

## UNIT-IV

### Classification

#### • Supervised learning (Classification)

— New data classified based on training set

#### • Unsupervised learning (Clustering)

— Establishing classes or clusters to identify unknown data

### Classification vs Numeric prediction

— Classification (discrete, Nominal data) to predict class for new data

— Numeric prediction (models continuously valued function)

→ Predict unknown or missing values.

Regression analysis  
is used

#### Applications:

- fraud detection
- medical diagnosis

### Classification

Two steps

#### 1. model construction

- describing a set of predetermined classes [class-label attribute]
- Training set used
- model represented as rules, decision trees or formula

#### 2. model usage

• estimate accuracy [Compare Predicted vs Actual]

↓  
Accuracy rate = % of samples correctly classified

If (Accuracy) is great  
then use model to classify new data

### Classification Algorithm

#### Classification (Model)



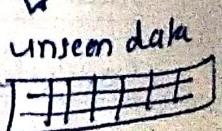
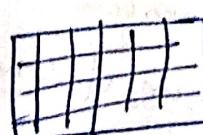
Predict if (Accuracy)  
is great

#### classification

Trained

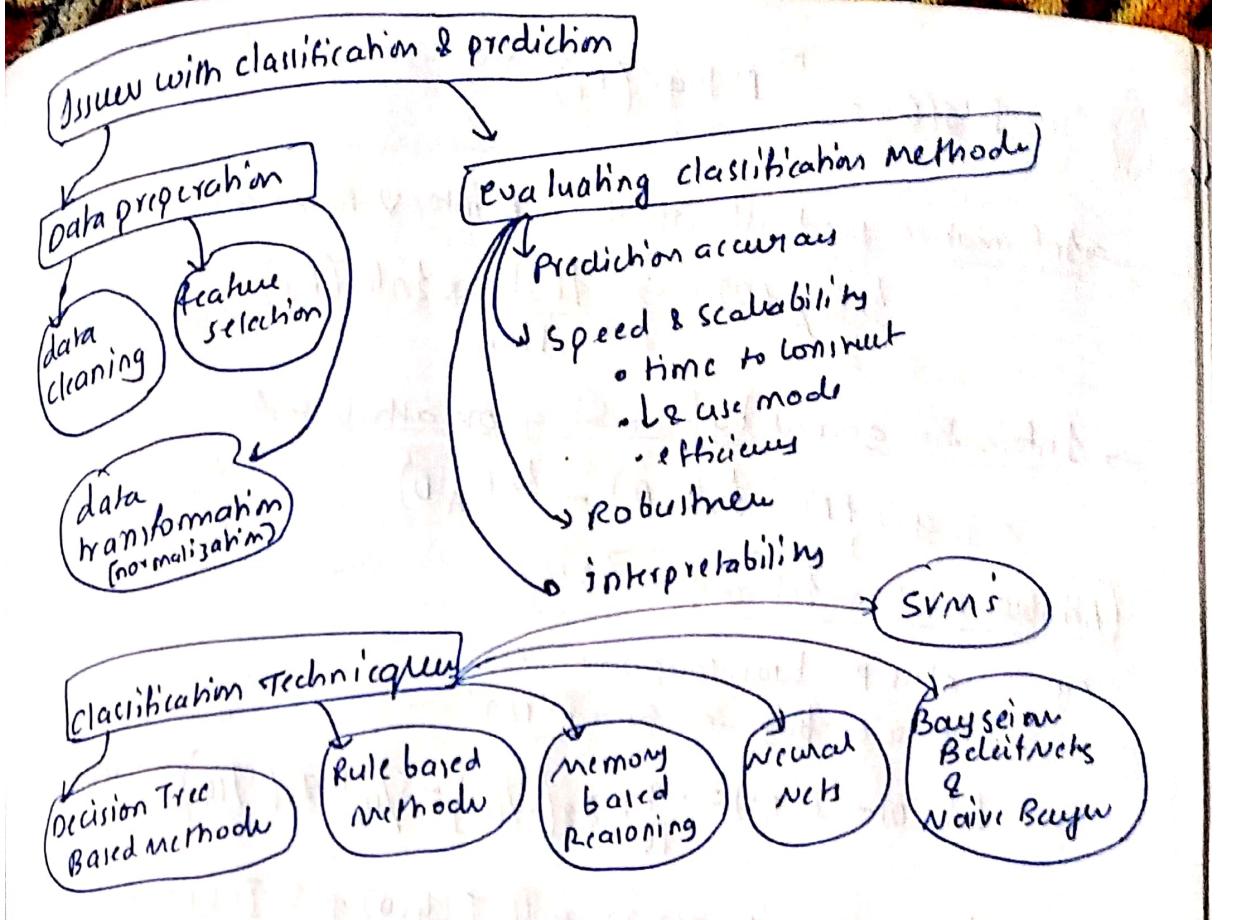
#### classification

Testing data



Predict.

