Getting started with Alpha

Api, then Cosi, then R2D2 and Compsys, then Cairn* Revision of January 2, 2009

June 2004

Abstract

This document is an introduction to the Alpha language and to its use for regular program description, transformation, evaluation, and hardware implementation in the MMAlpha software. The Alpha syntax is presented by means of examples. Basic manipulations of Alpha programs are first shown. Then hardware generation and several advanced transformations – pipelining, change of basis, substitution, normalization, and scheduling, – are introduced and illustrated. Finally, the use of Alpha subsystems and the Alphard hardware description language are presented.

1 Introduction

This document¹ should be read by all Alpha beginners. It briefly presents the main features of the Alpha language and the basic transformations of Alpha programs which are available in the MMAlpha environment.

MMALPHA is a free software, available under the Gnu Public License. What is said here applies to Version 2.0 or MMALPHA, which currently you may get by sending a mail to

patrice.quinton@irisa.fr

To be run, it requires Mathematica version 3.0 or later.

If you have any problem while reading this document or while trying the MMALPHA software, please send an e-mail to alpha@irisa.fr

\$MMALPHA/doc/Quickstart/AlphaStart.tex

and this file is in

\$MMALPHA/doc/QuickStart/AlphaStart.pdf

^{*}Api, Cosi, R2D2 and Cairn are the names of the research groups that successively hosted research related on Alpha and MMAlpha at Irisa, Rennes, France. From 2001, Compsys in ENS Lyon also participated in the development of MMAlpha. Recently, Tanguy Risset moved to Insa de Lyon.

¹The source of this document is in:

What is Alpha?

Alpha is a functional data parallel language invented at Irisa in Rennes (France). The first definition of Alpha was proposed by Mauras [Mau89] in 1989. The original motivation was to provide a language for expressing algorithms in an extended version of the formalism of recurrence equations proposed by Karp, Miller and Winograd [KMW67]. Other basic references are [Mol82, Qui84, RF86]. The goal of Alpha is to provide a high-level tool for the synthesis of parallel regular VLSI architectures.

Although Alpha stands for the language itself, it is often also associated with the environment in which it is currently developed: MMAlpha. MMAlpha is an interface based on the Mathematica software from which one can manipulate Alpha programs.

MMALPHA is still under development at Irisa and at INSA in Lyon (France).

What is Alpha for?

ALPHA is a research tool for various computer science fields such as functional language semantics, parallelization, code generation, optimization, polyhedral theory, VLSI synthesis, systolic arrays, etc.

One important long term goal of Alpha is to promote the use of high-level functional languages for the synthesis of (parallel) VLSI architectures. From the short term, Alpha can be useful for:

- Providing a correct recurrence equation specification for a particular algorithm (see Sections 4 and 5).
- Simulating such a specification (see Section 5.6).
- Transforming and simplifying a recurrence equation specification (see Sections 5 and 7).
- Computing on convex polyhedra (see also http://www.irisa.fr/polylib).
- Scheduling programs and detecting parallelism (see Section 5.7).

If you are ready to invest a little more time on MMALPHA, you will probably be able to:

- Generate VHDL from this description.
- Provide a design path from the high-level functional specification of an algorithm to the layout description of a VLSI algorithm which implements it.

The remaining of this document is organized as follows. Section 2 presents the MMAL-PHA interface; Section 3 explains the installation procedure; in Section 4, the Alpha language is briefly presented, while in Section 5, basic operations on Alpha programs are described; hardware generation is presented in Section 6; in Section 7, other transformations of Alpha programs are explained, and in Section 8, we explain how structured Alpha programs can be structured and transformed. Finally, Section 9 concludes and gives some additional references for further exploration of MMAlpha.

2 How does MMALPHA work?

MMALPHA is written in C and in Mathematica, but a user should only see it through its Mathematica interface.

Mathematica provides an interpreted language with high-level built-in functions for symbolic computations: MMALPHA uses these facilities for transforming ALPHA programs. Mathematica embeds also a general-purpose programming language.

The basic principle of the MMALPHA environment is the following one: Mathematica stores an internal representation of an Alpha program (called Abstract Syntax Tree or AST) and performs computations on this internal representation via the user's commands or functions. These commands can be for example: view an Alpha program, check its correctness, generate C code to simulate it, generate VHDL code, etc. All these transformations are done on the AST which is stored in a Mathematica variable named \$result.

Specific C functions are used for two purposes: parse and unparse Alpha programs or expressions, and perform computations on polyhedra. All C functions are called via Mathematica. Most of them are available separately in the POLYLIB polyhedral library which constitutes the computationnal kernel of the MMALPHA environment. Mathematica also uses the PiP software designed by Paul Feautrier (See http://www.piplib.org/).

3 Installing MMALPHA

Before going on, you should install the MMALPHA environment. The installation procedure is explained in Appendix 3 of this document. MMALPHA can be downloaded from the MMALPHA web site (http://www.irisa.fr/cosi/ALPHA).

The easiest way to use MMALPHA is to access it through its notebook interface. To do so, type mathematica under Unix, or start Mathematica in the Programs menu of Windows NT². We assume in the following that you use Mathematica through its Notebook interface.

Once MMALPHA is installed, open a new Mathematica notebook and evaluate the command start[] in this notebook³. This command opens a demonstration notebook which is part of the MMALPHA distribution.

Then open the synthesis notebook by clicking on the Synthesis button (in the Section called *New: synthesis notebooks*⁴). In this notebook, you will find several demonstrations examples: a FIR filter, a distance calculation program, a matrix-vector multiplication, a matrix-matrix multiplication, and a string alignment program called Samba. Currently, the documentation on the syn command is available in

\$MMALPHA/doc/Synthesis/Synthesis.pdf

²Any Mathematica version later than 3.0 will work.

³Type the command, then press simultaneously the Shift and Enter keys.

⁴For the reader who is not yet familiar with Mathematica's notebooks, notebooks are organized as a tree of cells. Each cell is delimited by a brackets at its right. Selecting a cell (and all its subcells) is done by clicking once its bracket. To open a cell, double-click the bracket once the cell is selected.

Another possibility is to open the cell named "Introduction Notebooks", and click on button "Getting started". This opens a notebook where all the examples of this document are shown.

4 The Alpha language

In this section, we present the syntax of the Alpha language.

4.1 Alpha through examples

We introduce here the basic features of the language on the matrix-vector multiplication example shown in Fig. 1.

```
system prodVect: {N | N>1}
  (a : {i,j|1 <= i,j <= N} of integer;
  b : {i|1 <= i <= N} of integer)
returns (c : {i|1 <= i <= N} of integer);
var
  C : {i,j|1 <= i <= N; 0<= j <=N} of integer;
let
  C[i,j] =
    case
    {|j=0} : 0[];
    {|j>=1} : C[i,j-1] + a[i,j] * b[j];
    esac;
  c[i]=C[i,N];
tel;
```

Figure 1: Alpha program describing the matrix vector product

Systems, variables, domains and parameters

An Alpha program is a *system*. Alpha variables⁵ are generalized arrays which can have any shape (not just rectangles). The set of indices of the array is called the *domain* of the variable. Example 4.1 below shows the declaration of a variable **a** whose domain is the set of points (i, j) in the triangle $\{0 \le i \le j; j \le 10\}$.

Exemple 4.1

⁵In Alpha, identifiers are case sensitive. Undescores are accepted, as in A₋₁ but *should be avoided*, as Mathematica identifiers cannot contain undescores and in some situations, this may result in unexpected errors. Moreover, avoid using variables that are distinguished only by there case, as in x and X; since eventually, your program will be translated in VHDL that is not case sensitive.

```
a : \{i, j \mid 0 \le i \le j; j \le 10\} \text{ of integer}
```

In the example of Fig. 1, domains are indexed by a parameter N which is declared, together with its domain, right after the system name. The values of the parameters can be constrained by any kind of affine constraints. In general, parameters allow generic descriptions of algorithms to be specified.

