Reg.Ras$AREA/ 1000, by= list(Reg.Ras$LIBCOM), sum)
names(fig.dat) <- c("LIBCOM", "BGOR", "BOUR", "VILL", "PCRU", "GCRU")
fig.dat$LIBCOM <- factor(fig.dat$LIBCOM, lev= rev(levels(fig.dat$LIBCOM)))
fig.crd <- t(apply(fig.dat[, -1], 1, function(t) cumsum(t)- t/2))
fig.lab <- round(t(apply(fig.dat[, -1], 1, function(t) t/ sum(t)))* 100)
my.pal <- brewer.pal(n= 9, name = "BuPu")[ 2: 8]
barchart(LIBCOM~ BGOR+ BOUR+ VILL+ PCRU+ GCRU, xlim= c(-100, 10200),
  xlab="Vineyards delineated as Geographical Indications (hectare)",
  data= fig.dat, horiz= T, stack= T, col= my.pal, border= "black",
  par.settings= list(superpose.polygon= list(col= my.pal)),
  auto.key= list(space= "top", points= F, rectangles= T, columns= 5,
    text=c("Coteaux b.", "Bourgogne",
      "Village", "Premier cru", "Grand cru"))),
panel=function(x, y, ...) {
  panel.grid(h= 0, v = -11, col= "grey60")
  panel.barchart(x, y, ...)
  ltext(fig.crd, y, lab= ifelse(fig.lab> 0, fig.lab, ""))})
```

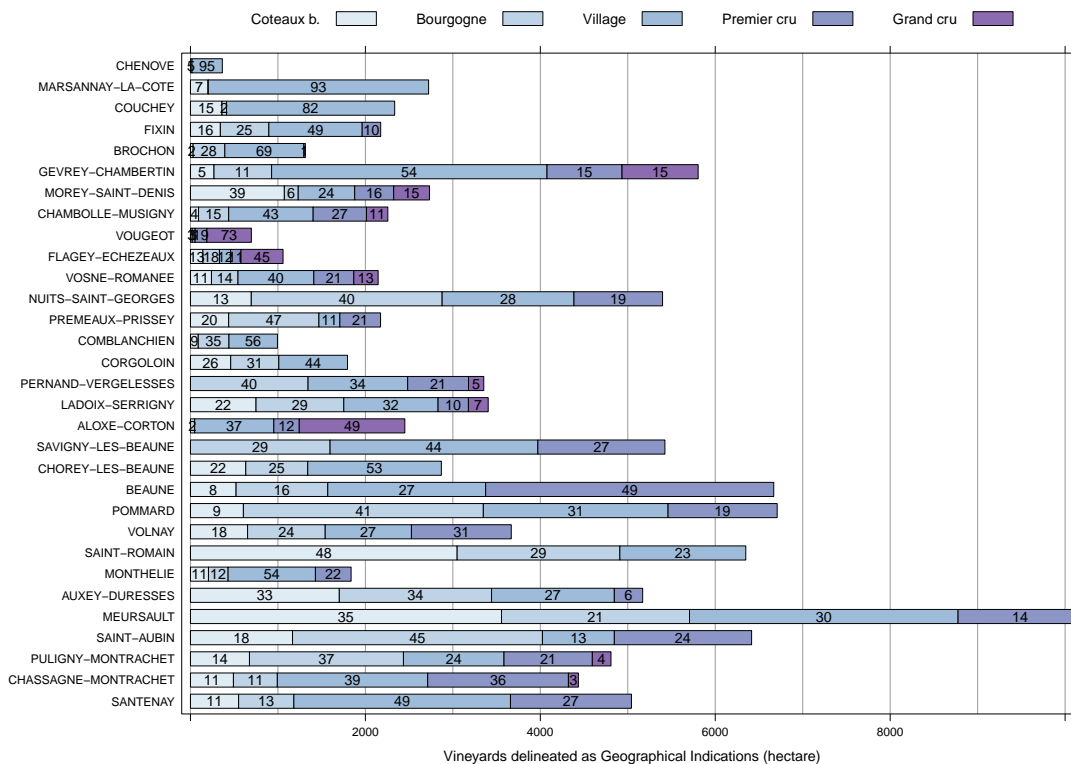


Figure 1: Cross distribution of GI levels among communes

## 2 Models of GI designation

### 2.1 Parametric ordered logit

We first estimate the benchmark parametric ordered logistic model `polm1` that corresponds to model ( 0 ) of Table 1 in the working paper. Model `polm1a` is the auxiliary regression used to test the presence of omitted *terroir* effect. Model `polm1b` is also auxiliary to compute the Fisher statistics associated to spatial smoothing terms in Table 1. We use for this the standard `polr` function from `MASS` package.

---

```
library(MASS)
polm1 <- polr(factor(AOC)~ 0+ LIBCOM+ EXPO+ GEOL+ PEDO
              + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
              + poly(X, 3)* poly(Y, 3), data= Reg.Ras, Hess= TRUE)
polm1a <- polr(factor(AOC)~ 0+ EXPO+ GEOL+ PEDO
               + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
               + poly(X, 3)* poly(Y, 3), data= Reg.Ras, Hess= TRUE)
polm1b <- polr(factor(AOC)~ 0+ LIBCOM+ EXPO+ GEOL+ PEDO
               + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
               , data= Reg.Ras, Hess= TRUE)
```

---

Warning messages:

- ```
1: In polr(factor(AOCc) ~ 0 + LIBCOM + EXPO + poly(DEM, 2) + poly(SLOPE, 2) :
  une coordonnée à l'origine est nécessaire et assumée
2: In polr(factor(AOCc) ~ 0 + LIBCOM + EXPO + poly(DEM, 2) + poly(SLOPE, 2) :
  le plan ne semble pas de rang plein, des coefs seront ignorés
```

The warning messages are due to the choice to drop of intercept to obtain a coefficient for each *commune* (through the variable `LIBCOM`) in order to compute the ordinal superiority measures. They can be neglected as this has no impact on the estimation.

## 2.2 Ordered generalized additive

The following code presents 2 loops that allow to estimate the OGAM models of GIs designations. Models (I) to (V) reported in Table XX are only a subset of all models estimated here. The `gamod` object contains the full models, the `gammod` object contains the auxiliary regression to test the omitted *terroir* effects. Because of the complexity of the models, each loop needs about 2 days to run (Dell Precision 7520, 64Go of RAM). I advice the reader to not run the loop entirely but pick some value of `listk` for the maximum degree of freedom and run the models individually. The objects `gamod.Rda` and `gammod.Rda` are available from the git repo mentioned in the first page.

---

```
library(mgcv)
listk <- c(50, 100, 200, 300, 400, 500, 600, 700, 800, 900)
gamod <- vector("list", length(listk))
system.time(
  for (i in 1: length(listk)){
    gamod[[ i]] <- gam(AOCc~ 0+ LIBCOM+ EXPO+ s(DEM)+ s(SLOPE)+ s(RAYAT)
                      + s(X, Y, k= listk[ i])
                      , data= Reg.Rank, family= ocat(R= 5))
  })
names(gamod) <- paste0("gam", listk)
save(gamod, file= "Inter/gamod.Rda")

gammod <- vector("list", length(listk))
system.time(
  for (i in 1: length(listk)){
    gammod[[ i]] <- gam(AOCc~ 0+ EXPO+ s(DEM)+ s(SLOPE)+ s(RAYAT)
                      + s(X, Y, k= listk[ i])
                      , data= Reg.Rank, family= ocat(R= 5))
  })
names(gammod) <- paste0("gam", listk)
save(gammod, file= "Inter/gammod.Rda")

library(mgcv)
listk <- c(50, 100, 200, 300, 400, 500, 600, 700)
gamodM <- vector("list", length(listk))
system.time(
  for (i in 1: length(listk)){
    gamodM[[ i]] <- gam(AOC~ 0+ LIBCOM+ EXPO+ s(DEM)+ s(SLOPE)+ s(RAYAT)
                      + s(X, Y, k= listk[ i])+ GEOL+ PEDO
                      , data= Reg.Ras, family= ocat(R= 5))
  })
names(gamodM) <- paste0("gam", listk)
save(gamodM, file= "Inter/gamodM.Rda")
## Timing stopped at: 2.645e+05 1109 2.656e+05

gammodM <- vector("list", length(listk))
system.time(
  for (i in 1: length(listk)){
    print(i)
    gammodM[[ i]] <- gam(AOC~ 0+ EXPO+ s(DEM)+ s(SLOPE)+ s(RAYAT)
                      + s(X, Y, k= listk[ i])+ GEOL+ PEDO
                      , data= Reg.Ras, family= ocat(R= 5))
  }
)
names(gammodM) <- paste0("gam", listk)
save(gammodM, file= "Inter/gammodM.Rda")
```

```
## utilisateur      système      écoulé
##      47749.1      235.7      47988.9

library(mgcv) ; load("Inter/gamodM.Rda")
## system.time(
##
gam900 <- gam(AOC~ 0+ LIBCOM+ EXPO+ GEOL+ PEDO
##
+ s(DEM)+ s(SLOPE)+ s(RAYAT)+ s(X, Y, k= 900)
##
, data= Reg.Ras, family= ocat(R= 5))
## )
## utilisateur
système
écoulé
##
32271.43
93.78
32366.00
## save(gam900, file= "Inter/gam900.Rda")
```

---

|             |         |         |
|-------------|---------|---------|
| utilisateur | système | écoulé  |
| 56177.4     | 384.9   | 56565   |
| utilisateur | système | écoulé  |
| 42413.2     | 262.8   | 42679.6 |

### 3 Diagnostics

#### 3.1 Significance

We first reports the Chi-square statistics for the joint significance of the model ( 0 ) of Table XX in the working paper.

---

```
library(car)
resla <- anova(por1, por1b)
(res1 <- Anova(por1))

quesla <- anova(qor1, qor1b)
(qes1 <- Anova(qor1))
```

---

Analysis of Deviance Table (Type II tests)

Response: factor(AOCc)

|                | LR    | Chisq | Df | Pr(>Chisq) |
|----------------|-------|-------|----|------------|
| LIBCOM         | 14609 | 31    |    | <2e-16 *** |
| EXPO           | 1209  | 7     |    | <2e-16 *** |
| poly(DEM, 2)   | 5308  | 2     |    | <2e-16 *** |
| poly(SLOPE, 2) | 400   | 2     |    | <2e-16 *** |

```

poly(RAYAT, 2)          1934  2      <2e-16 ***
poly(X, 3)              2484  3      <2e-16 ***
poly(Y, 3)              647   3      <2e-16 ***
poly(X, 3):poly(Y, 3)   9526  9      <2e-16 ***
---
codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Then, we compute the same statistics for the OGAMs, also reported in Table XX in the main paper.

