

Package ‘stationaryracsinference’

February 9, 2019

Type Package

Title Gliding Box Lacunarity and Other Estimators for Random Closed Sets in 2D

Version 0.5-01

Date 2019-01-16

Author Kassel Liam Hingee

Maintainer Kassel Liam Hingee

<kassel.hingee@research.uwa.edu.au>

Description Functions for estimating properties of random closed sets in 2D from binary maps and for simulating 2D Boolean models. Here a binary maps are usually taken to be a rasterised image with each pixel labelled TRUE, FALSE or NA, with NA representing unobserved pixels. A demo for extracting a such a binary map from geospatial data formats (e.g. presence-absence maps or two-class landcover maps) is provided. The binary map may also be represented in non-rasterised form using a polygonal set as the foreground. Empirical gliding box lacunarity and improved, covariance-based, estimators of gliding box lacunarity are included. Also included are anisotropic estimators of covariance, centred covariance and pair-correlation based on estimators proposed by Picka. Additional estimators for properties of random closed sets are available in the spatstat package. The package is based on research conducted during the author's PhD studies.

License GNU General Public License

Depends spatstat

Imports RcppRoll

Suggests raster,
maptools,
rgdal,
testthat

ByteCompile true

RoxygenNote 6.1.0

R topics documented:

stationaryracsinference-package	2
cencovariance	4
contagdiscstate	6
contagpixelgrid	8
coverageprob	9
cppicka	10
gbl	12
gblc	14
gblcc	15
gblemp	16
gblg	18
innerprod.im	19
isbinarymap	20
paircorr	21
placegrainsfromlib	23
pluginvc	25
racscovariance	26
rbdd	29
rbdr	31
rblnd	32
rbpto	33
secondorderprops	35
summary.imlist	36
Index	37

stationaryracsinference-package

*Gliding Box Lacunarity and Other Estimators for Random Closed Sets
in 2D*

Description

Functions for estimating properties of random closed sets in 2D from binary maps and for simulating 2D Boolean models. Here a binary maps are usually taken to be a rasterised image with each pixel labelled TRUE, FALSE or NA, with NA representing unobserved pixels. A demo for extracting a such a binary map from geospatial data formats (e.g. presence-absence maps or two-class landcover maps) is provided. The binary map may also be represented in non-rasterised form using a polygonal set as the foreground. Empirical gliding box lacunarity and improved, covariance-based, estimators of gliding box lacunarity are included. Also included are anisotropic estimators of covariance, centred covariance and pair-correlation based on estimators proposed by Picka. Additional estimators for properties of random closed sets are available in the spatstat package. The package is based on research conducted during the author's PhD studies.

Details

Background is available for RACS (Chiu et al., 2013; Molchanov, 2005), gliding box lacunarity (GBL) (Hingee et al., 2017) and contagion for RACS (Hingee, 2016). A forthcoming PhD thesis by (Hingee, 2019) will provide additional background for GBL, and for RACS in landscape metrics (which includes contagion).

This package expects RACS observations to be in the form of binary maps either in raster format, or as a set representing foreground with a second set giving the observation window. If in raster format, the object is expected to be a **spatstat** `im` object with pixel values that are only 1 and 0, or are logically valued (i.e. TRUE or FALSE). In both cases the observation window is taken to be the set of pixels with values that are not NA (i.e. NA values are considered outside the observation window). The foreground of the binary map, corresponding to locations within the realisation of the RACS, is taken to be pixels that have value 1 or TRUE. If the binary map is in set format then a **spatstat** `owin` object is used to represent foreground and a second `owin` object is used to represent the observation window.

We will usually denote a RACS as Ξ and a realisation of Ξ observed as a binary map as x_i . We will usually denote the observation window as `obswin`.

A demonstration converting remotely sensed data into a binary map in `im` format can be accessed by typing `demo("import_remote_sense_data", package = "stationaryracsinference")`. A short example of estimating RACS properties can be found in the vignette `estimate_RACS_properties`, which can be accessed with `vignette("estimate_RACS_properties")`.

The key functions within this package for estimating properties of RACS are:

- `coverageprob` estimates the coverage probability of a stationary RACS
- `raccovariance` estimates the covariance of a stationary RACS
- `gbl` estimates the GBL of a stationary RACS
- `cencovariance` estimates the centred covariance of a stationary RACS
- `paircorr` estimates the pair-correlation of a stationary RACS
- `secondorderprops` estimates GBL, covariance and other second order properties of stationary RACS
- `contagdiscstate` estimates the disc-state contagion of a stationary RACS

Key function for simulating RACS are:

- `rbdd` simulates a Boolean model with grains that are discs with fixed radius (deterministic discs).
- `rbdr` simulates a Boolean model with grains that are rectangles of fixed size and orientation.
- `rbpto` simulates a Boolean model with grains that of fixed shape and random scale distributed according to a truncated Pareto distribution.
- `placegrainsfromlib` randomly places grains on a set of points (used to simulate Boolean models and other germ-grain models).

Author(s)

Kassel Liam Hingee

Maintainer: Kassel Liam Hingee <kassel.hingee@research.uwa.edu.au>

References

- Chiu, S.N., Stoyan, D., Kendall, W.S. and Mecke, J. (2013) *Stochastic Geometry and Its Applications*, 3rd ed. Chichester, United Kingdom: John Wiley & Sons.
- Hingee, K.L. (2016) Statistics for patch observations. *International Archives of the Photogrammetry, Remote Sensing and Spatial Information Sciences* pp. 235-242. Prague: ISPRS.
- Hingee, K.L. (2019) *Spatial Statistics of Random Closed Sets for Earth Observations*. PhD: Perth, Western Australia: University of Western Australia. Submitted.
- Hingee K, Baddeley A, Caccetta P, Nair G (2017). Computation of lacunarity from covariance of spatial binary maps. *Journal of Agricultural, Biological and Environmental Statistics*. Submitted.
- Molchanov, I.S. (2005) *Theory of Random Sets*. USA: Springer.

Examples

```
#Estimates using the heather data in spatstat
xi_owin <- heather$coarse
xi_owin_obswin <- Frame(heather$coarse)

#convert to an im object (optional)
xi <- as.im(xi_owin, value = TRUE, na.replace = FALSE)

cphat <- coverageprob(xi)
cvchat <- racscovariance(xi, estimator = "pickaH")
gblhat <- gbl(xi, seq(0.1, 5, by = 0.1), estimators = "GBLcc.pickaH")
contagds <- contagdiscstate(Hest(xi), Hest(!xi), p = cphat)

#simulate a Boolean model with deterministic discs in a square window
xi_sim <- rbdd(10, 0.1, owin())
```

cencovariance

Centred covariance estimation

Description

This function estimates the centred covariance of a stationary RACS. Available estimators are the plug-in moment centred covariance estimator, two ‘balanced’ estimators suggested by Picka (2000), and a third ‘balanced’ estimator inspired by one of Picka’s pair-correlation estimators.

Usage

```
cencovariance(xi, obswin = NULL, setcov_boundarythresh = NULL,
  estimators = "all", drop = FALSE)

cencovariance.cvchat(cvchat, cpp1 = NULL, phat = NULL,
  setcov_boundarythresh = NULL, estimators = "all", drop = FALSE)
```

Arguments

xi	An observation of a RACS of interest as a full binary map (in <code>im</code> format) or as the foreground set (in <code>owin</code> format). In the latter case the observation window, <code>obswin</code> , must be supplied. See stationaryracsinference-package for details.
obswin	If <code>xi</code> is an <code>owin</code> object then <code>obswin</code> is an <code>owin</code> object that specifies the observation window.
setcov_boundarythresh	Any vector v such that set covariance of the observation window is smaller than this threshold is given a covariance of NA to avoid instabilities caused by dividing by very small areas,
estimators	A list of strings specifying estimators to use. See details. <code>estimators = "all"</code> will select all available estimators.
drop	If TRUE and one estimator selected then the returned value will be a single <code>im</code> object and not a list of <code>im</code> object.
cvchat	The plug-in moment estimate of covariance in <code>im</code> format. Typically created with plugincvc .
cpp1	Picka's reduced window estimate of coverage probability in <code>im</code> format - used in improved (balanced) covariance estimators. Can be generated using cppicka .
phat	The usual estimate of coverage probability, which is the observed foreground area in <code>xi</code> divided by the total area of the observation window. See coverageprob for more information.