If test set is used to select model  
then it is called validation/test



### Decision Tree induction

- Basic algorithm:
  - Tree is constructed in Topdown recursive divide & conquer manner
  - Starting, Training examples at root (all)
  - Attributes are categorical (if continuous valued, discretized in advance)
  - Examples are partitioned recursively based on selected attributes
  - Test attributes are selected on basis of Statistical Measure (Information gain)
- Conditions for stopping partitioning:
  - All samples of a given node belong to same class
  - no remaining attributes. (Majority voting applied for classifying leaf)
  - no samples left

Entropy [A measure of uncertainty]

- high entropy  $\rightarrow$  high uncertainty
- low entropy  $\rightarrow$  low uncertainty

Conditional entropy

$$H(Y|X) = \sum_x P(x) H(Y|x=x)$$

Attribute Selection measure : [Information gain  $103/14.5$ ]

- select attribute with highest information gain

$\rightarrow$  expected information (entropy)

let  $D \rightarrow$  Tuple,  $P \rightarrow$  Probability  
 $C \rightarrow$  Class

succession  
of

$$\text{Info}(D) = \sum_{i=1}^m p_i \log_2(p_i)$$

→ Information need after splitting D into V partitions using A

$$\text{Info}_A(D) = \sum_{j=1}^V \frac{|D_j|}{|D|} \times \text{Info}(D_j)$$

→ Information gained by branching on attribute A:

$$\text{gain}(A) = \text{Info}(D) - \text{Info}_A(D)$$

### (Attribute Selection: Information Gain)

e.g.: class 'P': buys-computer = "Yes"

class 'N': buys-computer = "NO"

$$\text{Info}(D) = I(9,5) = -\frac{9}{14} \log_2\left(\frac{9}{14}\right) - \frac{5}{14} \log_2\left(\frac{5}{14}\right) = 0.940$$

$$\text{Info}_{\text{age}}(D) = \frac{5}{14} I(2,3) + \frac{4}{14} I(4,0) + \frac{5}{14} I(3,1) = 0.694$$

age	$p_i$	$n_i$	$I(p_i, n_i)$
$\leq 30$	2	3	0.971
31..40	4	0	0
$> 40$	3	2	0.971

- 5 samples out of 14 for age  $\leq 30$
- 2 Yes & 3 No.

$$\text{Gain}(\text{age}) = \text{Info}(D) - \text{Info}_{\text{age}}(D) = 0.246$$

- similarly

$$\text{Gain}(\text{income}) = 0.029$$

$$\text{Gain}(\text{student}) = 0.151$$

$$\text{Gain}(\text{credit-rating}) = 0.048$$

age	income	student	credit-rating

### Computing Information Gain for continuous valued attributes

- Let  $A \rightarrow$  continuous valued attribute

steps:-

1. sort A in increasing order

2. find mid  $(a_1 + a_{n-1})/2$  and select it as

Best Split point

3. split tuple 'D' into  $D_1$  &  $D_2$

$$A(\leq \text{midpoint}) \rightarrow D_1$$

$$A(> \text{midpoint}) \rightarrow D_2$$

### Gain ratio for attribute selection

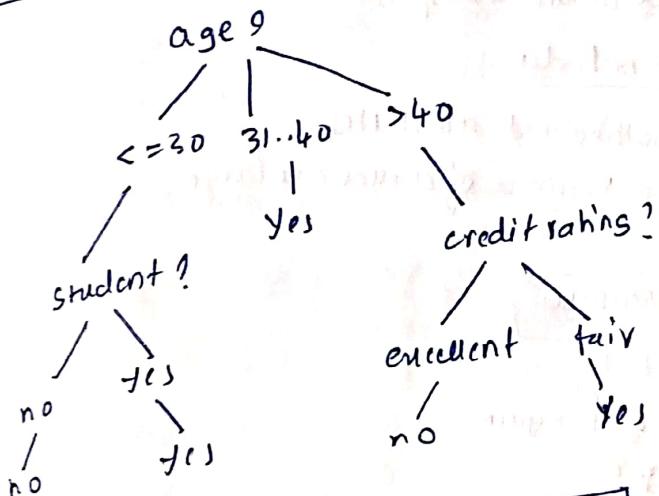
Information gain measure is biased towards attributes with many values.