---

```

load("Inter/gamod.Rda") ; load("Inter/gamodM.Rda")
resume <- function(mod){
  tmp <- anova(mod)
  res <- c(as.vector(rbind(tmp$s.table[, 3], tmp$s.table[, 1])),
           as.vector(rbind(tmp$pTerms.tab[, 2], tmp$pTerms.tab[, 1])))
  names(res) <- c(as.vector(rbind(rownames(tmp$s.table), rep("", 4))),
                 as.vector(rbind(rownames(tmp$pTerms.tab), rep("", 2))))
  round(res, 1)
}
sapply(gamod[ 1: 5* 2], resume)
sapply(gamodM[ c(1, 1: 4* 2)], resume)

```

---

|          | gam100  | gam300  | gam500  | gam700   | gam900   |
|----------|---------|---------|---------|----------|----------|
| s(DEM)   | 5020.2  | 2385.4  | 1677.7  | 1692.6   | 1766.8   |
|          | 9.0     | 8.9     | 8.8     | 8.8      | 8.8      |
| s(SLOPE) | 1281.1  | 458.2   | 266.1   | 225.3    | 243.6    |
|          | 8.5     | 8.5     | 8.5     | 8.4      | 8.4      |
| s(RAYAT) | 2491.6  | 1196.5  | 667.3   | 554.7    | 557.9    |
|          | 8.3     | 8.2     | 7.7     | 7.6      | 7.5      |
| s(X,Y)   | 41458.2 | 73705.5 | 94094.8 | 103941.0 | 107522.8 |
|          | 98.7    | 295.2   | 483.1   | 666.7    | 844.7    |
| LIBCOM   | 6793.2  | 6079.7  | 4594.7  | 3555.0   | 2894.5   |
|          | 31.0    | 31.0    | 31.0    | 31.0     | 31.0     |
| EXPO     | 110.3   | 123.2   | 222.3   | 153.5    | 160.8    |
|          | 7.0     | 7.0     | 7.0     | 7.0      | 7.0      |

### 3.2 Goodness of fit

Here are the goodness-of-fit measures for model (0) also reported in Table XX: McFadden  $R^2$ , Akaike information criteria, and percent of good predictions.

---

```

psR2 <- function(x) 1- (logLik(x)/ logLik(update(x, . ~ + 1)))
round(c(McFaddenR2= psR2(por1), AIC= AIC(por1)/ 1000,
        Pcgpp= sum(diag(table(predict(por1), Reg.Rank$AOCc)))/nrow(Reg.Rank)), 2)

round(c(McFaddenR2= psR2(qor1), AIC= AIC(qor1)/ 1000,
        Pcgpp= sum(diag(table(predict(qor1), Reg.Ras$AOC)))/nrow(Reg.Ras)), 2)

```

---

| McFaddenR2 | AIC | Pcgpp |
|------------|-----|-------|
|------------|-----|-------|



0.29      119.40      0.59

The same goodness of fit measures for OGAMs.

---

```
pcgp <- function(x){
  sum(diag(table(cut(x$line, c(-Inf, x$family$getTheta(TRUE), Inf)),
    x$model[, 1])))/ nrow(x$model)* 100
}
rbind(Pcgp= sapply(gamod[ 1: 5* 2], pcgp), AIC= sapply(gamod[ 1: 5* 2], AIC))
sapply(gamod, psR2)

rbind(Pcgp= sapply(gamodM[ 1: 4* 2], pcgp), AIC= sapply(gamodM[ 1: 4* 2], AIC))
sapply(gamodM, psR2)
```

---

|      | gam100   | gam300   | gam500   | gam700   | gam900   |
|------|----------|----------|----------|----------|----------|
| Pcgp | 73.89    | 79.94    | 84.23    | 86.94    | 89.15    |
| AIC  | 82412.10 | 64710.89 | 54941.54 | 48291.33 | 43535.14 |

### 3.3 Omitted variable

Bootstrapped statistics for the Fisher about omitted *terroir* variables, with 100 replications for parametric ordered logistic. The absence of correlated effects is strongly rejected. We use the `sure` package for surrogate residual.

---

```
library(lmtest) ; library(sandwich) ; library(sure)
wall <- rep(NA, times= nsim <- 100)
for (i in 1: nsim){
  tmp <- surrogate(porla)- porla$lp
  wall[ i] <- waldtest(lm(tmp~ Reg.Rank$LIBCOM), . ~ 1, vcov= vcovHC)$F[ 2]
}
quantile(wall, c(.05, .5, .95))

xall <- rep(NA, times= nsim)
for (i in 1: nsim){
  tmp <- surrogate(qorla)- qorla$lp
  xall[ i] <- waldtest(lm(tmp~ Reg.Ras$LIBCOM), . ~ 1, vcov= vcovHC)$F[ 2]
}
quantile(xall, c(.05, .5, .95))
```

---

|  | 5%    | 50%   | 95%   |
|--|-------|-------|-------|
|  | 268.0 | 274.2 | 279.6 |

A passer en `Reg.Rank`, introduire la fonction sur les surrogate residuals des modèles gams en in the Appendix. Not exactly the same because of bootstrap.

---

```
load("Inter/gammod.Rda") ; load("Inter/gammodM.Rda") ; source("myFcts.R")
omitVar <- function(mod, var, nsim= 100){
  usq <- rep(NA, nsim)
  for(i in 1: nsim) {
```

```

RES <- sureOGAM(mod)
tmp <- lm(I(RES- mod$linear.pred)~ factor(var))
usq[ i] <- waldtest(tmp, . ~ 1, vcov= vcovHC)$F[ 2]
}
usq
}
wal2 <- sapply(gammod, function(x) omitVar(x, RRank$LIBCOM, nsim= 100))
apply(wal2[, 1: 5* 2], 2, function(x) quantile(x, c(.05, .5, .95)))

xal2 <- sapply(gammodM, function(x) omitVar(x, Reg.Ras$LIBCOM, 100))
apply(xal2[, 1: 4* 2], 2, function(x) quantile(x, c(.05, .5, .95)))

```

---

|     | gam100 | gam300 | gam500 | gam700 | gam900 |
|-----|--------|--------|--------|--------|--------|
| 5%  | 17.38  | 6.060  | 3.377  | 2.004  | 1.704  |
| 50% | 18.94  | 6.806  | 4.130  | 2.525  | 2.181  |
| 95% | 20.15  | 7.746  | 4.864  | 3.060  | 2.760  |

The following plot resumes the specification diagnostics and shows the relevance of OGAMs to control for omitted spatial effects. It corresponds to Figure XX in the working paper, the bootstrapped nature of the statistics individual values change.

---

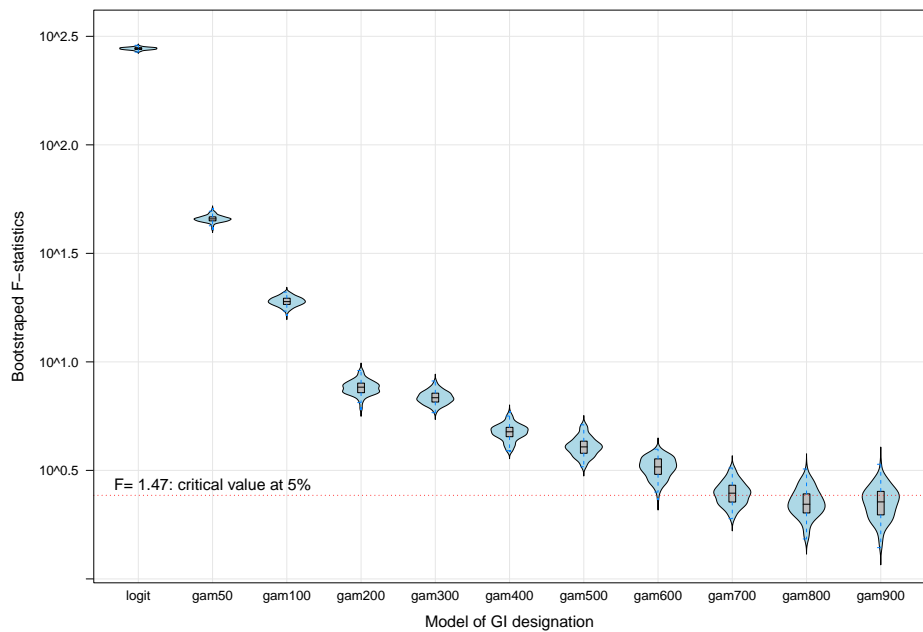
```

library(lattice)
pltdat <- stack(data.frame(logit= wal1, wal2))
pltdat <- stack(data.frame(logit= xal1, xal2))

bwplot(values~ ind, data= pltdat, type=c("l","g"), horizontal= FALSE,
       xlab='Model of GI designation', ylab='Bootstraped F-statistics',
       par.settings = list(box.rectangle=list(col='black'),
                           plot.symbol = list(pch='.', cex = 0.1)),
       scales=list(y= list(log= TRUE)),
       panel = function(..., box.ratio) {
         panel.grid(h= -1, v = -11)
         panel.violin(..., col = "lightblue",
                      varwidth = FALSE, box.ratio = box.ratio)
         panel.bwplot(..., col='black',
                      cex=0.8, pch='|', fill='gray', box.ratio = .1)
         panel.abline(h= log(1.47), col= "red", lty= 3)
         panel.text(2, log(1.55), "F= 1.47: critical value at 5%")})

```

---



### 3.4 Specification

Surrogate residuals can also be used to test specification, results not reported.

---

```
library(sure) ; library(ggplot2) ; library(gridExtra)
var <- c("DEM", "SLOPE", "RAYAT", "EXPO", "LIBCOM", "X", "Y")
plots <- lapply(var, function(.x)
  autoplot(por1, what= "covariate", x= Reg.Rank@data[, .x], xlab= .x))
do.call(grid.arrange, c(list(autoplot(por1, what= "qq")), plots))

plots <- lapply(var, function(.x)
  autoplot(qor1, what= "covariate", x= Reg.Ras@data[, .x], xlab= .x))
do.call(grid.arrange, c(list(autoplot(qor1, what= "qq")), plots))

restmp <- sureOGAM(gamod$gam900)- gamod$gam900$line
plot(qlogis(1: nrow(RRank)/ nrow(RRank), scale= 1), sort(restmp))
abline(0, 1)
pltSURE <- function(resid, xvar, lab){
  plot(xvar, resid, xlab= lab, main= paste("Surrogate Analysis", lab))
  abline(h= 0, col= "red", lty= 3, lwd= 2)
  lines(smooth.spline(resid ~ xvar), lwd= 3, col= "blue")
}
par(mfrow= c(3, 3)) ; for (i in var) pltSURE(restmp, RRank@data[, i], i)

restmp <- sureOGAM(gamodM$gam700)- gamodM$gam700$line
plot(qlogis(1: nrow(Reg.Ras)/ nrow(Reg.Ras), scale= 1), sort(restmp))
abline(0, 1)
par(mfrow= c(3, 3)) ; for (i in var) pltSURE(restmp, Reg.Ras@data[, i], i)
```

---

## 4 Marginal effects

### 4.1 Parametric ordered logit

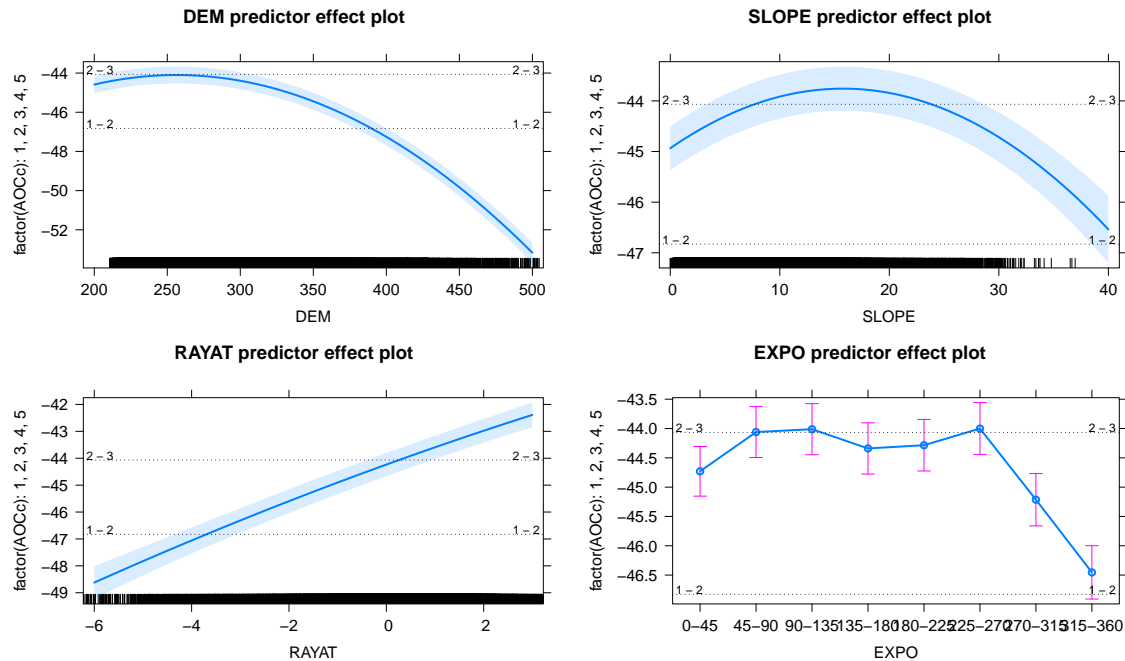
Marginal effects from parametric models, corresponds to the dotted lines in Figure XX of the working paper.