Details

The centred covariance of a stationary RACS is

$$\kappa(v) = C(v) - p^2.$$

The estimators available are (see (Section 3.4, Hingee, 2019) for information):

- `plugin` the plug-in moment centred covariance estimator
- `mattfeldt` an estimator inspired by an 'intrinsically' balanced pair-correlation estimator from Picka (1997) that was later studied in an isotropic situation by Mattfeldt and Stoyan (Mattfeldt and Stoyan, 2000)
- `pickaint` Picka's intrinsically' balanced centred covariance estimator (Picka, 2000).
- `pickaH` Picka's additively' balanced centred covariance estimator (Picka, 2000).

Currently computes centred covariance using [racscovariance](#).

Value

If `drop = TRUE` and a single estimator requested then a `im` object containing the centred covariance estimate. Otherwise a named `imlist` of `im` objects containing the centred covariance estimates for each requested estimator.

Functions

- `cencovariance`: Centred covariance estimates from a binary map.
- `cencovariance.cvchat`: Generates centred covariances estimates from a plug-in moment estimate of covariance, Picka's reduced window estimate of coverage probability, and the plug-in moment estimate of coverage probability. If these estimates already exist then `cencovariance.cvchat` can save significant computation time.

Author(s)

Kassel Liam Hingee

References

- Hingee, K.L. (2019) *Spatial Statistics of Random Closed Sets for Earth Observations*. PhD: Perth, Western Australia: University of Western Australia. Submitted.
- Mattfeldt, T. and Stoyan, D. (2000) Improved estimation of the pair correlation function of random sets. *Journal of Microscopy*, 200, 158-173.
- Picka, J.D. (1997) *Variance-Reducing Modifications for Estimators of Dependence in Random Sets*. Ph.D.: Illinois, USA: The University of Chicago.
- Picka, J.D. (2000) Variance reducing modifications for estimators of standardized moments of random sets. *Advances in Applied Probability*, 32, 682-700.

Examples

```
xi <- heather$coarse
obswin <- Frame(xi)
cencovariance(xi, obswin, estimators = "all")
```

contagdiscstate	<i>Disc State Contagion</i>
-----------------	-----------------------------

Description

Calculates the disc-state contagion LPI as described in (Hingee, 2016; Hingee, 2019). The disc-state contagion LPI describes the entropy (mixing) between four possible states of a disc:

1. the disc is completely contained in Ξ
2. the disc does not intersect Ξ
3. the centre of the disc is in Ξ but the disc is not contained in Ξ
4. the disc intersects Ξ but the centre is outside Ξ

Disc-state contagion is a function of the disc radius.

The main difference to classical contagion (O'Neill, 1988) is that disc-state contagion is based on the spherical contact distribution instead of pixel neighbours. One impact of this design is that the distance with which to quantify the mixing between Ξ and the background may be chosen by the user by choosing the disc radius (for classical contagion this distance is fixed by the image resolution).

Usage

```
contagdiscstate(XiH, Xich, p, normalise = FALSE)
```

Arguments

XiH	Conditional spherical contact distribution function for Ξ . Typically this is an fv object but could also be a vector of values. In applications XiH would likely be estimated from a binary map using Hest in spatstat .
Xich	Conditional spherical contact distribution for the complement of Ξ . This is called the Conditional Core Probability in Hingee 2016. Typically this is an fv object but could also be a vector of values. In applications XiH would likely be estimated from an image using Hest in spatstat .
p	The coverage probability of Ξ . In applications to images an estimate of the coverage probability can be obtained using coverageprob .
normalise	Optional. If TRUE contagdiscstate normalises the results so that all RACS return a value between 0 and 1. Default is FALSE.

Details

XiH should be a function of radius that gives (or estimates) the probability of a disc of radius r not intersecting Ξ if the disc's centre is not in Ξ

$$\text{XiH}(r) = P(B_r(x) \subseteq \Xi^c | x \in \Xi^c).$$

Similarly Xich should be an estimate of the probability of a disc being fully contained in Ξ given its centre is in Ξ

$$\text{Xich}(r) \approx P(B_r(x) \subseteq \Xi | x \in \Xi).$$

These can both be obtained using [Hest](#) in **spatstat**. For Xich take care to apply Hest to the complement of Ξ with the observation window W .

If normalise is TRUE then the result is divided by $-2\ln(2)$ and increased by 1 so that contagion will always be between 0 and 1.

Value

If XiH is an fv object then an fv object is returned, otherwise if XiH is a vector then returns a vector the same length as XiH corresponding to the contagion at each r value of XiH.

References

- Hingee, K.L. (2016) Statistics for patch observations. *International Archives of the Photogrammetry, Remote Sensing and Spatial Information Sciences* pp. 235-242. Prague: ISPRS.
- Hingee, K.L. (2019) *Spatial Statistics of Random Closed Sets for Earth Observations*. PhD: Perth, Western Australia: University of Western Australia. Submitted.
- O'Neill, R.V., Krummel, J.R., Gardner, R.H., Sugihara, G., Jackson, B., DeAngelis, D.L., et al. (1988) Indices of landscape pattern. *Landscape Ecology*, 1, 153-162.

Examples

```
xi <- heather$coarse
obswindow <- Frame(heather$coarse)
p <- coverageprob(xi, Frame(xi))
xiH <- Hest(xi, W = obswindow) #Sph. Contact Distrution Estimate
xicH <- Hest(complement.owin(xi), W = obswindow) #Conditional Core Prob. Estimate
# plot(xiH, type = "l", col = "red")
# lines(xicH, type = "l", col = "black")

contagion <- contagdiscstate(xiH, xicH, p)
# plot(contagion)
```

contagpixelgrid	<i>Pixel Adjacency Contagion</i>
-----------------	----------------------------------

Description

Function for calculating the classic pixel-adjacency contagion LPI from a binary map (O'Neill, 1988).

Usage

```
contagpixelgrid(xi, obswin, normalise = FALSE)

adjacency(xi, obswin = NULL)
```

Arguments

xi	An observation of a RACS of interest as a full binary map (in im format) or as the foreground set (in owin format). In the latter case the observation window, obswin, must be supplied. See stationaryracsinference-package for details. If xi is an owin object it must be of mask type.
obswin	If xi is an owin object then obswin is an owin object that specifies the observation window.
normalise	If TRUE will divide result by $2\ln(2)$ and add 1 to make contagion between 0 and 1 for any binary map

Details

The unnormalised contagion LPI of categorical map is defined as

$$\sum_i \sum_j P_{ij} \ln(P_{ij}),$$

where P_{ij} is the probability of randomly selected adjacent pixels being in class i and class j respectively, and m is the number of classes.

Here $m = 2$ as xi is a binary map and we have defined 'adjacent' pixels using the 4-neighbourhood regime.

Contagion is calculated from an adjacency matrix created using `adjacency`.

Functions

- `contagpixelgrid`: Pixel-adjacency contagion LPI of a binary map.
- `adjacency`: Calculates the adjacency matrix used in the pixel contagion

Warning

Will fail if map is either all foreground or all background.

References

O'Neill, R.V., Krummel, J.R., Gardner, R.H., Sugihara, G., Jackson, B., DeAngelis, D.L., et al. (1988) Indices of landscape pattern. *Landscape Ecology*, 1, 153-162.

Examples

```
xi <- heather$coarse
obswin <- owin(xrange = c(0,7),yrange=c(0,16))
adjmat <- adjacency(xi,obswin)
adjmat
contagion <- contagpixelgrid(xi,obswin)
contagion
#Finer resolution
xi <- heather$medium
obswin <- owin(xrange = c(0,7),yrange=c(0,16))
contagion <- contagpixelgrid(xi,obswin)
contagion
```

coverageprob

Estimate the coverage probability of a stationary RACS

Description

Computes the proportion of the observation window that is foreground, which is the usual estimate for the coverage probability of a stationary RACS from a binary map.

Usage

```
coverageprob(xi, obswin = NULL)
```

```
coveragefrac(xi, obswin = NULL)
```

```
cp(xi, obswin = NULL)
```

Arguments

<code>xi</code>	An observation of a RACS of interest as a full binary map (in <code>im</code> format) or as the foreground set (in <code>owin</code> format). In the latter case the observation window, <code>obswin</code> , must be supplied. See stationaryracsinference-package for details.
<code>obswin</code>	The window of observation (not necessarily rectangular) also in <code>owin</code> format.

Details

The coverage probability of a stationary RACS is the probability that an arbitrary point is covered by the RACS. Given a binary map, `xi`, of a realisation of stationary RACS Ξ in a window W , this function computes the fraction of W covered by foreground, which is an estimate of the coverage probability. See [1, section 6.4.2] for more details.