$$\text{SplitInfo}(A) = - \sum_{j=1}^J \frac{|D_j|}{|D|} \times \log_2 \left( \frac{|D_j|}{|D|} \right)$$

$$\text{GAIN Ratio} = \text{Gain}(A) / \text{splitInfo}(A)$$

→ attribute with max gain ratio is selected as splitting attribute.

### Decision tree - attr Information gain



### Gini Index (CART, IBM Intelligent Miner)

- If a dataset  $D$  contains examples from  $n$  classes, then gini index

$$\text{gini}(D) = 1 - \sum_{j=1}^n p_j^2 \quad p_j = \text{relative frequency of class } j \text{ in } D$$

If  $D$  on  $A$  is split into  $D_1$  &  $D_2$

$$\text{gini}_A(D) = \frac{|D_1|}{|D|} \text{gini}_A(D_1) + \frac{|D_2|}{|D|} \text{gini}_A(D_2)$$

Reduction in Impurity

$$\Delta \text{gini}(A) = \text{gini}(D) - \text{gini}_A(D)$$

e.g.:  $D \rightarrow$  tuples in buys-computer = 4 "yes" & 5 in "no"

$$\text{gini}(D) = 1 - \left(\frac{9}{14}\right)^2 - \left(\frac{5}{14}\right)^2 = 0.459$$

Suppose  $D \rightarrow D_1 \& D_2$

$$\begin{matrix} 10 \\ 4 \end{matrix} \xrightarrow{\text{low, medium}} \text{medium}, \text{high}$$

$$\begin{aligned}
 &= 10/14 \left( 1 - \left(\frac{7}{10}\right)^2 - \left(\frac{3}{10}\right)^2 \right) + 4/14 \left( 1 - \left(\frac{2}{4}\right)^2 - \left(\frac{2}{4}\right)^2 \right) \\
 &\quad + \left(\frac{4}{14}\right) \text{gini}(D_1)
 \end{aligned}$$

$$= 0.443$$

$$= \text{gini}_{\text{income}} \in \{\text{high}\}$$

- $\text{Gini}_{\text{low, high}}$  is 0.458,  $\text{gini}_{\text{medium, high}}$  is 0.458  
∴ split the {low, medium} & {high}

### disadvantages of Gini Ratio

- tends to prefer unbalanced splits

### disadvantages of gini index

- biased to multivalued attributes

- difficult when number of classes are large

### Other popular Selection Measure

- CHAID: based on  $\chi^2$  test
- C-SEP: better than gini & gain
- G-statistic: closer to  $\chi^2$
- MDL (minimum description length) → prefers simple solution
- CART: find multivariate split based on linear combination of attributes.

### Overtfitting & Tree pruning

- Overtfitting :- A induced tree may overfit the training data
  - Too many branches, noise
  - Poor accuracy for unseen samples
- Two approaches to avoid overfitting
- Pre-pruning : Halt tree construction early & remove branches failing below a goodness threshold
- Post-pruning :- Remove branches from fully grown trees

## Enhancements to Basic Decision Tree Induction

- Allow for continuous valued attributes.
- Handle missing attribute values
- attribute construction.
  - create new attributes based on existing
  - reduces fragmentation, repetition & replication

classification in large databases → Why decision trees so popular?

- can classify millions of examples & hundreds of attributes using reasonable speed in decision trees.
- Scalable
- relatively faster running speed.
- convertible to simple rules.

## Scalability framework for Rainforest

- Builds an AVC list (AVC Attribute, value, class-label)
- AVC-set (of attribute X)
  - Projection of training data onto attribute X

- AVC-group (of a node N)
  - set of AVC sets. of projection attributes at node N

e.g.: AVC set on income

		Buys-computer	
income		yes	no
high	2	2	
	4	2	
	3	1	

## BOAT (Bootstrapped Optimistic Algorithm for Tree Construction)

- uses a statistical technique called bootstrapping to create several smaller samples (subsets), each fit in memory.
- each subset creates a new tree, resulting in several trees
- Adv: requires only two scans of DB, an incremental alg.