---

```
library(effects)
plot(predictorEffects(por1, ~ DEM+ SLOPE+ RAYAT+ EXPO, latent= TRUE,
  xlevels=list(DEM= 200: 500,
    SLOPE= 0: 400/ 10, RAYAT= -60: 30/ 10)))

plot(predictorEffects(qor1, ~ DEM+ SLOPE+ RAYAT+ EXPO, latent= TRUE,
  xlevels=list(DEM= 200: 500,
    SLOPE= 0: 400/ 10, RAYAT= -60: 30/ 10)))
```

---



### 4.2 Ordered generalized additive

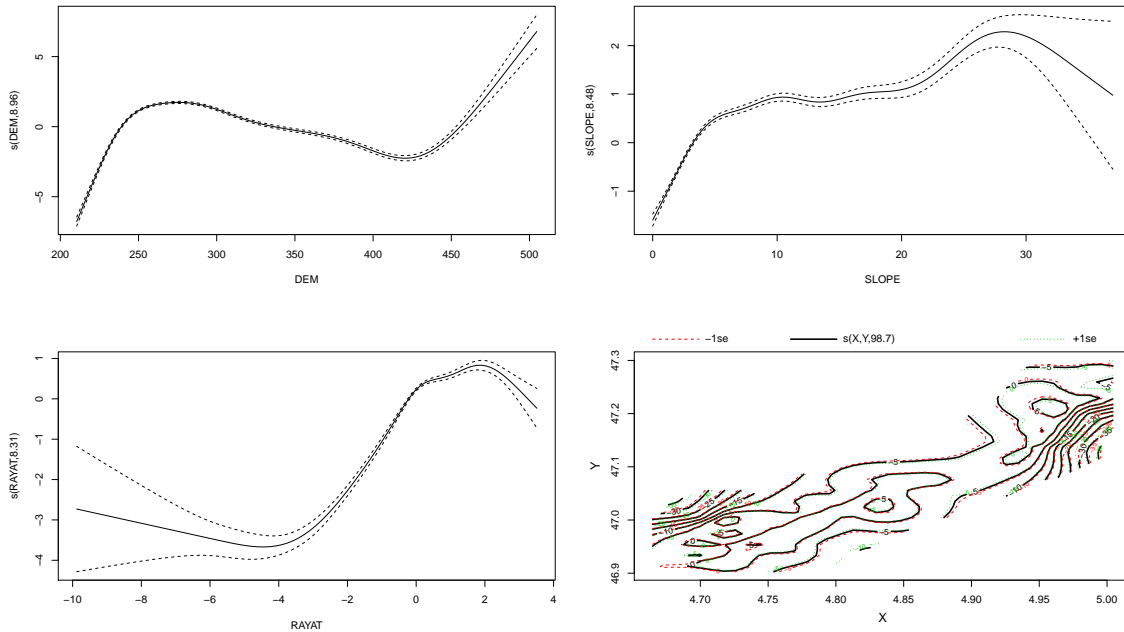
On voit bien que le lissage est le même que le papier. Can be changed by indexing the list gamod, below is the reported effect for a maximum effective degrees of freedom of 100. For all models of gamod, we obtain the grey curves of Figure XX of the working paper.

---

```
plot(gamod[[ 1]], pages= 1, scale= 0)

plot(gamodM[[ 1]], pages= 1, scale= 0)
```

---



### 4.3 Ordinal superiority figure

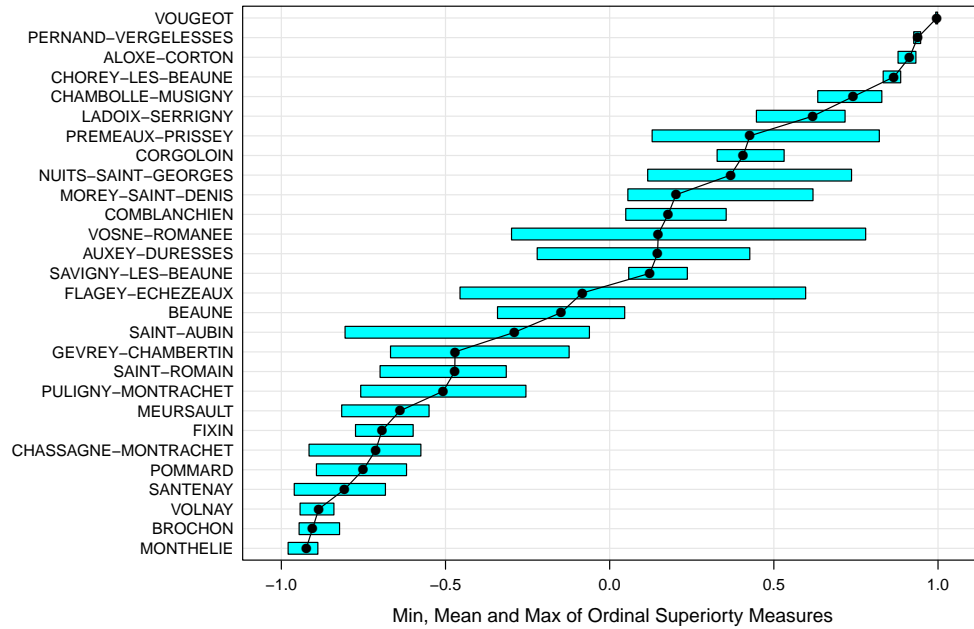
From the equation XX of the working paper, we compute ordinal superiority measures for each OGAMs relatively to the average. It produces the Figure XX of the main text. Drop Chenôve, Marsannay, Couchey, for which the method is not appropriate.

---

```
library(latticeExtra)
plogi <- function(x) exp(x/ sqrt(2))/ (1+ exp(x/ sqrt(2)))
xx <- data.frame(sapply(gamod, function(x)
  2* plogi(I(x$coeff[ 4: 31]- mean(x$coeff[ 4: 31]))- 1))
ww <- data.frame(xx,
  LIBCOM= substr(names(gamod[[1]]$coef[ 4: 31]), 7, 30),
  MIN= apply(xx[ 7: 10], 1, min),
  MAX= apply(xx[ 7: 10], 1, max),
  MEAN= apply(xx[ 7: 10], 1, mean))
segplot(reorder(factor(LIBCOM), MEAN)~ MIN+ MAX, length= 5, draw.bands= T,
  data= ww[order(ww$MEAN), ], center= MEAN, type= "o",
  unit = "mm", axis = axis.grid, col.symbol= "black", cex= 1,
  xlab= "Min, Mean and Max of Ordinal Superiority Measures")

yy <- data.frame(sapply(gamodM, function(x)
  2* plogi(I(x$coeff[ 4: 31]- mean(x$coeff[ 4: 31]))- 1))
zz <- data.frame(yy,
  LIBCOM= substr(names(gamodM[[1]]$coef[ 4: 31]), 7, 30),
  MIN= apply(yy[ 5: 8], 1, min),
  MAX= apply(yy[ 5: 8], 1, max),
  MEAN= apply(yy[ 5: 8], 1, mean))
segplot(reorder(factor(LIBCOM), MEAN)~ MIN+ MAX, length= 5, draw.bands= T,
  data= zz[order(zz$MEAN), ], center= MEAN, type= "o",
  unit = "mm", axis = axis.grid, col.symbol= "black", cex= 1,
```

```
xlab= "Min, Mean and Max of Ordinal Superiority Measures")
```



#### 4.4 Correlation between *Communes*

Below an unreported Figure to illustrate the claim that "*commune* with higher GIs do not have a preferential treatment" (p.XX) of the working paper. It correlates the average vertical GI score with the ordinal superiority measures from OGAM with XX maximum effective degrees of freedom.

```
library(plyr) ; library(ggrepel)
yy <- ddply(RRank@data, .(LIBCOM),
            function(x) weighted.mean(x$AOCc, x$Area))
zz <- merge(ww, yy, by= "LIBCOM")
m <- lm(V1~ MEAN, data= zz)
a <- signif(coef(m)[1], digits = 2)
b <- signif(coef(m)[2], digits = 2)
c <- signif(summary(m)$r.sq, digits = 2)
textlab <- paste("y = ", a, " + ", b, " x ", " ", R2 = " ", c, sep= "")
ggplot(zz, aes(MEAN, V1, label= LIBCOM)) +
  geom_smooth(method= lm, aes(MEAN, V1))+
  geom_text_repel(point.padding = NA) +
  annotate("text", x= -.75, y= 4, label= textlab, size= 4, parse= F)+
  xlab("Reputation (ordinal superiority)") +
  ylab("Average GI grade (between 0 and 5)")

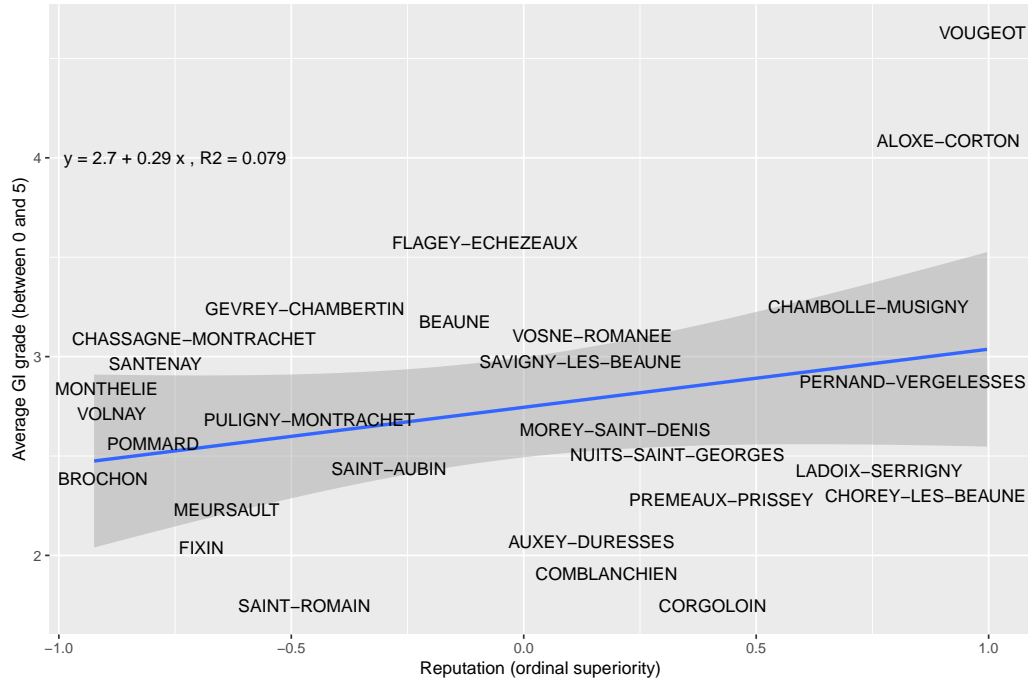
aa <- ddply(Reg.Ras@data, .(LIBCOM),
            function(x) weighted.mean(x$AOC, x$AREA))
bb <- merge(zz, aa, by= "LIBCOM")

m <- lm(V1~ MEAN, data= bb)
a <- signif(coef(m)[1], digits = 2)
```

```

b <- signif(coef(m)[2], digits = 2)
c <- signif(summary(m)$r.sq, digits = 2)
textlab <- paste("y = ", a, " + ", b, " x ", " , R2 = ", c, sep= "")
ggplot(bb, aes(MEAN, V1, label= LIBCOM)) +
  geom_smooth(method= lm, aes(MEAN, V1))+
  geom_text_repel(point.padding = NA) +
  annotate("text", x= -.75, y= 4, label= textlab, size= 4, parse= F)+
  xlab("Reputation (ordinal superiority)") +
  ylab("Average GI grade (between 0 and 5)")