If `xi` is in `im` format then `xi` must be an image of 1s, 0s and NAs representing inside the set, outside the set and outside the observation window respectively. `coverageprob` will not accept a `obswin` argument if `xi` is in `im` format.

Value

An estimate of the coverage probability

Author(s)

Kassel Liam Hingee

References

[1] Chiu, S.N., Stoyan, D., Kendall, W.S. and Mecke, J. (2013) Stochastic Geometry and Its Applications, 3rd ed. Chichester, United Kingdom: John Wiley & Sons.

Examples

```
xi <- heather$coarse
obswindow <- Frame(heather$coarse)
cp <- coverageprob(xi, obswindow)
```

cppicka

Picka's Reduced Window Estimator of Coverage Probability

Description

This function provides estimates of coverage probability from subsets of the observation window, which are a key component of balanced estimators of covariance, centred covariance, pair-correlation and gliding box lacunarity.

Usage

```
cppicka(xi, obswin = NULL, setcov_boundarythresh = NULL)
```

Arguments

<code>xi</code>	An observation of a RACS of interest as a full binary map (in <code>im</code> format) or as the foreground set (in <code>owin</code> format). In the latter case the observation window, <code>obswin</code> , must be supplied. See stationaryracsinference-package for details.
<code>obswin</code>	If <code>xi</code> is an <code>owin</code> object then <code>obswin</code> is an <code>owin</code> object that specifies the observation window.
<code>setcov_boundarythresh</code>	Any vector v such that set covariance of the observation window is smaller than this threshold is given a covariance of NA to avoid instabilities caused by dividing by very small areas,

Details

The plug-in moment covariance estimators uses less of the observation window than the usual coverage probability estimators. Picka (1997, 2000) created new 'balanced' estimators of centred covariance and pair-correlation that accounted for this difference. A key component of Picka's estimators is an estimate of the coverage probability from the subregion of the binary map that is the intersection between W and W shifted by vector v , where W is the observation window (p.~687, Picka, 2000). If we treat X and W as indicator functions representing the foreground and observation window respectively, this coverage probability estimator used by Picka is

$$\frac{\int X(u)W(u)W(u-v)du}{\int W(u)W(u-v)du}.$$

`cppicka` produces these estimates for an array of vectors v using fast Fourier transforms.

Value

An `im` object. Pixel values correspond to estimates of the coverage probability from the subregion of the observation window, W , that is the intersection of W and W shifted by vector v , where v is the pixel location.

Author(s)

Kassel Liam Hingee

References

- Picka, J.D. (1997) *Variance-Reducing Modifications for Estimators of Dependence in Random Sets*. Ph.D.: Illinois, USA: The University of Chicago.
- Picka, J.D. (2000) Variance reducing modifications for estimators of standardized moments of random sets. *Advances in Applied Probability*, 32, 682-700.

Examples

```
xi <- heather$coarse
obswindow <- Frame(heather$coarse)
cp <- coverageprob(xi, obswindow)
cpp1 <- cppicka(xi, obswindow)
```

gbl

*Gliding box lacunarity estimation using all estimators***Description**

Estimates gliding box lacunarity (GBL) using all estimators described in (Hingee et al., 2017) from binary maps for square boxes. It calls the functions [gblc](#), [gblg](#), [gblcc](#) and [gblemp](#).

Usage

```
gbl(xi, boxwidths, estimators = c("GBLg.mattfeldt", "GBLg.pickaint",
  "GBLg.pickaH", "GBLcc.mattfeldt", "GBLcc.pickaint", "GBLc", "GBLemp"),
  obswin = NULL, includenormed = FALSE,
  setcov_boundarythresh = 1e-06)

gbl.cvchat(boxwidths, estimators = c("GBLg.mattfeldt", "GBLg.pickaint",
  "GBLg.pickaH", "GBLcc.mattfeldt", "GBLcc.pickaint", "GBLc"),
  phat = NULL, cvchat = NULL, cpp1 = NULL)
```

Arguments

xi	An observation of a RACS of interest as a full binary map (in im format) or as the foreground set (in owin format). In the latter case the observation window, obswin, must be supplied. See stationaryracsinference-package for details.
boxwidths	A list of box widths
estimators	A list of estimator names - see details for possibilities. estimators = "all" will select all estimators.
obswin	If xi is an owin object then obswin is an owin object that specifies the observation window.
includenormed	A logical value. If TRUE then GBL estimates normalised by the GBL values at zero will be included in a returned list of fv objects
setcov_boundarythresh	Any vector v such that set covariance of the observation window is smaller than this threshold is given a covariance estimate (and other similar estimate) of NA to avoid instabilities caused by dividing by very small areas. If NULL is supplied (default) then 1E-6 is used.
phat	The fraction foreground area in the observation window, which is the usual estimator of coverage probability.
cvchat	The plug-in moment covariance estimate (often from plugincvc).
cpp1	Picka's estimate of coverage probability for subsets of the observation window. See cppicka .

Details

As empirical GBL is one of the GBL estimators available through this function, non-square boxes are not allowed. To estimate GBL for non-square boxes use `gblcc` or `gblg` directly.

If `xi` is in `owin` format then `obswin` and `xi` are converted into a binary map in `im` format using `as.im`

The estimators available are

- "GBLc" The unmodified (unbalanced) covariance estimator provided by `gblc`
- "GBLemp" Empirical gliding box lacunarity (Allain and Cloitre, 1991). Calls `gblemp`
- "GBLg.mattfeldt" See help for `gblg`
- "GBLg.pickaint" See help for `gblg`
- "GBLg.pickaH" See help for `gblg`
- "GBLcc.mattfeldt" See help for `gblcc`
- "GBLcc.pickaint" See help for `gblcc`
- "GBLcc.pickaH" See help for `gblcc`

Value

An `fv` object.

Functions

- `gbl`: Computes GBL estimates from a binary map.
- `gbl.cvchat`: Computes covariance-based estimator of GBL from the plug-in moment estimate of covariance, Picka's reduced window coverage probability estimates (see `cppicka`) and the usual coverage probability estimate, `phat`.

References

Allain, C. and Cloitre, M. (1991) Characterizing the lacunarity of random and deterministic fractal sets. *Physical Review A*, 44, 3552-3558.

Hingee K, Baddeley A, Caccetta P, Nair G (2017). Computation of lacunarity from covariance of spatial binary maps. *Journal of Agricultural, Biological and Environmental Statistics*. Submitted.

Examples

```
xi <- heather$coarse
xi <- as.im(xi, value = TRUE, na.replace = FALSE)
if (interactive()) {
  boxwidths <- seq(1, 10, by = 0.5)
} else {
  boxwidths <- seq(1, 10, by = 1)
}
gblests <- gbl(xi, boxwidths)
```

gblc	<i>Gliding box lacunarity estimator using plug-in moment covariance estimator</i>
------	-----------------------------------------------------------------------------------

Description

Can be used to estimate the gliding box lacunarity (GBL) of a stationary RACS from a binary map using the plug-in moment covariance estimator (Hingee et al., 2017). It can also calculate the GBL of a RACS from a given covariance function and coverage probability.

Usage

```
gblc(boxes, covariance = NULL, p = NULL, xiim = NULL)
```

Arguments

boxes	Either a list of sidelengths for square boxes or a list of <code>owin</code> objects of any shape.
covariance	A <code>im</code> object containing the covariance function
p	The coverage probability. Typically estimated by the fraction of the observation window covered by the set of interest.
xiim	An observation of a stationary RACS in <code>im</code> format. <code>xiim</code> must have values of either 1, 0 or NA; 1 denotes inside the RACS, 0 denotes outside, and NA denotes unobserved.

Details

Computes a numerical approximation of

$$\int \gamma_B(v)C(v)dv/(p^2|B|^2).$$

where B is a given set (often called a box), γ_B is the set covariance of B , $|B|$ is the area of B , p is the coverage probability of a stationary RACS, and $C(v)$ is the covariance of a stationary RACS. This can be used to compute the GBL from model parameters by passing `gblc` the covariance and coverage probability of the model.

If a binary map is supplied then p and $C(v)$ are estimated using the usual coverage probability estimator and the plug-in moment covariance estimator, respectively (see [coverageprob](#) and [plugincvc](#)).

Value

If `boxes` is a list of numerical values then GBL is estimated for square boxes with side length given by `boxes`. The returned object is then an `fv` object containing estimates of GBL, box mass variance and box mass mean. If `boxes` is a list of `owin` objects then `gblc` returns a dataframe of with columns corresponding to estimates of GBL, box mass variance and box mass mean.

Note if NA or NaN values in the covariance object are used then `gblc` will return NA or NaN.