## Bayesian classification) why?

- A statistical classification → does probabilistic prediction
- works on Bayes Theorem
- good performance relatively along with Neural Net & Decision trees
- Incremental: improves with data
- standard: Bayesian methods are intractable & provides decision making

## Bayes theorem: Basics

- Total probability theorem:

$$P(B) = \sum_{i=1}^M P(B|A_i) P(A_i)$$

- Bayes theorem:

$$P(H|x) = \frac{P(x|H) P(H)}{P(x)}$$

x → data sample  
H → hypothesis that  
x belong to class

→ classification is to determine  $P(H|x)$  [posterior probability]

$P(H)$  → initial probability

$P(x)$  → Probability that Sample data is observed

$P(x|H)$  → likelihood.

Theorem:-

(TC) Given training data  $X$ , Posteriori probability of a hypothesis  $H$ ,  $P(H|x)$  follows Bayes theorem

$$P(H|x) = \frac{P(x|H) P(H)}{P(x)}$$

Simply  $\Rightarrow$  Posteriori = likelihood × Prior/evidence

→ let attributes  $X = \{x_1, x_2, \dots, x_n\}$

→ classes  $C_1, C_2, \dots, C_m$

→ classification → max Posteriori

$$\therefore P(c_i/x)$$

$$\therefore P(c_i/x) = \frac{P(x/c_i) P(c_i)}{P(x)}$$

as  $P(x)$  is constant for all classes

$$P(c_i/x) = P(x/c_i) P(c_i)$$

### Naive Bayes classification

- If attributes are conditionally independent, then it greatly reduces the computational cost.

$$\therefore P(x/c_i) = \prod_{k=1}^n P(x_k/c_i) = P(x_1/c_i) \times \dots \times P(x_n/c_i)$$

Dataset

age	income	student	credit-rating	buys-computer
$\leq 30$	high	no	fair	no
$\leq 30$	high	no	excellent	no
$31..40$	high	no	fair	yes
$> 40$	medium	no	fair	yes
$> 40$	low	yes	fair	yes
$> 40$	low	yes	excellent	no
$31..40$	low	yes	excellent	yes
$\leq 30$	medium	no	fair	no
$\leq 30$	low	yes	fair	yes
$> 40$	medium	yes	fair	yes
$\leq 30$	medium	yes	excellent	yes
$31..40$	medium	no	excellent	yes
$31..40$	high	yes	fair	yes
$> 40$	medium	no	excellent	no

e.g:-

- $P_i(l) :=$

$$P(\text{buys-computer} = "yes") = 9/14 = 0.643$$

$$P(\text{buys-computer} = "no") = 5/14 = 0.357$$

- Compute  $P(x_i | l_i)$  for each class

$$P(\text{age} \leq 30 | \text{buys-computer} = "yes") = 2/9 = 0.222$$

$$P(\text{age} \leq 30 | \text{buys-computer} = "no") = 3/5 = 0.6$$

$$P(\text{income} = "medium" | \text{buys-computer} = "yes") = 4/9 = 0.444$$

$$P(\text{income} = "medium" | \text{buys-computer} = "no") = 2/5 = 0.4$$

$$P(\text{student} = "not" | \text{buys-computer} = "yes") = 6/9 = 0.667$$

$$P(\text{student} = "not" | \text{buys-computer} = "no") = 1/5 = 0.2$$

$$P(\text{credit} = "fair" | \text{buys-computer} = "yes") = 6/9 = 0.667$$

$$P(\text{credit} = "fair" | \text{buys-computer} = "no") = 2/5 = 0.4$$

- $x = (\text{age} \leq 30, \text{income} = \text{medium}, \text{student} = \text{Yes}, \text{credit} = \text{fair})$

$$P(x | l_i) : P(x | \text{buys-computer} = "yes")$$

$$= 0.222 \times 0.444 \times 0.667 \times 0.667$$

$$= 0.044$$

$$: P(x | \text{buys-computer} = "no")$$

$$= 0.6 \times 0.4 \times 0.2 \times 0.4 = 0.019$$

$$P(x | l_i) * P(l_i) : P(X | \text{buys-computer} = "yes") *$$

$$P(\text{buys-computer} = "yes")$$

$$= 0.044 \times 0.643 = 0.028$$

$$P(X | \text{buys-computer} = "no") * P(\text{buys-computer} = "no") = 0.007$$

$\therefore x$  belongs to class ("buys-computer = yes")

