$$\exp\left(y_{t}\right) = \exp\left(c_{M_{t}}\right) + \exp\left(x_{t}\right) \tag{1}$$

$$(1-a) b (1-\eta) \exp((-C_t) e + e c_{H_t} - h_{H_t}) = (1-b) \exp((-l_t))$$
(2)

$$a b (1 - \tau_h) (1 - \theta) \exp(y_t + (-C_t) e + c_{M_t} (e - 1) - h_{M_t}) = (1 - b) \exp((-l_t))$$
(3)

$$\beta \exp(e(-C_{t+1})) \left(a(1-\delta_H) \exp((e-1) c_{M_{t+1}}) + (1-a) \eta \exp(e c_{H_{t+1}} - k_{H_t})\right) = a \lambda \exp((-C_t) e + c_{M_t} (e-1))$$
(4)

$$\beta \exp\left(e\left(-C_{t+1}\right) + (e-1) c_{M_{t+1}}\right) \left(1 + \exp\left(r_{t+1}\right) \left(1 - \tau_k\right) + \tau_k \delta_M - \delta_M\right) = \lambda \exp\left(\left(-C_t\right) e + c_{M_t} \left(e-1\right)\right)$$
(5)

$$\theta \exp\left(y_t - k_{Mt-1}\right) = \exp\left(r_t\right) \tag{6}$$

$$(1 - \theta) \exp(y_t - h_{Mt}) = \exp(w_t) \tag{7}$$

$$\exp(y_t) = \exp(\theta \, k_{M_{t-1}} + (1 - \theta) \, (h_{M_t} + z_{M_t})) \tag{8}$$

$$\exp(C_t) = (a \exp(c_{M_t} e) + (1 - a) \exp(e c_{H_t}))^{\frac{1}{e}}$$
(9)

$$\exp(l_t) = 1 - \exp(h_{Ht}) - \exp(h_{Mt}) \tag{10}$$

$$\exp(c_{Ht}) = \exp(\eta k_{Ht-1} + (1-\eta)(h_{Ht} + z_{Ht})) \tag{11}$$

$$\exp\left(x_{Mt}\right) = \lambda \, \exp\left(k_{Mt}\right) - \left(1 - \delta_M\right) \, \exp\left(k_{Mt-1}\right) \tag{12}$$

$$\exp(x_{Ht}) = \lambda \exp(k_{Ht}) - (1 - \delta_H) \exp(k_{Ht-1})$$
(13)

$$\exp\left(x_{t}\right) = \exp\left(x_{M_{t}}\right) + \exp\left(x_{H_{t}}\right) \tag{14}$$

$$\exp\left(k_{t}\right) = \exp\left(k_{Ht}\right) + \exp\left(k_{Ht}\right) \tag{15}$$

$$\exp(T_t) = \tau_h \, \exp(h_{Mt} + w_t) + \tau_k \, \exp(k_{Mt-1} + r_t) - \tau_k \, \delta_M \, \exp(k_{Mt-1})$$
(16)

$$z_{Mt} = \rho_M z_{Mt-1} + \epsilon_{Mt} \tag{17}$$

$$z_{Ht} = \rho_H z_{Ht-1} + \epsilon_{Ht} \tag{18}$$