# Putting Home Economics into Macroeconomics Greenwood et al. (1993)

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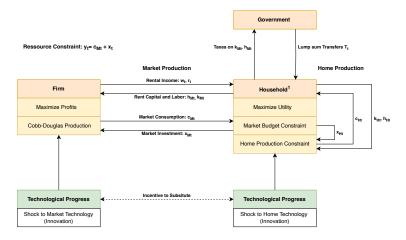
Future Research

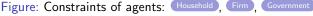
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#### Motivation

- ► Paper focuses on the home sector by introducing a home production function into a standard RBC model
  - Households can produce goods and services at home (substitute to market production)
- Why should you focus on the home sector?
  - 25 percent of discretionary time spent on unpaid work at home, in contrast to 33 percent spent on paid work (Greenwood et al., 1993)
    - e.g. cooking, cleaning, caretaking
  - Investment in household capital exceeds investment in business capital by about 15 percent (Greenwood et al., 1993)
    - e.g. consumer durables, housing
  - Value of household production between 20 and 50 percent of the value of GDP (Eisner, 1988)

#### Model





<sup>&</sup>lt;sup>1</sup>Increased willingness to substitute

## Model Specifications

- ▶ Model 1: Home production minimized
- ▶ Model 2: Increased willingness to substitute between home and market consumption
- Model 3: Increased incentive to substitute between home and market
  - ▶ Note: Models 2 & 3 should deliver similar results
- ► **Model 4**: More general home production function and highly correlated technology shocks

## Business Cycle Properties I

- ➤ Compare the business cycle properties of simulated models with U.S. data from 1947 and 1987
- Model 1 is the benchmark model
- Ratios of standard deviations
  - ► Total investments (x) relative to output
  - Market consumption  $(c_M)$  relative to output
  - Market hours  $(h_M)$  relative to output
  - Real wages or productivity (w) relative to output
  - Market hours relative to productivity
- Correlations
  - ► Market hours and productivity (c<sub>M</sub> and w)
  - ightharpoonup Market and home investments ( $x_M$  and  $x_H$ )

## Business Cycle Properties II

- ► Model 2 & 3 (similar results):
  - Ratios of standard deviations: More accurate than the benchmark
  - ► Correlations: Bad performance ( comovement problem )
- ► Model 2a
  - ► Increasing standard deviation of home technology shock
  - More accurate correlation between the market hours and productivity
  - Worse performance in most other properties compared to the benchmark
- Model 4 and 4a
  - Setting degree of substitution within home production
  - More accurate correlation between the market and home investments
  - Worse performance in other properties compared to the benchmark

#### Discussion Results

- ▶ Better performance in terms of volatility than the benchmark
- Potential to improve the accuracy of comovement of variables
- Model calibration is crucial
  - Lacking evidence for some parameter values
  - E.g., the elasticity of substitution of home production
- Further results:
  - Detailed results of the business cycle properties and solutions to the comovement problem → Appendix
  - ► All Results (Dynare outputs, impulse response functions, ...): manuelbieri.ch/Greenwood\_1993/

# Existing Research Extension (Selection)

- Government spending and taxes
  - ► Christiano and Eichenbaum (1992)
  - ► McGrattan et al. (1993)
  - ► McGrattan et al. (1997)
- International Markets
  - Canova and Ubide (1998)
- Market and home sector as complements
  - Fisher (1997)
- Endogenous Shocks
  - Einarsson and Marquis (1997)

# Research Extensions (Selection)

- ► Multiple Sectors (Plosser, 1989)
- Introduce heterogeneity amongst the consumers
  - Evidence that the importance of the household side changes (Baxter and Jermann, 1999)
- ► Comparison between countries Chart Time Use
  - Evidence of the relative importance of the household sector in a country (Aguiar and Hurst, 2005)
  - ▶ Developed vs. developing countries (Hicks, 2015)

#### Conclusion

- Including a home production function improves Real Business Cycle (RBC) model's ability to better model economic fluctuations
- ► Fragile model
  - Depends highly on the parameters chosen
  - ► Little evidence for the parameter values
- Performance of an RBC with home production only valid for the post-war U.S. economy

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Agents

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Further Material

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## Representative Household I

The household maximizes:

$$U = \sum_{t=0}^{\infty} \beta^{t} [b \log(C_{t}) + (1-b) \log(I_{t})]$$
 (1)

▶ Allocation of time between paid work  $(h_{Mt})$ , unpaid work  $(h_{Ht})$  and leisure  $(I_t)$ 

$$I_t = 1 - h_{Mt} - h_{Ht} \tag{2}$$

Consumption from the market  $(c_{Mt})$  or from home production  $(c_{Ht})$ 

$$C_t = \left[ac_{Mt}^e + (1-a)c_{Ht}^e\right]^{\frac{1}{e}} \tag{3}$$

Further Material

## Representative Household II

▶ Allocation of capital between the market and the household

$$c_{Mt} + x_t = w_t(1 - \tau_h)h_{Mt} + r_t(1 - \tau_k)k_{Mt} + \delta_M \tau_k k_{Mt} + T_t$$
 (4)