## Problem in Bayesian

- Naive Bayesian prediction requires each condition prob be non-zero, otherwise the predicted probability will be zero.

$$P(X/c_i) = \prod_{k=1}^n P(x_k/c_i)$$

, we use Laplacian correction

## Advantages of Naive Bayes classification

- easy to implement
- good results in most of cases

## disadvantage

- If there is class conditional independence accuracy is lost

## Rule-Based classification

organizing the knowledge in the form of if-then rules

R: If age=youth and student = yes then buys-Computer = yes

Rule antecedent / Precondition      Condition

• Assessment of Rule is done by Accuracy & coverage

$n_{covers}$  = number of tuples covered by R

$n_{correct}$  = number of tuples correctly classified by R

$$\text{Coverage}(R) = \frac{n_{covers}}{|D|} \rightarrow \text{Training data set}$$

$|D| \rightarrow$  Training data set

$$\text{accuracy}(R) = \frac{n_{correct}}{n_{covers}}$$

• If more than one rule are triggered, we need conflict resolution.

- size ordering

- class based ordering : decreasing order of prevalence

- Rule-based ordering (decision/Priority list).

## Rules extraction from decision tree

- Rules are easier to understand
- One rule for each path from root to leaf
  - leaf holds class prediction
- Rules are mutually exclusive & exhaustive

## Rule induction : Sequential Covering method

- Sequential covering algorithm :-  
extracts rules directly from training data.

Eg: Algorithms are: FOIL, AQ, CN2, RIPPER

TC Rules are learned sequentially, each for given class  $c_i$ , will cover many tuples of  $C \cup D$

### Steps:-

1. Rules are learned one at a time
2. each time a rule is learned, the tuples covered by rule are removed
3. Repeat the process until no more training examples left

while(enough target tuples left)

  generate a rule

  remove positive target tuples satisfying this rule

#### - Rule generation

  while(true)

    find best predicate  $P$

    if foil-gain( $P$ ) > threshold then add  $P$  to current rule  
    else break.

## How to learn one rule

- Start with most general rule possible (condition = empty)

- add new attributes by adopting a greedy depth-first strategy
- Rule quality measure (in FOIL & RIPPER)
  - allow info-gain

$$\text{FOIL-Prune}(R) = \frac{\text{Pos} - \text{Neg}}{\text{Pos} + \text{Neg}}$$

true examples  
-ve examples

$$\text{FOIL-Gain}(R) = \text{Pos}' \times \left( \log_2 \frac{\text{Pos}'}{\text{Pos} + \text{Neg}'} - \log_2 \frac{\text{Pos}}{\text{Pos} + \text{Neg}} \right)$$

### Model evaluation & selection

- use validation test set of class-labelled tuples instead of Training set when assessing accuracy
- methods for estimating a classifier's efficiency.

- Holdout method, random Subsampling
- cross-validation
- Bootstrap (.632 bootstrap)  $N = \text{number of tuples}$
- comparing classifiers:
  - confidence interval
  - cost-benefit analysis & ROC curves

partitioned into  
random independent  
subsets  
& cross-validated

K-fold ( $K=10$ )  
randomly partition  
data into K mutually  
exclusive subsets  
of equal size

### Classification evaluation metrics

- precision: % of tuples labelled by classifier as true

$$\text{Precision} = \frac{\text{TP}}{\text{TP} + \text{FP}}$$

[exactness]

- Recall: % of what tuples did classifier labelled as true

$$\text{Recall} = \frac{\text{TP}}{\text{TP} + \text{FN}}$$

Perfect score is 1.0

- F measure (F-score): harmonic mean of precision & recall

$$F = \frac{2 \times \text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$$

- $F_\beta$  (weighted measure of Precision & Recall)

$$F_\beta = \frac{(1+\beta)^2 \times \text{Precision} \times \text{Recall}}{\beta^2 \times \text{Precision} + \text{Recall}}$$

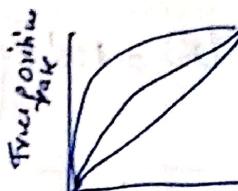
Estimating confidence interval : null hypothesis

