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Factor Interpreter: Arithmetic
                     FACTOR INTERPRETER
-- An interpreter for a subset of the language Factor, comprising:
     integers, and the operators . + - * / % drop dup lift sink
type Token = String
type Stack = [ Integer ]
-- factor fileName : interpret the Factor program in 'fileName'
factor :: String -> IO ( )
factor fileName = do
                    source <- readFile fileName
                    putStr ( "SOURCE = " ++ source )
                    putStr ( "RESULT = " ++ eval source )
-- eval source : the result of interpreting the program in 'source'
eval :: String -> String
eval source = eval' ( words source ) [ ]
-- eval' tokens stack : the result of interpreting the token list 'tokens'
                     using the stack 'stack'
eval' :: [ Token ] -> Stack -> String
eval'[]
                  = ""
eval' ( t : ts ) stack = if isInteger t then
                           eval' ts ( read t : stack )
                        else
                        case t of
                          "." -> let ( s1 : ss ) = stack in
                                      show s1 ++ " " ++ eval' ts ss
                                 -> eval' ts ( apply'plus stack )
                                 -> eval' ts (apply'minus stack)
                           11 * 11
                                 -> eval' ts ( apply'times stack )
                                 -> eval' ts ( apply'div stack )
                                 -> eval' ts (apply'mod stack)
                           "drop" -> eval' ts ( apply'drop stack )
                           "dup" -> eval' ts (apply'dup stack)
                           "lift" -> eval' ts ( apply'lift stack )
                           "sink" -> eval' ts (apply'sink stack)
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-- isInteger t : does 't' represent an integer constant ?
isInteger :: Token -> Bool
isInteger ( '-' : t ) = isNonNegInteger t
-- isNonNegInteger t : does 't' represent a non-negative integer constant ?
isNonNegInteger :: Token -> Bool
isNonNegInteger t = ( t /= "" ) && ( all ( c -> c >= '0' && c <= '9' ) t )
-- apply'* stack : apply the corresponding operator to the top of stack 'stack'
apply'plus, apply'minus, apply'times, apply'div, apply'mod,
          apply'drop, apply'dup, apply'lift, apply'sink
   :: Stack -> Stack
apply'plus (s1:s2:ss) = (s2 + s1):ss
apply'minus (s1:s2:ss) = (s2-s1): ss
apply'times ( s1 : s2 : ss ) = ( s2 * s1 ) : ss
apply'div (s1:s2:ss) = (s2'div's1):ss
apply'mod (s1:s2:ss) = (s2'mod's1): ss
apply'drop (s1:ss)
                         = ss
apply'dup (s1:ss)
                        = s1 : s1 : ss
apply'lift ( k : ss ) = lift k ss
apply'sink (k:ss)
                      = sink k ss
-- lift k stack : the stack 'stack', with its 'k'th item now up on top
lift :: Integer -> Stack -> Stack
                = ss
lift k (s1 : ss) = s' : s1 : ss' where (s' : ss') = lift (k - 1) ss
-- sink k stack : the stack 'stack', with its top item now down in position 'k'
sink :: Integer -> Stack -> Stack
sink 1 ss
                   = 88
sink k (s1:s2:ss) = s2:sink (k-1) (s1:ss)
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**Factor Interpreter : Arithmetic** > factor "prog1" SOURCE = 2 3 + 4 \*. RESULT = 20 > factor "prog2" SOURCE = 2 3 4 \* + . RESULT = 14 > factor "prog3"
SOURCE = 7 3 / 7 3 % - . RESULT = 1 > factor "prog4" SOURCE = 4 3 2 1 dup 4 lift 5 sink drop . . . . RESULT = 1 2 4 3