References

Hingee K, Baddeley A, Caccetta P, Nair G (2017). Computation of lacunarity from covariance of spatial binary maps. *Journal of Agricultural, Biological and Environmental Statistics*. Submitted.

Examples

```
xi <- heather$coarse
covar <- plugincvc(xi, Frame(xi))
p <- area(xi) / area(Frame(xi))
if(interactive()){
  sidelengths <- seq(0.3, 14, by = 0.2)
} else {
  sidelengths <- seq(0.3, 14, by = 1)
}
gblest <- gblc(sidelengths, covar, p)
# plot(gblest)
# what is the GBL estimates for boxes that are discs?
discboxes <- lapply(sidelengths / 2, disc)
discgbls <- gblc(discboxes, covar, p)
# points(sidelengths, discgbls$GBL)
```

gblcc

Centred covariance based estimates of gliding box lacunarity

Description

Estimates the gliding box lacunarity (GBL) of a stationary RACS using centred covariance estimates (Hingee et al., 2017). The centred covariance and coverage probability can be provided or estimated from binary map.

Usage

```
gblcc(boxes, cencovar = NULL, p = NULL, xiim = NULL,
      estimator = "pickaH")
```

Arguments

boxes	Either a list of sidelengths for square boxes or a list of <code>owin</code> objects of any shape.
cencovar	A <code>im</code> object containing the centred covariance function
p	The coverage probability. Typically estimated by the fraction of the observation window covered by the set of interest.
xiim	An observation of a stationary RACS in <code>im</code> format. <code>xiim</code> must have values of either 1, 0 or NA; 1 denotes inside the RACS, 0 denotes outside, and NA denotes unobserved.
estimator	If an observation <code>xiim</code> is passed then <code>estimator</code> will select the balancing method that <code>ccvc</code> uses to estimate the centred covariance.

Details

If we denoted the estimated centred covariance by $\hat{\kappa}(v)$ and coverage probability \hat{p} then the estimate of GBL is

$$1 + \frac{1}{\hat{p}^2 |B|^2} \int \gamma_B(v) \hat{\kappa}(v) dv$$

Value

If boxes is a list of numerical values then GBL is estimated for square boxes with side length given by boxes. The returned object is then an fv object containing estimates of GBL, box mass variance and box mass mean.

If boxes is a list of owin objects then gblcc returns a dataframe of with columns corresponding to estimates of GBL, box mass variance and box mass mean. Note if NA or NaN values in the covariance object are used then gblc will return NA or NaN instead of an GBL value.

References

Hingee K, Baddeley A, Caccetta P, Nair G (2017). Computation of lacunarity from covariance of spatial binary maps. *Journal of Agricultural, Biological and Environmental Statistics*. Submitted.

Examples

```
xi <- heather$coarse
cencovar <- cencovariance(xi, obswin = Frame(xi), estimators = c("pickaH"), drop = TRUE)
p <- area(xi) / area(Frame(xi))
if (interactive()) {
  sidelengths <- seq(0.3, 14, by = 0.2)
} else {
  sidelengths <- seq(0.3, 14, by = 1)
}
gblceest <- gblcc(sidelengths, cencovar, p)
# what is the GBL estimates for boxes that are discs?
discboxes <- lapply(sidelengths / 2, disc)
discgbls <- gblcc(discboxes, cencovar, p)
# points(sidelengths, discgbls)

#direct to an image
xiim <- as.im(xi, na.replace = 0)
gblceest <- gblcc(sidelengths, xiim = xiim, estimator = "pickaH")
```

Description

Calculates empirical gliding box lacunarity of a binary map, which was proposed by Allain and Cloitre (1991).

Usage

```
gblemp(boxwidths, xiim, obswin = Frame(xiim))

gbltrad(boxwidths, xiim, obswin = Frame(xiim))
```

Arguments

boxwidths	A list of suggested box widths in the same units as xiim. Note the actual box widths used by gblemp will be the closest multiple of an odd number of pixel widths.
xiim	An image of pixels valued either 0, 1 or NA. NA valued pixels are assumed to be outside the observation window.
obswin	Optional observation window. The observation window used for the estimator will be the intersection of obswin and the pixels that are not NA in xiim.

Details

Calculates empirical gliding box lacunarity (Allain and Cloitre, 1991) for a given range of square box sizes,

$$1 + \text{Var}(\text{area}(B.xi)) / E[\text{area}(B.xi)]^2,$$

where B is a box that has a random location in the observation window and $\text{area}(B.xi)$ is the (random) area of the foreground in B . This is an estimate of the gliding box lacunarity of a RACS (Hingee et al., 2017).

The algorithm uses the pixel locations in xiim as an array of box centre locations to compute the mean and variance of the area in a random box of a given size. Locations where the box is not completely within the observation window are ignored.

Value

An fv object containing empirical GBL, variance of the area in the box and mean of the area in the box. The box widths (labelled s) are always odd multiples of the pixel width.

Functions

- gbltrad: An alias of gblemp used in past versions of this package. This alias may be removed in future versions.

WARNING

gblemp uses the [roll_sum](#) function in **RcppRoll** to operate. **RcppRoll** must be installed.

Note: The side lengths are rounded such that they are an odd number of pixels across.

References

Allain, C. and Cloitre, M. (1991) Characterizing the lacunarity of random and deterministic fractal sets. *Physical Review A*, 44, 3552-3558.

Hingee K, Baddeley A, Caccetta P, Nair G (2017). Computation of lacunarity from covariance of spatial binary maps. *Journal of Agricultural, Biological and Environmental Statistics*. Submitted.

Examples

```
xiim <- as.im(heather$coarse, na.replace = 0)
boxwidths <- seq(0.2, 14, by = 0.2) #in units of xiim
gblest <- gblemp(boxwidths, xiim)
```

gblg

*Pair-correlation based estimates of gliding box lacunarity***Description**

Estimates the gliding box lacunarity (GBL) of a stationary RACS by estimating pair-correlation from a binary map (Hingee et al., 2017). It can also calculate the GBL of a RACS from a provided pair-correlation function.

Usage

```
gblg(boxes, paircorr = NULL, xiim = NULL)
```

Arguments

boxes	Either a list of sidelengths for square boxes or a list of <code>owin</code> objects of any shape.
paircorr	A <code>im</code> object containing the pair-correlation function
xiim	An observation of a stationary RACS in <code>im</code> format. <code>xiim</code> must have values of either 1, 0 or NA; 1 denotes inside the RACS, 0 denotes outside, and NA denotes unobserved.

Details

If we denoted the estimated pair-correlation by $\hat{g}(v)$ then the estimate of GBL is

$$\frac{1}{|B|^2} \int \gamma_B(v) \hat{g}(v) dv.$$

Value

If `boxes` is a list of numerical values then GBL is estimated for square boxes with side length given by `boxes`. The returned object is then an `fv` object containing estimates of GBL. If `boxes` is a list of `owin` objects then `gblg` returns a dataframe of with columns corresponding to estimates of GBL.

Note if NA or NaN values in the `paircorr` object are used then `gblg` will return NA or NaN instead of an GBL value.

References

Hingee K, Baddeley A, Caccetta P, Nair G (2017). Computation of lacunarity from covariance of spatial binary maps. *Journal of Agricultural, Biological and Environmental Statistics*. Submitted.

Examples

```
xi <- heather$coarse
pcln <- paircorr(as.im(xi, na.replace = 0), estimators = "pickaH", drop = TRUE)
if (interactive()) {
  sidelengths <- seq(0.3, 14, by = 0.2)
} else {
  sidelengths <- seq(0.3, 14, by = 1)
}
gblgest <- gblg(sidelengths, pcln)
# what is the GBL estimates for boxes that are discs?
discboxes <- lapply(sidelengths / 2, disc)
discgbls <- gblg(discboxes, pcln)
# points(sidelengths, discgbls)
```

innerprod.im

Inner Product of Two Functions Represented as Images

Description

Given two functions, f and g , that map from 2D space to 1D, and values of f and g represented as `im` objects then `innerprod.im` computes the (function space) inner product

$$\int f(v)g(v)dv.$$

Usage

```
innerprod.im(A, B, outsideA = NA, outsideB = NA, na.rm = FALSE)
```

Arguments

<code>A</code>	An <code>im</code> object containing function values representing function f .
<code>B</code>	An <code>im</code> object containing function values representing function g .
<code>outsideA</code>	The value of f outside the domain of A . Typically will be 0 or NA. Default is NA.
<code>outsideB</code>	The value of g outside the domain of B . Typically will be 0 or NA. Default is NA.
<code>na.rm</code>	Logical. If TRUE NA values are skipped in the summation of the product of the images.