Input, output and local variables

An Alpha system has input and output variables. Here inputs are a and b, and output is c. It may have local variables, such as C here. Local variables are declared after the keyword var.

Equations and expressions

Each variable is defined by a unique equation which usually has the form of a recurrence equation.

The case construct allows one to define different values in different parts of the domain.

Exemple 4.2

```
a[i,j] =
  case
  {| j = 0 } : 0[];
  {| j > 0 } : a[i,j-1]+1[];
  esac;
```

The Alpha expression of example 4.2 defines the values of a[i,0] to be zero⁶ and recursively defines a at all other points in its domain. This equation defines a variable a such that a[i,j]=j.

In Fig. 1, variable C is also defined as a recurrence equation, and its value at point (i, j) is $\sum_{j=1}^{j=i} a_{i,j} \times b_j$.

4.2 Array notation and standard notation

The above equations use the so-called *array notation* of Alpha. The real syntax of Alpha is sligthly less readable but more consistent and logical from a semantic point of view. To illustrate this, example 4.3 shows the same definition of a in standard notation.

Exemple 4.3

⁶Syntactic note: constants are zero dimensional arrays hence the empty brackets in O[].

```
a =
   case
   {i,j | j = 0 } : 0.(i,j -> );
   {i,j | j > 0 } : a.(i,j -> i,j-1) + 1.(i,j -> );
   esac;
```

In such an expression, a denotes a variable, i.e., a function whose type is

```
integer \times integer \rightarrow integer
```

Expression (i, j->i, j-1) denotes a dependence function, i.e., the affine function

```
integer \times integer \rightarrow integer \times integer
```

which maps (i,j) to (i,j-1). Expression expr = a.(i,j-i,j-1) denotes the composition of a and the dependency function (i,j->i,j-1). In other words, expr[i,j] has the value a[i,j-1] at each point (i,j) such that (i,j-1) is in the domain of a.

Similarly expr2 = 0.(i,j-) means that expr2[i,j] has value 0 for all (i,j). This notation describes the extension (or broadcasting) of the constant 0 to all integral points (i,j) of the space.

An expression such as $\{i,j \mid j > 0\}$: a.(i,j->i,j-1) + 1.(i,j->) represents the restriction of expression a.(i,j->i,j-1) + 1.(i,j->) to the domain $\{i,j \mid j > 0\}$ (functions of ALPHA are partial).

Finally, expr = case exp1; exp2; esac denotes a case definition, where exp1 and exp2 are expressions on disjoint domains.

In summary, any Alpha expression is either a variable, the composition of a variable and of a dependence function, a restriction, or a case statement⁷.

Note that the order of the equations as well as the order of the expressions in a case statement is meaningless as Alpha is declarative: interchanging the two branches of the case in example 4.2 would define exactly the same value for a.

The evaluation order is implicit and there are tools for finding schedules for a given program. As Alpha is a functional language, the only constraint that any evaluation order must follow is that data dependencies between instances of variables must be respected. In example 4.2, obviously a[i,j] must be computed after a[i,j-1].

4.3 More on the syntax of Alpha

Section 8 describes structured Alpha programs. More details on the syntax of Alpha can be found in appendix A. Note that Alpha is case sensitive, and that underscores are allowed in identifiers. Avoid using underscores, as you might get into trouble when trying to generate VHDL for example.

⁷There exists another construct, the use statement, which allows calls to subsystems to be written. This statement is explained in section 8.

5 Basic operations on Alpha programs

This section presents the first commands that you should learn in order to deal with ALPHA programs.

Write an Alpha program (such as the one of Fig. 1 for instance) using your favourite text editor.

Let us say you called this file prodVect.alpha. The commands described in this section allow you to load your program in Mathematica, view the program in Mathematica (array notation or standard notation), save the program in another file, perform a static analysis and simulate the program.

All these examples are also available in the Getting started notebook accessible by the Master notebook of MMALPHA (after starting Mathematica, type the Mathematica command start[] in your notebook to access the Master notebook of MMALPHA.)

If you are not familiar with Mathematica, the Introduction notebooks section of the Master notebook points towards a brief introduction to Mathematica.

5.1 Loading and viewing an Alpha program

Once Mathematica has been started, commands can be send to the kernel through Input cells. The name of the working directory can be printed out by typing:

Directory[]

If you see that this directory is not the one where you have put prodVect.alpha, change it by typing:

SetDirectory["pathname"]

where pathname is the directory that you want to become the current directory of MMALPHA (see the Mathematica Help or type ?Directory).

You can now load the Alpha program into Mathematica by typing:

load["prodVect.alpha"];

Note that most often, it is useful to end MMALPHA commands with a semi-colon. Indeed, MMALPHA commands are Mathematica functions, which return the AST of a transformed Alpha program. If you forget the ; symbol, Mathematica just displays the result of the function evaluation, which may sometimes take a few pages...

As a side effect, the load command assigns the AST of the parsed program to the global Mathematica variable **\$result**. In general, **\$result** contains the result of the most recent transformation.

Troubleshooting Syntax errors in Alpha programs are sometimes difficult to understand. Here is a list of frequent errors.

- In domains, inequalities are separated by semicolons, not colons. For example: {i | i<10 ; i> 20 }. Notice that the domain {i,j | 1< i,j <20 } represents the domain $\{i,j|1 < i < 20 \land 1 < j < 20\}$, as the colon allows inequalities to be factorized.
- Input variables are separated by semicolons.
- All equations (even the last one) are ended by a semicolon.
- All branches of a case (even the last one) are ended by a semicolon.
- In the array notation, indexes of a right-hand side expression should appear in the right-hand side variable. For example, a[i,j] = b[k] is wrong, as k is not an index of a. Note that indexes represent positions, not absolute names. It is perfectly possible to use different index names in the declaration of a variable, and in its definition, although this is a bad practice...
- Constants, such as 1[] end up with brackets; boolean constants are true[] and false[].
- Restrictions on branches of a case expression start with {|.

Bugs The div operator is available, but should be replaced by a simple /. The asave function forgets to add a space after the div operator, so that a div 2[] becomes a div2[]...

5.2 Viewing Alpha programs

You can view the program that has been stored in **\$result** by evaluating:

ashow[]

By default, ashow pretty prints the program contained in \$result in array notation, but more generally, ashow[var] pretty prints the program contained in the Mathematica variable var.

To display a program in standard notation use the show[] command.

5.3 On-line documentation and options

All Mathematica functions have an on-line documentation: ?ashow gives the help on ashow. Commands may also have options. Type Options[command] to list the options of command together with their default value.

The documentation of MMALPHA is far from complete. Documentation notebooks are in directory

\$MMALPHA/doc/packages/

and demos notebooks are available in

\$MMALPHA/demos/NOTEBOOKS/

Documentation notebooks can be accessed using the command docLink["topic"], and demos can be open using demoLink["demo"]: both commands paste an active button in the current notebook. Try for example

demoLink["Getting-started"]

5.4 Saving a program

To save the Alpha program in a file, use the command asave (or save which saves in standard notation). For instance:

```
asave["myFile.alpha"]
```

writes the program of Fig. 1 in file myFile.alpha in the current directory. This command is useful in order to save the content of \$result after some transformations.

5.5 Analyzing an Alpha program

Now that you have loaded an Alpha program, you can start working on it. Your first action should always be to check it for so-called *static errors* by using the **analyze** command:

analyze[]

Information about potential errors in the Alpha program is printed out.

If the analysis is successful, the result is **True**. The static analyzer of Alpha does essentially two kinds of verification: it checks the type of all expressions – this is not a fantastic novelty – but it also checks that variables are defined in any point of their definition domain. This second kind of verification is very powerful, and is much more original.

Notes.

- It is very important that your program passes successfully the analyze test. Indeed, some transformations assume that the program is correct.
- Correcting the mistakes of an Alpha program may sometimes be difficult. Especially hard to fix are errors involving values of the parameters. Do not hesitate to send a program to alpha@irisa.fr if you have some trouble: experts will try to help you!
- The analyze command allows structured systems to be checked by means of the recurse option. See ?recurse.