- If we can reject null hypothesis ( $M_1 \neq M_2$  or distributions are the same). then the difference between  $M_1$  &  $M_2$  is statistically significant [choose however rate one]

→ t-test → pairwise comparison

### Model selection: ROC curve

- Receiver operating characteristic curve for visual comparison of classifiers.
- A model with perfect accuracy will have an area



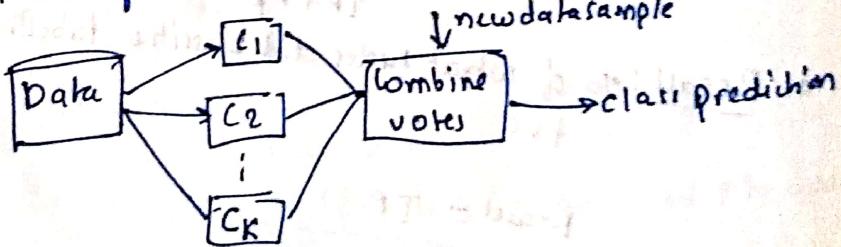
### Issues affecting model selection

- Accuracy
- Speed
- Robustness
- Scalability
- Interpretability

### Techniques to improve classification Accuracy

#### ensemble methods

- use a combination of models to increase accuracy
- combine a series of  $K$  learned models  $M_1, M_2, \dots, M_K$  with aim of creating an improved model  $M^*$



#### ensemble methods

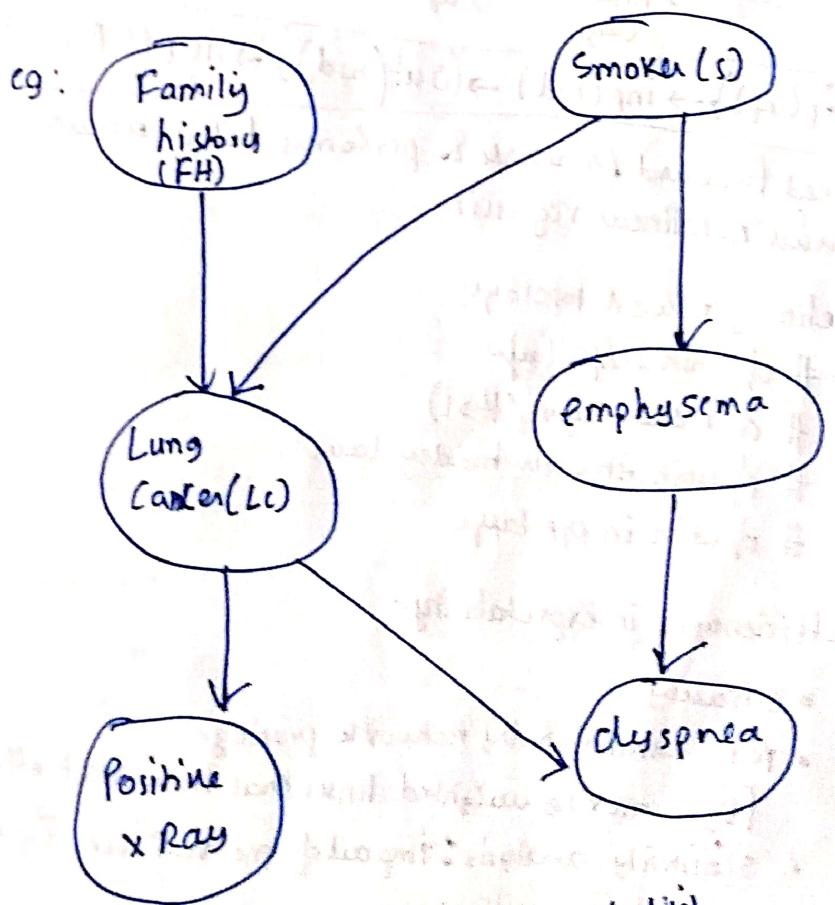
- Bagging [diagnosis based on multiple doctors Majority vote]
- Ada Boost [consult several doctors, based on combination of weighted diagnosis - weight assigned on previous diagnosis accuracy]
- Boosting [Random forest] → Forest-R1 (random input selection) → Forest-R2 (random linear combination)

## Handling different kinds of cases in classification

- Traditional methods assumes a balanced distribution of data.
- Typical methods for imbalance data in 2-class classification
  - oversampling :- re-sampling of data from positive class
  - under sampling :- randomly eliminate tuples from negative class
  - Threshold moving : moves the decision threshold so that rare-class tuples are easy to classify
  - ensemble methods : ensemble multiple classifiers are discussed below.

