

Testing models of accreting stars in massive binaries on ζ Ophiuchi

M. RENZO,^{1,2} Y. GÖTBERG,³ AND ■ [TBD] ■

¹*Department of Physics, Columbia University, New York, NY 10027, USA*

²*Center for Computational Astrophysics, Flatiron Institute, New York, NY 10010, USA*

³*The Observatories of the Carnegie Institution for Science, 813 Santa Barbara Street, Pasadena, CA 91101, USA*

ABSTRACT

Binarity dominates the evolution of massive stars, and the nearest O-type star to Earth, ζ Ophiuchi, has long been proposed to be a product of binary evolution. Despite this, most stellar models have tried unsuccessfully to reproduce its observable properties relying on single-star rotating models. ■ [Here we do better] ■

Keywords: stars: individual: ζ Ophiuchi – stars: massive – stars: binaries

1. INTRODUCTION

■ [alternative structure:

- accretors are common
- the nearest O type star to Earth has good reasons to be considered a former accretor

] ■

The nearest O-type star to Earth is ζ Ophiuchi¹ (spectral type O9.5IVnn, Sota et al. 2014), at a distance of ~ 110 pc (e.g., Neuhäuser et al. 2020, and references therein). It was originally identified as a runaway star through its large proper motion by Blaauw (1952). Unfortunately, the *Gaia* data for this object are not of sufficient quality to improve previous astrometric results, but estimates of the peculiar velocity range in $30 - 50 \text{ km s}^{-1}$ (e.g., Zehe et al. 2018; Neuhäuser et al. 2020). The large velocity with respect the surrounding interstellar material is also confirmed by the presence of a prominent bow-shock (e.g., Bodensteiner et al. 2018).

Because of its young apparent age, extremely fast rotation ($v \sin(i) \gtrsim 400 \text{ km s}^{-1}$, e.g., Zehe et al. 2018), and nitrogen (N) and helium (He) rich surface (e.g., Herrero et al. 1992; Blaauw 1993; Villamariz & Herrero 2005; Marcolino et al. 2009), ζ Oph is a prime candidate for the binary supernova scenario (Blaauw 1961; Renzo et al. 2019). In this scenario, after a phase of mass transfer in a massive binary which can spin up the accreting star (e.g., Packet 1981), the core-collapse of the donor star disrupts the binary. This results in the

ejection of the former accretor as a fast rotator and with its pre-explosion orbital velocity as peculiar velocity.

Many studies have suggested ζ Oph might have accreted mass from a companion before acquiring its large velocity, both from spectroscopic and kinematic considerations (e.g., Blaauw 1993; Hoogerwerf et al. 2000, 2001; Tetzlaff et al. 2010; Neuhäuser et al. 2020) and using stellar modeling arguments (e.g., van Rensbergen et al. 1996). Recently, Neuhäuser et al. (2020) suggested that a supernova in Upper-Centaurus-Lupus produced the pulsar PSR B1706-16, ejected ζ Oph, and also injected the short-lived radioactive isotope ^{60}Fe on Earth about ~ 1.5 Myr ago. This argues strongly for a successful supernova explosion accompanied by a large $\sim 250 \text{ km s}^{-1}$ natal kick, which in most cases would be sufficient to disrupt the binary.

Although the nature of ζ Oph as a binary product is well established, its large rotation rate has lead most attempts to explain the surface composition to rely on rotational mixing (e.g., Maeder & Meynet 2000). Even the binary models of van Rensbergen et al. (1996) assumed spin-up due to mass accretion (e.g., Packet 1981) to drive rotational mixing from the interior of the accreting star (see also Cantiello et al. 2007). However, Villamariz & Herrero (2005) were unable to find good fit for the stellar spectra using the rotating models from Meynet & Maeder (2000).

This may not be surprising: rotational mixing has lower efficiency for metal-rich and relatively low mass stars because of the increased importance of mean molecular weight gradients and longer thermal timescales compared to more massive stars (e.g., Yoon et al. 2006; Perna et al. 2014). The parent association of ζ Oph has $Z = 0.01 - 0.02 \simeq Z_{\odot}$ (e.g., Murphy

¹ also known as HD 149 757.

et al. 2021), and mass estimates for the star range from $13 - 25 M_{\odot}$, at the lower end of the range where efficient mixing might bring He and CNO-processed material to the surface (chemically homogeneous evolution).