```



## 5 Informational content

### 5.1 Decomposition table

see appendix for the detailed presentation of the R code to implement the decomposition decompositions. The following code for all OGAMs some computation times, allow the reader to compute the models individually.

```

load("Inter/gamod.Rda") ; source("myFcts.R")
ddtt <- data.frame(AOCc= RRank$AOCc, LIBCOM= RRank$LIBCOM,
  sapply(gamod[ 1: 5* 2], function(x)
    rowSums(predict(x, type= 'terms')[, -1])))
dcmp <- sapply(names(ddtt[, 3: 7]), function(x)
  c("Total Signal"= var(ddtt[, x]), "Total Noise"= pi^2/ 3,
    jointSignal(ddtt, x), jointNoise(ddtt, x),
    vertiSignal(ddtt, x), vertiResid(ddtt, x), vertiNoise(ddtt, x),
    horizSignal(ddtt, x), horizResid(ddtt, x), horizNoise(ddtt, x)))
round(t(apply(dcmp, 1, function(x) x/ (pi^2/ 3+ dcmp[1, ])* 100)), 1)

```

```
ddtt <- data.frame(AOC= Reg.Ras$AOC, LIBCOM= Reg.Ras$LIBCOM,
                  sapply(gamodM[ 1: 4* 2], function(x)
                        rowSums(predict(x, type= 'terms')[, -1])))

dcmp <- sapply(names(ddtt[, 3: 6]), function(x)
c("Total Signal"= var(ddtt[, x]), "Total Noise"= pi^2/ 3,
  jointSignal(ddtt, x, vt= "AOC"),
  jointNoise(ddtt, x, vt= "AOC"),
  vertiSignal(ddtt, x, vt= "AOC"),
  vertiResid(ddtt, x, vt= "AOC"),
  vertiNoise(ddtt, x, vt= "AOC"),
  horizSignal(ddtt, x, vt= "AOC"),
  horizResid(ddtt, x, vt= "AOC"),
  horizNoise(ddtt, x, vt= "AOC")))

round(t(apply(dcmp, 1, function(x) x/ (pi^2/ 3+ dcmp[1, ]* 100)), 1)
```

---

|               | gam100 | gam300 | gam500 | gam700 | gam900 |
|---------------|--------|--------|--------|--------|--------|
| Signal        | 84.8   | 94.7   | 95.9   | 96.8   | 97.6   |
| Noise         | 15.2   | 5.3    | 4.1    | 3.2    | 2.4    |
| Joint Signal  | 68.9   | 78.5   | 76.0   | 77.9   | 78.7   |
| Joint Noise   | 16.0   | 16.2   | 20.0   | 18.9   | 18.9   |
| Rank Signal   | 55.1   | 40.3   | 56.8   | 61.3   | 57.6   |
| Rank Residual | 13.8   | 38.2   | 19.2   | 16.5   | 21.2   |
| Rank Noise    | 29.7   | 54.4   | 39.1   | 35.4   | 40.0   |
| Com Signal    | 21.3   | 37.2   | 24.6   | 27.5   | 29.1   |
| Com Residual  | 47.6   | 41.3   | 51.4   | 50.4   | 49.7   |
| Com Noise     | 63.5   | 57.5   | 71.3   | 69.3   | 68.5   |

## 6 Models for GIs of 1936

### 6.1 Descriptive statistics

I present here the detail of the analysis with past GIs, to show that *communes* influences have decreased and informational content has increased since then. It typically makes the same analysis than for actual GIs, first some descriptive statistics.

---

```
Reg.Old <- subset(Reg.Rank, !is.na(Reg.Rank$AOC36lv1) &
                  !Reg.Rank$LIBCOM %in%
                  c("CHENOVE", "MARSANNAY-LA-COTE", "COUCHEY",
                    "COMBLANCHIEN", "CORGOLOIN", "SAINT-ROMAIN"))
Reg.Old$LIBCOM <- factor(Reg.Old$LIBCOM)
Reg.Old$AOCc <- as.numeric(ifelse(Reg.Old$AOC36lv1== "0", 1,
                                  ifelse(Reg.Old$AOC36lv1== "3", 2, 3)))
table(Reg.Old$AOC36lv1, Reg.Old$AOCc)
#table(Reg.Old$LIBCOM, Reg.Old$AOCc)

Reg.Old <- subset(Reg.Ras, !is.na(Reg.Ras$AOC36lv1) &
                  !Reg.Ras$LIBCOM %in%
                  c("CHENOVE", "MARSANNAY-LA-COTE", "COUCHEY",
                    "COMBLANCHIEN", "CORGOLOIN", "SAINT-ROMAIN"))
```



```
Reg.Old$LIBCOM <- factor(Reg.Old$LIBCOM)
Reg.Old$AOC <- as.numeric(ifelse(Reg.Old$AOC361v1== "0", 1,
                                ifelse(Reg.Old$AOC361v1== "3", 2, 3)))
table(Reg.Old$AOC361v1, Reg.Old$AOC)
# table(Reg.Old$LIBCOM, Reg.Old$AOC)
```

---

|   | 1    | 2     | 3     | 4    | 5    |
|---|------|-------|-------|------|------|
| 0 | 7204 | 12605 | 4120  | 567  | 39   |
| 3 | 15   | 662   | 15378 | 8017 | 261  |
| 5 | 0    | 1     | 13    | 3    | 1604 |

## 6.2 Estimation

The estimation of both the parametric and OGAMs, long computation times for the latter, prefer to fit models individually.

---

```
library(MASS)
por2 <- polr(factor(AOC)~ 0+ LIBCOM+ EXPO
             + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
             + poly(X, 3)* poly(Y, 3), data= Reg.Old, Hess= T)
por2a <- polr(factor(AOC)~ 0+ EXPO
             + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
             + poly(X, 3)* poly(Y, 3), data= Reg.Old, Hess= T)
por2b <- polr(factor(AOC)~ 0+ LIBCOM+ EXPO
             + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
             , data= Reg.Old, Hess= T)

qor2 <- polr(factor(AOC)~ 0+ LIBCOM+ EXPO+ GEOL+ PEDO
             + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
             + poly(X, 3)* poly(Y, 3), data= Reg.Old, Hess= T)
qor2a <- polr(factor(AOC)~ 0+ EXPO+ GEOL+ PEDO
             + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
             + poly(X, 3)* poly(Y, 3), data= Reg.Old, Hess= T)
qor2b <- polr(factor(AOC)~ 0+ LIBCOM+ EXPO+ GEOL+ PEDO
             + poly(DEM, 2)+ poly(SLOPE, 2)+ poly(RAYAT, 2)
             , data= Reg.Old, Hess= T)

library(mgcv)
listk <- c(50, 75, 100, 150, 200, 250, 300)
gamoldM <- vector("list", length(listk))

system.time(
  for (i in 1: length(listk)){
    gamoldM[[ i]] <- gam(AOC~ 0+ LIBCOM+ EXPO
                      + s(DEM)+ s(SLOPE)+ s(RAYAT)
                      + s(X, Y, k= listk[ i])+ GEOL+ PEDO
                      , data= Reg.Old, family= ocat(R= 3))
  }
)
names(gamoldM) <- paste0("gam", listk)
save(gamoldM, file= "Inter/gamoldM.Rda")
## utilisateur      système      écoulé
##      24064.0      178.8      24243.2
```

```

gammold <- vector("list", length(listk))
system.time(
for (i in 1: length(listk)){
  gammold[[ i]] <- gam(AOCo~ 0+ EXPO+ s(DEM)+ s(SLOPE)+ s(RAYAT)
    + s(X, Y, k= listk[ i])
    , data= Reg.Old, family= ocat(R= 3))
})
names(gammold) <- paste0("gam", listk)
save(gammold, file= "Inter/gammold.Rda")

```

---

|             |         |         |
|-------------|---------|---------|
| utilisateur | système | écoulé  |
| 12259.5     | 144.1   | 12405.5 |
| utilisateur | système | écoulé  |
| 9582.37     | 78.69   | 9661.62 |

### 6.3 Significance

Significance of all models of GIs designation, corresponds to Table XX in Appendix of the working paper.

---

```

load("Inter/gamold.Rda") ; load("Inter/gamoldM.Rda")
res2a <- anova(por2, por2b)
qes2a <- anova(qor2, qor2b)

res2 <- Anova(por2)
sapply(gammold[ 3: 7], resume)

qes2 <- Anova(qor2)
sapply(gamoldM[ 3: 7], resume)

```

---

|          |         |         |         |         |         |
|----------|---------|---------|---------|---------|---------|
|          | gam100  | gam150  | gam200  | gam250  | gam300  |
| s(DEM)   | 499.8   | 647.4   | 702.3   | 541.9   | 344.5   |
|          | 8.5     | 8.2     | 8.8     | 8.4     | 7.7     |
| s(SLOPE) | 387.3   | 314.0   | 254.4   | 244.3   | 153.0   |
|          | 8.7     | 8.7     | 8.6     | 8.6     | 8.3     |
| s(RAYAT) | 242.0   | 160.1   | 127.1   | 122.9   | 105.2   |
|          | 8.5     | 8.3     | 8.1     | 5.0     | 5.9     |
| s(X,Y)   | 17520.5 | 20194.2 | 22301.7 | 23507.2 | 23801.4 |
|          | 98.3    | 146.3   | 194.4   | 239.8   | 286.6   |
| LIBCOM   | 2782.5  | 1843.0  | 1642.4  | 1283.0  | 1049.4  |
|          | 25.0    | 25.0    | 25.0    | 25.0    | 25.0    |
| EXPO     | 119.8   | 91.8    | 91.9    | 96.1    | 90.2    |
|          | 7.0     | 7.0     | 7.0     | 7.0     | 7.0     |

### 6.4 Goodness of fit

Goodness of fit measures from the same Table XX in Appendix.

