
MODULE *JustInTimePaxos*

EXTENDS *Naturals, Sequences, FiniteSets, TLC*

The set of *Paxos* replicas

CONSTANT *Replicas*

The set of *Paxos* clients

CONSTANT *Clients*

The set of possible values

CONSTANT *Values*

An empty value

CONSTANT *Nil*

Request/response types

CONSTANTS

MClientRequest,
MClientResponse,
MRepairRequest,
MRepairResponse,
MAbortRequest,
MAbortResponse,
MViewChangeRequest,
MViewChangeResponse,
MStartViewRequest

Replica statuses

CONSTANTS

SNormal,
SAborting,
SViewChange

Entry types

CONSTANTS

TValue,
TNoOp

A sequence of replicas used for deterministic primary election

VARIABLE *replicas*

$globalVars \triangleq \langle replicas \rangle$

The set of all messages on the network

VARIABLE *messages*

$messageVars \triangleq \langle messages \rangle$

Local client state

Strictly increasing representation of synchronized time

VARIABLE $cTime$

The highest known view ID for a client

VARIABLE $cViewID$

The current sequence number for a client

VARIABLE $cSeqNum$

A client response buffer

VARIABLE $cResps$

A set of all commits - used for model checking

VARIABLE $cCommits$

$clientVars \triangleq \langle cTime, cViewID, cSeqNum, cResps, cCommits \rangle$

Local replica state

The current status of a replica

VARIABLE $rStatus$

A replica's commit log

VARIABLE $rLog$

The current view ID for a replica

VARIABLE $rViewID$

The current sequence number for each session

VARIABLE $rSeqNum$

The highest known timestamp for all sessions

VARIABLE $rTimestamp$

The last known normal view

VARIABLE $rLastViewID$

The set of received view change responses

VARIABLE $rViewChanges$

The point ($client$ + sequence number) in the log currently being aborted

VARIABLE $rAbortPoint$

The set of abort responses received

VARIABLE $rAbortResps$

$replicaVars \triangleq \langle rStatus, rLog, rViewID, rSeqNum, rTimestamp, rAbortResps \rangle$

$rLastViewID, rViewChanges, rAbortPoint, rAbortResps\rangle$

$vars \triangleq \langle globalVars, messageVars, clientVars, replicaVars \rangle$

This section provides helpers for the spec.

RECURSIVE $SeqFromSet(-)$

$SeqFromSet(S) \triangleq$

IF $S = \{\}$ THEN

$\langle \rangle$

ELSE LET $x \triangleq \text{CHOOSE } x \in S : \text{TRUE}$

IN $\langle x \rangle \circ SeqFromSet(S \setminus \{x\})$

$Pick(S) \triangleq \text{CHOOSE } s \in S : \text{TRUE}$

RECURSIVE $SetReduce(-, -, -)$

$SetReduce(Op(-, -), S, value) \triangleq$

IF $S = \{\}$ THEN

$value$

ELSE

LET $s \triangleq Pick(S)$

IN $SetReduce(Op, S \setminus \{s\}, Op(s, value))$

$Max(s) \triangleq \text{CHOOSE } x \in s : \forall y \in s : x \geq y$

$Sum(S) \triangleq \text{LET } _op(a, b) \triangleq a + b$

IN $SetReduce(_op, S, 0)$

$IsQuorum(s) \triangleq Cardinality(s) * 2 \geq Cardinality(Replicas)$

$Quorums \triangleq \{r \in \text{SUBSET } Replicas : IsQuorum(r)\}$

$Primary(v) \triangleq replicas[(v \% Len(replicas)) + (\text{IF } v \geq Len(replicas) \text{ THEN } 1 \text{ ELSE } 0)]$

$IsPrimary(r) \triangleq Primary(rViewID[r]) = r$

This section models the network.

Send a set of messages

$Sends(ms) \triangleq messages' = messages \cup ms$

Send a message

$Send(m) \triangleq Sends(\{m\})$

Reply to a message with a set of responses

$Replies(req, resps) \triangleq messages' = (messages \cup resps) \setminus \{req\}$

Reply to a message

$Reply(req, resp) \triangleq Replies(req, \{resp\})$

Discard a message
 $Discard(m) \triangleq messages' = messages \setminus \{m\}$

This section models client requests.

