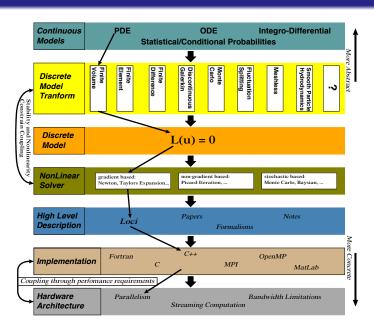
# A Tutorial for Loci

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#### What is Loci?

- Loci was originally developed in 1999 as part of National Science Foundation funding supporting the development of advanced multidisciplinary simulation software.
- Loci is a sophisticated auto-parallelizing framework that simplifies the task of constructing complex simulation software.
- Loci is free software available under the Lesser GNU Public License.
- The Loci paradigm is domain specific but powerful and able to capture a wide range of numerical application software.



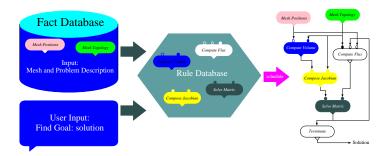
#### Loci and C++

- The *Loci* framework is built using the C++ language.
- A preprocessor (lpp) translates Loci code into the native C++ code
- Generally users of Loci only need to know a small amount of C++ to be effective
- It is possible to interface to external applications and subroutines such as Fortran, however this is an advanced topic and there can be many limitations particularly when executing in parallel

## What is a declarative programming model?

- Most traditional programming models are imperative, that is they are implicitly a list directions that will be performed in a specified order (e.g. How to solve a problem)
- Declarative programming models work by declaring properties of objects without specifying a recipe for solution. (e.g. focusing on describing the components that will solve the problem, but not how they will be used)
- In the declarative approach the assembly of components to solve the problem (the how) is determined by the application of logical inferences from the component specification.
- Getting used to thinking about problems in a declarative way is the main learning curve for Loci programming.

## **Declarative Programming in Loci**



## **Loci programming preliminaries**

- Most Loci programs will include "Loci.h"
- All Loci programs will need to be initialized and finalized
- When using MPI, calls to MPI initialization/finalization are not needed

#### **Loci Initialization Code**

```
#include <Loci.h>
int main(int argc, char *argv[]) {
   // Initialize Loci
  Loci::Init(&argc, &argv);
  // ...
  // Loci Program
  // ...
   // Call finalize for Loci clean up.
   Loci::Finalize();
   return 0 ;
```

### **Entities, Sets, and Sequences**

- Entities are an important concept in Loci
- Entities are what gives an object an identity in Loci
- All entities have a unique identifier and can be used to see which object we are addressing
- Groups of entities can be represented efficiently as a set called an entitySet
- A group of consecutively numbered entities can be represented in a compact form as an interval
- A ordered sequence of entities is called a sequence

### **Entity Sets**

- entitySet stores sets in a compressed form as a sorted sequence of non-overlapping intervals
- Thus the set A = 1,2,3,5,6,7,8,9,10,100 will be represented in an entitySet as
   ([1,3],[5,10],[100,100]).
- The UNIVERSAL set which includes all possible entities is represented with the special notation ([#, #]).
- The EMPTY set is represented as ()
- Set operations supported are Union (+), Intersection (&),
   Difference (-), Complement (~) (show EXAMPLE)

#### **Loci Containers**

- Loci provides methods for associating values with entities or associating entities with other entities.
- The data types that perform this association are called containers.
- Four main types of containers types include store, parameter, map, and constraint

store	parameter	index map	constraint
relates indices	relates many indices	relates indices	specifies a subset
to values	to a single value	to indices	of indices
0	n → 1	0 → m 0 → 0 0 → 0 0 → 0	88 88

#### **Container Themes**

- store<T>: associates value type T with entities
- storeVec<T>: associates n value typesT with entities
- multiStore<T>: associates variable number of types with entities
- Map: associates 1 entity per entity
- mapVec<n>: associates n entities per entity
- multiMap : associates variable number of entities per entity

### **Container Examples**

```
// We create a store of floats
store<float> x :
// We create a store of std::vectors
store<std::vector<float> > particles ;
// allocate stores x and particles
entitySet alloc_set = interval(1,100);
x.allocate(alloc set);
particles.allocate(alloc set);
// initialize the container to the value zero
for ( int i=0; i<101; ++i) {
  x[i] = 0;
  particles[i].push back(0);
```