---

```

round(c(McFaddenR2= psR2(por2), AIC= AIC(por2)/ 1000,
        Pcgp= sum(diag(table(predict(por2), Reg.Old$A0Co)))/ nrow(Reg.Old)), 2)
rbind(Pcgp= sapply(gamold, pcgp), AIC= sapply(gamold, AIC))
# sapply(gamold, psR2)

round(c(McFaddenR2= psR2(qor2), AIC= AIC(qor2)/ 1000,
        Pcgp= sum(diag(table(predict(qor2), Reg.Old$A0Co)))/ nrow(Reg.Old)), 2)
rbind(Pcgp= sapply(gamoldM, pcgp), AIC= sapply(gamoldM, AIC))
sapply(gamoldM, psR2)

```

---

| McFaddenR2 | AIC      | Pcgp    |          |          |          |         |          |
|------------|----------|---------|----------|----------|----------|---------|----------|
| 0.38       | 51.29    | 0.79    |          |          |          |         |          |
|            | gam50    | gam75   | gam100   | gam150   | gam200   | gam250  | gam300   |
| Pcgp       | 84.34    | 85.9    | 87.08    | 89.26    | 90.28    | 91.4    | 92.54    |
| AIC        | 40789.58 | 36833.3 | 33810.36 | 30271.01 | 27574.12 | 24526.6 | 22482.20 |

## 6.5 Omitted variable

Bootstrapped statistics for omitted variables, not reported in the working paper, mentioned at p.XX, .

---

```

library(lmtest) ; library(sandwich) ; library(sure)
wal3 <- rep(NA, nsim= 100)
for (i in 1: nsim){
  tmp <- surrogate(qor2a)- qor2a$lp
  wal3[ i] <- waldtest(lm(tmp~ Reg.Old$LIBCOM), . ~ 1, vcov= vcovHC)$F[ 2]
}
quantile(wal3, c(.05, .5, .95))
load("Inter/gammold.Rda") ; load("Inter/gammoldM.Rda") ; source("myFcts.R")
wal4 <- sapply(gammold, function(x) omitVar(x, SRank$LIBCOM, nsim= 100))
wold <- data.frame(logit= wal3, wal4)
apply(wold, 2, function(x) quantile(x, c(.05, .5, .95)))

```

---

|     | logit | gam50 | gam75  | gam100 | gam150 | gam200 | gam250 | gam300 |
|-----|-------|-------|--------|--------|--------|--------|--------|--------|
| 5%  | 168.1 | 7.408 | 7.340  | 4.714  | 3.498  | 2.057  | 1.178  | 1.091  |
| 50% | 173.6 | 8.553 | 8.843  | 5.894  | 4.310  | 2.709  | 1.832  | 1.488  |
| 95% | 179.8 | 9.958 | 10.501 | 6.858  | 5.396  | 3.851  | 2.495  | 2.057  |

The same plot as for current GIs, same evidences about the relevance of spatial smoothing terms, the non significance is reach for smaller degrees of freedom (p.XX)

---

```

library(lattice)
poldat <- stack(wold)
bwplot(values~ ind, data= poldat, type=c("l","g"), horizontal= FALSE,
       xlab='Model of GI designation', ylab='Bootstraped F-statistics',
       par.settings = list(box.rectangle=list(col='black'),
                           plot.symbol = list(pch='.', cex = 0.1)),
       scales=list(y= list(log= TRUE)),
       panel = function(..., box.ratio) {
         panel.grid(h= -1, v = -11)
       })

```

---

```

panel.violin(..., col = "lightblue",
              varwidth = FALSE, box.ratio = box.ratio)
panel.bwplot(..., col='black',
              cex=0.8, pch='|', fill='gray', box.ratio = .1)
panel.abline(h= log(1.47), col= "red", lty= 3)
panel.text(2, log(1.55), "F= 1.47: critical value at 5%"))

```

---

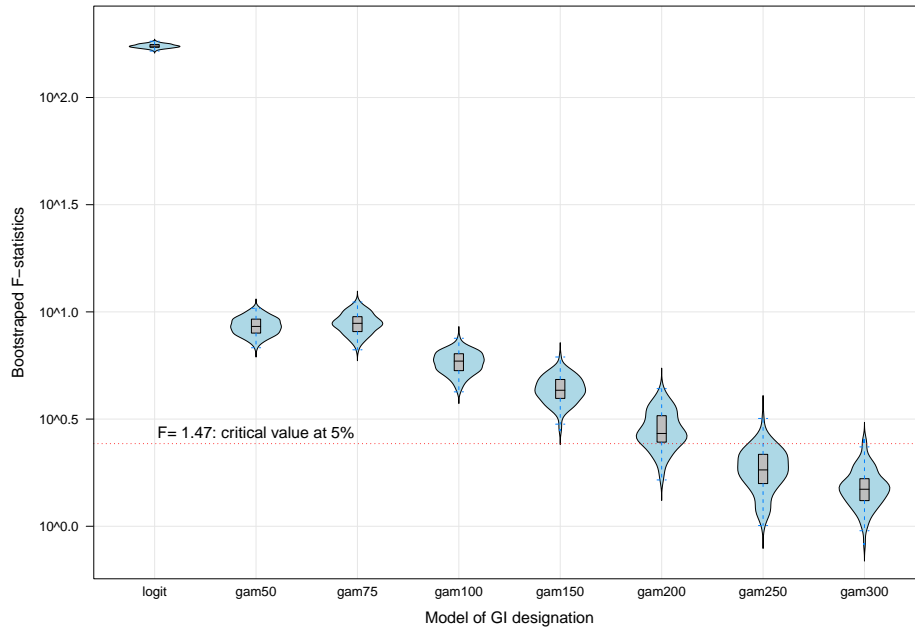


Figure 2: Effects of model XX

## 6.6 Specification

results not reported, parler de ce qu'il se passe moins bien mais qui n'est pas grave. Dans le gam 300 il y a un point qui fait n'imp, probablement un trou dans la carte de Florian.

---

```

library(sure) ; library(ggplot2) ; library(gridExtra)
var <- c("DEM", "SLOPE", "RAYAT", "EXPO", "LIBCOM", "X", "Y")
plots <- lapply(var, function(.x)
  autoplot(por2, what= "covariate", x= Reg.Old@data[, .x], xlab= .x))
do.call(grid.arrange, c(list(autoplot(por2, what= "qq")), plots))

restmp <- sureOGAM(gamold$gam300)- gamold$gam300$line
plot(qlogis(1: nrow(SRank)/ nrow(SRank), scale= 1), sort(restmp))
abline(0, 1)
var <- c("DEM", "SLOPE", "RAYAT", "EXPO", "LIBCOM", "X", "Y")
par(mfrow= c(3, 3)) ; for (i in var) pltSURE(restmp, SRank@data[, i], i)

```

---

## 6.7 Marginal effects

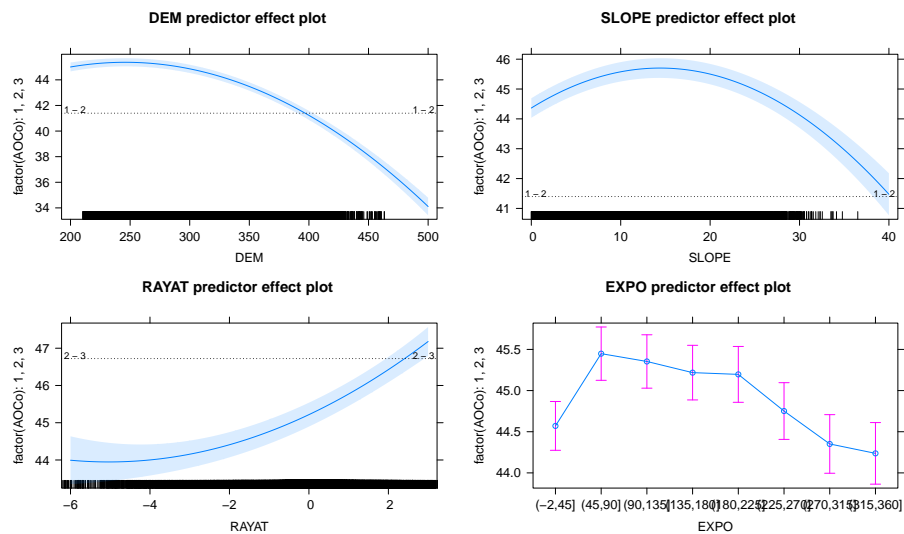
Marginal effect can be assessed, corresponds to Figure XX in the appendix in the working paper.

---

```
library(effects)
plot(predictorEffects(por2, ~ DEM+ SLOPE+ RAYAT+ EXPO, latent= TRUE,
                     xlevels=list(DEM= 200: 500,
                                   SLOPE= 0: 400/ 10, RAYAT= -60: 30/ 10)))
plot(gamold$gam300, pages= 1, scale= 0)

plot(predictorEffects(qor2, ~ DEM+ SLOPE+ RAYAT+ EXPO, latent= TRUE,
                     xlevels=list(DEM= 200: 500,
                                   SLOPE= 0: 400/ 10, RAYAT= -60: 30/ 10)))
plot(gamoldM$gam300, pages= 1, scale= 0)
```

---



## 6.8 Ordinal superiority

Ordinal superiority of *commune* from the GIs of 1936, same equation XX of the working paper and Figure XX in the appendix.

---

```
xxx <- data.frame(sapply(gamold, function(x)
  2* plogi(I(x$coeff[ 1: 25]- mean(x$coeff[ 1: 25]))- 1))
www <- data.frame(xxx,
  LIBCOM= substr(names(gamold[[ 1]]$coef[ 1: 25]), 7, 30),
  MIN= apply(xxx[ 6: 7], 1, min),
  MAX= apply(xxx[ 6: 7], 1, max),
  MEAN= apply(xxx[ 6: 7], 1, mean))
segplot(reorder(factor(LIBCOM), MEAN)~ MIN+ MAX, length= 5, draw.bands= T,
  data= www[order(www$MEAN), ], center= MEAN, type= "o",
  unit = "mm", axis = axis.grid, col.symbol= "black", cex= 1,
  xlab= "Min, Mean and Max of Ordinal Superiority Measures")

xxx
summary(gamoldM[[7]])
```

---

```

xxx <- data.frame(sapply(gamoldM, function(x)
  2* plogi(1(x$coeff[ 1: 25]- mean(x$coeff[ 1: 25]))) - 1))
www <- data.frame(xxx,
  LIBCOM= substr(names(gamoldM[[ 1]]$coef[ 1: 25]), 7, 30),
  MIN= apply(xxx[ 6: 7], 1, min),
  MAX= apply(xxx[ 6: 7], 1, max),
  MEAN= apply(xxx[ 6: 7], 1, mean))
segplot(reorder(factor(LIBCOM), MEAN)~ MIN+ MAX, length= 5, draw.bands= T,
  data= www[order(www$MEAN), ], center= MEAN, type= "o",
  unit = "mm", axis = axis.grid, col.symbol= "black", cex= 1,
  xlab= "Min, Mean and Max of Ordinal Superiority Measures")