Client 'c' sends value 'v' to all replicas

$ClientRequest(c, v) \triangleq$
 $\wedge cTime' = cTime + 1$
 $\wedge cSeqNum' = [cSeqNum \text{ EXCEPT } ![c] = cSeqNum[c] + 1]$
 $\wedge Sends(\{[src \mapsto c,$
 $\quad dest \mapsto r,$
 $\quad type \mapsto MClientRequest,$
 $\quad viewID \mapsto cViewID[c],$
 $\quad seqNum \mapsto cSeqNum'[c],$
 $\quad value \mapsto v,$
 $\quad timestamp \mapsto cTime'] : r \in Replicas\})$
 $\wedge \text{UNCHANGED } \langle globalVars, replicaVars, cViewID, cResps, cCommits \rangle$

Client 'c' handles a response 'm' from replica 'r'

$HandleClientResponse(c, r, m) \triangleq$
 $\wedge \vee \wedge m.viewID = cViewID[c]$
 $\wedge cResps' = [cResps \text{ EXCEPT } ![c] = cResps[c] \cup \{m\}]$
 $\wedge \text{LET}$
 $\quad seqNumResps \triangleq \{n \in cResps[c] : n.seqNum = m.seqNum\}$
 $\quad goodResps \triangleq \{n \in seqNumResps : n.viewID = cViewID[c] \wedge n.succeeded\}$
 $\quad isCommitted \triangleq \wedge \exists n \in goodResps : n.src = Primary(n.viewID)$
 $\quad \wedge \{n.src : n \in goodResps\} \in Quorums$
 IN
 $\wedge \vee \wedge isCommitted$
 $\quad \wedge cCommits' = [cCommits \text{ EXCEPT } ![c] = cCommits[c] \cup$
 $\quad \quad \{CHOOSE n \in goodResps : n.src = Primary(n.viewID)\}]$
 $\vee \wedge \neg isCommitted$
 $\quad \wedge \text{UNCHANGED } \langle cCommits \rangle$
 $\quad \wedge \text{UNCHANGED } \langle cViewID, cSeqNum \rangle$
 $\vee \wedge m.viewID > cViewID[c]$
 $\quad \wedge cViewID' = [cViewID \text{ EXCEPT } ![c] = m.viewID]$
 $\quad \wedge cSeqNum' = [cSeqNum \text{ EXCEPT } ![c] = 0]$
 $\quad \wedge cResps' = [cResps \text{ EXCEPT } ![c] = \{\}]$
 $\quad \wedge \text{UNCHANGED } \langle cCommits \rangle$
 $\vee \wedge m.viewID < cViewID[c]$
 $\quad \wedge \text{UNCHANGED } \langle cCommits \rangle$
 $\wedge Discard(m)$
 $\wedge \text{UNCHANGED } \langle globalVars, replicaVars, cTime, cSeqNum \rangle$

This section models the replica protocol.

Replica 'r' requests a repair of the client 'c' request 'm'

$$\begin{aligned} Repair(r, c, m) &\triangleq \\ \wedge \text{Replies}(m, \{ &\begin{array}{ll} \text{src} &\mapsto r, \\ \text{dest} &\mapsto d, \\ \text{type} &\mapsto MRepairRequest, \\ \text{viewID} &\mapsto rViewID[r], \\ \text{client} &\mapsto c, \\ \text{seqNum} &\mapsto m.seqNum, \\ \text{timestamp} &\mapsto m.timestamp \} : d \in Replicas \}) \end{array} \end{aligned}$$

Replica 'r' aborts the client 'c' request 'm'