Troubleshooting If you use non conventional types, such as signed or unsigned short integer (denoted as integer [S,5] for example), analyze is unable to check the type correctness of expressions. Use the option scalarTypeCheck -> False option to avoid error messages.

More information A notebook giving more details on the static analyzer can be accessed using demoLink["Static"].

5.6 Simulating a program

The second step of your design flow should be a simulation. To do so, you should first schedule the program, then generate a C program ⁸.

First, schedule the program by evaluating the command

schedule[]

This command should give you a schedule of the program, unless there is a dependence cycle in the program, or the program does not have a unidimensional schedule (see section 5.6 for more information on the scheduler.)

If the scheduler is successful, a C program can be generated using cGen:

```
cGen["prodVect.c", {"N"-> 10}]
```

The {"N"-> 10} argument indicates that the value of the parameter N will be set to 10 (the C code generator is not parameter independent). If there are more than one parameter, they are given in a list such as {"N"-> 10, "M" -> 32, ...}. By default, this program, once compiled, reads its input from the standard input (stdin) and prints its results on the standard output (stdout).

On Unix, gcc -o prodVect prodVect.c followed by ./prodVect will compile, then execute the simulated program in the current directory. By default, this program will prompt you for the values of the input instances.

Notes Options of cGen allow various forms of C programs to be generated. See the documentation notebook on code generation (demoLink["cGen"]).

Troubleshooting As already mentioned, the scheduled may fail for several reasons.

If your program describes an infinite calculation (for example, a filter), the scheduler will fail to find a schedule, as by default, it tries to minimize the total computation time. You can get a schedule by using the command

```
schedule[ optimizationType -> Null ]
```

⁸Several C code generators are available. As of the date of the current revision of this document, the simplest one is cGen, and we do not present the other ones here.

Note that infinite calculations can also be represented by Alpha programs where the iteration domain is bounded by a parameter. This avoids the above problem.

Your program may not admit a unidimensional schedule. To check this, call it with the appropriate option

schedule[multiDimensional -> True];

You may then get a result, where variables are ordered with a multi-dimensional time. The C-code generator also works with multi-dimensional schedules.

If this is not successful, your program may contain a dependence cycle. Checking this property is undecidable, and therefore, nothing can be done to help you. In general, this happens because the program contains an error, and a careful check of the equations reveals it. (Removing some equations before scheduling may help localizing the fault(s).)

More on C program generation See the demoLink["CodeGen"] notebook.

5.7 Scheduling

Principles The schedule command looks for a schedule for an Alpha program. The basic goal of the scheduler is to find a valid and good evaluation order. Here, the term *good* depends on the optimization criterion chosen: most often, it is the total evaluation time of the program, but one may also consider other criteria.

The time is considered as a discrete single rate clock. The overall idea of the scheduling process is to build a linear program (LP) and to solve it with a software tool: this may be PiP[FT90], or LP-Solve, or even the Mathematica linear solver. The Alpha scheduler provides several options to schedule a program. We consider here the simplest one (by default), called *monodimensional affine-by-variable schedule*. This esoteric name means that the evaluation date $T_{\rm A}(i,j)$ of a given variable instance A[i,j] is given by an affine function of the indices and parameters:

$$T_{\mathbf{A}}(i,j) = \tau_{\mathbf{A}}^{i}i + \tau_{\mathbf{A}}^{j}j + \tau_{\mathbf{A}}^{N}N + \alpha_{\mathbf{A}}$$

where N is a parameter of the Alpha program. The coefficients τ_{A}^{j} of this function are (in general) different for each variable in the system.

As already seen, the Mathematica command to schedule a program is:

schedule[]

By default, it schedules **\$result** and the resulting schedule is placed in a global variable named **\$schedule**. To visualize the current content of the **\$schedule** variable, use the command **showSchedResult**[]. The **schedule** function has many options. Type **Options**[schedule] for further information. Type **schedule**[opt1->value1] to change the default value of a particular option opt1.

Refining the schedule Once a monodimensional schedule is found, the scheduler may be used to refine the schedule, in order to obtain a "good" architecture. Two options can be used to do so.

The addConstraints option allows one to fix the values of the coefficients of a particular timing-function, or even to set the timing-function of a variable. Say for example, that you want the a variable to be available at time $\tau_{\mathbf{a}}(i,j) = i+j$, and the b variable to be available at time $\tau_{\mathbf{b}}(i) = i$, then use the command

```
\label{eq:constraints} $$ -> {$$$$$$$$$} Ta[i,j,N]=i+j", "Tb[i,N]=i"} ]
```

where Ta[i,j,N]=i+j sets the schedule of a and Tb[i,N]=i sets the schedule of b. Notice that the parameters – here N – must be included in the indexes of the timing-functions.

The addConstraints option allows also coefficients to be set. Coefficient $\tau_{\mathbf{A}}^{j}$ of the timing-function of a variable A is named TADj, and constant $\alpha_{\mathbf{A}}$ is named CA. To constrain the scheduler to set the first coefficient of the timing-function of a and the constant of the same timing-function to be 1, evaluate:

```
schedule[ addConstraints -> {"TaD1==1", "Ca==1"} ]
```

The durations option allows one to fix the number of cycles needed to evaluate a given equation of the Alpha program. With the current version of the scheduler, the durations option allows you to specify how many time steps you allocate to the evaluation of one equation. Say for example that you would like to associate a duration of 7 to the evaluation of C and of 19 to the evaluation of c. Then you should use

```
schedule[ durations -> {0, 0, 19, 7} ]
```

The list of integer values corresponds to the input variables first, then the output variables (in their order of appearance in the header of the program), then the local variables (in their order of declaration), {a, b, c, C} in our example. (Notice that assigning a duration to input variables is meaningless.)

How to schedule Here is a typical approach to schedule a program.

- Use the plain **schedule**[] command first. It will immediately reveal if the program has a unidimensional schedule, in which case, *la vie est belle...*
- Remember that if your program describes an infinite calculation, you should set the optimizationType parameter to Null, or bound your iteration space in the Alpha program.
- If this does not provide a schedule, use the multi-dimensional option to find a multi-dimensional schedule. But notice that MMALPHA cannot generate hardware for a multi-dimensional schedule... At least, you will be able to simulate the Alpha program.
- Once a schedule has been found, refine it by adding constraints to the coefficients.

Troubleshooting The scheduler is probably the most important step of the design flow. As already seen, the scheduler is unable to find out a schedule if the program does not admit a mono-dimensional schedule, or, if the program contains dependence cycles.

Currently, MMALPHA does not generate hardware for multi-dimensional scheduled programs⁹.

The scheduler is quite robust, and not too slow. For very big programs, it is better to use structured programs, and to use the structured scheduler (see section 8).

Be careful if you use additional constraints or durations: you may specify constraints that cannot be met by the scheduler...

A frequent mistake: if you specify in the additional constraints a wrong coefficient, the scheduler fails badly with a quite non specific message. For example, say you add a constraint such as:

TAD4 == 1

although variable A has only 2 dimensions, then the scheduler fails, since it does not check the correctness of this constraint and therefore, calls Mathematica's optimizer with wrong arguments.

More information The schedule function is explained in more detail in the scheduler documentation given in file:

\$MMALPHA/doc/Users/Scheduler_user_manual.pdf

5.8 Mapping the program to a parallel array

Once a schedule (either mono or multi-dimensional) has been found, the program can be mapped to an architecture using the appSched function, for example:

appSched[]

The plain form rewrites the **\$result** program by applying space-time transformations to all variables in such a way that the first component of the index is the time, and the other components represent the coordinates of a processor (also called, the allocation function).

Notes When appSched is called in its simplest form, the allocation function is chosen automatically by MMALPHA. Sometimes, this allocation is not convenient. For example, it may happen that the processor dimension is mapped to an infinite dimension of the calculation domain.