```

---

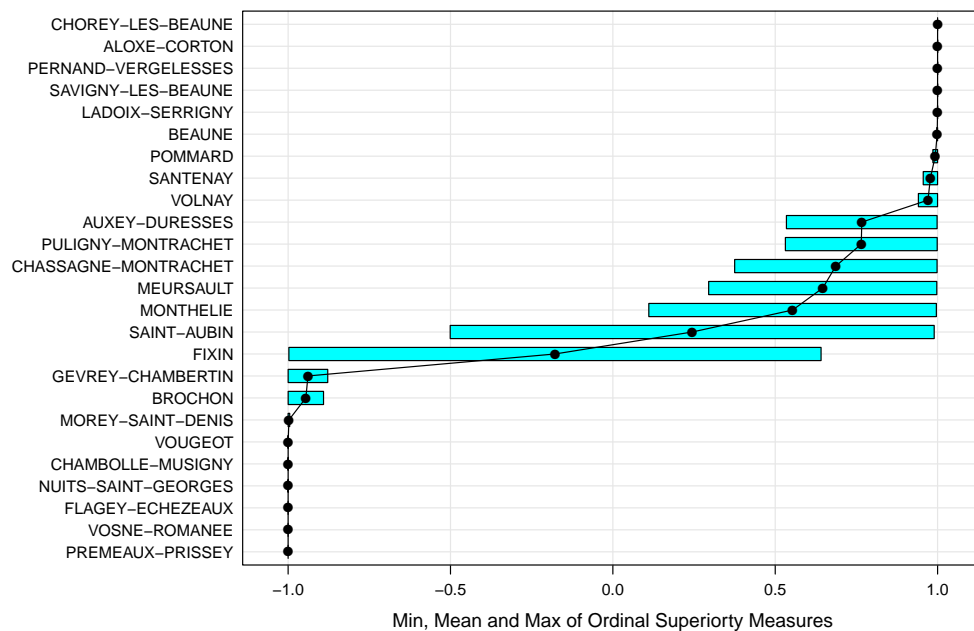


Figure 3: Effects of model XX

## 6.9 Correlation between models

An additional unreported Figure to show the claim that "the importance of *communes* has decreased since the 1936 scheme" (p.XX)

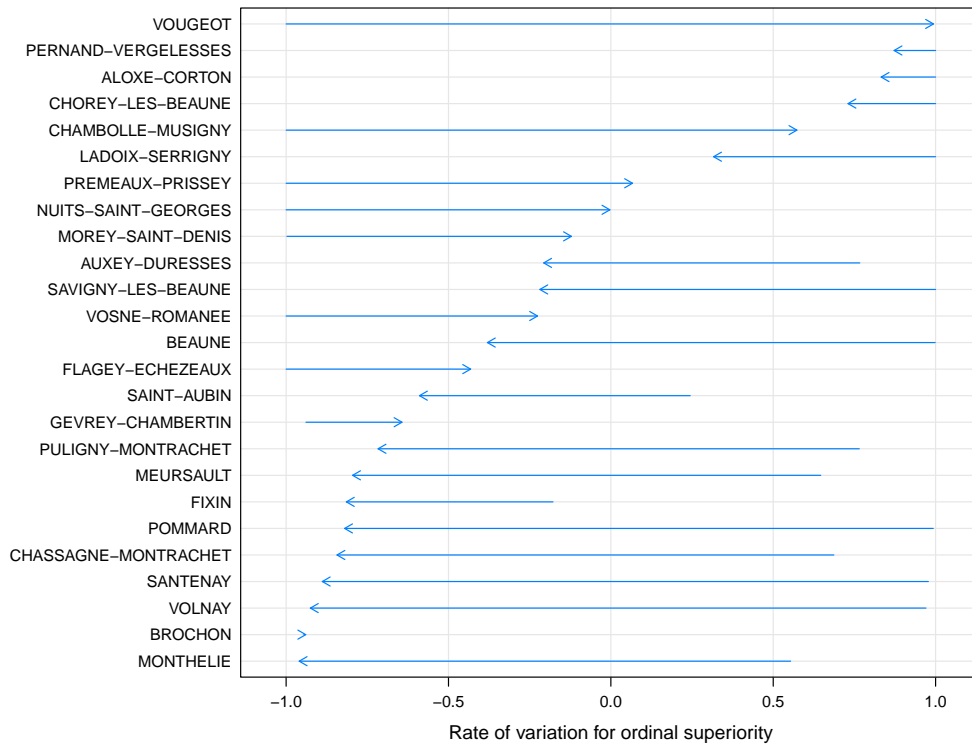
---

```

zzz <- merge(ww, www, by= "LIBCOM")
segplot(reorder(factor(LIBCOM), MEAN.x)~ MEAN.y+ MEAN.x, data= zzz,
  segments.fun = panel.arrows, length = 2, unit = "mm",
  draw.bands= F, axis = axis.grid,
  xlab= "Rate of variation for ordinal superiority")

```

---



## 6.10 Decomposition table

And then the decomposition table unreported in the main text that show the "smaller joint informational content of GIs in 1936" (p.XX).

---

```
load("Inter/gamold.Rda") ; source("myFcts.R")
ddoo <- data.frame(AOCavt= SRank$AOCavt, LIBCOM= SRank$LIBCOM,
  apply(gamold, function(x)
    rowSums(predict(x, type= 'terms')[, -1])))
dcop <- apply(names(ddoo[, 3: 9]), function(x)
  c("Total Signal"= var(ddoo[, x]), "Total Noise"= pi^2/ 3,
    jointSignal(ddoo, x, "AOCavt"), jointNoise(ddoo, x, "AOCavt"),
    vertiSignal(ddoo, x, "AOCavt"), vertiResid(ddoo, x, "AOCavt"), vertiNoise(ddoo, x, "AOCavt"),
    horizSignal(ddoo, x, "AOCavt"), horizResid(ddoo, x, "AOCavt"), horizNoise(ddoo, x, "AOCavt")))
round(t(apply(dcop, 1, function(x) x/ (pi^2/ 3+ dcop[1, ])* 100)), 1)
```

---

|               | gam50 | gam75 | gam100 | gam150 | gam200 | gam250 | gam300 |
|---------------|-------|-------|--------|--------|--------|--------|--------|
| Signal        | 95.6  | 93.1  | 95.4   | 98.7   | 98.1   | 99.5   | 99.5   |
| Noise         | 4.4   | 6.9   | 4.6    | 1.3    | 1.9    | 0.5    | 0.5    |
| Joint Signal  | 78.7  | 63.2  | 55.3   | 75.2   | 47.9   | 75.0   | 45.1   |
| Joint Noise   | 16.9  | 29.9  | 40.2   | 23.5   | 50.3   | 24.5   | 54.5   |
| Rank Signal   | 5.8   | 18.1  | 24.1   | 16.4   | 20.6   | 14.9   | 22.7   |
| Rank Noise    | 89.8  | 75.0  | 71.3   | 82.4   | 77.5   | 84.6   | 76.8   |
| Rank Residual | 72.9  | 45.1  | 31.2   | 58.8   | 27.3   | 60.1   | 22.4   |

|              |      |      |      |      |      |      |      |
|--------------|------|------|------|------|------|------|------|
| Com Signal   | 67.5 | 39.6 | 29.4 | 62.3 | 24.0 | 62.7 | 22.6 |
| Com Noise    | 28.1 | 53.5 | 66.0 | 36.4 | 74.1 | 36.8 | 77.0 |
| Com Residual | 16.0 | 33.3 | 43.7 | 20.9 | 35.3 | 20.6 | 43.7 |

## 7 Alternative GI designations

### 7.1 Change latent vineyard quality

We conclude this work with the simulations of alternative GIs designations schemes. Below are scenarios XX from XX, need to run the code. Put the equations here.

---

```
load("Inter/gamod.Rda")
prdd <- predict(gamod$gam900, type= 'terms')
thsld <- c(-Inf, gamod$gam900$family$getTheta(TRUE), Inf)
litt0 <- rowSums(prdd)- (sureOGAM(gamod$gam900)- gamod$gam900$line)
litt1 <- rowSums(prdd)
litt2 <- mean(prdd[, 1])+ rowSums(prdd[, -1])-
  (sureOGAM(gamod$gam900)- gamod$gam900$line)
litt3 <- mean(prdd[, 1])+ rowSums(prdd[, -1])
## CHANGER RRank$AOCcvt
Simu <- data.frame(RRank, litt= rowSums(prdd[, -1]),
  OLD= RRank$AOCcvt, S0= cut(litt0, thsld),
  SI= cut(litt1, thsld), SII= cut(litt2, thsld),
  SIII= cut(litt3, thsld))
table(Simu$AOCc, Simu$S0) ; table(Simu$AOCc, Simu$SI)
table(Simu$AOCc, Simu$SII) ; table(Simu$AOCc, Simu$SIII)
```

---

|               | OLD  | CF1  | CF2  | CF3  | CF4  | CF5  | CF6  |
|---------------|------|------|------|------|------|------|------|
| Signal        | 97.1 | 97.1 | 97.1 | 97.1 | 97.1 | 97.1 | 97.1 |
| Noise         | 2.9  | 2.9  | 2.9  | 2.9  | 2.9  | 2.9  | 2.9  |
| Joint Signal  | 51.4 | 80.1 | 81.2 | 82.2 | 79.4 | 80.0 | 79.2 |
| Joint Noise   | 45.8 | 17.1 | 15.9 | 15.0 | 17.7 | 17.1 | 18.0 |
| Rank Signal   | 38.9 | 70.7 | 64.5 | 73.5 | 62.2 | 62.8 | 62.0 |
| Rank Noise    | 58.2 | 26.4 | 32.6 | 23.6 | 34.9 | 34.3 | 35.1 |
| Rank Residual | 12.5 | 9.4  | 16.7 | 8.7  | 17.2 | 17.2 | 17.2 |
| Com Signal    | 28.5 | 28.5 | 28.5 | 28.5 | 28.5 | 28.5 | 28.5 |
| Com Noise     | 68.6 | 68.6 | 68.6 | 68.6 | 68.6 | 68.6 | 68.6 |
| Com Residual  | 22.9 | 51.6 | 52.7 | 53.7 | 50.9 | 51.5 | 50.7 |

### 7.2 Add a vertical level in GIs

Below are the simulations from scenarios XX, XX, and XX, according to changing XX. Put the equations here.

---

```
thrldBOUR <- mean(litt0[RRank$AOCc== 2])
thrldVILL <- mean(litt0[RRank$AOCc== 3])
thrldPCR <- mean(litt0[RRank$AOCc== 4])
Simv <- data.frame(Simu,
```



```

SIV= ifelse(RRank$AOCc< 2, RRank$AOCc,
  ifelse(RRank$AOCc== 2 & ltt0< thrldBOUR, 2,
    ifelse(RRank$AOCc== 2 & ltt0>= thrldBOUR, 3,
      RRank$AOCc+ 1))),
SV = ifelse(RRank$AOCc< 3, RRank$AOCc,
  ifelse(RRank$AOCc== 3 & ltt0< thrldVILL, 3,
    ifelse(RRank$AOCc== 3 & ltt0>= thrldVILL, 4,
      RRank$AOCc+ 1))),
SVI= ifelse(RRank$AOCc< 4, RRank$AOCc,
  ifelse(RRank$AOCc== 4 & ltt0< thrldPCRUI, 4,
    ifelse(RRank$AOCc== 4 & ltt0>= thrldPCRUI, 5,
      RRank$AOCc+ 1))))
table(Simv$AOCc, Simv$SIV)
table(Simv$AOCc, Simv$SV) ; table(Simv$AOCc, Simv$SVI)