■ [maybe paragraph below goes in discussion] ■ On top of the surface abundances, its extreme rotation rate, and the peculiar space velocity, ζ Oph poses a number of other puzzles: its wind mass-loss rate is about two orders of magnitude lower than theoretical predictions (weak wind problem, Marcolino et al. 2009), the star exhibits spectral variability with occasional appearance of H α in emission (e.g., Walker et al. 1979), and is potentially magnetic ■ [true?ref?] ■.

Given the challenges in explaining the surface composition of ζ Oph with rotational mixing from the stellar interior and the strong evidence for its past as a member of a binary system, this star offers a unique opportunity to constrain the evolution of accreting stars in massive binary systems, which is hard to model because of the interplay of rotation, mixing, and accretion (e.g. Hellings 1983, 1984; Braun & Langer 1995).

■ [maybe move paragraph below upwards] ■ While we focus here on this particular star, we emphasize that understanding the evolution of accretors in massive binaries has wider and crucial implications. Observed stellar populations might contain $\sim 10\%$ of presently single O-type that accreted mass previously (Renzo et al. 2019), gravitational-wave progenitors in isolated binary formation scenarios go through a common envelope phase initiated by the originally less massive accretor after the formation of the first compact object (e.g., Belczynski et al. 2016; Tauris et al. 2017; Law-Smith et al. 2020), ■ [more reasons?] ■

Here, we present the first self-consistent binary evolution model for ζ Oph computing simultaneously the coupled evolution of *both* donor and accretor star. After presenting our calculations in Sec. 2, we show our best model which reproduces the majority of the salient features of this star in Sec. 3. In this model, the surface abundances of ζ Oph are explained by pollution from the former companion, rather than upward mixing from the interior of ζ Oph itself. We discuss the sensitivity of our results to the admittedly many free parameters required for this kind of computations in Sec. 4. Finally, we conclude in Sec. 6.

2. MASSIVE BINARIES WITH MESA

■ [missing Z] ■ Modeling the evolution of massive binaries ($M_1 \gtrsim 20 M_{\odot} \geq M_2$) is challenging because of the intricate and coupled role of several notoriously difficult stellar physics ingredients (differential rotation, mixing, high mass-loss rates, accretion, etc.) Here we

follow self-consistently in one dimension the coupled evolution of two massive stars in a binary system using MESA (version 15140). Our choice of input parameters and our numerical results are available at ■ [link] ■. We discuss here only the main relevant physical parameters, and Appendix A gives more details on our choice of input physics.

We adopt the Ledoux criterion to determine convective stability and a mixing length parameter of 1.5. Semiconvection and a thermohaline mixing are included with an efficiency of 1.0 for both using the algorithms from Langer et al. (1983) and Kippenhahn et al. (1980), respectively. We use the exponential core overshooting from Herwig (2000) with free parameters $(f, f_0) = (4.25 \times 10^{-2}, 10^{-3})$ which were chosen to reproduce the width of the main sequence from Brott et al. (2011) following Claret & Torres (2017). We also use the superadiabaticity reduction introduced in MESA 15140.

We treat rotation in the “shellular” approximation and initialize it assuming tidal synchronization at the beginning of the evolution. Our models include in a diffusive approximation the effect of Eddington-Sweet circulations (Sweet 1950), which dominates the chemical mixing due to rotation. We also include the secular and dynamical shear instabilities, and the Goldreich-Schubert-Fricke instability as in Gotberg et al. (2017); Götberg et al. (2018); Laplace et al. (2020, 2021). We assume a Spruit-Tayler dynamo for the transport of angular momentum (Spruit 2002), and chose the same free parameters as Heger et al. (2000) ■ [check this statement] ■. This also includes the rotational enhancement of wind mass loss as in Langer (1998).