Some options of appSched allow one to set the allocation direction. The projMatrix option allows one to define the projection matrix, that is to say, the linear function which defines the indices where the processor are mapped. For example:

⁹This is planned, but not yet realized...

```
appSched[ projMatrix -> {{1,0,0}, {0,0,1}} ]
```

says that the processor indexes will be the first and the third one (assuming that there is no parameters.)

The projVector option is another way of specifying the allocation function:

```
appSched[ projVector -> {{0,1,0}} ]
```

also projects on indexes 1 and 3.

Both projVector and projMatrix can be used only when all variables have the same dimension and are in the same space.

If necessary, one can apply appSched variable by variable, by using the variables option. For example:

```
appSched[ variables -> {"A", "b"}, projMatrix -> {{1,0,0}, {0,0,1}} ]
```

applies the projection only on variables A and b.

Another way of specifying the allocation function is to define what index has to be replaced by the schedule. For example:

```
appSched[ timeDimensions -> {2} ]
```

says that the second dimension of the variables can be replaced by the schedule.

This way of specifying the projection can be combined with the variables option:

```
appSched[ variables -> { {"A",{2}}, {"b",{1}}, {other,{3}} ]
```

specifies that for variable A, the second dimension has to be replaced by the schedulig, for variable b, the first dimension, and for the other variables, the third dimension.

If none of these possibilities works, the ultimate solution is to do the change of basis by hand. Help may be obtained by running

```
appSched[ verbose->True ]
```

as this command will list the changes of bases that are applied.

Troubleshooting Remember that no change of basis can be done on input or output variables! Indeed, the change of basis preserves the semantics of an Alpha program, and this is not compatible with a reindexing of inputs or outputs. If you really want to reindex inputs or outputs, just add local variables where you copy the inputs or store the outputs.

6 Generating Hardware

Once a system is scheduled and allocated, generating hardware can be done in the following way.

First, transform the program into Alpha0, a subset of the language:

toAlpha0v2[];

After execution of toAlpha0v2, \$result contains one single program, whose expressions can be interpreted as hardware components.

It is often a good idea to clean-up a little bit the program after execution of toAlphaOv2. One can simplify the system by the command

```
simplifySystem[ alphaFormat -> Alpha0 ]
```

Be careful not to forget the alphaFormat option, as otherwise, the simplification would destroy the case expressions which represent multiplexers.

Warning: do not remove identity equations using

```
removeIdEqus[];
```

as it would remove the so-called $mirror\ equations$ that were added by toAlphaOv2 for the outputs of the system.

Then rewrite it into Alphard, using the command:

alphaOToAlphard[];

After this command, the program becomes a set of structured systems contained in \$library, and \$result contains the main subsystem (see also Section 8 for more information on structured systems). Fix the value of the parameters:

```
fixParameter[ "N", 10 ];
```

Finally, generate VHDL code

a2v[]

Function a2v generates in the current directory one VHDL file for each subsystem of \$library, except maybe the main subsystem which cannot be translated into VHDL.

To see the VHDL code in the notebook, get as the current system the subsystem that you want to see (getSystem[name]), then evaluate showVhdl[].

Troubleshooting Functions to Alpha 0v2 and alpha 0To Alphard require the program in \$result to meet very specific constraints, and fail if these constraints are not met.

toAlphaOv2 requires that \$result has been scheduled and allocated.

alphaOToAlphard has to be executed after toAlphaOv2 (and cannot be executed twice!). If the outputs of the system are not mirror equations (of the form out = var or out = var.dep) it will fail. If all equations do not have the same dimension, both toAlphaOv2 and alphaOToAlphard will fail.

a2v will almost always fail on the main calling system which cannot be translated into VHDL: you can just ignore this error message. An alternative is to remove the calling subsystem of \$library, before calling a2v.

The most common problem with a2v is that the parameter values are not fixed: then a2v fails to produce the controler and the modules. To see this, just display the current system using ashow.

To generate a VHDL file for only one subsystem of the library, get this subsystem as the current system using getSystem, then run a2v[\$result].

Notes Recently, to Alpha Ov2 and alpha OTo Alphard were extended in order to accept that some subsystems and/or variables are kept untouched. For example

```
toAlphaOv2[ exceptions -> {sys, var} ]
```

ignores all uses of subsystem sys as well as the definition of var. In a similar fashion

```
alpha0ToAlphard[ exceptions -> {sys, var} ]
```

will put in the interface system (i.e., the calling program) all uses of subsystem **sys** as well as the definition of **var**. This works only if the use is without extension, and if the inputs of the use are simple variables.

7 Other transformations of Alpha programs

In this section we briefly review a few more advanced manipulations of Alpha.

7.1 Pipelining

Pipelining is a transformation widely used in systolic synthesis. It is also called *localization* or *uniformization*. It consists basically of replacing a broadcasted value by the pipeline of this value through all the computations that need it.

For instance, in the program of Fig. 1, we see (last term in the second branch of the case expression) that b[j] is used for the computation of C[i,j] for all $i, 0 \le i \le N$. This means that b[j] will be broadcasted to all processors computing C[i,j].

To introduce a new variable B1 which will pipeline the b[j] value from the computation of C[j,0] to C[j,1], ..., C[j,N], we use the following command:

```
pipall["C", "b.(i, j->j)", "B1.(i, j->i+1, j)"];
```

In this expression, the first argument is the variable whose equation is to be modified, and the second argument is the expression to be pipelined (standard notation is mandatory here) and the last argument indicates the *direction* of the pipeline (i,j->i+1,j) as well as the name B1 of the new variable introduced. After the execution of this command, the program contained in \$result is the one shown in Fig. 2. Note that the direction of pipeline gives the dependence vector of the pipeline, and not the flow direction of the pipelined variable (see the definition of B1 in Fig. 2.)

```
system prodVect :{N | 2<=N}</pre>
  (a : \{i, j \mid 1 \le i \le N; 1 \le j \le N\} of boolean;
   b : \{i \mid 1 \le i \le N\} \text{ of boolean}\}
returns (c : {i | 1<=i<=N} of boolean);
var
  B1 : \{i, j \mid 1 \le i \le N; 1 \le j \le N; 2 \le N\} of boolean;
  C: \{i,j \mid 1 \le i \le N; 0 \le j \le N\} \text{ of boolean};
let
  B1[i,j] =
       case
          {| i=1; 1<=j<=N; 2<=N} : b[j];
          \{ | 2 \le i \le N; 1 \le j \le N \} : B1[i-1,j];
  C[i,j] =
       case
          {| j=0} : False[];
          \{|1 <= j\} : C[i,j-1] + a[i,j] * B1;
       esac;
  c[i] = C[i,N];
tel;
```

Figure 2: Alpha program of Fig. 1 after pipelining of b in the definition of C

Unlike previous transformations, pipelining changes the Alpha program, but the resulting program is equivalent to the initial one. The modifications performed automatically by pipeAll are:

- 1. Determine the domain of B1 and add a declaration for it.
- 2. Build the definition of B1 based on the dependency (i,j->i+1,j) and the given initialization equation (here, b.(i,j->j)).
- 3. Replace the original expression b.(i,j->j) by B1.

Related functions pipeline, pipeInfo, pipeVars.

Troubleshooting The pipeline transformations are difficult to use, as they are not intuitive.

7.2 Change of basis

The change of basis is another important transformation in systolic array design. It allows variables to be re-indexed, and is often used to map indices to time and space.