- Home production function
  - Note: Home production can only be consumed

$$c_{Ht} = g(h_{Ht}, k_{Ht}, z_{Ht}) = k_{Ht}^{\eta} (z_{Ht} h_{Ht})^{1-\eta}$$
 (5)

▶ More general home production function (model 4)

$$c_{Ht} = g(h_{Ht}, k_{Ht}, z_{Ht}) = [\eta k_{Ht}^{\Psi} + (1 - \eta)(z_{Ht}h_{Ht})^{\Psi}]^{\frac{1}{\Psi}}$$
 (6)

## Representative Firm

- ▶ Profit maximizing firm with Cobb-Douglas production function
- Maximizes profits by choosing input factors  $k_{Mt}$  and  $h_{Mt}$

$$y_t = k_{Mt}^{\theta} (z_{Mt} h_{Mt})^{1-\theta} \tag{7}$$

### Government

ightharpoonup Government income is transferred entirely back to the households via a lump-sum transfer  $T_t$ 

$$G_t = w_t \tau_h h_{Mt} + r_t \tau_k k_{Mt} - \delta_M \tau_k k_{Mt} - T_t = 0$$
 (8)

## Resource Constraint

References

► Feasibility implies that market output is allocated across market consumption, total investment, and government spending (=0)

$$y_t = c_{Mt} + x_t \tag{9}$$

- Real Business Cycle model including a home production function
- Agents
  - ▶ Representative Household → Utility maximizing
    - Allocation of consumption  $(C_t = [ac_{Mt}^e + (1-a)c_{Ht}^e]^{\frac{1}{e}})$
    - ▶ Allocation of time  $(I_t = 1 h_{Mt} h_{Ht})$
    - ightharpoonup Allocation of investment  $(x_{Mt}, x_{Ht})$
    - ► Home Production Function:  $c_{Ht} = k_{Ht}^{\eta} (z_{Ht} h_{Ht})^{1-\eta}$
  - ▶ Representative Firm → Profit maximizing
    - $\mathbf{v}_t = k_{Mt}^{\theta} (z_{Mt} h_{Mt})^{1-\theta}$
  - ▶ Government → Absent (zero spending)
    - $G_t = W_t \tau_h h_{Mt} + r_t \tau_k k_{Mt} \delta_M \tau_k k_{Mt} T_t = 0$
- Exogenous shocks to home and market technology ("innovation")

## **Business Cycle Properties**

Table: Effects of Adding Home Production to RBC Model

	$\sigma_y$	$\frac{\sigma_{x}}{\sigma_{y}}$	$\frac{\sigma_{c_M}}{\sigma_{\gamma}}$	$\frac{\sigma_{h_M}}{\sigma_{\gamma}}$	$\frac{\sigma_w}{\sigma_y}$	$\frac{\sigma_{h_M}}{\sigma_w}$	$\rho_{h_M,w}$	$\rho_{x_M,x_H}$
Data	1.96	2.61	0.54	0.78	0.73	1.06	-0.12	0.30
1	1.40	2.81	0.40	0.41	0.60	0.69	0.96	-0.13
2	1.56	2.56	0.60	0.50	0.55	0.91	0.84	-0.90
2a	2.36	2.73	1.36	0.94	0.35	2.66	-0.01	-1.00
3	1.47	2.45	0.55	0.48	0.54	0.88	0.94	-0.83
4	1.13	4.09	0.41	0.29	0.74	0.40	0.86	-0.60
4a	1.30	3.10	0.38	0.37	0.64	0.57	0.96	0.26

- ► The data corresponds to the U.S. time series between 1947 and 1987
- ▶ Numbers correspond to the model specifications

## Comovement Problem I

#### Productivity vs. Market Hours

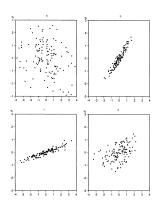


Figure: Market Hours vs. Productivity (Benhabib et al., 1991)

▶ a: U.S. Data; b: Standard Model; c and d: Home Production

#### Comovement Problem II

- ▶ Data: Small negative correlation  $(\rho_{h_{M},w})$  → less hours required to earn same income
- Standard model: Only shock to labor demand → positive correlation
- Model with home production: Additional shock to labor supply through home technology innovations
  - Increase standard deviation of home technology innovation to further shift labor supply  $\rightarrow$  decreases the correlation

Variables and Parameters

- Problem: Most papers use very similar standard deviation for the home technology shock (e.g., Benhabib et al., 1991; Hansen and Wright, 1992; Fisher, 2007)
- No evidence for a much higher standard deviation

#### Comovement Problem III

#### Market Investment vs. Home Investment

- ▶ Data: Positive correlation  $(\rho_{XM,XH})$
- Standard model (Fisher, 2007)
  - Business capital produces market consumption and investment goods
  - Household capital produces only home consumption goods
  - Incentive to substitute away from household capital toward business capital after a market technology shock  $\rightarrow$  negative correlation