Details

Harmonises the two input images, multiplies them together and returns the integral of the resulting image. `outsideA` and `outsideB` are used to determine result if the inner product requires values outside the domain of A or B . For example if `outsideA=0` and the domain of B is larger than A 's domain then the inner product can still be computed. However if A is NA outside (e.g. not known/not provided) and the domain of B is larger than A 's domain then the inner product can not be computed and the returned value is NA

Value

If the inner product can be computed then returns `sum(A * B)`, otherwise returns NA.

Examples

```
xi <- heather$coarse
covar <- pluginvc(xi, Frame(xi))
B <- setcov(square(1))
innerprod.im(covar, B, outsideB = 0)
```

isbinarymap

Test if an im object is a binary map

Description

Tests whether `xi` is a binary map. The pixel values must be of logical type (TRUE, FALSE and NA only), or numerical with values of 1, 0 and NA.

Usage

```
isbinarymap(xi, requiretrue = FALSE)
```

Arguments

`xi` an image object

`requiretrue` Logical. If TRUE then isbinarymap will error if `xi` is NOT a binary map.

Value

Logical value. TRUE if `xi` is a binary map. Otherwise FALSE. If `requiretrue = TRUE` and `xi` is not a binary map then an error will occur.

Examples

```
#The following returns TRUE
isbinarymap(as.im(heather$coarse, na.value = 0))
isbinarymap(as.im(heather$coarse, na.value = FALSE, value = TRUE))
#
#the following returns FALSE
isbinarymap(as.im(heather$coarse, na.value = 0.2, value = 1))
isbinarymap(as.im(heather$coarse, na.value = 0, value = 1.5))
```

paircorr	<i>Balanced estimation of pair-correlation.</i>
----------	-------------------------------------------------

Description

Estimates the pair-correlation function of a stationary RACS. The plug-in moment pair-correlation estimator and three ‘balanced’ estimators suggested by Picka (2000) are available.

Usage

```
paircorr(xi, obswin = NULL, setcov_boundarythresh = NULL,
         estimators = "all", drop = FALSE)

paircorr.cvchat(cvchat, cpp1 = NULL, phat = NULL, estimators = "all",
               drop = FALSE)
```

Arguments

xi	An observation of a RACS of interest as a full binary map (in <code>im</code> format) or as the foreground set (in <code>owin</code> format). In the latter case the observation window, <code>obswin</code> , must be supplied. See stationaryracsinference-package for details.
obswin	If <code>xi</code> is an <code>owin</code> object then <code>obswin</code> is an <code>owin</code> object that specifies the observation window.
setcov_boundarythresh	Any vector v such that set covariance of the observation window is smaller than this threshold is given a covariance of NA to avoid instabilities caused by dividing by very small areas,
estimators	A list of strings specifying estimators to use. See details. <code>estimators = "all"</code> will select all available estimators.
drop	If TRUE and one estimator selected then the returned value will be a single <code>im</code> object and not a list of <code>im</code> object. <code>estimators = "all"</code> will select all inbuilt estimators. See details.
cvchat	The plug-in moment estimate of covariance in <code>im</code> format. Typically created with plugincvc .
cpp1	Picka’s reduced window estimate of coverage probability in <code>im</code> format - used in improved (balanced) covariance estimators. Can be generated using cppicka .
phat	The plug-in moment estimate of coverage probability, which is the observed foreground area in <code>xi</code> divided by the total area of the observation window. See coverageprob for more information.

Details

The pair-correlation of a stationary RACS is

$$g(v) = C(v)/p^2.$$

The estimators available are (see (Hingee, 2019) for more information):

- `plugin` the plug-in moment pair-correlation estimator which is $\hat{C}hat(v)/(\hat{p}hat^2)$, where $\hat{C}hat$ and $\hat{p}hat$ are the plug-in moment estimate of covariance and the usual estimate of coverage probability, respectively.
- `mattfeldt` an ‘intrinsically’ balanced pair-correlation estimator suggested by Picka (1997). A similar isotropic pair-correlation estimator was later studied by Mattfeldt and Stoyan (2000).
- `pickaint` Picka’s ‘intrinsically’ balanced pair-correlation estimator (Picka, 2000).
- `pickaH` Picka’s ‘additively’ balanced pair-correlation estimator (Picka, 2000).

Value

If `drop = TRUE` and a single estimator requested then a `im` object containing the pair-correlation estimate. Otherwise a named `imlist` of `im` objects containing the pair-correlation estimates for each requested estimator.

Functions

- `paircorr`: Estimates pair-correlation from a binary map.
- `paircorr.cvchat`: Generates pair-correlation estimates from the plug-in moment estimates of covariance, Picka’s reduced window estimate of coverage probability, and the coverage fraction (which is an unbiased estimate of the coverage probability). If these estimates already exist then `paircorr.cvchat` can save significant computation time.

Author(s)

Kassel Liam Hingee

References

- Hingee, K.L. (2019) *Spatial Statistics of Random Closed Sets for Earth Observations*. PhD: Perth, Western Australia: University of Western Australia. Submitted.
- Mattfeldt, T. and Stoyan, D. (2000) Improved estimation of the pair correlation function of random sets. *Journal of Microscopy*, 200, 158-173.
- Picka, J.D. (1997) *Variance-Reducing Modifications for Estimators of Dependence in Random Sets*. Ph.D.: Illinois, USA: The University of Chicago.
- Picka, J.D. (2000) Variance reducing modifications for estimators of standardized moments of random sets. *Advances in Applied Probability*, 32, 682-700.

Examples

```
xi <- heather$coarse
#estimate directly from a binary map
pclns_direst <- paircorr(as.im(xi, na.replace = 0), estimators = "all")

#estimate using plug-in moment covariance estimates, coverage
#probability estimate and Picka's reduced window coverage probability
#estimates.
obswin <- Frame(xi)
phat <- coverageprob(xi, obswin = Frame(xi))
cvchat <- pluginvcv(xi, obswin)
cpp1 <- cppicka(xi, obswin = Frame(heather$coarse))
pclns_frcvc <- paircorr.cvchat(cvchat, cpp1, phat, estimators = "all")
```

placegrainsfromlib	<i>Place grains randomly on a point pattern</i>
--------------------	-------------------------------------------------

Description

Places subsets (grains) of two dimension space randomly on a given point pattern. This is useful for simulating germ-grain models such as Boolean models. Also described here a functions for computing summary properties of the a list of grains.

Usage

```
placegrainsfromlib(pp, grainlib, replace = TRUE, prob = NULL,
  w = NULL, xy = NULL)

meanarea.grainlib(grainlib, weights = rep(1/length(grainlib),
  length(grainlib)))

meansetcov.grainlib(grainlib, weights = rep(1/length(grainlib),
  length(grainlib)), xy)

covar.grainlib(lambda, grainlib, weights, xy)
```

Arguments

pp	A point pattern (in ppp format).
grainlib	A list of grains as owin objects in a solist .
replace	passed directly to sample . When TRUE grains are chosen from library with replacement.
prob	A list of probability weights for each grain in the library. Passed directly to sample . If NULL the grains are selected with equal probability.
w	Optional desired observation window. If this is non-null then any grains with Frame outside the Frame of w will be ignored. This reduces polygonal intersection calculations for very large buffer distances

xy	An im or binary mask object that is used to specify the pixel array of objects.
weights	Probability of selecting each grain in the library
lambda	Intensity of germs of a Boolean model - for computing the covariance of a Boolean model that has grain distribution given by grainlib and weights.

Details

Germ-grain models have two components, a point process (called germs) and a process that creates grains that are centred on the germs. The point process of germs can be easily simulated using a number of **spatstat** functions (e.g. `rpoispp` for Boolean models). To simulate a germ-grain model in a window W the germ process must be simulated in a larger window because grains centred outside W can intersect W . The result must then be cropped to W to achieve a realisation of the germ-grain process within W .

`placegrainsfromlib` randomly samples from a library of grains (`grainlib`) and places these on the points in `pp`. Sampling of the grain is independent of the location of the point in `pp`. It can be used to simulate the grain process in some germ-grain models.

Value

Returns an `owin` object.

