

## **Solutions Week 4: Global States**

### **Exercises**

15.

- (a) Provide the vector timestamps at each send, receive and concurrent event.
- (b) Provide an example of a consistent and inconsistent cut.

16. Consider the following: Two processes  $P$  and  $Q$  are connected in a ring using two channels, and they constantly rotate a message  $m$ . At any one time, there is only one copy of  $m$  in the system. Each process's state consists of the number of times it has received  $m$ , and  $P$  sends  $m$  first. At a certain point,  $P$  has the message and its state is 102. Immediately after sending  $m$ ,  $P$  initiates the chandy-lamport snapshot algorithm. Explain the operation of the algorithm in this case, giving the possible global state(s) reported by it.

17. Consider the following figure

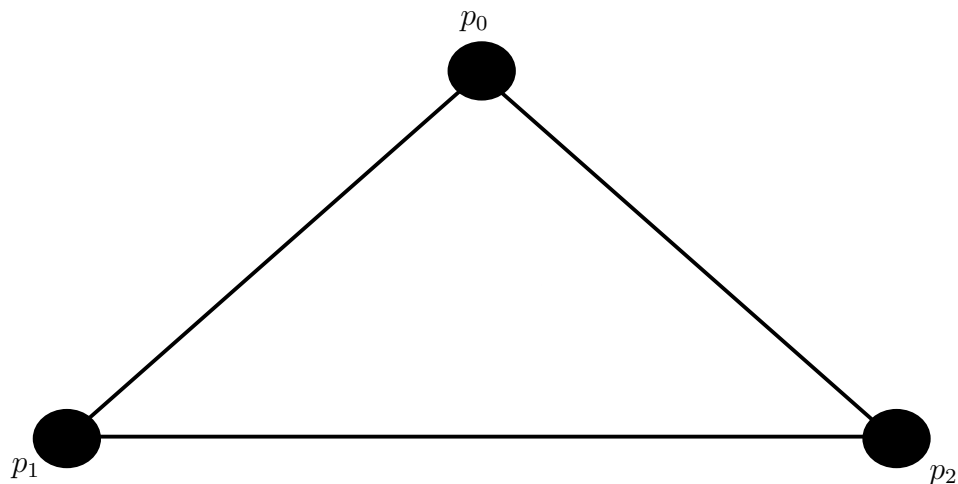


Figure 1: Channel complete communication with three processors

In the above system, each process calculates it's next message it will send, using the first message that exists in it's buffer as follows.

$$next(msg_i) = \begin{cases} \frac{msg_i}{2} & msg_i \bmod 2 = 0 \\ 3 \cdot msg_i + 1, & msg_i \bmod 2 = 1 \end{cases}$$

Likewise, each process  $m$  decides which corresponding neighbour  $k$  to send this message to as follows:

$$target(msg_i, m) = \begin{cases} (m + 1) \bmod 3 & msg_i \bmod 2 = 0 \\ (m - 1) \bmod 3, & msg_i \bmod 2 = 1 \end{cases}$$

Assume each node holds no local state, only processing it's buffer in a FIFO manner. Initially, each node has it's buffer contain a single value:

$$p_0 = \{50\}, p_1 = \{150\}, p_2 = \{450\}$$

- (a) After some sequence of messages, each nodes buffer is as follows:  $p_0 : \theta, p_1 : \{169, 58\}, p_2 : \{113\}$ . Is this a possible (globally consistent) state?

- (b) Assume in the above scenario, process  $p_0$  initiates the chandy-lamport snapshot algorithm. Explain the operation of the algorithm in this case, giving the possible global state(s) reported by it.