## **Parameter Example**

```
param<real> Twall ; // Create wall temperature
Twall = 300 ;
// Constraint Twall to only apply to
// boundary entities (as given)
entitySet wallBoundary = interval(1000,1500) ;
Twall.set_entitySet(wallBoundary) ;
```

## **Constraint Example**

```
// set inflow constraint
constraint inflow;
*inflow = entitySet(interval(1,3));
constraint viscous;
*viscous = EMPTY; // default not set
if(mu_set) // if viscous set to
   *viscous = ~EMPTY; // UNIVERSE
```

#### **The Fact Database**

- The fact database is a repository for containers in the Loci Framework
- The fact database is used to define the initial facts that define the problem setup
- It is defined by the fact\_db data type in Loci
- Containers are added to the fact\_db using the create\_fact member function
- Containers can be retrieved from the fact\_db using the get\_fact member function.
- The fact database does a "shallow copy" of the containers.
   E.g. the reference to the container (called a storeRep) is what is actually stored.

#### What Are Rules?

- Rules are ways to express how one set of facts can be transformed into another set of facts
- Rules come in several forms:
  - default Default rules are used to define parameters that can be redefined in the vars file (text version of the fact database)
  - optional Optional rules tell Loci about the type of data that may be placed in the vars file. Since they do not have a default value their existence implies entry in the vars file.
  - pointwise A point by point application entity by entity
  - singleton Used to perform computations on the single values of parameters
  - unit and apply are used to form reductions

#### The Rule Database

- In Loci rules are used to define transformations from on set of values to another.
- Users develop applications in Loci by defining transformation rules (Much more on this later!)
- The rule database is used to create combined sets of rules that you wish to use to solve your problem.
- When rules are created in Loci they are automatically added to a list of rules to be processed. This list is called the global\_rule\_list.
- Rules can be added to the rule database by using the add\_rules member function. Typically this will look like rdb.add\_rules(global\_rule\_list);

### The Query

- In Loci applications are developed through making queries to the fact database using a prescribed set of rules.
- The application that is created as a result of the query depends on the data provide in the fact database (also called the *extensive* facts), the provided transformations, and the query.
- The schedule is generated through a process of generating derived facts (intensive facts)
- A schedule is generated by using the makeQuery call:

```
// Query for intensive fact 'temperature'
if(!Loci::makeQuery(rdb, facts, "temperature"))
  cerr << "query failed!" << endl ;</pre>
```

### **Loci Helper Classes**

- Loci provides helper classes that can simplify program development
- Helper classes include:
  - Array<T, n>
     Provides proper semantics for arrays suitable for storing in Loci containers. Do not put C++ arrays in containers!
  - vector3d<T>
     Provides operators for addition, scalar multiplication, dot and cross products
  - vector2d<T>
     Provides operators for addition, scalar multiplication, dot and cross products
- (Go through example)

### The options\_list class

- For many solvers inputs may be complex and hierarchical.
- The options\_list class is provided to help standardize the input of this sort of data.
- It is used in most Loci solvers for inputting boundary condition data.
- The general form is a list of assignments of values to named terms called options.
- In general the value assigned to a name may be a real number, a real number with units, a double, a string, a name, a list, or a function.
- Lists or functions may be viewed as a nested options list making the input method very powerful.

### options\_list member functions

- optionExists: Returns a true value of the provided name is in the list of attributes
- getOptionNameList: Returns a list of attributes that have definitions
- getOptionValueType: Returns the type of the data that was assigned to the attribute. This may be REAL, NAME, FUNCTION, LIST, STRING, BOOLEAN, or UNIT\_VALUE.
- getOption: Returns the value associated with the attribute. The second argument is the returned value and may be the types bool, double, string, or options\_list::arg\_list.
- getOptionUnits: This returns a double value in the requested units.

