



DBMS : 1A2

Q.1. Consider relation R with five attributes ABCDE. The dependencies are  $A \rightarrow B$ ,  $BC \rightarrow E$  and  $ED \rightarrow A$ .

a). List all the keys for R.

b). Is R in 3NF?

c). Is R in BCNF?

Q.2. Suppose you are given relation with four attributes ABCD. The dependencies are,

a).  $C \rightarrow D$ ,  $C \rightarrow A$ ,  $B \rightarrow C$

b).  $B \rightarrow C$ ,  $D \rightarrow A$

c).  $ABC \rightarrow D$ ,  $D \rightarrow A$ .

Find all candidate keys for each subquestion & identify the best normal form & why.

Q.1. ABCDE :  $A \rightarrow B$   
 $BC \rightarrow E$   
 $ED \rightarrow A$

a). Since all RHS does not have CD,  
So,  $(CD)^+ = CD$ .

Now, for combination of 3-length,  
 $(ABC \ ACD)^+ = ABCDE$

$(BCD)^+ = ABCDE$

$(ECD)^+ = ABCDE$

The lowest number of attributes required to get the complete relation is 3.

$\therefore$  The keys are ACD, BCD, ECD.

b).  $A \rightarrow B$  ,  $BC \rightarrow E$  ,  $CD \rightarrow A$

In the RHS of dependencies, B, E, A, all attributes are prime attributes.

$\therefore$  They are all part of key.

Hence, relation R is 3NF.

c). Here,

A  $\rightarrow$  B , BC  $\rightarrow$  E , ED  $\rightarrow$  A

NOT SUPERKEY

$\therefore$  Even 1 FD is violated, it will not be considered to be BCNF.

Hence, relation is not BCNF.

Q.2. a).  $C \rightarrow D$  ,  $C \rightarrow A$  ,  $D \rightarrow C$

Here, candidate key is B.

R is in 2NF, however,

$$(ABCD)^+ = ABCD$$

$$(ABC)^+ = ABCD$$

$$(AB)^+ = ABCD$$

$$(B^*)^+ = ABCD$$

$\therefore$  The candidate key for this dependency is B.

$\therefore$  The non prime attributes (D, A) are functionally dependent (through C) on the prime candidate key (B). The following is in 2NF.





b).  $B \rightarrow C, D \rightarrow A$   
 $(ABCD)^+ = ABCD$   
 $(BCD)^+ = ABCD$   
 $(BD)^+ = ABCD$

$\therefore$  The primary key is BD.

$\therefore$  R is in 1NF form, since each attribute has only one dependency, i.e., relation contains an atomic value since, the non-prime attributes are not functionally dependent, candidate key is not 2NF, similarly for 3NF.

c).  $ABC \rightarrow D, D \rightarrow A$

$$(ABCD)^+ = ABCD$$
$$(ABC)^+ = ABCD$$
$$(BCD)^+ = ABCD.$$

For BCD, non-prime attribute A is functionally dependent (through D) on candidate key BCD. The following is in 2NF form.

Since, there is no transitive partial dependency & is in 2NF form, the following relation R is in 3NF.

Since, there are more than one candidate keys, the following is not in BCNF.