In the example of Fig. 2, suppose that we wish to express the computations in a new index basis i', j' such that i'=i+j, j'=j. We can perform the following change of basis:

```
changeOfBasis["C.(i,j->i+j,j)"];
```

This simply indicates that the transformation is to be applied to variable C and that the new coordinates in term of the old ones are given by the linear function (i,j->i+1,j). Note that a change of basis is meaningful only if this linear function admits an integral left inverse: in this example, its left inverse is obviously (i,j->i-1,j). The resulting program is shown in Fig. 3 (after its normalization).

```
system prodVect :{N | 2<=N}</pre>
                    (a : \{i,j \mid 1 \le i \le N; 1 \le j \le N\} of boolean;
                     b : \{i \mid 1 \le i \le N\} \text{ of boolean}
                   (c : {i | 1<=i<=N} of boolean);
var
  B1 : \{i, j \mid 1 \le i \le N; 1 \le j \le N; 2 \le N\} of boolean;
  C : \{i,j \mid j+1 \le i \le j+N; 0 \le j \le N\} of boolean;
  B1[i,j] =
       case
          {| i=1; 1<=j<=N; 2<=N} : b[j];
          \{|\ 2 \le i \le N;\ 1 \le j \le N\} : B1[i-1,j];
       esac;
  C[i,j] =
       case
          {| j=0} : False[];
          \{|1 \le j\} : C[i-1, j-1] + a[i-j, j] * B1[i-j, j];
       esac;
  c[i] = C[i+N,N];
tel;
```

Figure 3: Alpha program of Fig. 2 after the change of basis on C

Notes The changeOfBasis transformation can be used to rename the indexes of a variable, for example:

```
changeOfBasis[ "C.(t,p->t,p)" ]
```

It can also be used to place a local variable in a higher-dimensional space. For example

```
changeOfBasis[ "C.(i,j->i,j,1)", {"i","j","k"} ]
```

will add one dimension to the local C variable, and let its indexes become i, j and k. Finally, note that changeOfBasis returns an non normalized program.

More information See the ChangeOfBasis notebook docLink["ChangeOfBasis"].

7.3 Substitution

Substitution allows a variable occurrence to be replaced by its definition. For example:

```
substituteInDef[ "c", "C" ]
```

substitutes the definition of C in equation defining c.

Notes. The substitution does not normalize the program.

Troubleshooting. The substitution should normally be restricted by the context domain of the expression, but this is not done... Sometimes, the result is not correct.

More information ... available using docLink["Substitution"].

7.4 Normalization

The normalization transformation simplifies an Alpha program into a particular normal form called *case-restriction-dependency*. This function is very useful when one performs several automatic transformations that may render the program less and less readable. The command is simply:

```
normalize[];
```

Another useful command is

```
simplifySystem[];
```

which normalizes and simplifies a program.

More information See the Normalization notebook (docLink["Normalization"].)

8 Structured Alpha programs

Alpha programs can be structured: this section explains how this can be done.

8.1 Simple structures

Let us write an Alpha program for the addition of two integers (or fixed-point numbers) expressed as bit vectors. A binary adder is classically described as a sequence of *full adder* operations with the propagation of a carry bit from one full adder to the next one, as shown in Fig.4.

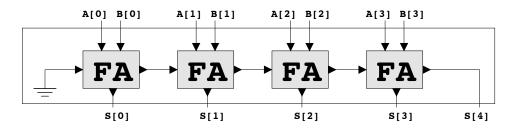


Figure 4: Addition of two integers (coded as bit vectors), using full adders.

The following Alpha system describes a full adder:

To build an adder using this program, we need to instanciate a collection of such systems, as shown in Fig.4. The shape of this collection may be expressed as the Alpha domain { b | 0<=b<W } where W is a size parameter giving the number of bits of the adder.

The **use** construct of Alpha allows precisely that. The following system describes in Alpha the adder given in Fig. 4:

```
-- 10
    esac;
  use {b| 0<=b<W} FullAdder[] (A,B,Cin) returns(X, Cout);</pre>
                                                                             -- 11
  S[b] =
                                                                             -- 12
                                                                             -- 13
    case
       \{ \mid b < W \} : X;
                                                                             -- 14
       \{ | b=W \} : Cout[W-1];
                                                                             -- 15
                                                                             -- 16
    esac;
                                                                             -- 17
tel;
```

In this system, line 11 reads as follows:

"Use (or instantiate) a collection of instances of the subsystem FullAdder. This collection has the shape of the extension domain $\{ b \mid 0 \le b \le W \}$ and is thus indexed by index b. Let the inputs of the b-th instance be the variables A, B and Cin at point b, and similarly let the outputs of this collection of instances be the variables X and Cout."

Lines 6-10 describe the carry propagation, and lines 12-16 define the output of this binary adder.

In other words, line 11 is a shortcut for the following equations, which are those of the system FullAdder whith the dimension of the variables extended from zero to one:

```
X[b] = A[b] \times B[b] \times Cin[b];
Cout[b] = (A[b] \text{ and } B[b]) \text{ or } (A[b] \text{ and } Cin[b]) \text{ or } (B[b] \text{ and } Cin[b]);
```

Note. In general, the extension indexes are added *to the left* of the existing indexes. This cannot be seen in this example, since the full adder subsystem has no indexes.

8.2 Handling structured programs

A structured program is stored in MMALPHA as a Mathematica list of systems called a *library*. The default library is stored in the global variable \$library.

A structured program may be written in one single file or several distinct files. In the former case the load[] function returns a library composed of all the systems contained in the file, and stores this library in \$library.

In addition, two functions, putSystem[] and getSystem[], may be used to get a system from a library as the current system \$result, and conversely and to put back a modified system into a library. Typically a system is extracted from the library as the *current* system, modified by some program transformation, and then put back in the library.

The commands to be used are getSystem[] and putSystem[].

8.3 Program transformations associated with structures

Most MMALPHA functions handle parameterized programs and use statements. There are, however, some major exceptions such as the cGen translator which generates code only for

flat Alpha programs without subsystems. MMAlpha provides functions to transform a structured program into a flat equivalent one:

- assignParameterValue[] gives a value to a size parameter, i.e. it refines a generic system into a specialized one.
- inlineSubSystem[] expands a *use* statement, replacing it with the equations of the corresponding subsystem, properly modified to take the dimension extension into account.
- inlineAll[] recursively flattens a structured Alpha program. inlineAll[exceptions->{sys}] inlines all subsystems but those whose names appear in the exception list.

More on subsystems For more information see the subsystem documentation in file \$MMALPHA/doc/Users/SubSystems.pdf

If you are interested in scheduling structured subsystem, see an example in the More section of the Master notebook.

Troubleshouting There is a nasty bug in inlineSubSystem and inlineAll. If you try to inline, with extension, a scalar equation, this equation must be given in standard notation, not in array notation. In Example 8.1, the equation in the called system must not be written out[] = 2[] + in[].

Exemple 8.1

```
system called (in: integer) returns (out: integer);
let
   -- This works
   out = 2.(->) + in;
tel;
system caller : {N | N>=1}
   (v: {i| 0< i <= N} of integer)
   returns (w: {i| 0< i <= N} of integer);
let
   use {i| 0<i<=N} called (v) returns (w);
tel;</pre>
```

9 And now?

In this document, we have presented a few possibilities of MMALPHA. You should now know if you are interested in using the MMALPHA software.

If this is the case, you will find in the Alpha distribution some additional examples. See appendix C.