## A Simple Example: 1-D diffusion

Consider the finite volume method solution to this simple one dimensional diffusion equation:

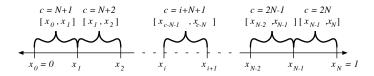
$$u_t = \nu u_{xx}, \ x \in (0,1), t > 0,$$
  $u(x,0) = f(x), \ x \in [0,1],$   $u_x(0,t) = g(t), \ \text{where } g(0) = f_x(0), \ \text{and}$   $u(1,t) = h(t), \ \text{where } h(0) = f(1).$ 

#### **Finite Volume Discretization**

- Divide the interval [0,1] into N-1 cells by defining N nodes such that  $x = \{(i,x_i)|i \in [0,\cdots,N], x_i = i/N\}$
- Cells are defined by their interfaces to the left and right:

$$il = \{(c, l) | c \in [N+1, \cdots, 2N], l = c - N - 1\},$$

$$ir = \{(c, r) | c \in [N+1, \cdots, 2N], r = c - N\}.$$



### **Indirection Operators**

- To implement the finite volume scheme we will need to be able to access values at interfaces, this will be done through composition
- For example, to access the left and right nodes of a given cell we could compose the interface maps with the x coordinates with the composition operator:

$$iI \to x = \{(c, x_I) | (c, I) \in iI, (I, x_I) \in x\}.$$

 Using this operator we can now define other attributes that will be needed to perform numerical integration such as the cell center:

$$x_c = (ir \rightarrow x + il \rightarrow x)/2.$$

## **Numerical Integration**

 Using a midpoint rule to numerically integrated in space and a first order explicit Euler integration for time, the numerical solution to the 1-D diffusion equation can be written as:

$$R(u) = \nu \frac{ir \to u_x - il \to u_x}{L}$$
$$u^{n+1} = u^n + \Delta t R(u^n)$$

# **Summary of Definitions for Diffusion Problem**

fact	meaning
$\nu$	given diffusion constant
f(x)	given initial condition
g(t)	given left bc
h(t)	given right bc
$\Delta t$	given time-step
X	$\{(i,x_i) i\in[0,\cdots,N],x_i=i/N\}$
il	$\{(c,l) c\in[N+1,\cdots,2N],l=c-N-1\}$
ir	$\{(c,r) c\in[N+1,\cdots,2N], r=c-N\}$
cl	$\{(i, l) i \in [1, \cdots, N], l = i + N\}$
cr	$\{(i,r) i\in[0,\cdots,N-1],r=i+N+1\}$

# **Summary of Transformation Rules**

Rule	Rule Signature	Equation
Rule 1	$x_c \leftarrow (ir, il) \rightarrow x$	(3.8)
Rule 2	$L \leftarrow (ir, il) \rightarrow x$	(3.11)
Rule 3	$u_{x} \leftarrow (cr, cl) \rightarrow (u, x_c)$	(3.13)
Rule 4	$u_x \leftarrow h, t, constraint\{dom(cl) \land \neg dom(cr)\}$	(3.14)
Rule 5	$u_x \leftarrow g, t, constraint\{dom(cr) \land \neg dom(cl)\}$	(3.15)
Rule 6	$R \leftarrow \nu, L, (ir, il) \rightarrow u_{x}$	(3.16)
Rule 7	$u^{n+1} \leftarrow u^n, R^n, \Delta t$	(3.17)
Rule 8	$u^{n=0} \leftarrow f, x_c, constraint\{(il, ir) \rightarrow x\}$	(3.19)

## Setting up the fact database

- First we create the maps and install them in the fact database (this is the 1-D mesh)
   Go through example online
- Then we can setup default parameters as a Loci program:

```
// How many nodes
$type N param<int>;
// diffusion coefficient
$type nu param<float>;
$rule default(N) { $N=50;}
$rule default(nu) { $nu = 1.0;}
```

### **Writing the Rules**

### Most of the rules translate directly into Loci rules:

```
// Rule 1: compute the cell center from
// node positions
$rule pointwise(xc<-(il,ir)->x) {
   $xc = .5*($il->$x + $ir->$x);
}
// Neuman boundary condition at left boundary,
// ux = h(t)
$rule pointwise(ux<-h), constraint(left_boundary) {
   $ux = $h;
}</pre>
```