$$\begin{aligned}
\text{Abort}(r, c, m) &\triangleq \\
&\wedge \text{IsPrimary}(r) \\
&\wedge r\text{Status}[r] = \text{SNormal} \\
&\wedge r\text{Status}' = [r\text{Status} \quad \text{EXCEPT } ![r] = \text{SAborting}] \\
&\wedge r\text{AbortResps}' = [r\text{AbortResps} \quad \text{EXCEPT } ![r] = \{\}] \\
&\wedge r\text{AbortPoint}' = [r\text{AbortPoint} \quad \text{EXCEPT } ![r] = [\text{client} \mapsto c, \text{seqNum} \mapsto m.\text{seqNum}]] \\
&\wedge \text{Replies}(m, \{[\text{src} \mapsto r, \\
&\quad \text{dest} \mapsto d, \\
&\quad \text{type} \mapsto \text{MAbortRequest}, \\
&\quad \text{viewID} \mapsto r\text{ViewID}[r], \\
&\quad \text{client} \mapsto c, \\
&\quad \text{seqNum} \mapsto m.\text{seqNum}, \\
&\quad \text{timestamp} \mapsto m.\text{timestamp}] : d \in \text{Replicas}\})
\end{aligned}$$

Replica 'r' handles client 'c' request 'm'

[illegible]

$$\begin{aligned}
& \wedge isLinear \\
& \wedge rLog' = append(entry) \\
& \wedge rSeqNum' = [rSeqNum \text{ EXCEPT } ![r] = [rSeqNum[r] \text{ EXCEPT } ![c] = m.seqNum]] \\
& \wedge rTimestamp' = [rTimestamp \text{ EXCEPT } ![r] = m.timestamp] \\
& \wedge Reply(m, [src \mapsto r, \\
& \quad \quad \quad dest \mapsto c, \\
& \quad \quad \quad type \mapsto MClientResponse, \\
& \quad \quad \quad viewID \mapsto rViewID[r], \\
& \quad \quad \quad seqNum \mapsto m.seqNum, \\
& \quad \quad \quad index \mapsto index, \\
& \quad \quad \quad value \mapsto m.value, \\
& \quad \quad \quad succeeded \mapsto TRUE]) \\
& \wedge \text{UNCHANGED } \langle rStatus, rAbortPoint, rAbortResps \rangle \\
\vee & \wedge \vee \wedge \neg isSequential \\
& \quad \wedge m.seqNum > rSeqNum[r][c] + 1 \\
& \quad \vee \neg isLinear \\
& \wedge \vee \wedge IsPrimary(r) \\
& \quad \wedge Abort(r, c, m) \\
& \quad \vee \wedge \neg IsPrimary(r) \\
& \quad \quad \wedge Repair(r, c, m) \\
& \quad \quad \wedge \text{UNCHANGED } \langle rStatus, rAbortPoint, rAbortResps \rangle \\
& \quad \wedge \text{UNCHANGED } \langle rLog, rSeqNum, rTimestamp \rangle \\
\vee & \wedge m.viewID < rViewID[r] \\
& \wedge Reply(m, [src \mapsto r, \\
& \quad \quad \quad dest \mapsto c, \\
& \quad \quad \quad type \mapsto MClientResponse, \\
& \quad \quad \quad viewID \mapsto rViewID[r], \\
& \quad \quad \quad seqNum \mapsto m.seqNum, \\
& \quad \quad \quad succeeded \mapsto FALSE]) \\
& \quad \wedge \text{UNCHANGED } \langle rStatus, rLog, rSeqNum, rTimestamp, rAbortPoint, rAbortResps \rangle \\
& \wedge \text{UNCHANGED } \langle globalVars, clientVars, rViewID, rLastViewID, rViewChanges \rangle
\end{aligned}$$

Replica 'r' handles replica 's' repair request 'm'

$$\begin{aligned}
HandleRepairRequest(r, s, m) & \triangleq \\
& \wedge m.viewID = rViewID[r] \\
& \wedge IsPrimary(r) \\
& \wedge rStatus[r] = SNormal \\
& \wedge \text{LET } offset \triangleq Len(rLog[r][m.client]) - (rSeqNum[r][m.client] - m.seqNum) \\
& \text{IN} \\
& \vee \wedge offset \leq Len(rLog[r][m.client]) \\
& \quad \wedge Reply(m, [src \mapsto r, \\
& \quad \quad \quad dest \mapsto s, \\
& \quad \quad \quad type \mapsto MRepairResponse, \\
& \quad \quad \quad viewID \mapsto rViewID[r], \\
& \quad \quad \quad client \mapsto m.client,
\end{aligned}$$