We treat wind mass loss with the Vink et al. (2000, 2001) hot wind, and de Jager et al. (1988) with a scaling factor of 1. This effectively means our wind mass loss rate post-mass transfer is overestimated by almost a factor of 100 (weak wind problem, see Marcolino et al. 2009).

Both stars are evolved simultaneously on the same timesteps until after the donor detaches from the Roche lobe. We follow Kolb & Ritter (1990) to calculate the mass transfer rate from optically thick layers of the donor star during Roche lobe overflow (RLOF), and assume that the transferred layers reach the accretor with the accretor’s specific surface angular momentum. Mass transfer is conservative until the accretor reaches critical rotation, after which rotationally enhanced mass loss governs the accretion efficiency.

To define RLOF detachment, we take advantage of the fact that we focus here on post-main sequence (case B, Kippenhahn & Weigert 1967) interactions among massive stars which are not expected to hundreds of R_{\odot}

during He shell burning at the metallicity we consider (e.g., Laplace et al. 2020). We define RLOF detachment as the moment after the onset of RLOF, when the donor has a surface He mass fraction larger than 0.35 (indicating that a significant amount of envelope has been lost or transferred), a radius smaller than its terminal-age main sequence (TAMS) radius, and no mass is being transferred anymore. At this point in time, we save a model for the accreting star, and continue its evolution as a single star until TAMS with the same setup.

3. BEST MODEL

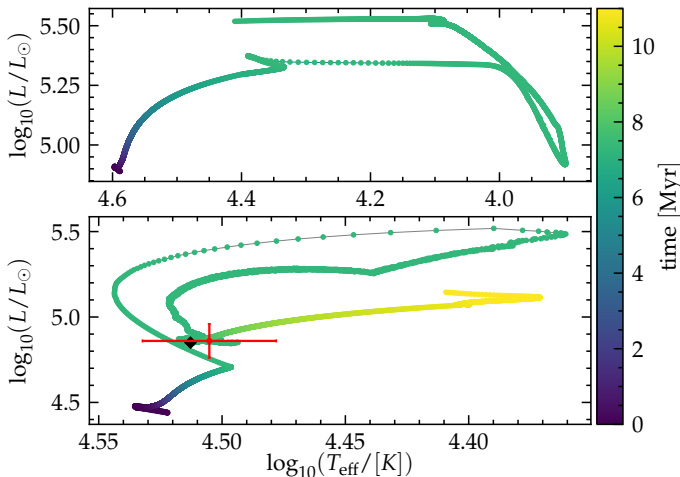


Figure 1. Hertzsprung-Russell diagram for the donor star (top) and accretor star (bottom) of the progenitor binary of ζ Oph. The tracks are colored with the stellar age, the red datapoint shows the position of ζ Oph according to Villamariz & Herrero (2005), and the black diamond marks the post-RLOF position of the accreting star. We continue its evolution as a single star from there until core H depletion, hence the bottom panel shows a longer time. Note the different scale on the two panels.

We describe here the evolution of a binary system with initial masses $M_1 = 25 M_\odot$, $M_2 = 17 M_\odot$ on a period of 100 days at $Z = 0.01$. Fig. 1 shows the Hertzsprung-Russell diagrams of both stars. The donor star (top panel) evolves off the main sequence and ~ 8400 years later, when the donor’s effective temperature reaches about $T_{\text{eff}} \simeq 10^4$ K, mass transfer starts. This results in a stable case B RLOF. We refer to Gotberg et al. (2017); Laplace et al. (2021); Blagorodnova et al. (2021) and references therein for a detailed description of the evolution of massive donor stars in binaries: although our models here are significantly more massive than those presented there, the qualitative behavior is similar.

At the onset of RLOF, the accretor star (bottom panel) is still on the main sequence with $T_{\text{eff}} \simeq 10^{4.5}$ K.