### **Temporal Integration**

## The temporal iteration is then specified

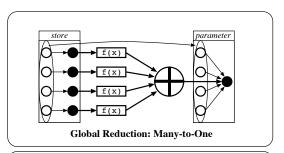
```
// Rule 7: initialization of iteration (build rule)
$rule pointwise(u{n=0}<-xc) {
   $u{n=0} = f($xc);
}

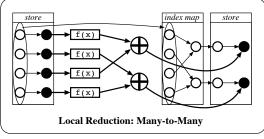
// Rule 8: time advance using explicit Euler time
   integration algorithm
$rule pointwise(u{n+1}<-u{n},dt{n},R{n}) {
   $u{n+1} = $u{n}+$dt{n}*$R{n};
}</pre>
```

### **Terminating The Iteration**

```
$rule pointwise(solution<-u{n}),</pre>
      conditional(simulation_finished{n}) {
  solution = su\{n\};
$type max_iteration param<int> ;
$type simulation_finished param<bool> ;
// When is iteration is complete?
$rule singleton(simulation finished<-</pre>
                                $n, max_iteration) {
   \$simulation finished = (\$$n >= \$max iteration) ;
```

### **Reduction Rules**





## Components of a reduction

- An operator that is associative (and commutative)
- A part that initializes values to the identity of the operator (the unit)
- A part the produces values that will be combined using the operator (the apply)

## **Stable Timestep Using Global Reductions**

```
$type dt param<float> ; // simulation timestep
$rule unit(dt), constraint(UNIVERSE) {
                                   // largest allowble timestep
                           $dt = std::numeric_limits<float>::max();
$rule apply(dt<-L,nu)[Loci::Minimum] {</pre>
                                    // Stable timestep
                                    float local_dt = \frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}+\frac{1}{2}
                                    // combine local with global
                                     join($dt,local dt);
```

#### **Some Pitfalls**

```
$rule apply(sum<-terms)[Loci::Summation] {
    // Error! Result depends on order of sum!
    if($sum < 1)
        join($sum,$terms);
}
$rule apply(sum<-terms)[Loci::Summation] {
    // OK, result is independent of summing order
    if($terms < 1)
        join($sum,$terms);
}</pre>
```

## **More Pitfalls**

```
$rule unit(sum), constraint(UNIVERSE){
    // Error, not identity of summation!
    $sum = 1.0;
}
$rule apply(sum<-terms)[Loci::Summation] {
    join($sum,$terms);
}</pre>
```

# Going to the Implementation

- After assembling the rules and facts we can see what kind of application Loci assembles
- Loci provides options that allow you to inspect what it has done. To see what type of program it will generate enter:

```
./heat --scheduleoutput --nochomp
```

 Loci will also perform different operations depending on what you query. The default query is "solution" but we can also get other schedules by querying other variables:

```
./heat --scheduleoutput --nochomp -q dt
```

Run and Inspect Example Code

### **Loci Reduction Alternative**

```
\label{eq:continuous} $$ \text{subspace}(xc<-(il,ir)->x) $$ \{ $xc = .5*($il->$x + $ir->$x) ; $$ \}$
```

#### Convert to use cl and cr maps instead:

#### Note: We cannot combine two apply rules into:

```
$rule apply((cl,cr)->xc <- x)[Loci::Summation]
{    join($cl->$xc,.5*$x) ;
    join($cr->$xc,.5*$x) }
```

### **Parametric Rules**

```
$type cellIntegrate(X) store<float>;
$type X store<float>;
$rule pointwise(cellIntegrate(X)<-(il,ir)->X) {
    $cellIntegrate(X) = $ir->$X - $il->$X;
}

// The 1d diffusion residue
$rule pointwise(R<-nu,cellIntegrate(ux),L)
    { $R = $nu*$cellIntegrate(ux)/$L;}

// We find the length of an interval by integrating the position x
$rule pointwise(L<-cellIntegrate(x)) { $L = $cellIntegrate(x);}</pre>
```

# Parametric unit/apply rules

```
// A general function for integrating over a cell boundary
$rule unit(cellIntegrate(X)),constraint(geom_cells) {
    $cellIntegrate(X) = 0;
}
$rule apply(cl->cellIntegrate(X)<-X)[Loci::Summation] {
    join($cl->$cellIntegrate(X),$X);
}
$rule apply(cr->cellIntegrate(X)<-X)[Loci::Summation] {
    join($cr->$cellIntegrate(X)<-X)[Loci::Summation] {
    join($cr->$cellIntegrate(X),-$X);
}
```

