

# Analysis and comparison of matrix vector multiplication codes

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# Introduction

- Kernel:  $\text{result}[i] = \text{result}[i] + A[i,j] * \text{vector}[i]$
- Matrix size changing:  $n_1 = 40$ ,  $n_2 = 400$ ,  $n_3 = 1000$
- Different optimization flags
- What is Eigen? How to change the kernel to match its performance?

# Tools

- Stream → Bandwidth 6000 MB/s
- LIKWID: topology and perfctr
- Hardware: Interlagos 12-core Opteron processor.

# Roofline model

- Performance model used to determine bottlenecks: bandwidth and algorithm performance.
- $P_{max} = f_{max} * \frac{n_{operations}}{n_{cycles}} * v$
- $P = \min(P_{max}, \text{Bandwidth} * \text{Computational intensity})$
- Computational intensity is algorithm dependent, the main focus is to maximize it.

# Naive

- Simplest possible code, useful for benchmark.
- $P_{max} = \frac{2.6}{8} \frac{Gflops}{s}$ , not exploiting pipelines of sum and product
- Computational intensity =  $\frac{2}{32} \frac{Flops}{Bytes}$

# Temporary variable

- Additional temporary variable in outer loop to speed up cache lookup
- $P_{max} = \frac{2.6}{8} \frac{Gflops}{s}$ , still not exploiting pipelines of sum and product
- Computational intensity =  $\frac{2}{16} \frac{Flops}{Bytes}$

# Loop unrolling

- Manually split two loops four by four to exploit pipelines of sum and product
- $P_{max} = 2.6 \frac{Gflops}{s}$
- Computational intensity =  $\frac{32}{160} \frac{Flops}{Bytes}$
- Peaked at assembly code to understand inner functionalities



# Comparing the Mflops/s

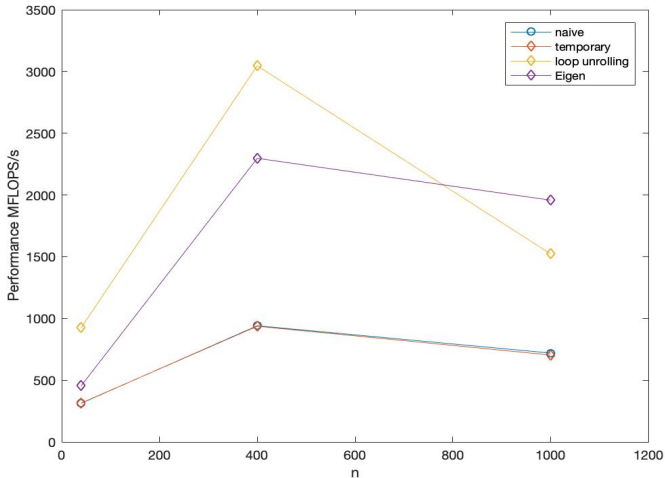
O0	naive	with_tmp	loop unrolling	eigen
n = 40	195	204	313	59
n = 400	328	332	453	70
n = 1000	327	328	445	94

O1	naive	with_tmp	loop unrolling	eigen
n = 40	302	255	882	464
n = 400	948	345	2346	2339
n = 1000	740	344	1544	1922

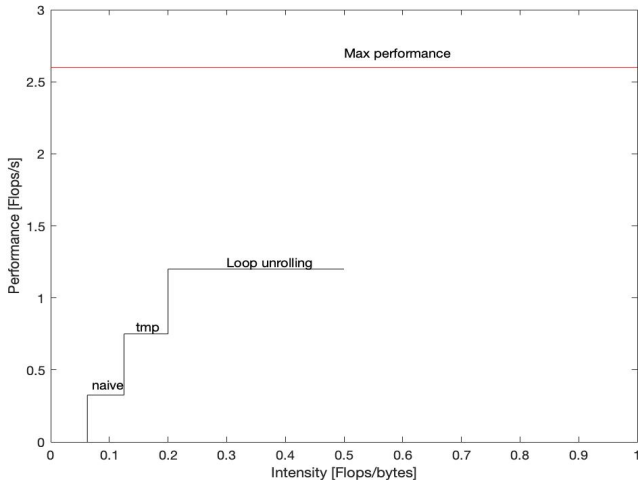
O2	naive	with_tmp	loop unrolling	eigen
n = 40	313	315	926	455
n = 400	941	937	3046	2297
n = 1000	720	704	1523	1958

O3	naive	with_tmp	loop unrolling	eigen
n = 40	315	321	915	383
n = 400	936	961	2935	3429
n = 1000	761	766	1538	2024

# Data visualization



# Roofline graph

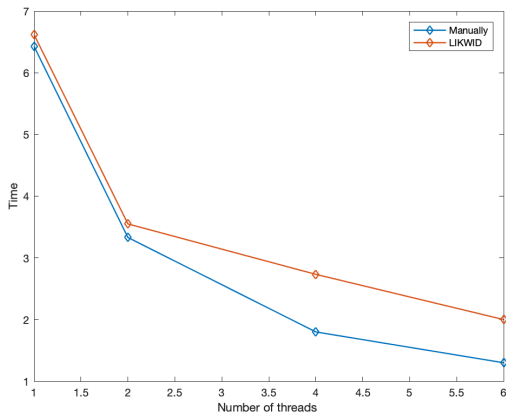


# What is OMP?

- API that supports multi-platform shared memory multiprocessing.
- Used for parallelism within a multi-core node.
- Based on threads: processes that can share memory.

# Case study

With  $n = 50000$ , *O3* flag and different number of threads:



# Achievements

- Outperformed Eigen when  $n = 40$
- Outperformed Eigen when  $n = 400$  and O2 flag.

# Future directions

- Cache aware roof line model
- SIMD vectorization
- Understanding GCC behaviour when matrix is saved in L1