Functions

- `placegrainsfromlib`: Place grains randomly from a list of grains.
- `meanarea.grainlib`: Compute mean area of a random grain given by the library
- `meansetcov.grainlib`: Computes the mean of the set covariance of the grains in `grainlib`. `xy` is required because the set covariance function must rasterise the `owin` objects.
- `covar.grainlib`: Compute the covariance of a Boolean model with random grain given by the library

Author(s)

Kassel Liam Hingee

Examples

```
#Generate a germ-grain models where germs are a Poisson point process
# and grains are 2 or 3 different disc sizes.
grainlib <- solist(disc(radius = 1), disc(radius = 1.9), disc(radius = 0.2))
bufferdist <- 2 #chosen to be larger than the largest radius in library

w <- owin(xrange = c(0, 10), yrange = c(0, 10))

#simulate the germ process in an enlarged window
pp <- rpoispp(lambda = 0.1, win = dilation(w, bufferdist), nsim = 1, drop = TRUE)

# plot(w)
xibuffer <- placegrainsfromlib(pp, grainlib)
# plot(xibuffer, add = TRUE, lty = "dashed")
```



```

# get final simulation by intersection with desired window
xi <- intersect.owin(xibuffer, w)
# plot(xi, hatch = TRUE, add = TRUE)

# demonstration that involves rasterisation.
xibuffer <- placegrainsfromlib(pp, grainlib, xy = as.mask(w, eps = 0.1))
# plot(xibuffer)
# plot(w, add = TRUE)

# Demo of covariance and set covariance computations: test on Boolean model
lambda <- 0.1
discr <- 10
weights <- c(0.9999, 0.0001)
grainlib <- solist(disc(r = discr), disc(r = 2*discr))
meanarea.grainlib(grainlib, weights)
# plot(meansetcov.grainlib(grainlib, weights, xy = as.mask(w, eps = 0.1)))
truecovartest <- covar.grainlib(lambda, grainlib, weights, xy = as.mask(w, eps = 0.1))
truecovariance <- bddcovar(
  c(-10, 10), c(-10, 10), c(0.1, 0.1), lambda, discr)
# plot(solist(truecovartest, truecovariance), clipwin = disc(r = 3))
# plot(truecovartest - truecovariance, clipwin = disc(r = 3))
range(truecovartest - truecovariance)

```

plugincvc

Plug-in moment covariance estimator

Description

This function computes the plug-in moment covariance estimate of a stationary RACS from a binary map. For a stationary RACS, Ξ , the covariance for a vector v is the probability of two points separated by a vector v are covered by Ξ

$$C(v) = P(\{x, x + v\} \subseteq \Xi).$$

Usage

```
plugincvc(xi, obswin = NULL, setcov_boundarythresh = NULL)
```

Arguments

xi	An observation of a RACS of interest as a full binary map (in <code>im</code> format) or as the foreground set (in <code>owin</code> format). In the latter case the observation window, <code>obswin</code> , must be supplied. See stationaryracsinference-package for details.
obswin	If <code>xi</code> is an <code>owin</code> object then <code>obswin</code> is an <code>owin</code> object that specifies the observation window.
setcov_boundarythresh	Any vector v such that set covariance of the observation window is smaller than this threshold is given a covariance of NA to avoid instabilities caused by dividing by very small areas,

Details

The plug-in moment covariance estimator is (Serra, 1982)

$$\hat{C}(v) = \frac{\gamma_{W \cap X}(v)}{\gamma_W(v)}$$

where $\gamma_W(v)$ is the set covariance of the observation window W and $\gamma_{W \cap X}(v)$ is the set covariance of the foreground within W . `plugincvc` uses Fourier transforms to calculate the set covariance (using the `setcov` of the foreground and observation window. Vectors with small $\gamma_W(v)$ are eliminated using `setcov_boundarythresh` as division by small values is numerically unstable.

Value

A **SpatStat** `im` object containing the estimated covariance.

Author(s)

Kassel Liam Hingee

References

Serra, J.P. (1982) *Image Analysis and Mathematical Morphology*. London; New York: Academic Press.

Examples

```
xi <- heather$coarse
covar <- plugincvc(xi, Frame(xi))
covar <- plugincvc(as.im(heather$coarse, na.replace = 0))
```

racscovariance

Covariance Estimation

Description

Estimates the covariance of a stationary RACS. The plug-in moment covariance estimator and newer balanced estimators based on (Picka, 1997; Picka, 2000) are available.

Usage

```
racscovariance(xi, obswin = NULL, setcov_boundarythresh = NULL,
  estimators = "all", drop = FALSE)

racscovariance.cvchat(cvchat, cpp1 = NULL, phat = NULL,
  estimators = "all", drop = FALSE)
```

Arguments

<code>xi</code>	A binary map. Either an <code>im</code> object or a <code>owin</code> object. If an <code>im</code> object then pixel values of 1 or <code>TRUE</code> represent foreground, 0 or <code>FALSE</code> values represent background, and <code>NA</code> values represent outside the observation window. If an <code>owin</code> object then <code>xi</code> represents foreground and <code>obswin</code> is required to specify the observation window.
<code>obswin</code>	The observation window in <code>owin</code> format if <code>xi</code> is also in <code>owin</code> format.
<code>setcov_boundarythresh</code>	Any vector v such that set covariance of the observation window is smaller than this threshold is given a covariance of <code>NA</code> to avoid instabilities caused by dividing by very small areas,
<code>estimators</code>	A list of strings specifying covariance estimators to use. See details. Passing <code>estimators = "all"</code> will select all available estimators.
<code>drop</code>	If <code>TRUE</code> and one estimator is selected then the returned value will be a single <code>im</code> object and not a list of <code>im</code> object.
<code>cvchat</code>	The plug-in moment estimate of covariance in <code>im</code> format. Typically created with pluginvc .
<code>cpp1</code>	Picka's reduced window estimate of coverage probability in <code>im</code> format - used in improved (balanced) covariance estimators. Can be generated using cppicka .
<code>phat</code>	The classical estimate of coverage probability, which is the observed area in <code>xi</code> divided by the total area of the observation window. See coverageprob for more information.

Details

The covariance of a RACS is also known as the two-point coverage probability, and is closely related to the semivariogram. The covariance of a stationary RACS Ξ given a vector v is the probability that two points separated by a vector v are covered by Ξ .

Given a vector v , the plug-in moment covariance estimate from a binary map is the volume of the set of points, x , such that both x and $x + v$ are observed to be in the foreground relative to the volume of points, x , for which both x and $x + v$ are in the observation window (Hingee, 2019). Picka (1997, 2000) suggested a number of improvements to centred covariance estimation (see [cencovariance](#)) that 'balanced' the data used to estimate covariance with the data used to estimate coverage probability. These lead to covariance estimators that give estimates for the covariance of Xi that are a constant offset from covariance estimates for the complement of Xi (note the constant offset depends on the coverage probability), which appears to avoid some surprising behaviour that the plug-in moment covariance estimator suffers (Hingee, 2019). These estimators are called `pickaint` and `pickaH` in this package.

Another improved estimator, inspired by an 'intrinsic modification' briefly mentioned by Picka (1997) for pair-correlation estimators, is also available. We have called this estimator `mattfeldt` as a similar isotropic estimator for pair-correlation was studied by Mattfeldt and Stoyan (2000).

The estimators available are (see (Hingee, 2019) for information):

- `plugin` the plug-in moment covariance estimator
- `mattfeldt` an estimator inspired by an 'intrinsically' balanced pair-correlation estimator from Picka that was later studied in an isotropic situation by Mattfeldt and Stoyan (2000)

- pickaint an estimator inspired by an ‘intrinsically’ balanced centred covariance estimator from Picka (2000).
- pickaH an estimator inspired by the ‘additively’ balanced centred covariance estimator from Picka (2000).

Value

If drop = TRUE and only one estimator is requested then an im object containing the covariance estimate. Otherwise a named imlist of covariance estimates corresponding to each requested estimator.

Functions

- racscovariance: Estimates covariance from a binary map.
- racscovariance.cvchat: Computes covariance estimates from a plug-in moment estimate of covariance, Picka’s reduced window estimate of coverage probability, and the usual estimate of coverage probability. If these estimates already exist then racscovariance.cvchat can save significant computation time.

Author(s)

Kassel Liam Hingee

References

- Hingee, K.L. (2019) *Spatial Statistics of Random Closed Sets for Earth Observations*. PhD: Perth, Western Australia: University of Western Australia. Submitted.
- Mattfeldt, T. and Stoyan, D. (2000) Improved estimation of the pair correlation function of random sets. *Journal of Microscopy*, 200, 158-173.
- Picka, J.D. (1997) *Variance-Reducing Modifications for Estimators of Dependence in Random Sets*. Ph.D.: Illinois, USA: The University of Chicago.
- Picka, J.D. (2000) Variance reducing modifications for estimators of standardized moments of random sets. *Advances in Applied Probability*, 32, 682-700.