```

---

|   | 1    | 2    | 3    | 4     | 5    | 6    |
|---|------|------|------|-------|------|------|
| 1 | 9759 | 0    | 0    | 0     | 0    | 0    |
| 2 | 0    | 8931 | 6577 | 0     | 0    | 0    |
| 3 | 0    | 0    | 0    | 24151 | 0    | 0    |
| 4 | 0    | 0    | 0    | 0     | 8577 | 0    |
| 5 | 0    | 0    | 0    | 0     | 0    | 1906 |

|   | 1    | 2     | 3     | 4     | 5    | 6    |
|---|------|-------|-------|-------|------|------|
| 1 | 9759 | 0     | 0     | 0     | 0    | 0    |
| 2 | 0    | 15508 | 0     | 0     | 0    | 0    |
| 3 | 0    | 0     | 13275 | 10876 | 0    | 0    |
| 4 | 0    | 0     | 0     | 0     | 8577 | 0    |
| 5 | 0    | 0     | 0     | 0     | 0    | 1906 |

|   | 1    | 2     | 3     | 4    | 5    | 6    |
|---|------|-------|-------|------|------|------|
| 1 | 9759 | 0     | 0     | 0    | 0    | 0    |
| 2 | 0    | 15508 | 0     | 0    | 0    | 0    |
| 3 | 0    | 0     | 24151 | 0    | 0    | 0    |
| 4 | 0    | 0     | 0     | 4970 | 3607 | 0    |
| 5 | 0    | 0     | 0     | 0    | 0    | 1906 |

### 7.3 Decomposition table

And the decomposition Table which corresponds to Table XX in the working paper.

```

decf <- sapply(names(Simv[, 100: 107]), function(x)
  c("Total Signal"= var(Simv[, "ltt"]), "Total Noise"= pi^2/ 3,
    jointSignal(Simv, "ltt", vt= x), jointNoise(Simv, "ltt", vt= x),
    vertiSignal(Simv, "ltt", vt= x), vertiResid(Simv, "ltt", vt= x), vertiNoise(Simv, "ltt", vt= x),
    horizSignal(Simv, "ltt", vt= x), horizResid(Simv, "ltt", vt= x), horizNoise(Simv, "ltt", vt= x)))
round(t(apply(decf, 1, function(x) x/ (pi^2/ 3+ decf[1, ]* 100)), 1)

```

---

OLD   S0   SI   SII   SIII   SIV   SV   SVI

|                     |      |      |      |      |      |      |      |      |
|---------------------|------|------|------|------|------|------|------|------|
| Total Signal        | 97.6 | 97.6 | 97.6 | 97.6 | 97.6 | 97.6 | 97.6 | 97.6 |
| Total Noise         | 2.4  | 2.4  | 2.4  | 2.4  | 2.4  | 2.4  | 2.4  | 2.4  |
| Joint Signal        | 50.7 | 78.4 | 80.7 | 81.1 | 82.8 | 79.2 | 79.7 | 79.0 |
| Joint Noise         | 46.9 | 19.2 | 16.8 | 16.5 | 14.8 | 18.4 | 17.9 | 18.6 |
| Vertical Signal     | 35.9 | 56.8 | 59.8 | 70.7 | 73.1 | 58.1 | 58.5 | 58.0 |
| Vertical Residual   | 14.9 | 21.6 | 21.0 | 10.4 | 9.7  | 21.1 | 21.2 | 21.1 |
| Vertical Noise      | 61.7 | 40.8 | 37.8 | 26.9 | 24.5 | 39.4 | 39.1 | 39.6 |
| Horizontal Signal   | 29.1 | 29.1 | 29.1 | 29.1 | 29.1 | 29.1 | 29.1 | 29.1 |
| Horizontal Residual | 21.6 | 49.3 | 51.7 | 52.0 | 53.7 | 50.1 | 50.6 | 50.0 |
| Horizontal Noise    | 68.5 | 68.5 | 68.5 | 68.5 | 68.5 | 68.5 | 68.5 | 68.5 |

## 8 Session information

---

```
sessionInfo()
```

---

```
R version 3.5.3 (2019-03-11)
```

```
Platform: x86_64-pc-linux-gnu (64-bit)
```

```
Running under: Ubuntu 18.04.2 LTS
```

```
Matrix products: default
```

```
BLAS: /usr/lib/x86_64-linux-gnu/blas/libblas.so.3.7.1
```

```
LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.7.1
```

```
locale:
```

```
[1] LC_CTYPE=fr_FR.UTF-8      LC_NUMERIC=C
[3] LC_TIME=fr_FR.UTF-8      LC_COLLATE=fr_FR.UTF-8
[5] LC_MONETARY=fr_FR.UTF-8  LC_MESSAGES=fr_FR.UTF-8
[7] LC_PAPER=fr_FR.UTF-8     LC_NAME=C
[9] LC_ADDRESS=C             LC_TELEPHONE=C
[11] LC_MEASUREMENT=fr_FR.UTF-8 LC_IDENTIFICATION=C
```

```
attached base packages:
```

```
[1] stats4      stats      graphics  grDevices  utils      datasets
[7] methods     base
```

```
other attached packages:
```

```
[1] gridExtra_2.3      xtable_1.8-3      ggrepel_0.8.0
[4] ggplot2_3.1.0      plyr_1.8.4        latticeExtra_0.6-28
[7] RColorBrewer_1.1-2 effects_4.0-3      lattice_0.20-38
[10] truncdist_1.0-2    evd_2.3-3         sure_0.2.0
[13] sandwich_2.5-0     lmtest_0.9-36     zoo_1.8-4
[16] mgcv_1.8-28        nlme_3.1-137      car_3.0-2
[19] carData_3.0-1      MASS_7.3-51.1     sp_1.3-1
```

```
loaded via a namespace (and not attached):
```

```
[1] Rcpp_1.0.0          assertthat_0.2.0  R6_2.3.0
[4] cellranger_1.1.0    survey_3.33-2     pillar_1.3.0
[7] rlang_0.3.0.1       lazyeval_0.2.1    curl_3.2
[10] readxl_1.1.0        minqa_1.2.4       data.table_1.11.4
[13] nloptr_1.0.4        Matrix_1.2-17     labeling_0.3
[16] splines_3.5.3       rgdal_1.3-6       lme4_1.1-18-1
[19] foreign_0.8-71      munsell_0.5.0     compiler_3.5.3
[22] pkgconfig_2.0.2     nnet_7.3-12       tidyselect_0.2.5
[25] tibble_1.4.2        rio_0.5.10        crayon_1.3.4
[28] dplyr_0.7.8         withr_2.1.2       grid_3.5.3
[31] gtable_0.2.0        magrittr_1.5      scales_1.0.0
[34] zip_1.0.0           bindrcpp_0.2.2    openxlsx_4.1.0
```

|      |                 |                  |             |
|------|-----------------|------------------|-------------|
| [37] | tools_3.5.3     | forcats_0.3.0    | glue_1.3.0  |
| [40] | purrr_0.2.5     | hms_0.4.2        | abind_1.4-5 |
| [43] | survival_2.43-3 | colorspace_1.3-2 | bindr_0.1.1 |
| [46] | haven_1.1.2     |                  |             |

## A Custom functions

### A.1 Translation of geology

---

```
trans_geol <- data.frame(  
  GEOL= Reg.Ras$GEOL[!duplicated(Reg.Ras$GEOL)],  
  GEOf= c(  
    "Calcaires massifs de \"Comblanchien\" (Bathonien sup.)",  
    "Marnes et calcaires divers (Callovien inférieur)",  
    "Marnes et calcaires argileux (Oxfordien moyen)",  
    "Eboulis ordonnés cryoclastiques et colluvions diverses",  
    "Oolithe ferrugineuse (Oxfordien moyen-sup)",  
    "Calcaires hydrauliques de Molesmes et Noiron (Oxfordien sup.)",  
    "Colluvions diverses",  
    "Dépôts argilo-limoneux, sables et graviers du Villafranchien",  
    "Calcaires de Tonnerre, Oisellemont et calcaires á Astartes",  
    "Eboulis et glissements de terrains",  
    "Calcaires grenus bicolores (Bathonien terminal)",  
    "Terrasse argilo-limoneuse de Saint-Usage",  
    "Formation de Saint-Cosme (marnes fluvio-lacustres varvées)",  
    "Alluvions anciennes indifférenciées, argilo-limoneuses",  
    "Calcaires bioclastiques, graveleux, á oolithes (Bathonien inf.)"  
  ),  
  GEOe= c(  
    "Massive limestones from \"Comblanchien\" (upper Bathonian)",  
    "Various marls and limestones (lower Callovian)",  
    "Marls and argillaceous limestones (middle Oxfordian)",  
    "Ordered cryoclastic scree and various colluviums",  
    "Ferruginous Oolite (middle-upper Oxfordian)",  
    "Hydraulic limestones of Molesmes and Noiron (upper Oxfordian)",  
    "Various colluviums",  
    "Clay-silt deposits, sand and gravel from Villafranchien",  
    "Limestones of Thunder, Oisellemont and limestones in Astartes",  
    "Scree and landslides",  
    "Two-tone gray limestones (terminal Bathonian)",  
    "Clay-silty terrace of Saint-Usage",  
    "Formation of Saint-Cosme (varnished fluvio-lacustrine marls)",  
    "Undifferentiated ancient alluvium, clay-silty",  
    "Bioclastic limestones, gravelly, with oolites (lower Bathonian)"  
  )  
)
```

---

## A.2 Translation of pedology

---

```
trans_pedo <- data.frame(  
  PEDO= Reg.Ras$PEDO[!duplicated(Reg.Ras$PEDO)],  
  PEDf= c(  
    "Vignoble de la Côte de de Beaune",  
    "Cônes de déjection du pied de Côte",  
    "Côteaux viticoles des Hautes Côtes de Nuits",  
    "Courtes pentes marneuses des plateaux plio-pléistocène",  
    "Piedmont de la côte viticole",  
    "Versants pentus des Hautes Côtes de Beaune",  
    "Sommetts des collines des Hautes Côtes de Beaune",  
    "Alluvions récentes calcaires des vallées (Ouche, Tille, Meuzin)",  
    "Pentes liasiques du Haut-Auxois",  
    "Basses terrasses gravelo-caillouteuses des plaines alluviales",  
    "Basses terrasses argileuses des plaines alluviales",  
    "Terrasse argilo-limoneuse de Saint-Usage",  
    "Vignoble de la Côte de Nuits",  
    "Rebord oriental des plateaux calcaires dominant la Côte viticole"  
  ),  
  PEDe= c(  
    "Vineyard of the Côte de Beaune",  
    "Coot footing cones",  
    "Wine hills of Hautes Côtes de Nuits",  
    "Oxfordian limestone-marly trays of the Hautes Côtes",  
    "Short marly slopes of Plio-Pleistocene plateaus",  
    "Piedmont of the vineyard of the Côte",  
    "Sloping slopes of the Hautes Côtes de Beaune",  
    "Summits of the hills of the Hautes Côtes de Beaune",  
    "Recent alluvial limestone valleys (Ouche, Tille, Meuzin)",  
    "Liastic slopes of Haut-Auxois",  
    "Gravelo-stony low terraces of alluvial plains",  
    "Low clay terraces of alluvial plains",  
    "Vineyard of the Côte de Nuits",  
    "Eastern edge of the limestone plateaus overlooking the Côte"  
  )  
)
```

---

### A.3 Surrogate Residuals

The R package `sure` allows to simulate the surrogate residuals from a large panel of ordered parametric models (<https://koalaverse.github.io/sure/index.html>) but not for the semiparametric ordered generalized additive model fitted with the package `mgcv`. We first define the `truncLogis` function for the simulation of random draws from a truncated logistic distribution with a vector of inputs (locations and thresholds) as the package `truncdists` is only designed for a given value of location and thresholds. Then, we code the function `surePOLR` which simulate surrogate residuals from `polr` models from the `MASS` package. The code is test against the surrogate simulations from `sure` for a random ordered logistic model.