$seqNum \mapsto m.seqNum,$
 $value \mapsto rLog[r][m.client][offset].value,$
 $timestamp \mapsto rLog[r][m.client][offset].timestamp]$
 $\wedge \text{UNCHANGED } \langle rStatus, rAbortPoint, rAbortResps \rangle$
 $\vee \wedge offset = Len(rLog[r][m.client]) + 1$
 $\wedge Abort(r, m.client, m)$
 $\wedge \text{UNCHANGED } \langle globalVars, clientVars, rLog, rSeqNum, rTimestamp, rViewID, rLastViewID, rViewChan$

Replica 'r' handles replica 's' repair response 'm'
 $HandleRepairResponse(r, s, m) \triangleq$
 $\wedge HandleClientRequest(r, m.client, [m \text{ EXCEPT } !.src = m.client])$

Replica 'r' handles replica 's' abort request 'm'
 $HandleAbortRequest(r, s, m) \triangleq$
 $\wedge m.viewID = rViewID[r]$
 $\wedge rStatus[r] \in \{SNormal, SAborting\}$
 $\wedge \text{LET}$
 $offset \triangleq Len(rLog[r][m.client]) - (rSeqNum[r][m.client] - m.seqNum)$
 $entry \triangleq [type \mapsto TNoOp, timestamp \mapsto m.timestamp]$
 $replace(l, i, e) \triangleq [j \in 1 .. Max(\{Len(l), i\}) \mapsto \text{IF } j = i \text{ THEN } e \text{ ELSE } l[j]]$
 IN
 $\wedge offset \leq Len(rLog[r][m.client]) + 1$
 $\wedge rLog' = [rLog \text{ EXCEPT } ![r] = [rLog[r] \text{ EXCEPT }$
 $![m.client] = replace(rLog[r][m.client], offset, entry)]]$
 $\wedge rTimestamp' = [rTimestamp \text{ EXCEPT } ![r] = Max(\{rTimestamp[r], m.timestamp\})]$
 $\wedge rSeqNum' = [rSeqNum \text{ EXCEPT } ![r] = [rSeqNum[r] \text{ EXCEPT }$
 $![m.client] = Max(\{rSeqNum[r][m.client], m.seqNum\})]$
 $\wedge Replies(m, \{[src \mapsto r,$
 $dest \mapsto Primary(rViewID[r]),$
 $type \mapsto MAbortResponse,$
 $viewID \mapsto rViewID[r],$
 $client \mapsto m.client,$
 $seqNum \mapsto m.seqNum],$
 $[src \mapsto r,$
 $dest \mapsto m.client,$
 $type \mapsto MClientResponse,$
 $viewID \mapsto rViewID[r],$
 $seqNum \mapsto m.seqNum,$
 $succeeded \mapsto FALSE]\})$
 $\wedge \text{UNCHANGED } \langle globalVars, clientVars, rStatus, rAbortPoint,$
 $rAbortResps, rViewID, rLastViewID, rViewChanges \rangle$

Replica 'r' handles replica 's' repair response 'm'
 $HandleAbortResponse(r, s, m) \triangleq$
 $\wedge rStatus[r] = SAborting$
 $\wedge m.viewID = rViewID[r]$

$$\begin{aligned}
& \wedge \text{IsPrimary}(r) \\
& \wedge m.\text{seqNum} = r\text{AbortPoint}[r].\text{seqNum} \\
& \wedge r\text{AbortResps}' = [r\text{AbortResps} \text{ EXCEPT } ![r] = r\text{AbortResps}[r] \cup \{m\}] \\
& \wedge \text{LET } \text{resps} \triangleq \{ \text{res}.\text{src} : \text{res} \in \{ \text{resp} \in r\text{AbortResps}'[r] : \\
& \quad \wedge \text{resp}.\text{viewID} = r\text{ViewID}[r] \\
& \quad \wedge \text{resp}.\text{client} = r\text{AbortPoint}[r].\text{client} \\
& \quad \wedge \text{resp}.\text{seqNum} = r\text{AbortPoint}[r].\text{seqNum} \} \} \\
& \quad \text{isQuorum} \triangleq r \in \text{resps} \wedge \text{resps} \in \text{Quorums} \\
& \text{IN} \\
& \quad \vee \wedge \text{isQuorum} \\
& \quad \wedge r\text{Status}' = [r\text{Status} \text{ EXCEPT } ![r] = S\text{Normal}] \\
& \quad \vee \wedge \neg \text{isQuorum} \\
& \quad \wedge \text{UNCHANGED } \langle r\text{Status} \rangle \\
& \wedge \text{UNCHANGED } \langle \text{globalVars}, \text{messageVars}, \text{clientVars}, r\text{Log}, r\text{SeqNum}, r\text{Timestamp}, \\
& \quad r\text{AbortPoint}, r\text{ViewID}, r\text{ViewChanges}, r\text{LastViewID} \rangle
\end{aligned}$$

