

[**N.B.** – The figures of the right margin indicate full marks. Read the stems carefully and answer the associated questions. Answer any **FIVE** questions taking at least two questions from each group]

Group - A

1. $P(A|B) = \frac{1}{8}, P(A) = \frac{1}{2}, P(B) = \frac{1}{5}$
- (a) What is a compound event.

(b) Find $P(A \cap B)$.

(c) Find $P(A|\bar{B})$.

(d) Are the probabilities $P(A|B)$ and $P(B|A)$ equal? Justify
2. In a survey of 150 people, it is found that 70 own a car, 90 own a house, and 50 own both.
- (a) What is a certain event?

(b) What does it mean when events are mutually exclusive?

(c) Are the events of owning a car and owning a house independent?

(d) If a person is selected randomly, and if they do not own a house, what is the probability that they own a car?
3. The probability density function of a continuous random variable is
- $$f(x) = \begin{cases} f(z) = \frac{2}{9}(3z - z^2); 0 \leq z \leq 3 \\ 0, & otherwise \end{cases}$$
- (a) What is the formula of cumulative distribution function for a continuous variable

(b) Compute the definite integral of x^2 from 0 to 3.

(c) Examine whether the probability density function is appropriate.

(d) Find the probability that the value of z is not more than 2.

Group - B

4. A random variable is distributed as below:
- $$P(X) = \frac{3 - |4 - x|}{k}; x = 2, 3, 4, 5, 6$$
- (a) What is the Expectation equivalent to?

(b) Find the value of k.

(c) Determine the value of the expectation.

(d) Find $V(2X - 1)$
5. The probability density function (pdf) of a continuous random variable is given below:
- $$f(x) = \frac{1}{30}(k + 2x); 2 < x < 5$$
- (a) What is a random variable?

(b) Is probability a discrete variable? Explain in brief.

(c) Find the value of k.

(d) Determine the expectation and variance.

6. The monthly sales (in units) of laptops at a major electronics store are recorded below:

Month	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug
Sales	120	150	130	170	160	180	200	210

- (a) Give an example of a time series data.1
- (b) What are the components of Time Series?2
- (c) Compute the trend using a three-monthly moving average method.3
- (d) Illustrate the trend graphically and estimate the expected laptop sales for September.4

“Absence of evidence is not evidence of absence. ”
– Carl Sagan

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Group - A

1. A jar contains 5 red marbles and 7 yellow marbles. Three marbles are drawn at random.
- (a) What is a sample space?

1
- (b) In how many ways can 3 books be chosen from a set of 8 books?

2
- (c) What is the probability that all marbles are yellow?

3
- (d) What is the probability that a marble has a different color?

4
2. An unbiased coin is tossed 10 times.
- (a) If a coin is flung 3 times, how many outcomes are generated?

1
- (b) If a coin is flung n times, show how many outcomes are generated.

2
- (c) What is the probability of getting a) at least 3 heads, b) at most 3 heads?

3
- (d) Are these probabilities equal? a) Getting at least 2 heads & b) Getting at least 2 tails.
Also justify logically.

4
3. The probability density function of a continuous random variable is
- $$f(x) = \begin{cases} k(x + 1), & 0 \leq x \leq 1 \\ 0, & otherwise \end{cases}$$
- (a) What is a random variable?

1
- (b) Find the value of k

2
- (c) Find the probability that the values of x would lie between 0 and 0.5.

3
- (d) What is the probability that X is greater than 0.8?

4

Group - B

4. The joint probability function of two random variables X & Y is given below:

$$P(x, y) = \frac{1}{21}(x + y); x = 1, 2, 3 \text{ \& } y = 1, 2$$

- (a) What is a probability density function (pdf)?

1
- (b) What is P(X=a) in a pdf, where a is an arbitrary number?

2
- (c) Find the marginal probabilities.

3
- (d) Find $P(x|y)$, $P(x|1)$ and $P(y|4)$

4
5. The probability distribution of a random X is provided below:
- | | | | | | |
|------|----------------|---------------|---------------|---------------|----------------|
| X | -1 | 0 | 1 | 2 | 3 |
| P(x) | $\frac{3}{20}$ | $\frac{1}{5}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{3}{20}$ |
- (a) What is the expectation of a constant m?

1
- (b) Find $E(X)$.

2
- (c) Find $E(Y)$, where $Y = \frac{X}{2}$

3
- (d) Find Variance of $(2X+3)$.

4

6. Bangladesh foreign debt has been increasing rapidly in recent years. The Bangladesh bank provides the follwoing data.

Fiscal Year	2015-16	2016-17	2017-18	2018-19	2019-20	2020-21	2021-22	2022-23	2023-24
Debt	41.17	45.81	56.01	62.63	68.55	81.62	95.45	98.94	~130.00

- (a) Name the components of time series.1
- (b) What are linear and non-linear trends?2
- (c) Find 3-yearly moving avergae from the data and plot.3
- (d) Whaich components of time series may underlie the data? Analyze.4

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