## Bayesian Belief Networks / Bayesian networks

- Bayesian belief networks / probabilistic networks allow class conditional independencies between subsets of variables.
- uses a directed acyclic graph.



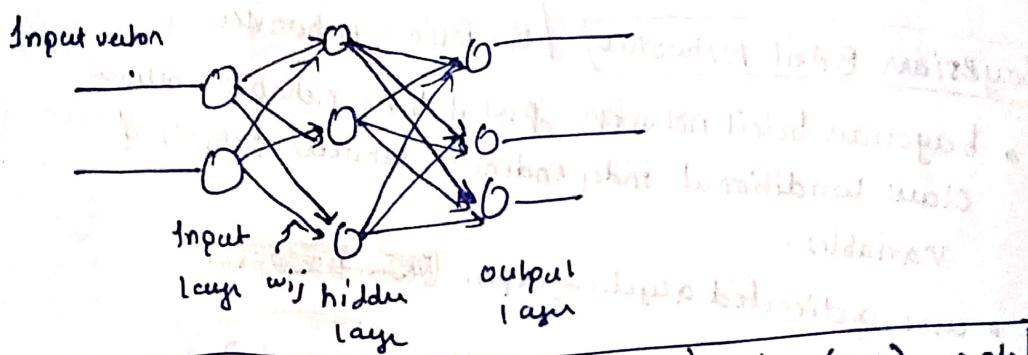
→ uses conditional probability -

## Classification by backpropagation [Connectionist learning]

- A neural network learning algorithm
- A set of connected ip/op units where each connection has a weight associated with it.
- During learning phase, the network learns by adjusting weights to minimize mean squared error.
- Modifications are made in backward direction

## Neural Network as a classifier

- Advantages:
- high tolerance to noisy data
  - Ability to classify untrained patterns.
  - Algorithms are parallel.
- disadvantages:
- long training time



→ Feed forward Network & performs better when used non linear regression

### - defining network topology

# of units in ip layer

# of hidden layers ( $H > 1$ )

# of units in each hidden layer.

# of units in o/p layer

### - efficiency & interpretability

• efficiency

• Rule extraction by network pruning

[By removing weighted links that have least effect]

• Sensitivity analysis: impact of one variable input on network output.

