

## Supplementary Material

### 1 MODEL EQUATIONS AND PARAMETERS

The asymptotic function for the calcium conductance  $m_\infty$  is given by

$$m_\infty(v) = \frac{1}{2} (1 + \tanh((v - v_A)/v_B)). \quad (\text{S1})$$

The voltage and potassium nullclines,  $v_\infty(v)$  and  $w_\infty(v)$ , are

$$v_\infty(v) = \frac{-g_l(v - v_l) - g_{ca}m_\infty(v)(v - v_{ca}) + I - \bar{g}s(v - v_s)}{g_k(v - v_k)}, \quad (\text{S2})$$

$$w_\infty(v) = \frac{1}{2} (1 + \tanh((v - v_C)/v_D)). \quad (\text{S3})$$

Model parameters were adapted from Bose and Booth (2011) and are given in table S1:

Table S1. Default parameters for coupled Morris-Lecar model.

Parameter	value
$g_L$	0.15 mS/cm <sup>2</sup>
$g_{Ca}$	0.3 mS/cm <sup>2</sup>
$g_K$	0.6 mS/cm <sup>2</sup>
$v_L$	−50 mV
$v_{Ca}$	100 mV
$v_K$	−70 mV
$v_A$	1 mV
$v_B$	14.5 mV
$v_C$	4 mV
$v_D$	15 mV
$I$	3.8 μA/cm <sup>2</sup>
$\tau_w$	100 ms
$\tau_a$	1000 ms
$\tau_b$	100 ms
$\tau_\kappa$	100 ms
$\tau_\gamma$	0.0001 ms
$v_\theta$	0 mV
$v_s$	−80 mV
$T$	376 ms
$T_{act}$	49 ms
$T_{inact}$	327 ms
$g^*$	0.0068 mS/cm <sup>2</sup>
$g_{bif}$	0.0038 mS/cm <sup>2</sup>
$\lambda := \exp(-T_{act}/\tau_b)$	0.612
$\rho := \exp(-T_{inact}/\tau_a)$	0.721

## 2 COMPUTING BIFURCATION DIAGRAM NUMERICALLY

The bifurcation diagram of stable  $n - n$  solutions of the two-cell network in ?? is obtained numerically as follows: We initialise the coupling strength at parameter values associated with one type of  $n - n$  solution, that is we choose the values  $\bar{g} = 0.4, 0.7, 0.8, 0.9, 0.98$  for the  $1 - 1$ ,  $2 - 2$ ,  $3 - 3$ ,  $4 - 4$ , and  $5 - 5$  solutions respectively. For each  $\bar{g}$  the system is then numerically integrated sufficiently long for any transients to fully subside. We then identify one period of the solution by finding the first return of the depression variable  $d_1$ . That is, we choose some value  $d_k$  at a spike time  $t_k$ , and by iterating from spike to spike find some subsequent value  $d_{k+1}$  at spike time such that  $|d_{k+1} - d_k| < \epsilon$ . If a periodic solution of type  $n - n$  is found in such way,  $\bar{g}$  is step-wise increased/decreased, and the above algorithm is repeated. Otherwise, the set of all previously found solutions and the corresponding values  $\bar{g}$  are returned.

Note that applying conventional methods of numerical continuation is not straightforward for our model, as the discontinuous resets in ?? and (??) make the root finding challenging (e.g. see Kuznetsov, 2004, for continuation methods).

## REFERENCES

- Bose A, Booth V. Co-existent activity patterns in inhibitory neuronal networks with short-term synaptic depression. *Journal of Theoretical Biology* 272 (2011) 42–54. doi:10.1016/j.jtbi.2010.12.001.
- Kuznetsov A. *Elements of applied bifurcation theory* (Springer Science & Business Media) (2004). doi:10.1007/978-1-4757-3978-7.