References

- [AC97] Api-Cosi. MMAlpha Reference Manual, 1997.
- [BQRR98] S. Balev, P. Quinton, S. V. Rajopadhye, and T. Risset. Linear programming models for scheduling systems of affine recurrence equations a comparative study –. In 10th ACM Symposium on Parallel Algorithms and Architectures (SPAA), 1998.
- [DQR95] F. D. De Dinechin, P. Quinton, and T. Risset. Structuration of the alpha language. In W.K Giloi, S. Jahnichen, and B.D. Shriver, editors, *Massively Parallel Programming Models*, pages 18–24. IEEE Computer Society Press, 1995.
- [dRR97a] F. de Dinechin, T. Risset, and S. Robert. Hierarchical static analysis for improving the complexity of linear algebra algorithms. In *Parallel computing*, 1997.
- [DRR97b] Florent Dupont De Dinechin, Sophie Robert, and Tanguy Risset. Structured scheduling of recurrence equations. Technical Report 1140, IRISA, Rennes, France, 1997.
- [FT90] Paul Feautrier and Nadia Tawbi. Résolution de systèmes d'inéquations linéaires; mode d'emploi du logiciel pip. Technical Report 90-2, Institut Blaise Pascal, UPMC, Laboratoire MASI, January 1990.
- [KMW67] R.M. Karp, R.E. Miller, and S. Winograd. The organization of computations for uniform recurrence equations. *Journal of the ACM*, 14(3):563–590, July 1967.
- [Mau89] C. Mauras. Alpha: un langage équationnel pour la conception et la programmation d'architectures parallèles synchrones. PhD thesis, Université de Rennes 1, IFSIC, December 1989.
- [Mol82] D.I. Moldovan. On the analysis and synthesis of VLSI algorithms. *IEEE Transactions on Computers*, C-31(11), November 1982.
- [QRR96] P. Quinton, S. V. Rajopadhye, and T. Risset. Extension of the Alpha language to recurrences on sparse periodic domains. In *Int. Conf. on Application Specific Array Processors*, 1996.
- [QRR97] P. Quinton, S. V. Rajopadhye, and T. Risset. On manipulating z-polyhedra using a canonical representation. *Parallel Processing Letters*, 7(2):181–194, June 1997.
- [Qui84] P. Quinton. Automatic synthesis of systolic arrays from recurrent uniform equations. In 11th Annual Int. Symp. Computer Arch., Ann Arbor, pages 208–214, June 1984.
- [RF86] S.V. Rajopadhye and R.M. Fujimoto. Systolic array synthesis by static analysis of program dependencies. Technical report, University of Oregon, 1986.

A Definition of ALPHA

A.1 Meta Syntax

```
phrase*===zero or more repetitions of phrase.phrase1 | phrase2===alternation, either phrase1 or phrase2.[...]===optional phrase.(...)===syntactic grouping.bold===a terminal.Italic===a non-terminal.
```

A.2 Systems

Program stands for a library of Alpha programs. PDecl (or SystemDecl) is a single system. Name is a system name. ParamDecl is the declaration of a parameter domain. InputDeclList is the list of input declarations. OutputDeclList is the list of output declarations. LocalDeclList is the list of local declarations.

ParamDecl :: Domain

 $\begin{array}{lll} InputDeclList & :: & VarDeclList \\ OutputDeclList & :: & VarDeclList \\ LocalDeclList & :: & VarDeclList \end{array}$

A.3 Declarations of variables

VarDeclList stands for a variable declaration. Notice that scalar types have been extended to special hardware types, such as integer [S,10] – a signed 10 bit integer – or integer [U,10] – an unsigned 10 bit integer.

```
VarDeclaration * :: VarDeclaration * 
VarDeclaration :: IdentifierList : [ Domain of ] ScalarType ;
```

ScalarType :: integer | real | boolean

A.4 Domains

Domain stands for a domain declaration. IndexList is a list of indexes, and ConstraintList a list of constraints.

Notice that operations on domains such as intersection (&), union (|), complement () and preimage by an affine function are allowed. The parser does the corresponding operation.

I am not sure that the convex syntax, nor the domain expressions fully work...

ConstraintList is a list of constraints, each one being an increasing constraint, a decreasing constraint, or an inequality.

```
Domain
                       { IndexList | ConstraintList }
                  ::
                       Domain | Domain
                       Domain & Domain
                       Domain . Affine Function
                       ~ Domain
                       Domain .convex
                       ( Domain )
IndexList
                       [ IndexList , ] Identifier
                  ::
ConstraintList
                       [ ConstraintList; ] Constraint
                  ::
Constraint
                       IncreasingSeq | DecreasingSeq | EqualitySeq
                  ::
IncreasingSeq
                       ( IncreasingSeq | IndexExpList ) ( < | <= ) IndexExpList
                  ::
DecreasingSeq
                          DecreasingSeq | IndexExpList ) ( > | >= ) IndexExpList
                  ::
EqualitySeq.
                  ::
                          EqualitySeq | IndexExpList ) = IndexExpList
```

A.5 Equations

Equationblock is the block of equation declarations. Equation represents an equation, which can be either in array notation (when the lhs has the form var[...]) or in standard notation. An equation can also be a use statement. ¹⁰

¹⁰I am not sure of the syntax for the paramAssignation with the dot...

ParamAssignation:: AffineFunction

InputList :: [InputList ,] Expression

ExtensionDomain :: Domain

A.6 Expressions

Expressions can be case expressions, if statements¹¹, restrictions, affine dependencies, binary operations, unary operations, and reductions¹²

```
Expression :: case ExpressionList esac
```

if Expression then Expression else Expression

Domain: Expression

Expression . AffineFunction Expression [IndexExpList] Expression BinaryOp Expression

BinaryOp (Expression, Expression)

UnaryOp Expression

reduce (CommutativeOp , AffineFunction , Expression)

(Expression)

Identifier Constant

ExpressionList :: [ExpressionList] Expression;

BinaryOp :: $CommutativeOp \mid RelativeOp \mid - \mid div \mid mod$

CommutativeOp :: + | * | / | and | or | xor | min | max

RelativeOp :: = | <> | < | <= | > |

UnaryOp :: - | not | sqrt

Constant :: IntegerConstant | RealConstant | BooleanConstant

A.7 Dependance Functions and Index Expressions

AffineFunction stands for affine functions.

AffineFunction :: (IndexList -> IndexExpList)

¹¹Alpha conditional statements are strict, that is to say, both branches are evaluated, and moreover, the domain of the statement is the intersection of that of the condition and of the expressions.

¹²Reductions are allowed, but few transformations are currently available.

A.8 Terminals

```
IntegerConstant
                        [ - ] Number
RealConstant
                        [ - ] Number . Number
BooleanConstant ::
                        true | false | True | False
Number
                       Digit Digit *
                  ::
                        0 | 1 | . . . | 9
Digit
                  ::
                        Letter ( Letter | Digit ) *
Identifier
                  ::
Letter
                  ::
                        a |...| z | A |...| Z | _
```

Note: avoid using underscores...

B Description of the internal format of ASTs

This section describes the format of Abstract Syntax Trees (AST) of ALPHA programs, as handled by Mathematica. In other words, the AST of a program is the Mathematica expression that MMALPHA stores in variable **\$result** when the load command is executed. It can be displayed just by having Mathematica evaluate the expression **\$result**.

In the following description, non terminals are written inside angle brackets <>. For readability, keywords are written without the prefix Alpha' which is implicit. For example, the keyword system is actually represented by the symbol Alpha'system. The documentation is presented in five sections: Systems, Domains, Equations, Matrices and General.

B.1 Systems

```
library>
                ::= {<system> , ... , <system>}
<system>
                ::= system [ <system_id>,
                              <param_space>,
                              <in_var>,
                              <out_var>,
                              <local_var>,
                              <equation_list> ]
<param_space>::= <domain>
<in_var>
             ::= <declare_list>
<out_var>
             ::= <declare_list>
<local_var>
             ::= <declare_list>
             ::= decl [ <id>, <data_type>, <domain> ]
<declare>
             ::= integer | boolean | real | notype
<data_type>
```

B.2 Domains

The domain specification closely follows the internal format of the domain definition in the domain library. This was done to minimize the overhead of domain storage and of making library calls. In Mathematica, domains should only be changed by making calls to the domain library.

```
::= domain [ <dimension_number>,
<domain>
                          <id_list>,
                          <polyhedron_list> ]
<polyhedron> ::= pol [ <constraints_number>,
                       <rays_number>,
                       <equations_number>,
                       <lines_number>,
                       <constraint_list>,
                       <ray_list> ]
<constraint> ::= { <const_type>,
                   <number>, ..., <number> }
<const_type> ::= 0 | 1
                 0 / 1 = constraint is equality / inequality
<ray>
             ::= { <ray_type>,
                   <number>, ..., <number> }
<ray_type>
             ::= 0 | 1
                 0 / 1 = ray is line / ray
```