### - discriminating classifications

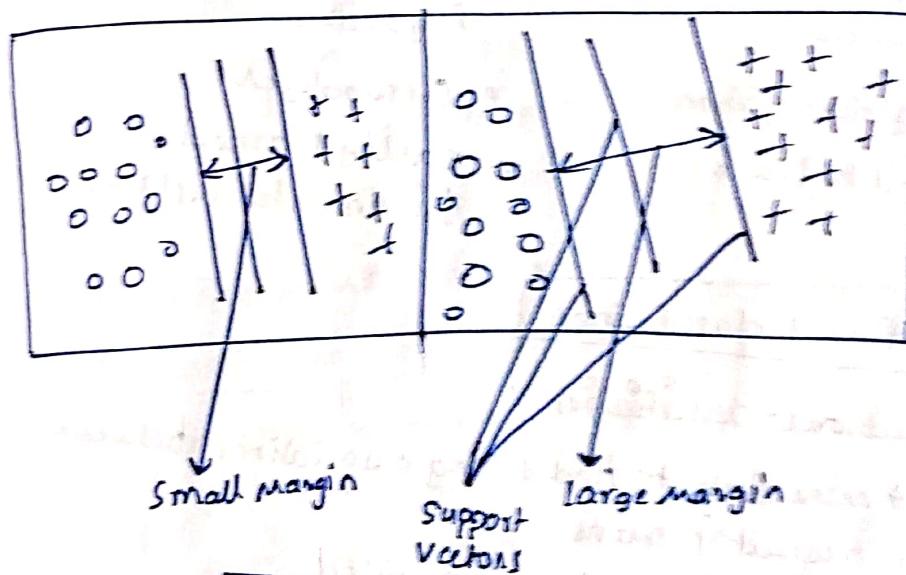
• high accuracy v/s long training time

## Support Vector Machines

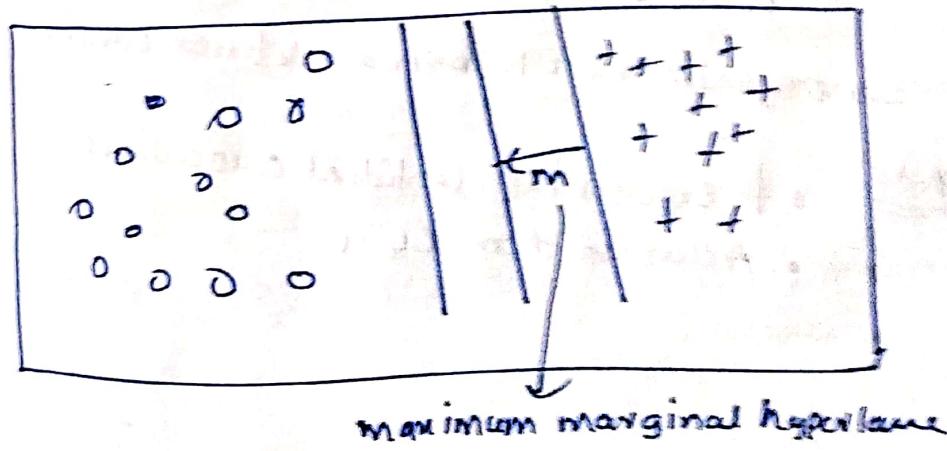
- A relatively new classification method for both linear & nonlinear data
- It uses a nonlinear mapping to transform the original training data into a higher dimension.
- With the new dimension, it searches for linear optimal separating hyperplane (decision boundary)
- With appropriate non linear mapping, data from two classes can always be separated by a hyperplane.
- SVM finds this hyperplane using support vectors ("essentially training tuples") & margins (defined by support vectors).

Applications : handwritten digit recognition, object recognition etc.

[Classification & numeric prediction ]



→ When data is linearly separable Concept



## Why SVM effective on high dimensional data

- The complexity of trained classifier is characterized by # of support vectors rather than dimensionality of data.
- With small # of support vectors, we can have good generalization

## SVM Linearly Separable

- Transform the original input data into a linearly higher dimensional space.
- Search for linear separating hyperplane in the new space.

## SVM v/s Neural Net

### SVM

- Deterministic Algorithm
- Nic generalization
- Hard to learn

### NN

- Non-deterministic Algorithm
- Generalizer
- easily learned in incremental fashion.

## Pattern Based classification

### Association classification :-

→ mine data to find strong associations between frequent patterns

→ Association rules are generated

$$P_1 \wedge P_2 \dots \wedge P_i \rightarrow "A \text{ class} = C" (\text{conf}, \text{sup})$$

→ Organise rules to form a rule based classifier

Adv :-

- It explores high confident associations

- Accurate than C4.5

## Typical Association classification methods

- o CBA (Classification based on Associations)
- o CMAR (Classification based on Multiple Association Rules)
- o CPAR (Classification based on Predictive Association Rules)

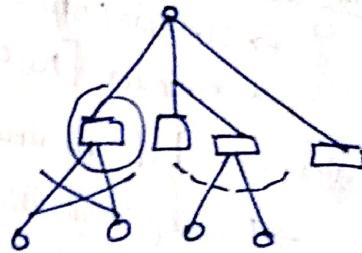
→ Discrimination frequent pattern - Based classification

- o DPP Mine (Branch & Bound search)
- o FPtree pruning

$$\text{Sup}(\text{child}) \leq \text{Sup}(\text{Parent})$$

$$\text{Sup}(b) \leq \text{Sup}(a)$$

$$\text{Maximize } \text{In}(C/b)$$



## Lazy v/s eager learning

- o lazy learning :- (instance-based learning)

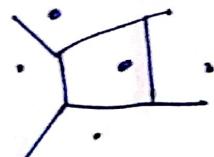
Simply stores data for mining processing & waits until it given a test tuple

- o early learning : constructs a classifier before receiving data to classify.

→ Instance Based methods

### ① K-nearest neighbour approach :-

- o Instances represented as points in Euclidean space



— nearest neighbour defined in terms of Euclidean distance ( $x_1, x_2$ )

— Target function can be real or discrete valued

— for discrete valued, K-NN returns most common value among K training examples.

Voronoi  
diagram  
is used

### ② Locally weighted regression (uses local approximation)

### ③ case-based reasoning (uses symbolic representations) q inference