Replica 'r' requests a view change

$$\begin{aligned}
& \text{ChangeView}(r) \triangleq \\
& \quad \wedge \text{Sends}(\{ \text{src} \mapsto r, \\
& \quad \quad \text{dest} \mapsto d, \\
& \quad \quad \text{type} \mapsto M\text{ViewChangeRequest}, \\
& \quad \quad \text{viewID} \mapsto r\text{ViewID}[r] + 1 : d \in \text{Replicas} \}) \\
& \quad \wedge \text{UNCHANGED } \langle \text{globalVars}, \text{clientVars}, \text{replicaVars} \rangle
\end{aligned}$$

Replica 'r' handles replica 's' view change request 'm'

$$\begin{aligned}
& \text{HandleViewChangeRequest}(r, s, m) \triangleq \\
& \quad \wedge r\text{ViewID}[r] < m.\text{viewID} \\
& \quad \wedge r\text{ViewID}' = [r\text{ViewID} \text{ EXCEPT } ![r] = m.\text{viewID}] \\
& \quad \wedge r\text{Status}' = [r\text{Status} \text{ EXCEPT } ![r] = S\text{ViewChange}] \\
& \quad \wedge r\text{ViewChanges}' = [r\text{ViewChanges} \text{ EXCEPT } ![r] = \{\}] \\
& \quad \wedge \text{Reply}(m, [\text{src} \mapsto r, \\
& \quad \quad \text{dest} \mapsto \text{Primary}(m.\text{viewID}), \\
& \quad \quad \text{type} \mapsto M\text{ViewChangeResponse}, \\
& \quad \quad \text{viewID} \mapsto m.\text{viewID}, \\
& \quad \quad \text{lastViewID} \mapsto r\text{LastViewID}[r], \\
& \quad \quad \text{logs} \mapsto r\text{Log}[r]]) \\
& \quad \wedge \text{UNCHANGED } \langle \text{globalVars}, \text{clientVars}, r\text{Log}, r\text{SeqNum}, r\text{Timestamp}, \\
& \quad r\text{AbortPoint}, r\text{AbortResps}, r\text{LastViewID} \rangle
\end{aligned}$$

Replica 'r' handles replica 's' view change response 'm'

$$\begin{aligned}
& \text{HandleViewChangeResponse}(r, s, m) \triangleq \\
& \quad \wedge \text{IsPrimary}(r) \\
& \quad \wedge r\text{ViewID}[r] = m.\text{viewID} \\
& \quad \wedge r\text{Status}[r] = S\text{ViewChange} \\
& \quad \wedge r\text{ViewChanges}' = [r\text{ViewChanges} \text{ EXCEPT } ![r] = r\text{ViewChanges}[r] \cup \{m\}] \\
& \quad \wedge \text{LET } \text{viewChanges} \triangleq \{ v \in r\text{ViewChanges}'[r] : v.\text{viewID} = r\text{ViewID}[r] \}
\end{aligned}$$

