$$(1-a) b (1-\eta) C_t^{(-e)} c_H^e_t h_H^{(-1)} = (1-b) l_t^{(-1)}$$

$$(1)$$

$$C_t^{(-e)} a b (1 - \tau_h) (1 - \theta) c_M_t^{e-1} y_t h_M_t^{(-1)} = (1 - b) l_t^{(-1)}$$
(2)

$$\beta C_{t+1}^{(-e)} \left(a \left(1 - \delta_H \right) c_{M_{t+1}}^{e-1} + \left(1 - a \right) \eta c_{H_{t+1}}^{e} k_{H_t}^{(-1)} \right) = c_{M_t}^{e-1} C_t^{(-e)} a \lambda$$
(3)

$$\beta C_{t+1}^{(-e)} c_M_{t+1}^{e-1} \left(1 + r_{t+1} \left(1 - \tau_k\right) + \tau_k \delta_M - \delta_M\right) = c_M_t^{e-1} C_t^{(-e)} \lambda \tag{4}$$

$$\theta \, y_t \, k_{M_{t-1}}^{\,(-1)} = r_t \tag{5}$$

$$h_{M_t}^{(-1)} (1 - \theta) y_t = w_t \tag{6}$$

$$y_t = k_M \theta_{t-1} \left(h_{M_t} z_{M_t} \right)^{1-\theta} \tag{7}$$

$$c_{Ht} = k_{Ht-1}^{\eta} \left(h_{Ht} z_{Ht} \right)^{1-\eta} \tag{8}$$

$$C_t = (a c_M_t^e + (1 - a) c_H_t^e)^{\frac{1}{e}}$$
(9)

$$l_t = 1 - h_{Ht} - h_{Mt} \tag{10}$$

$$x_{Mt} = \lambda k_{Mt} - k_{Mt-1} (1 - \delta_M) \tag{11}$$

$$x_{Ht} = k_{Ht} \lambda - (1 - \delta_H) k_{Ht-1} \tag{12}$$

$$x_t = x_{Mt} + x_{Ht} \tag{13}$$

$$k_t = k_{Ht} + k_{Mt} \tag{14}$$

$$T_t = h_{Mt} \tau_h w_t + k_{Mt-1} \tau_k r_t - \tau_k \delta_M k_{Mt-1}$$
(15)

$$y_t = c_{Mt} + x_t \tag{16}$$

$$\log(z_{Mt}) = \rho_M \log(z_{Mt-1}) + \epsilon_{Mt} \tag{17}$$

$$\log(z_{Ht}) = \rho_H \log(z_{Ht-1}) + \epsilon_{Ht} \tag{18}$$