### **Parametric Time Iteration**

```
// X is the residual, Y is the independent variable
$tvpe EulerIntegrate(X,Y) store<float> ;
$tvpe X store<float> :
$type Y store<float> ;
$type Y_ic store<float> ;
// Initialize the iteration using the initial conditions
$rule pointwise(EulerIntegrate(X,Y){n=0}<-Y ic)</pre>
 $ $EulerIntegrate(X,Y){n=0} = $Y_ic; }
// Collapse iteration when finished
$rule pointwise(EulerIntegrate(X,Y) <-EulerIntegrate(X,Y) {n}),</pre>
                conditional(eulerTimestepFinished{n}) {
  $EulerIntegrate(X,Y) = $EulerIntegrate(X,Y){n};
// Condition for terminating the timestepping algorithm
$rule singleton(eulerTimestepFinished<-$n,max_iteration)</pre>
      $eulerTimestepFinished = ($$n >= $max iteration) ; }
```

### **Parametric Time Iteration**

Note the use of the parametric keyword in last rule!

# **Euler Integration**

```
// Setup the initial conditions
$rule pointwise(u_ic<-xc) {
    $u_ic = initialCondition($xc);
}

// Ask to solve the problem by using the Euler Integration
// on the function residual, integrating the variable u
$rule pointwise(solution<-EulerIntegrate(R,u)) {
    $solution = $EulerIntegrate(R,u);
}</pre>
```

### **Schedule**

```
Iteration Loop{n} {
    eulerTimestepFinished\{n\} < - \{n\}, max_iteration\{n\} \text{ over sequence } ([11,20])
    if (eulerTimestepFinished{n}) {
       EulerIntegrate(R,u) <-EulerIntegrate(R,u) {n}, CONDITIONAL(eulerTimestepFinished{n}) over</pre>
    } // if(eulerTimestepFinished{n})
        ----- Exit of Loop{n}
    if(eulerTimestepFinished{n}) break ;
    cellIntegrate(ux) {n}<-CONSTRAINT(geom cells{n}) over sequence ([11,20])
    u{n}<-EulerIntegrate(R,u){n} over sequence ([11,20])
    ux\{n\} < -(c\{n\}, cr\{n\}) > (u\{n\}, xc\{n\}) over sequence ([1.9])
    ux\{n\} < -cl\{n\} > (u\{n\}, xc\{n\}), ub\{n\}, x\{n\}) over sequence ([10,10])
    cr\{n\} \rightarrow cellIntegrate(ux)\{n\} \leftarrow ux\{n\} \text{ over sequence } ([0,9])
    cl{n}->cellIntegrate(ux){n}<-ux{n} over sequence ([1.10])
    R\{n\} < -L\{n\}, cellIntegrate(ux)\{n\}, nu\{n\} over sequence ([11,20])
    EulerIntegrate (R, u) \{n+1\} < -\text{EulerIntegrate}(R, u) \{n\}, R\{n\}, dt\{n\} \text{ over sequence } ([11, 20])
} // {n}
solution <- Euler Integrate (R.u) over sequence ([11,20])
```

### A Three Dimensional Solver

- Next example is an implicit three dimensional heat solver
- Solves the equation  $\frac{\partial}{\partial t}(\rho e) = \nabla \cdot (k \nabla T)$
- Using standard FVM methods this becomes the discrete equation:

f∈faces

$$\mathcal{V}_{c} \frac{Q^{n+1} - Q^{n}}{\Delta t} = R(Q^{n+1}),$$
 $R = \sum_{i} \left[ \mathcal{A}_{f} k \left( \nabla T_{f} \cdot \vec{n}_{f} \right) \right].$ 

# The Implicit Formulation

• The residual can be linearized using Taylor's theorem:

$$R(Q^{n+1}) = R(Q^n) + \frac{\partial R(Q)}{\partial Q} \Delta Q + O(\Delta t^2),$$

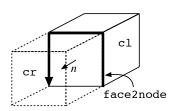
• which can then be used to form the following implicit form:

$$\left[\frac{\mathcal{V}_{c}}{\Delta t}I - \frac{\partial R(Q)}{\partial Q}\right]\Delta Q = R(Q).$$

 For this example we will be using the FVM facilities provided for Loci including mesh readers and a module of operators such as gradients.