$$\begin{aligned}
viewSources &\triangleq \{v.src : v \in viewChanges\} \\
isQuorum &\triangleq r \in viewSources \wedge viewSources \in Quorums \\
lastViewIDs &\triangleq \{v.lastViewID : v \in viewChanges\} \\
lastViewID &\triangleq (\text{CHOOSE } v1 \in lastViewIDs : \forall v2 \in lastViewIDs : v2 \leq v1) \\
lastViewChanges &\triangleq \{v2 \in viewChanges : v2.lastViewID = lastViewID\} \\
viewLogs &\triangleq [c \in Clients \mapsto \{v1.logs[c] : v1 \in lastViewChanges\}] \\
mergeEnts(es) &\triangleq \\
&\quad \text{IF } es = \{\} \vee \exists e \in es : e.type = TNoOp \text{ THEN} \\
&\quad \quad [type \mapsto TNoOp] \\
&\quad \text{ELSE} \\
&\quad \quad \text{CHOOSE } e \in es : e.type \neq TNoOp \\
range(ls) &\triangleq \text{Max}(\{Len(l) : l \in ls\}) \\
entries(ls, i) &\triangleq \{l[i] : l \in \{k \in ls : i \leq Len(k)\}\} \\
mergeLogs(ls) &\triangleq [i \in 1 \dots range(ls) \mapsto mergeEnts(entries(ls, i))] \\
viewLog &\triangleq [c \in Clients \mapsto mergeLogs(viewLogs[c])] \\
viewRange &\triangleq \text{Max}(\{Len(viewLog[c]) : c \in Clients\}) \\
viewTimestamp &\triangleq \text{IF } viewRange > 0 \text{ THEN} \\
&\quad \text{Max}(\text{UNION } \{\{l[i].timestamp : i \in \text{DOMAIN } l\} : \\
&\quad \quad l \in \{viewLog[c] : c \in Clients\}\}) \\
&\quad \text{ELSE } 0 \\
\text{IN} \\
&\vee \wedge isQuorum \\
&\quad \wedge Replies(m, \{[src \mapsto r, \\
&\quad \quad \quad dest \mapsto d, \\
&\quad \quad \quad type \mapsto MStartViewRequest, \\
&\quad \quad \quad viewID \mapsto rViewID[r], \\
&\quad \quad \quad timestamp \mapsto viewTimestamp, \\
&\quad \quad \quad log \mapsto viewLog] : d \in Replicas\}) \\
&\vee \wedge \neg isQuorum \\
&\quad \wedge Discard(m) \\
&\wedge \text{UNCHANGED } \langle globalVars, clientVars, rStatus, rViewID, rLog, rSeqNum, \\
&\quad rTimestamp, rAbortPoint, rAbortResps, rLastViewID \rangle
\end{aligned}$$

Replica 'r' handles replica 's' start view request 'm'

$$\begin{aligned}
HandleStartViewRequest(r, s, m) &\triangleq \\
&\wedge \vee rViewID[r] < m.viewID \\
&\quad \vee \wedge rViewID[r] = m.viewID \\
&\quad \wedge rStatus[r] = SViewChange \\
&\wedge rLog' = [rLog \text{ EXCEPT } ![r] = m.log] \\
&\wedge rSeqNum' = [rSeqNum \text{ EXCEPT } ![r] = [c \in Clients \mapsto 0]] \\
&\wedge rTimestamp' = [rTimestamp \text{ EXCEPT } ![r] = m.timestamp] \\
&\wedge rStatus' = [rStatus \text{ EXCEPT } ![r] = SNormal] \\
&\wedge rViewID' = [rViewID \text{ EXCEPT } ![r] = m.viewID] \\
&\wedge rLastViewID' = [rLastViewID \text{ EXCEPT } ![r] = m.viewID] \\
&\wedge Discard(m)
\end{aligned}$$

$$\wedge \text{UNCHANGED } \langle \text{globalVars}, \text{clientVars}, \text{rAbortPoint}, \text{rAbortResps}, \text{rViewChanges} \rangle$$

$$\begin{aligned} \text{InitMessageVars} &\triangleq \\ &\wedge \text{messages} = \{\} \end{aligned}$$

$$\begin{aligned} \text{InitClientVars} &\triangleq \\ &\wedge \text{cTime} = 0 \\ &\wedge \text{cViewID} = [c \in \text{Clients} \mapsto 1] \\ &\wedge \text{cSeqNum} = [c \in \text{Clients} \mapsto 0] \\ &\wedge \text{cResps} = [c \in \text{Clients} \mapsto \{\}] \\ &\wedge \text{cCommits} = [c \in \text{Clients} \mapsto \{\}] \end{aligned}$$