Examples

```
#direct from a binary map
xi <- heather$coarse
obswin <- Frame(xi)
balancedcvchats <- racscovariance(xi, obswin = obswin, estimators = "all")

# from a coverage probability estimate and a plug-in moment covariance estimate.
phat <- coverageprob(xi, obswin = obswin)
cvchat <- pluginvcv(xi, obswin)
cpp1 <- cppicka(xi, obswin = Frame(heather$coarse))
harmonised <- harmonise.im(cvchat = cvchat, cpp1 = cpp1)
cvchat <- harmonised$cvchat
cpp1 <- harmonised$cpp1
```

```
balancedcvchats <- racscovariance.cvchat(cvchat,
                                          cpp1, phat, estimators = "pickaH", drop = TRUE)
```

rbd

Simulation of Boolean Model of Deterministic Discs

Description

Functions for simulating a Boolean model with grains that are discs of fixed constant radius (the abbreviation ‘bdd’ is short for Boolean model with Deterministic Discs). A Boolean model is a two stage model, first the locations (called germs) of grains are randomly distributed according to a Poisson point process, then a random grain is placed on each germ independently. Introduction to Boolean models are available in many stochastic geometry books (Chiu et al., 2013). Also described here are functions for calculating the coverage probability, germ intensity, and covariance of a Boolean model with deterministic discs from model parameters.

Usage

```
rbd(lambda, discr, window, seed = NULL)

bddcoverageprob(lambda, discr)

bddlambda(coverp, discr)

bdddiscr(coverp, lambda)

bddcovar.iso(r, lambda, discr)

bddcovar(xrange, yrange, eps, lambda, discr)
```

Arguments

lambda	Intensity of the germ process (which is a Poisson point process)
discr	Radius of the discs
window	The window to simulate in (an owin object)
seed	Optional input (default in NULL). Is an integer passed to set.seed . Used to reproduce patterns exactly.
coverp	Coverage probability of the Boolean model
r	is the radius to calculate covariance
xrange	range of x values for bddcovar
yrange	range of y values for bddcovar
eps	list of length 2 of the steps between samples points in x and y respectively for bddcovar. If eps is of length 1 then the steps between sample points in the x and y directions will both be equal to eps.

Value

See Functions section.

Functions

- `rbdd`: Returns an `owin` that is a set generated by simulating a Boolean model with specified intensity and disc radius. The window information is not contained in this object. If the simulated set is empty then an empty `owin` object is returned. The point process of germs is generated using `spatstat`'s `rpoispp`.
- `bddcoverageprob`: Returns the true coverage probability given the intensity and disc radius.
- `bddlambda`: Returns the germ intensity given coverage probability and disc radius.
- `bdddiscr`: Returns the disc radius given coverage probability and germ intensity.
- `bddcovar.iso`: Returns the true covariance of points separated by a distance `r` given the intensity, `lambda` and disc radius `discr` of the model.
- `bddcovar`: Returns an image of the covariance as calculated from disc radius and intensity.

WARNING

The returned object of `rbdd` is only the contents of `Xi` and thus could be much smaller than the window (e.g. when the simulated set is empty).

References

Chiu, S.N., Stoyan, D., Kendall, W.S. and Mecke, J. (2013) *Stochastic Geometry and Its Applications*, 3rd ed. Chichester, United Kingdom: John Wiley & Sons.

Examples

```
#Boolean model with discs of radius 10.
#The intensity has been chosen such that the true coverage probability is very close to 0.5.
discr <- 10
w <- owin(xrange = c(0, 100), c(0, 100))
lambda <- 2.2064E-3
xi <- rbdd(lambda, discr, w)
# plot(xi)
# plot(w, add = TRUE)

#calculate theoretical values of the model
cp <- bddcoverageprob(lambda, discr)
cvc <- bddcovar(
  c(-10, 10), c(-10, 10), c(0.2, 0.2), lambda, discr)
```

rbdr

*Simulation of Boolean Model of Deterministic Rectangles***Description**

Functions for simulating a Boolean model with grains that are deterministic rectangles. A Boolean model is a two stage model, first the locations (called germs) of grains are randomly distributed according to a Poisson point process, then a random grain is placed on each germ independently. An introduction can be found in (Chiu et al., 2013). Also described in this help file are functions for calculating the coverage probability and covariance.

Usage

```
rbdr(lambda, grain, win, seed = NULL)
```

```
bdrcoverageprob(lambda, grain)
```

```
bdrcovar(lambda, grain, xy)
```

Arguments

lambda	Intensity of the germ process (which is a Poisson point process)
grain	Rectangle object specifying the grain
win	The window to simulate in (an owin object)
seed	Optional input (default in NULL). Is an integer passed to set.seed . Used to reproduce patterns exactly.
xy	A raster object that specifies the pixel coordinates of the desired covariance image. In the same vein and as.mask in spatstat.

Value

Depends on the function used (see Functions section).

Functions

- `rbdr`: Returns an `owin` that is a set generated by simulating a Boolean model with a specified intensity and fixed rectangular grain. The window information is not contained in this object. If the simulated set is empty then an empty `owin` object is returned. The point process of germs is generated using spatstat's [rpoispp](#).
- `bdrcoverageprob`: Returns the true coverage probability given the intensity and grain.
- `bdrcovar`: Returns an image of the covariance as calculated from disc radius and intensity.

WARNING

The returned object of `rbdr` is only the contents of `Xi` and thus could be much smaller than the window (e.g. when the simulated set is empty).

References

Chiu, S.N., Stoyan, D., Kendall, W.S. and Mecke, J. (2013) *Stochastic Geometry and Its Applications*, 3rd ed. Chichester, United Kingdom: John Wiley & Sons.

Examples

```
grain <- owin(xrange = c(-5, 5), yrange = c(-5, 5))
win <- owin(xrange = c(0, 100), c(0, 100))
lambda <- 4.2064E-3
xi <- rbdr(lambda, grain, win)
# plot(xi, col = "black")
# plot(win, add = TRUE)

#calculate theoretical values of the model
cp <- bdrcoverageprob(lambda, grain)
xy <- as.mask(dilationAny(win, win), eps = c(1, 1))
cvc <- bdrcovar(lambda, grain, xy)
```

rblnd

Simulate a Boolean model of discs with log normal disc radii

Description

Simulates a Boolean model of discs with log normal radii by first simulating a Poisson point process and then placing discs of random radii around each point (the radii are generated using a log normal distribution).

Usage

```
rblnd(obswin, bufferdist, lambda, meanlog, sdlog, seed = NULL)
```

Arguments

obswin	An owin object specifying the desired simulation region
bufferdist	A distance to expand obswin so that discs with centres near obswin are also simulated.
lambda	Intensity of the Poisson point process, passed to rpoispp . It could be either a single positive number, or any other object that rpoispp can understand.
meanlog	For the distribution of radii. The logarithm of the distribution is set to have mean meanlog.
sdlog	For the distribution of radii. The logarithm of the distribution is set to have standard deviation sdlog
seed	Optional input (default is NULL). Is an integer passed to set.seed . Used to reproduce patterns exactly.

Details

The point process needs to be simulated in a larger region than the desired observation window to account for the possibility of discs that intersect the observation window, but have germs outside the observation window.

The point process of germs is generated using spatstat's [rpoispp](#).

Value

Returns an owin object cropped to obswin.

Warning

A good choice of `bufferdist` is required and will be sensitive to the distribution of radii.

Examples

```
w <- owin(xrange = c(0, 10), yrange = c(0, 10))
xi <- rblnd(w, 2, 0.6, -1, 0.5)

# plot(w)
# plot(xi, add = TRUE)

#or with seed set
w <- owin(xrange = c(0, 10), yrange = c(0, 10))
xi <- rblnd(w, 2, 1, -1, 0.5, seed = 36)

# plot(w)
# plot(xi, add = TRUE)
```

rbpto

*Simulate Boolean Model with Grains Scaled According to a truncated
Pareto Distribution*

Description

Functions for simulation and computing theoretical values of a Boolean model with identically shaped grains with size given by a truncated Pareto distribution.