---

```
truncLogis <- function(n, spec, a = -Inf, b = Inf, ...) {
  p <- runif(n, min = 0, max = 1)
  G <- get(paste("p", spec, sep = ""), mode = "function")
  Gin <- get(paste("q", spec, sep = ""), mode = "function")
  G.a <- G(a, ...)
  G.b <- G(b, ...)
  pmin(pmax(a, Gin(G(a, ...) + p * (G(b, ...) - G(a, ...)), ...)), b)
}

surePOLR <- function(mod, newd= NULL){
  if (mod$method!= "logistic") stop("Logistic required")
  gg <- as.numeric(mod$zeta)
  if (is.null(newd)){
    g1 <- as.integer(model.response(model.frame(mod)))
    g6 <- mod$lp
  } else {
    g1 <- as.integer(newd[, "AOCC"])
    g6 <- gg[ 1]-qlogis(predict(mod, newdata= newd, type= 'probs')[, 1])
  }
  nn <- length(g1)
  suls <- sapply(g1, switch,
    "1"= c(-Inf , gg[ 1]), "2"= c(gg[ 1], gg[ 2]),
    "3"= c(gg[ 2], gg[ 3]), "4"= c(gg[ 3], gg[ 4]),
    "5"= c(gg[ 4], Inf ))
  sls <- data.frame(unlist(t(suls)))
  truncLogis(nn, spec= "logis", a= sls[, 1], b= sls[, 2],
    location= g6, scale= 1)
}
```

---

```
library(MASS) ; library(sure) ; library(truncdists)
fit.polr <- polr(factor(AOCC)~ poly(DEM, 2)+ poly(SLOPE, 2)
  + poly(RAYAT, 2)+ poly(ASPECT, 2)+ poly(PERMEA, 2)
  , data= Reg.Rank)
sure1 <- surrogate(fit.polr)+ fit.polr$zeta[ 1]
sure2 <- resids(fit.polr)
polr1 <- surePOLR(fit.polr) ; polr2 <- surePOLR(fit.polr)- fit.polr$lp
```

---

Now we use the same structure to simulate the surrogate residuals for the OGAM through the function `sureOGAM`. Again, the function is tested for a random OGAM.

---

```
sureOGAM <- function(mod, newd= NULL){
  if (is.null(newd)){
```

```

    g1 <- as.integer(mod$y)
    g6 <- mod$linear.predictors
  } else {
    g1 <- as.integer(newd[, names(mod$model[ 1])])
    g6 <- predict(mod, newdata= newd)
  }
  nn <- length(g1)
  gt <- data.frame(rep(NA, nn), rep(NA, nn))
  gg <- c(mod$family$getTheta(TRUE), Inf)
  kk <- c(- Inf, gg[ 1])
  for (j in 2: length(unique(g1))) kk <- rbind(kk, c(gg[ j- 1], gg[ j]))
  gt <- data.frame(t(sapply(g1, function(x) kk[x, ])))
  truncLogis(nn, spec= "logis", a= gt[, 1], b= gt[, 2], location= g6)
}

```

---

```

library(mgcv)
fit.ogam <- gam(AOCc~ poly(DEM, 2)+ poly(SLOPE, 2)
               + poly(RAYAT, 2)+ poly(ASPECT, 2)+ poly(PERMEA, 2)
               , family= ocat(R= 5), data= Reg.Rank)
ogam1 <- sureOGAM(fit.ogam)
ogam2 <- sureOGAM(fit.ogam)- fit.ogam$linear.pred

par(mfrow= c(3, 2))
plot(sure1, polr1)
abline(h= fit.polr$zeta, v= fit.polr$zeta, lty= 2, col= "blue")
abline(0, 1, col= "orange")
plot(sure2, polr2)
abline(0, 1, col= "orange")

plot(polr1, ogam1- mean(ogam1))
abline(h= fit.ogam$family$getTheta(TRUE)- mean(ogam1),
       v= fit.polr$zeta, lty= 2, col= "blue")
abline(0, 1, col= "orange")
plot(polr2, ogam2)
abline(0, 1, col= "orange")

plot(sure1, ogam1- mean(ogam1))
abline(h= fit.ogam$family$getTheta(TRUE)- mean(ogam1),
       v= fit.polr$zeta, lty= 2, col= "blue")
abline(0, 1, col= "orange")
plot(sure2, ogam2)
abline(0, 1, col= "orange")

```

---



## A.4 Decomposition terms

For each terms of the decomposition presented in the main text, we code a different functions presented below. For the ease of notations, we note for the values of the latent and the probabilities of being in each GIs  $x = y, p$ :

$$\bar{x}_{jc} = \frac{1}{N} \sum_{i=1}^N x_i \quad \text{and} \quad \bar{x}_j = \frac{1}{C} \sum_{c=1}^C x_{jc} \quad \text{and} \quad \bar{x}_{.c} = \frac{1}{J} \sum_{j=1}^J x_{jc} \quad (1)$$

The **joint signal** terms is the variance of the expected quality conditionally on vertical and horizontal dummies:

$$\mathbb{V}\{\mathbb{E}[q(X^*) | y, c]\} = \frac{1}{N + J + H} \sum_{i=1}^N \sum_{j=1}^J \sum_{h=1}^H [\mathbb{E}(q(X^*) | y = j, c = h) - \bar{q}_{jh}]^2 \quad (2)$$

---

```
jointSignal <- function(dat, lt, vt= "AOCc", hz= "LIBCOM"){
  jS <- rep(0, nrow(dat))
  for (i in unique(dat[, vt])){
    for (j in unique(dat[, hz])){
      tmp <- dat[, vt]== i & dat[, hz]== j
      jS[ tmp] <- mean(dat[tmp, lt])
    }
  }
  c("Joint Signal"= var(jS))
}
```

---

The **joint noise** terms is the expectation of the variance quality conditionally on vertical and horizontal dummies:

$$\mathbb{E}\{\mathbb{V}[q(X^*) | y, c]\} = \frac{1}{N + J + H} \sum_{i=1}^N \sum_{j=1}^J \sum_{h=1}^H [\mathbb{E}(q(X^*) | y = j, c = h) - \bar{q}_{jh}]^2 \quad (3)$$

---

```
jointNoise <- function(dat, lt, vt= "AOCc", hz= "LIBCOM"){
  jN <- 0
  for (i in unique(dat[, vt])){
    for (j in unique(dat[, hz])){
      tmp <- dat[, vt]== i & dat[, hz]== j
      if (sum(tmp) > 1) jN <- jN+ var(dat[ tmp, lt])* mean(tmp)
    }
  }
  c("Joint Noise"= jN)
}
```

---

The **vertical signal** terms is the variance of the expectation quality conditionally on vertical GI dummies:

$$\mathbb{V}\{\mathbb{E}[q(X^*) | y]\} = \frac{1}{N + J + H} \sum_{i=1}^N \sum_{j=1}^J \sum_{h=1}^H [\mathbb{E}(q(X^*) | y = j, c = h) - \bar{q}_{jh}]^2 \quad (4)$$

---

```

vertiSignal <- function(dat, lt, vt= "AOCC", hz= "LIBCOM"){
  vS <- rep(0, nrow(dat))
  for (i in unique(dat[, vt])){
    vS[ dat[, vt]== i] <- mean(dat[dat[, vt]== i, lt])
  }
  c("Vertical Signal"= var(vS))
}

```

---

The **vertical residual** terms is the expectation of the conditional on horizontal variance of the expectation quality conditionally on vertical GI dummies:

$$\mathbb{E}\{ \mathbb{V}[\mathbb{E}(q(X^*) | y, c) | y] \} = \frac{1}{N + J + H} \sum_{i=1}^N \sum_{j=1}^J \sum_{h=1}^H [\mathbb{E}(q(X^*) | y = j, c = h) - \bar{q}_{jh}]^2 \quad (5)$$


---

```

vertiResid <- function(dat, lt, vt= "AOCC", hz= "LIBCOM"){
  sig <- rep(0, nrow(dat)) ; vR <- 0
  for (i in unique(dat[, vt])){
    for (j in unique(dat[, hz])){
      tmp <- dat[, vt]== i & dat[, hz]== j
      sig[ tmp] <- mean(dat[ tmp, lt])
    }
  }
  for (i in unique(dat[, vt])){
    vR <- vR+ var(sig[dat[, vt]== i])* mean(dat[, vt]== i)
  }
  c("Vertical Residual"= vR)
}

```

---

The **vertical Noise** terms is the expectation of the variance of the quality conditionally on vertical GI dummies:

$$\mathbb{E}\{ \mathbb{V}[q(X^*) | y] \} = \frac{1}{N + J + H} \sum_{i=1}^N \sum_{j=1}^J \sum_{h=1}^H [\mathbb{E}(q(X^*) | y = j, c = h) - \bar{q}_{jh}]^2 \quad (6)$$


---

```

vertiNoise <- function(dat, lt, vt= "AOCC", hz= "LIBCOM"){
  vN <- 0
  for (i in unique(dat[, vt])){
    vN <- vN+ var(dat[dat[, vt]== i, lt])* mean(dat[, vt]== i)
  }
  c("Vertical Noise"= vN)
}

```

---

The **horizontal signal** terms is the variance of the expectation quality conditionally on horizontal GI

dummies:

$$\mathbb{V}\{\mathbb{E}[q(X^*) | c]\} = \frac{1}{N + J + H} \sum_{i=1}^N \sum_{j=1}^J \sum_{h=1}^H [\mathbb{E}(q(X^*) | y = j, c = h) - \bar{q}_{jh}]^2 \quad (7)$$

---

```

horizSignal <- function(dat, lt, vt= "AOCc", hz= "LIBCOM"){
  hS <- rep(0, nrow(dat))
  for (j in unique(dat[, hz])){
    hS[ dat[, hz]== j] <- mean(dat[dat[, hz]== j, lt])
  }
  c("Horizontal Signal"= var(hS))
}

```

---

The **horizontal residual** terms is the expectation of the conditional on vertical variance of the expectation quality conditionally on horizontal GI dummies:

$$\mathbb{E}\{\mathbb{V}[\mathbb{E}(q(X^*) | y, c) | y]\} = \frac{1}{N + J + H} \sum_{i=1}^N \sum_{j=1}^J \sum_{h=1}^H [\mathbb{E}(q(X^*) | y = j, c = h) - \bar{q}_{jh}]^2 \quad (8)$$

---

```

horizResid <- function(dat, lt, vt= "AOCc", hz= "LIBCOM"){
  sig <- rep(0, nrow(dat)) ; hR <- 0
  for (i in unique(dat[, vt])){
    for (j in unique(dat[, hz])){
      tmp <- dat[, vt]== i & dat[, hz]== j
      sig[ tmp] <- mean(dat[ tmp, lt])
    }
  }
  for (j in unique(dat[, hz])){
    hR <- hR+ var(sig[dat[, hz]== j]) * mean(dat[, hz]== j)
  }
  c("Horizontal Residual"= hR)
}

```

---

The **horizontal Noise** terms is the expectation of the variance of the quality conditionally on horizontal GI dummies:

$$\mathbb{E}\{\mathbb{V}[q(X^*) | c]\} = \frac{1}{N + J + H} \sum_{i=1}^N \sum_{j=1}^J \sum_{h=1}^H [\mathbb{E}(q(X^*) | y = j, c = h) - \bar{q}_{jh}]^2 \quad (9)$$

---

```

horizNoise <- function(dat, lt, vt= "AOCc", hz= "LIBCOM"){
  hN <- 0
  for (j in unique(dat[, hz])){
    hN <- hN+ (var(dat[dat[, hz]== j, lt]) * mean(dat[, hz]== j))
  }
  c("Horizontal Noise"= hN)
}

```

---

}

---