# **Provided Data Structures**

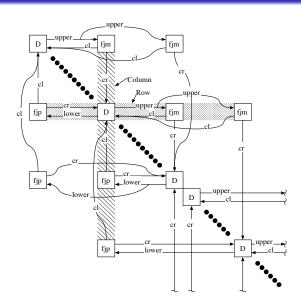
Fact	Туре	Location	Description
pos	store <vector3d></vector3d>	nodes	Node Positions
face2node	multiMap	faces	Nodes that form a face
cl	Map	faces	cell left of face
cr	Map	faces	cell right of face
ref	Map	boundary faces	map to referring category
boundary_names	store <string></string>	boundary categories	boundary category name
geom_cells	constraint	physical cells	set of actual cells
cells	constraint	cells	cells including ghost cells



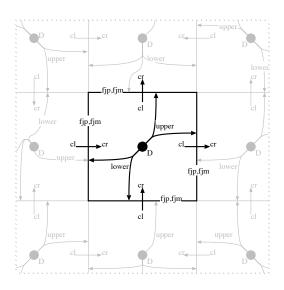
## database setup

```
rule db rdb ; // Create the rule database
rdb.add_rules(global_rule_list); // Add any user defined rules;
// Load in the finite-volume module called "fym"
Loci::load module("fvm",rdb);
// First read in user defined facts
string varsFile = "heat.vars";
facts.read vars(varsFile,rdb) :
// Next read in the grid file
string file = "heat.xdr"
if(!Loci::setupFVMGrid(facts,file)) {
  cerr << "unable to read grid file '" << file << "'" << endl ;
  Loci::Abort();
// Deconstruct boundary_conditions variable
setupBoundaryConditions(facts);
// Setup Matrix
createLowerUpper(facts) :
```

# **Matrix Setup**



# **Matrix Cell View**



# **Boundary Condition Rule Setup**

```
// Extract Twall from boundary condition options
$rule pointwise(Twall<-BC_options), constraint(Twall_BCoption) {
    $BC_options.getOptionUnits("Twall", "kelvin", $Twall);
}

// Temperature at wall set to specified condition
$rule pointwise(temperature_f<-ref->Twall), constraint(specified_BC) {
    $temperature_f = $ref->$Twall;
}

// Handle Boundary Conditions
// Adiabatic Wall, qdot = 0, grad(temperature) = 0
$rule pointwise(adiabatic::qdot), constraint(adiabatic_BC) {
    $qdot = 0;
```

### **Residual Evaluation**

```
// Compute the heat flux through faces
$rule pointwise(qdot<-conductivity,grads_f(temperature),area) {</pre>
 $qdot = $area.sada*$conductivity*dot($qrads_f(temperature),$area.n)
// Add up contributions from all faces, only define gresidual
$rule unit(gresidual).constraint(geom cells) {
 $gresidual = 0 ;
// Add to left cell
$rule apply(cl->gresidual<-gdot)[Loci::Summation],</pre>
 constraint(cl->geom_cells) {
  join($cl->$gresidual,$gdot);
// Add to right cell, note sign change due to normal pointing to cell
$rule apply(cr->gresidual<-gdot)[Loci::Summation],</pre>
 constraint(cr->geom_cells) {
  join($cr->$gresidual,-$gdot);
```

# **Residual Evaluation: Missing Part**

```
// Compute boundary temperatures for gradients
// adiabatic, dT/dx = 0, so copy temperature from cell to face
$rule pointwise(temperature_f<-cl->temperature),
    constraint(adiabatic_BC) {
    $temperature_f = $cl->$temperature;
}

// Temperature Specified Wall
$rule pointwise(temperature_f<-ref->Twall),constraint(specified_BC) {
    $temperature_f = $ref->$Twall;
}
```