Usage

```
rbpto(lambda, grain, win, xm, alpha, lengthscales, seed = NULL,
      xy = NULL)

bpto.coverageprob(lambda, grain, xm, alpha, lengthscales = 1:500)

bpto.germintensity(coverp, grain, xm, alpha, lengthscales = 1:500)

bpto.covar(lambda, grain, xm, alpha, lengthscales = 1:500, xy)
```

Arguments

<code>lambda</code>	Intensity of the germ process (which is a Poisson point process)
<code>grain</code>	A single owin object that gives the shape and size of the grain at scale 1
<code>win</code>	The window to simulate in (an owin object)
<code>xm</code>	A parameter governing the shape of the Pareto distribution used - see details
<code>alpha</code>	A parameter governing the shape of the Pareto distribution used - see details
<code>lengthscales</code>	A list of scales of the grain for which to approximate the Pareto distribution: The grain for a germ is chosen by selecting a scaled version of <code>grain</code> where <code>lengthscales</code> specifies the possible scales and the Pareto distribution is used to specify the probability of selection of each scale.
<code>seed</code>	Optional input (default in NULL). Is an integer passed to <code>set.seed</code> . Used to reproduce patterns exactly.
<code>xy</code>	A raster object that specifies pixel coordinates of the final simulated binary map. It is used the same way as <code>xy</code> is <code>as.mask</code> in <code>spatstat</code> . If non-null then the computations will be performed using rasters. Otherwise if <code>grain</code> and <code>win</code> are polygonal then computations may be all polygonal.
<code>coverp</code>	Coverage probability of the Boolean model.

Details

The parameters `xm` and `alpha` are such that the CDF of the Pareto distribution is $P(s \leq x) = 1 - (xm/x)^{\alpha}$. The distribution of grains scales is a step-function approximation to the CDF with steps at `lengthscales`.

Value

An owin object.

Functions

- `rbpto`: Simulate Boolean model with grain size distributed according to a truncated Pareto distribution.
- `bpto.coverageprob`: The coverage probability of the Boolean model with grain size distributed according to a truncated Pareto distribution.
- `bpto.germintensity`: The germ intensity of the Boolean model with grain size distributed according to a truncated Pareto distribution.
- `bpto.covar`: The covariance of the Boolean model with grain size distributed according to a truncated Pareto distribution. `xy` is required to specify resolution and offset of pixel grid.

Examples

```
lambda <- 1
win <- square(r = 10)
#grain <- owin(xrange = c(-0.2, 0.2), yrange = c(-0.2, 0.2))
grain <- disc(r = 0.2)
xm <- 0.01
```

```

alpha <- 2
if (interactive()){
lengthscales <- seq(1, 10, by = 0.1)
} else {
lengthscales <- seq(1, 5, by = 0.1)
}
xi <- rbpto(lambda, grain, win, xm, alpha, lengthscales = lengthscales)
# plot(xi, col = "black")
# plot(win, add = TRUE)

bpto.coverageprob(lambda, grain, xm, alpha, lengthscales = lengthscales)
covar <- bpto.covar(lambda, grain, xm, alpha, lengthscales = lengthscales,
  xy = as.mask(win, eps = 0.1))

```

secondorderprops

Estimate Second-Order Properties of a RACS

Description

Estimates many second order properties of RACS, gliding box lacunarity, covariance, centred covariance, and pair-correlation. This can be faster than computing estimates of multiple second order properties separately as Fourier transforms of the binary map are not repeated.

Usage

```

secondorderprops(xiim, gblargs = NULL, covarargs = NULL,
  cencovarargs = NULL, paircorrargs = NULL, returnnotmean = FALSE)

```

Arguments

xiim	A spatstat im object with pixel values that are either TRUE, FALSE or NA. TRUE represents foreground, FALSE represents background and NA represents unobserved locations.
gblargs	Arguments passed to gblemp and gbl.cvchat . If NULL then GBL will not be estimated. You can also request to
covarargs	Arguments passed to racscovariance.cvchat . If NULL then covariance will not be returned.
cencovarargs	Arguments passed to cencovariance.cvchat . If NULL then pair correlation will not be returned.
paircorrargs	Arguments passed to paircorr.cvchat . If NULL then pair correlation will not be returned.
returnnotmean	Logical. If FALSE the anisotropic estimates of covariance and pair-correlation will be returned as im objects. If TRUE then average covariance and pair-correlation over all directions will be returned as fv objects.

Examples

```
xi <- heather$coarse
xiim <- as.im(xi, value = TRUE, na.replace = FALSE)
gblargs = list(boxwidths = seq(1, 10, by = 1), estimators = c("GBLemp", "GBLc"))
covarargs = list(estimators = "all")
cencovarargs = list(estimators = "pickaH")
paircorrargs = list(estimators = "pickaH")
returnnotmean = TRUE
secondests <- secondorderprops(xiim,
  gblargs = gblargs,
  covarargs = covarargs,
  cencovarargs = cencovarargs,
  paircorrargs = paircorrargs,
  returnnotmean = FALSE)
```

summary.imlist

Pointwise summary of a list of im objects

Description

This function assumes that im objects are each realisations of the same (stochastic) object. It returns pointwise summaries such as observed sample mean and sample variance.

Usage

```
## S3 method for class 'imlist'
summary(object, ..., harmonizeobject = TRUE)
```

Arguments

object	A list of im objects
...	Ignored
harmonizeobject	If TRUE (default) the pixel dimensions of the images will be harmonized. Otherwise the object will be tested for compatibility.

Value

A list im objects containing the pointwise mean, variance and maxima and minima.

Author(s)

Kassel Hingee

Examples

```
obspatterns <- replicate(5, rbdd(10, 0.05, window = square(1)), simplify = FALSE)
ims <- solapply(obspatterns,
  function(x) racscovariance(x, obswin = square(1), estimators = "pickaH", drop = TRUE))
summ <- summary.imlist(ims, harmonizeobject = FALSE)
```

Index

*Topic **datagen**

- placegrainsfromlib, 23
- rbdd, 29
- rbdr, 31
- rblnd, 32

*Topic **nonparametric**

- cencovariance, 4
- contagdiscstate, 6
- coverageprob, 9
- cppicka, 10
- gblc, 14
- gblcc, 15
- gblemp, 16
- gblg, 18
- paircorr, 21
- placegrainsfromlib, 23
- plugincvc, 25
- racscovariance, 26

*Topic **package**

- stationaryracsinference-package, 2

*Topic **spatial**

- cencovariance, 4
- contagdiscstate, 6
- coverageprob, 9
- cppicka, 10
- gblc, 14
- gblcc, 15
- gblemp, 16
- gblg, 18
- paircorr, 21
- placegrainsfromlib, 23
- plugincvc, 25
- racscovariance, 26
- rbdd, 29
- rbdr, 31
- rblnd, 32
- stationaryracsinference-package, 2

adjacency (contagpixelgrid), 8

as.im, 13

as.mask, 34

bddcovar (rbdd), 29
bddcoverageprob (rbdd), 29
bdddiscr (rbdd), 29
bddlambda (rbdd), 29
bdrcovar (rbdr), 31
bdrcoverageprob (rbdr), 31
bpto.covar (rbpto), 33
bpto.coverageprob (rbpto), 33
bpto.germintensity (rbpto), 33

cencovariance, 3, 4, 27
cencovariance.cvchat, 6, 35
contagdiscstate, 3, 6
contagpixelgrid, 8
covar.grainlib (placegrainsfromlib), 23
coveragefrac (coverageprob), 9
coverageprob, 3, 5, 7, 9, 14, 21, 27
cp (coverageprob), 9
cppicka, 5, 10, 12, 13, 21, 27

gbl, 3, 12
gbl.cvchat, 35
gblc, 12, 13, 14
gblcc, 12, 13, 15
gblemp, 12, 13, 16, 35
gblg, 12, 13, 18
gbltrad (gblemp), 16

Hest, 7

innerprod.im, 19
isbinarymap, 20

meanarea.grainlib (placegrainsfromlib),
23

meansetcov.grainlib
(placegrainsfromlib), 23

paircorr, 3, 21

paircorr.cvchat, [35](#)
placegrainsfromlib, [3](#), [23](#)
pluginvc, [5](#), [12](#), [14](#), [21](#), [25](#), [27](#)

racscovariance, [3](#), [5](#), [26](#)
racscovariance.cvchat, [35](#)
rbdd, [3](#), [29](#)
rbdr, [3](#), [31](#)
rblnd, [32](#)
rbpto, [3](#), [33](#)
roll_sum, [17](#)
rpoispp, [24](#), [30–33](#)

sample, [23](#)
secondorderprops, [3](#), [35](#)
set.seed, [29](#), [31](#), [32](#), [34](#)
setcov, [26](#)
solist, [23](#)
stationaryracsinference
 (stationaryracsinference-package),
 [2](#)
stationaryracsinference-package, [2](#)
summary.imlist, [36](#)