#### Comovement Problem IV

- Model with general home production function:
  - lacktriangle Highly correlated shocks ightarrow shock to market and home at the same time
  - Move hours to the market but hours in the home are more effective
  - Degree of substitution in home production can imply the desire to increase capital in the home during market upswing  $\rightarrow$ positive correlation
- Lacking evidence for the elasticity of substitution in home production
- Other Solutions:
  - Add home capital to market production (Fisher, 2007)
  - Introduction of durable and non-durable goods (Baxter, 1996)

## Impulse Response Function I

References

Further Material

## Impulse Response Function II

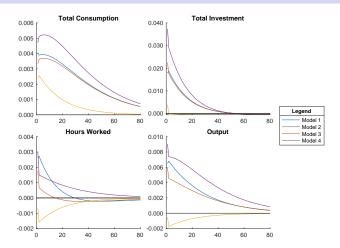


Figure: Impulse Response Functions for Home Technology Shock

## Impulse Response Function III

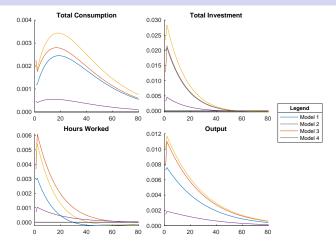


Figure: Impulse Response Functions for Market Technology Shock

References

#### Table: Endogenous Variables

	Meaning
a.C	
а <b>С</b>	Total consumption
<sup>а</sup> С <sub>Н</sub>	Goods and services produced in the home
$^{a}\mathcal{C}_{M}$	Goods and services purchased in the market
$^{b}h_{H}$	Labour hours spent working in the household
$^{b}h_{\mathcal{M}}$	Labour hours spent working in the market
ь <i> </i>	Leisure time $(1 - h_H - h_M)$
ck	Total capital
<sup>c</sup> k <sub>H</sub>	Household capital
$^{c}k_{M}$	Market capital
<sup>a</sup> r	Price at which business capital can be rented to firms
<sup>b</sup> T	Lump-sum transfer payment from the government

## Endogenous Variables II

	Meaning
b <sub>W</sub>	Real wage rate in the market
<sup>b</sup> X	Total investment
$^{b}x_{H}$	Investment in household capital
$^{b} x_{M}$	Investment in business capital
Ьy	Market output
c <sub>ZH</sub>	Technology level in the home
$^{c}Z_{M}$	Technology level in the market
<sup>c</sup> ž <sub>H</sub>	Shock resulting from technological changes in the home
c $\tilde{z}_M$	Shock resulting from technological changes in the market

- a denotes forward-looking variables (jumpers)
- b denotes static variables
- c denotes state variables

# Exogenous Variables

#### Table: Exogenous Variables

	Meaning	Standard deviation
$\epsilon_{H}$	Innovations in the home	$\sigma_H$
$\epsilon_{M}$	Innovations in the market	$\sigma_{M}$

References

#### Table: Parameters

	Meaning
а	Share of $c_{Mt}$ of total consumption
b	Weight factor of consumption vis-a-vis leisure
e	Willingness of a household to substitute between market
	consumption $c_{Mt}$ and home consumption $c_{Ht}$
$\beta$	Discount factor
$\delta_H$	Depreciation rate on household capital
$\delta_{M}$	Depreciation rate on business capital (tax-deductible)
$\eta$	Capital share in the home production function
$\gamma$	Measures the household's incentive, to move economic
	activity between the home and the market

References

	Meaning
$\rho_H$	Persistence of market technology shock
$ ho_{M}$	Persistence of home technology shock
$\sigma_{H}$	Standard deviation of innovations in the household
$\sigma_{M}$	Standard deviation of innovations in the market
$ au_{\pmb{k}}$	Tax rate on capital income
$ au_{h}$	Tax rate on labour income
$\theta$	Capital share in the market production function
$\lambda$	Growth rate of all endogenous variables besides
	$h_{Mt}$ , $h_{Ht}$ , $I_t$ and $r_t$
Ψ	Willingness of a household to substitute between
	capital $k_{Ht}$ and time $h_{Ht}$ in the home production

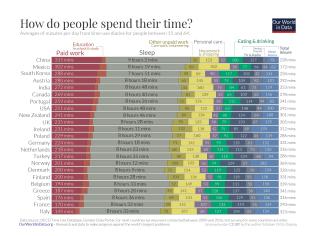


Figure: OECD Countries 2009 - 2016 (Ortiz-Ospina et al., 2020) Extensions

# Further Reading

- Standard home production model:
  - Greenwood and Hercowitz (1991)
  - Greenwood (2019)
  - Greenwood et al. (2020)
- More modern models with home production:
  - Davis and Heathcote (2005)
  - Fisher (2007)

Variables and Parameters