B.3 Equations

```
<equation>
             ::= equation [ <id>, <exp> ]
               | use [ <id>,
                       <extension>,
                       <param_assign>,
                       <exp_list>,
                       <id_list> ]
<extension> ::= <domain>
<param_assign> ::= <matrix>
             ::= var[<id>]
<exp>
               | const[<number>] | const[<boolean>] | const[<real>]
               | binop [ <bop>, <exp>, <exp>]
               | unop [ <uop>, <exp>]
               | if [ <exp>, <exp>, <exp>]
               | affine [ <exp>, <matrix> ]
               | restrict [ <domain>, <exp> ]
```

B.4 Matrices

B.5 General specifications

Numbers, ids, and lists, as used above, are defined generally (with <*> representing any nonterminal).

```
<*_number>
           ::= <number>
<*_id>
            ::= <id>
            ::= { <*>, <*>, ... , <*> }
<*_list>
<number>
            ::= [0-9][0-9]* | Infinity
<real>
            := <number>.<number>
            ::= True | False
<boolean>
            ::= "a name"
<id>
            ::= (* blah blah blah *)
<comment>
```

Reserved Keywords

Alphaʻaffine	Alpha'and	Alpha'binop
Alphaʻcall	Alpha'case	Alpha'const
Alpha'div	Alpha'domain	Alphaʻeq
Alpha'ge	Alphaʻgt	Alphaʻidiv
Alphaʻinteger	Alpha'le	Alphaʻlt
Alpha'max	Alpha'min	Alpha'mod
Alpha'ne	Alpha'neg	Alphaʻnot
Alpha'or	Alphaʻpol	Alphaʻreal
	Alpha'call Alpha'div Alpha'ge Alpha'integer Alpha'max Alpha'ne	Alpha'call Alpha'case Alpha'div Alpha'domain Alpha'ge Alpha'gt Alpha'integer Alpha'le Alpha'max Alpha'min Alpha'ne Alpha'neg

Alpha'reduce	Alpha'restrict	Alpha'sqrt	Alphaʻsub
Alphaʻsystem	Alphaʻunknown	Alphaʻunop	Alphaʻuse
Alphaʻvar	Alphaʻxor		

C A brief description of the MMALPHA distribution

C.1 The Master notebook

The master notebook is open by the start[] command. It contains 6 sections.

- The welcome section.
- The introduction notebooks: the getting-started notebook, and the mma-intro notebook.
- The simple examples section. It contains pointers to the matrix-vector, the Fir filter, the Fifo, and the delay line demonstrations.
- The advances examples section. Here are presented a demonstration of the Delayed Least-Mean Square filter, of the structured scheduler, and of the Samba architecture for DNA sequence alignment. ¹³
- More contains an access to the Domlib notebook, and some suggestion about the organization of your own notebooks. It explained how you can set the variables <code>%myNotebooks</code>, <code>%myMasterNotebook</code>, then use the <code>myStart[]</code> and the <code>link</code> commands to access directly your own working space.
- Finally, the Tests section gives access to a test notebook.

C.2 Documentation

To explore the MMALPHA distribution, you can follow the html files which are in each subdirectory of the distribution. The structure of the distribution is as follows. The main directory is called MMALPHA. It contains another directory called Mathematica which is the MMALPHA distribution properly speaking. In the MMALPHA directory, the file welcome.html gives access to the documentation.

The Mathematica directory is organized as follows:

- bin.cygwin and bin.solaris directories contain the binary files for execution of MMALPHA on the Windows NT and Solaris system respectively.
- config contains the configuration files.
- demos contains the demonstrations notebooks.

¹³Do the DLMS... Check the structured scheduler...

- doc contains the documentation notebooks.
- lib contains the Mathematica packages which form MMALPHA.
- sources contains the source files of the C programs and of the latex documentation files.
- tests containes the test programs for MMALPHA.

D Limitations of Mathematica

This section contains a few hints to overcome limitations of Mathematica or to cope with known difficulties. Some of these hints are already mentioned in the document.

D.1 The VHDL translater

Some situations may lead to unexpected errors when using the a2v command. Some of them are easy to avoid.

Parameters are forbidden!

First, remember that the main program should not contain parameters anymore. The value of the parameters must have been set, before calling a2v, by the fixParameter command. (Generating VHDL for parameterized programs is very difficult, except for very simple cases.)

Remove main program¹⁴!

Second, notice that after the alpha0ToAlphard command, the Alpha program is separated into a controller, cells, and a module. All these elements are themselves called by a main program – whose name is the name of the initial system – that cannot always be translated into VHDL. When calling a2v, the VHDL translator may then fail on this main program. This error has no consequence on the generation of VHDL for the other subsystems. If you want to avoid it, just remove the main program from the library using the removeSystem command before calling a2v.

Put a bound to your calculations!

ALPHA allows unbounded programs to be written, filters for example. This happens for example, by using variables with domains of the form

$x : \{ k \mid 0 \le k \} \text{ of integer};$

Currently, the a2v translator fails when generating a controller for such programs. To overcome this, write instead

¹⁴This is not a joke . . .

```
x : \{ k \mid 0 \le k \le B \} \text{ of integer};
```

where B is a parameter that will be set before calling a2v.

E How to install MMALPHA

This section contains MMAlpha installation instructions for Unix users, Windows NT or XP users, MacOsX and Linux users. ¹⁵

The MMALPHA sofware can be downloaded at url http://www.irisa.fr/cosi/ALPHA/. In case of problems, send a mail to patrice.quinton@irisa.fr.

E.1 Installing MMALPHA on Unix-like systems

By Unix-like, we mean Unix, Mac OS X, or Linux. The following procedure has been checked for Unix and Mac OS X, not for Linux.

1. This first action must be done only if MMALPHA has not yet been installed on the server or the computer you are using. If MMALPHA is already installed, go to step 2. The current distribution, as obtained from the MMALPHA web site, is a file named mmalphaV2-0-2.zip. Double-click on this file to expand this directory. You may also run the following command

```
unzip mmalphaV2-0-2.zip
```

from a shell window.

2. Create a MMALPHA environment variable containing the path of the directory where MMALPHA has been installed. If you use a csh shell, you have to type:

```
setenv MMALPHA path-of-mmalpha
```

and for a bash shell:

```
export MMALPHA=path-of-mmalpha
```

These commands may alternatively be added to your .cshrc or to your .bashrc file (or to your .login file) in order to be executed automatically when starting a shell.

3. You have then to set the PATH environment variable to contain the directory where the binary files of MMALPHA are. On Mac OS X, this directory is path-of-mmalpha/bin.darwin. For a csh shell:

¹⁵The source of this document is in the doc/Install directory. It appears also as an appendix of the AlphaStart document.

setenv PATH \${MMALPHA}/bin.darwin:\${PATH}

and for a bash shell:

export PATH=\${MMALPHA}/bin.darwin:\${PATH}

Again, you may add this command to your .cshrc or .bashrc file.

- 4. Copy the file \$MMALPHA/init.m to your Mathematica base directory¹⁶ (or append it to your base init.m file if it already exists). For users unfamiliar with Mathematica, recall that this init.m file is executed whenever Mathematica's kernel is launched.
- 5. It's ready! Run Mathematica by typing in a shell window the command:

mathematica

and once a notebook is started, type and evaluate in it the command

start[]

to launch the master notebook of MMALPHA. From this master notebook, examples and explanations are available.

6. To check that everything is OK, evaluate successively the following commands

test1[]

test2[]

test3[]

test4[]

Each one of these command starts a set of tests and shoul return the value True. If this is not the case, something in your installation is wrong. In case of problems, see Section E.3.

Notice that executing these commands generates a lot of error messages, and even, unexpected messages in the shell windows: as long as the final result of the test is True, this is not a problem.