## **Matrix Preliminaries, derivatives**

$$\frac{\partial \dot{q}}{\partial Q_I} = \frac{\partial \dot{q}}{\partial T_I} \frac{\partial T_I}{\partial Q_I} = \frac{\mathcal{A}_f k}{(\vec{x}_I - \vec{x}_r) \cdot \vec{n}_f} \frac{\partial T_I}{\partial Q_I},$$

and

$$\frac{\partial \dot{q}}{\partial Q_r} = \frac{\partial \dot{q}}{\partial T_r} \frac{\partial T_r}{\partial Q_r} = -\frac{A_f k}{(\vec{x}_l - \vec{x}_r) \cdot \vec{n}_f} \frac{\partial T_r}{\partial Q_r}$$

```
// Derivative of flux from left side
$rule pointwise(dqdotdQ1<-conductivity,(c1,cr)->cellcenter,area,c1->dTdQ) {
    real distance = dot($c1->$cellcenter-$cr->$cellcenter,$area.n);
    $dqdotdQ1 = $area.sada*$conductivity*$c1->$dTdQ/distance;
}

// Derivative of flux from right side
$rule pointwise(dqdotdQr<-conductivity,(c1,cr)->cellcenter,area,cr->dTdQ) {
    real distance = dot($c1->$cellcenter-$cr->$cellcenter,$area.n);
    $dqdotdQr = -$area.sada*$conductivity*$cr->$dTdQ/distance;
}
```

# **Matrix Assembly**

```
// To compute the diagonal term, we first must sum the diagonal
// contributions from the flux derivatives.
$type sumDiagonal store<real> :
// Add up diagonal contributions from flux derivatives
$rule unit(sumDiagonal), constraint(geom cells) { $sumDiagonal = 0 ;}
// Add contribution from face to left cells
// (e.g. d R(Ol,Or)/d Ol goes to diagonal of the left cell)
$rule apply(cl->sumDiagonal<-dqdotdQl)[Loci::Summation],</pre>
  constraint(cl->geom_cells) {
  join($cl->$sumDiagonal,$dgdotdQl);
// Add contribution from face to right cells
// (e.g. d R(Ol,Or)/d Or goes to diagonal of the right cell)
// Note sign change due to normal pointing into the cell
$rule apply(cr->sumDiagonal<-dgdotdQr)[Loci::Summation],</pre>
  constraint(cr->geom cells) {
  join($cr->$sumDiagonal,-$dgdotdOr);
$rule pointwise(heat D<-sumDiagonal,deltaT,vol) {</pre>
  $heat D = $vol/$deltaT - $sumDiagonal ;
```

# **Matrix Assembly**

```
$rule pointwise(heat B<-gresidual) {</pre>
 // Compute matrix lower term from flux derivatives
// Note, we are subtracting del R/del Q in the matrix so there is an
// extra sign change here
$rule pointwise(heat L<-dqdotdOl) {</pre>
 $heat L = $dqdotd01;
// Compute matrix upper term from flux derivatives
$rule pointwise(heat_U<-dqdotdQr) {</pre>
 // Solve linear system described by heat_B, heat_D, heat_L, heat_U
$rule pointwise(deltaQ<-petscScalarSolve(heat)) {</pre>
 $delta0 = $petscScalarSolve(heat) ;
```

## **Time Integration**

```
// Initial Conditions
$rule pointwise(O{n=0}<-Density,Cp,T initial) {</pre>
 $O{n=0} = $Densitv*$Cp*$T initial ;
// Advance the timestep using linear system solution
$rule pointwise(Q{n+1}<-Q{n},deltaQ{n}), constraint(geom_cells) {</pre>
 0{n+1} = 0{n} + delta0{n};
// Determine when we will finish timestepping
$rule singleton(finishTimestep<-$n,stop iter) {</pre>
 $finishTimestep = ($$n > $stop_iter);
// Collapse to solution when we are finished iterating
$rule pointwise(solution<-Q{n}),conditional(finishTimestep{n}),</pre>
 constraint(geom cells) {
 solution = solution :
```

# **Closing the Equations**

```
// Compute temperature from energy
$rule pointwise(temperature<-Q,Density,Cp), constraint(geom_cells) {
   $temperature = $Q/($Density*$Cp);
}
// Compute transformation derivative from temperature to Q
$rule singleton(dTdQ<-Density,Cp) {
   $dTdQ = 1./($Cp*$Density);
}</pre>
```

# **Running the case**

Run the case!