$$\begin{aligned} \text{InitReplicaVars} &\triangleq \\ &\wedge \text{replicas} = \text{SeqFromSet}(\text{Replicas}) \\ &\wedge \text{rStatus} = [r \in \text{Replicas} \mapsto \text{SNormal}] \\ &\wedge \text{rLog} = [r \in \text{Replicas} \mapsto [c \in \text{Clients} \mapsto \langle \rangle]] \\ &\wedge \text{rSeqNum} = [r \in \text{Replicas} \mapsto [c \in \text{Clients} \mapsto 0]] \\ &\wedge \text{rTimestamp} = [r \in \text{Replicas} \mapsto 0] \\ &\wedge \text{rAbortPoint} = [r \in \text{Replicas} \mapsto [\text{client} \mapsto \text{Nil}, \text{seqNum} \mapsto 0]] \\ &\wedge \text{rAbortResps} = [r \in \text{Replicas} \mapsto \{\}] \\ &\wedge \text{rViewID} = [r \in \text{Replicas} \mapsto 1] \\ &\wedge \text{rLastViewID} = [r \in \text{Replicas} \mapsto 1] \\ &\wedge \text{rViewChanges} = [r \in \text{Replicas} \mapsto \{\}] \end{aligned}$$

$$\begin{aligned} \text{Init} &\triangleq \\ &\wedge \text{InitMessageVars} \\ &\wedge \text{InitClientVars} \\ &\wedge \text{InitReplicaVars} \end{aligned}$$

The type invariant verifies that clients do not receive two commits at the same index with different values.

$$\begin{aligned} \text{TypeOK} &\triangleq \\ &\forall c1, c2 \in \text{Clients} : \\ &\quad \forall e1 \in \text{cCommits}[c1] : \\ &\quad \quad \neg \exists e2 \in \text{cCommits}[c2] : \\ &\quad \quad \quad \wedge e1.\text{index} = e2.\text{index} \\ &\quad \quad \quad \wedge e1.\text{value} \neq e2.\text{value} \end{aligned}$$

$$\begin{aligned} \text{Next} &\triangleq \\ &\forall \exists c \in \text{Clients} : \\ &\quad \exists v \in \text{Values} : \\ &\quad \quad \wedge \text{ClientRequest}(c, v) \\ &\forall \exists r \in \text{Replicas} : \end{aligned}$$

$$\begin{aligned}
& \wedge \text{ChangeView}(r) \\
\vee \exists m \in \text{messages} : & \\
& \wedge m.type = MClientRequest \\
& \wedge \text{HandleClientRequest}(m.dest, m.src, m) \\
\vee \exists m \in \text{messages} : & \\
& \wedge m.type = MClientResponse \\
& \wedge \text{HandleClientResponse}(m.dest, m.src, m) \\
\vee \exists m \in \text{messages} : & \\
& \wedge m.type = MRepairRequest \\
& \wedge \text{HandleRepairRequest}(m.dest, m.src, m) \\
\vee \exists m \in \text{messages} : & \\
& \wedge m.type = MRepairResponse \\
& \wedge \text{HandleRepairResponse}(m.dest, m.src, m) \\
\vee \exists m \in \text{messages} : & \\
& \wedge m.type = MAbortRequest \\
& \wedge \text{HandleAbortRequest}(m.dest, m.src, m) \\
\vee \exists m \in \text{messages} : & \\
& \wedge m.type = MAbortResponse \\
& \wedge \text{HandleAbortResponse}(m.dest, m.src, m) \\
\vee \exists m \in \text{messages} : & \\
& \wedge m.type = MViewChangeRequest \\
& \wedge \text{HandleViewChangeRequest}(m.dest, m.src, m) \\
\vee \exists m \in \text{messages} : & \\
& \wedge m.type = MViewChangeResponse \\
& \wedge \text{HandleViewChangeResponse}(m.dest, m.src, m) \\
\vee \exists m \in \text{messages} : & \\
& \wedge m.type = MStartViewRequest \\
& \wedge \text{HandleStartViewRequest}(m.dest, m.src, m) \\
\vee \exists m \in \text{messages} : & \\
& \wedge \text{Discard}(m) \\
& \wedge \text{UNCHANGED } \langle \text{globalVars}, \text{clientVars}, \text{replicaVars} \rangle
\end{aligned}$$

$$Spec \triangleq Init \wedge \Box[Next]_{vars}$$

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