¹⁶The Mathematica base directory used to be the user home directory in Mathematica versions prior to version 5. Under Mathematica, the home directory is given by evaluating the \$HomeDirectory Mathematica variable. Since version 5 (see documentation of Mathematica), the Mathematica base directory is given by the \$UserBaseDirectory variable. For example, in MacOS X, it is located in <code>~Library/Mathematica/Kernel</code> directory: this is where you should put the <code>init.m</code> file.

Remarks

• On MacOS X, Mathematica should be started from the Terminal application, as otherwise, the \$MMALPHA environment variable cannot be set (at least, I do not know how to set this variable...). Moreover, after installing Mathematica, it is needed to add an alias to start Mathematica. Usually, Mathematica is installed in directory

/Applications/Mathematica\ 5.1.app/Contents/MacOS/Mathematica

So, adding

E.2 Installing MMALPHA on Windows NT or Windows XP

Warning: version V2 has not been tested on Windows NT, since I do not have currently access to such a configuration. PQ, Jan. 2, 2009.

- 1. This first action must be done only if MMALPHA has not yet been installed in the server you are using. If MMALPHA is already installed, go to step 2. The current distribution is a file mmalphaV2-0-1.zip file. Double-click on this file to expand this directory.
- 2. You have to set two environment variables: MMALPHA and Path. To do so:
 - (a) Open the system configuration panel (start -> configuration panel)
 - (b) Double click on the "System" icon.
 - (c) Choose the "Advance" panel.
 - (d) Click on "Environment variables".
 - (e) Consider the user variable panel (top part).
 - (f) Create a MMALPHA variable whose value is the path of the directory where MMAL-PHA is installed. Typically, the value of this variable should be

```
C:\...\mmalphaV2-0-2
```

To create such a variable, click on New, and fill the name and value. This step allows Mathematica to know where MMALPHA is located.

(g) Append

;%MMALPHA%\bin.cygwin32

to the user Path environment variable. To do so, select the Path variable, click Modify, place the cursor at the end of the string and type

;%MMALPHA%\bin.cygwin32

¹⁷This step allows the Domlib library to be launched.

- 3. Copy the file \$MMALPHA/init.m to your Mathematica base directory¹⁸ (or append it to your base init.m file if it already exists). For users unfamiliar with Mathematica, recall that this init.m file is executed whenever Mathematica's kernel is launched.
- 4. It's ready! Start Mathematica. The first evaluation in the initial notebook should start MMALPHA. Normally, the Messages window of Mathematica opens and contains a few lines indicating that Mathematica was started successfully. Evaluate start[] in any notebook to launch the master notebook of Mathematica. From this master notebook, examples and explanations are available.
- 5. To check that everything is OK, evaluate successively the following commands

test1[]

test2[]

test3[]

test4[]

Each one of these command starts a set of tests and shoul return the value True. If this is not the case, something in your installation is wrong. In case of problems, see Section E.3. Notice that executing these commands generates a lot of error messages, and even, unexpected messages in the shell windows: as long as the final result of the test is True, this is not a problem.

E.3 In Case of Problems

Before reading this section, make sure that you have tried to evaluate the test1[] through test4[] commands.

Here are a few difficulties you may encounter, and some ways to overcome them. Additional information is given in the test documentation, in file

\$MMALPHA/doc/Tests/testing-MMALPHA.pdf

E.4 The MMALPHA environment variable is not set

To check this, evaluate

Environment["MMALPHA"]

¹⁷Or possibly, cygwin.

¹⁸The Mathematica base directory used to be the user home directory in Mathematica versions prior to version 5. Under Mathematica, the home directory is given by evaluating the \$HomeDirectory Mathematica variable. Since version 5 (see documentation of Mathematica), the Mathematica base directory is given by the \$UserBaseDirectory variable. For example, in Windows, it is probably located in 7Library/Mathematica/Kernel directory: this is where you should put the init.m file.

in your notebook. If it does not answer the proper value, there is a problem.

First, remember that you must start MMALPHA from a shell, otherwise, Mathematica does not inherit from your environment variables (this is true on Unix-like systems, not on Windows -like).

Second, it may be that your init.m file was not loaded: see next section.

E.4.1 The initialization file is not correctly installed

Most of the problems come with the fact that the init.m file may not be installed in the correct directory. If this is the case, evaluating test1[] for example will just return test1[] unevaluated, as Mathematica was not able to load MMALPHA: indeed, loading is done through the init.m file.

After launching Mathematica, make sure that the Kernel is also launched by evaluating any Mathematica expression (for example, 2+2). Before this evaluation is done, the Mathematica's Kernel should evaluate the content of the init.m file, which results in a message in the Messages window of Mathematica. This message ends with:

```
Alpha V2.0 Initialization
The Documentation can be found in ...
Current version in ...
Current directory is ...
If you use the notebook interface, you can open the master notebook:
In[1]:= start[];
```

If the Messages window is not opened, the init.m file was not called and may not be in the proper directory. To check this, evaluate the expression \$UserBaseDirectory in Mathematica, and then check that the init.m file is in the \$UserBaseDirectory/Kernel.

E.4.2 The Domlib does not start

This happen if in the Messages window, the following message appears:

```
Warning: could not install domlib
```

Also, if you run the test1[] command, you do have a True result. Several reasons may be the cause of this problem.

- 1. Variable \$PATH may not contain the directory where the Domlib is. The Domlib is in the directory \$MMALPHA/bin.ostype, where ostype is darwin for MacOS X, linux for Linux, and cygwin32 for Windows. On Unix-like systems, check the value of this variable by the command echo \$PATH. On Windows, check the value of the PATH environment variable.
- 2. The binary file for the domlib may not be in the proper directory. This means that MMALPHA has not been installed properly, or altered. Again, check that the directory \$MMALPHA/bin.ostype contains domlib. If this is not the case, unzip the MMALPHA distribution to get it (if you do not find it in the distribution... just send me a mail!)

3. The domlib binary does not fit with your configuration. You then have to recompile it. I have not yet been able to configure MMALPHA so that recompiling is easy, but I try. Please, refer to the test documentation first, then to the documentation about domlib.

E.4.3 Other problems

You may encounter other problems, for example, some tests are corrects, some other are not. After the execution of the test1[] through test4[] commands, you find a test report file in the \$MMALPHA/tests directory: send me this file, and I'll try to find out what is wrong in order to help you.

Contents

1	Introduction	1
2	How does MMALPHA work?	3
3	Installing MMALPHA	3
4	The Alpha language 4.1 Alpha through examples	4 4 5 6
5	Basic operations on Alpha programs 5.1 Loading and viewing an Alpha program 5.2 Viewing Alpha programs 5.3 On-line documentation and options 5.4 Saving a program 5.5 Analyzing an Alpha program 5.6 Simulating a program 5.7 Scheduling 5.8 Mapping the program to a parallel array	7 7 8 8 9 9 10 11 13
6	Generating Hardware	15
7	Other transformations of Alpha programs 7.1 Pipelining	16 18 19 19
8	Structured Alpha programs 8.1 Simple structures	20 20 21 21
9	And now?	22
\mathbf{A}	Definition of Alpha A.1 Meta Syntax	24 24 24 24 25 25

	A.6	Expressions	26
	A.7	Dependance Functions and Index Expressions	26
	A.8	Terminals	27
В	Des	cription of the internal format of ASTs	27
	B.1	•	27
	B.2		- · 28
	B.3		-0 28
	B.4	1	2 9
			29 29
	D.0	deneral specifications	10
\mathbf{C}	A b	rief description of the MMALPHA distribution	30
	C.1	The Master notebook	30
	C.2	Documentation	30
D	Lim	itations of Mathematica	31
	D.1	The VHDL translater	31
${f E}$	Hov	v to install MMALPHA	32
_	E.1		32
	E.2	O v	$\frac{32}{34}$
	E.3		35
	E.4		35
	Ľ.4		
		V	36
			36
		E.4.3 Other problems	37