Because of the accretion of matter it quickly becomes over-luminous ($L \simeq 10^{5.4} L_\odot$), and its radius increases dramatically from $\sim 7.5 R_\odot$ to $\sim 35 R_\odot$. Once the accretor reaches critical rotation (roughly at the lowest T_{eff} in the bottom panel of Fig. 1), the star begins contracting and its T_{eff} increases. At $T_{\text{eff}} \simeq 4.43$ K the material transferred from the companion star becomes progressively more He-rich, causing a “v-shaped” feature in the evolutionary track. This indicates that the outer layers of the donor core are uncovered by mass transfer, after the convective core recession in mass coordinate during the main sequence. This also starts vigorous thermohaline mixing in the accreting star, which progressively dilutes the surface He mass fraction and causes noisy features on the HR diagram (e.g., Cantiello et al. 2007).

Fig. 2 shows the rate of mass loss/accretion in both stars during the RLOF phase. The top panel focuses on the donor star which loses mass to RLOF (cyan line) and wind mass loss (thin red line). The combined effect of these is shown in the dashed blue line. The bottom panel shows instead the accreting star, which grows in mass because

The entire duration of this case B stable RLOF is about 10^4 years, and the mass transfer rates reaches very high values above $10^{-2.5} M_\odot \text{ yr}^{-1}$.

The total amount of mass lost transferred is \blacksquare [XXX] \blacksquare , of which on

\blacksquare [maybe paragraph below can be cut] \blacksquare

At the end of RLOF, the donor star briefly expands again ($T_{\text{eff}} \simeq 10^{4.1}$ K, $L \simeq 10^{5.5} L_\odot$). This is due to the partial recombination of the He rich material now at the surface, which causes a transient surface convection layer. We find this to be the culprit of difficulties in modeling massive binaries transferring mass in older MESA releases, because although only a very small amount of mass is involved, this would lead to large radial expansion much beyond the donor’s Roche lobe, and cause numerical problems.

\blacksquare [describe fig. 2] \blacksquare

After RLOF, the donor star is a $12.6 M_\odot$ core with surface He mass fraction of ~ 0.8 , and quickly contracts. Such a star would likely appear as a Wolf-Rayet \blacksquare [Ylva: want to comment on appearance with companion star next to it?] \blacksquare .

\blacksquare [fix this, and maybe goes into methods] \blacksquare We keep evolving the binary until core-He exhaustion of the donor \blacksquare [defined how?] \blacksquare . The evolutionary track of the top panel stops at this point. We then take the accretor, which has now a mass of $20.2 M_\odot$ and an orbital velocity of $\sim 52 \text{ km s}^{-1}$ (corresponding to a period of ~ 130 days) and continue its evolution as a single star with the same setup until

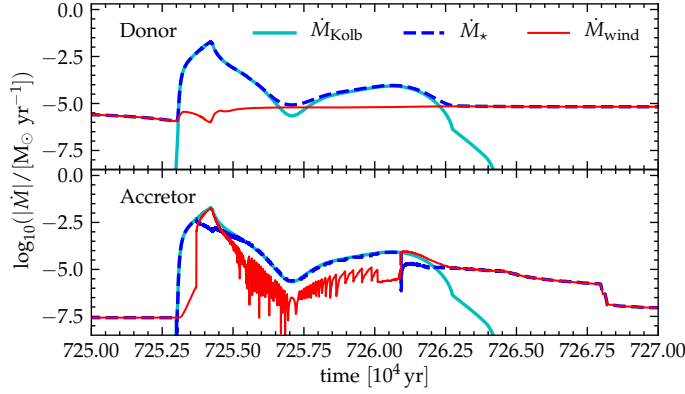


Figure 2. Mass transfer rates as a function of time during RLOF. The top (bottom) panel shows the donor (accretor) star. The cyan solid lines show the mass transfer rate between the two stars. The dashed blue lines show the actual change in the mass of the stars (due to the combination of wind, and accretion efficiency). The thin red lines show the wind mass loss rates. During RLOF the accretor reaches critical rotation, which leads to oscillations in the rotationally-enhanced wind mass loss.

its terminal age main sequence (shown in the bottom panel).

The orbital velocity would likely decrease a bit further due to wind-driven widening of the binary ■ [estimate and ref] ■, therefore one can expect this system to produce a runaway star of velocity comparable to ζ Oph if the stripped donor can successfully explode ??.

■ [discuss rotation rate and radius with fig. 3] ■

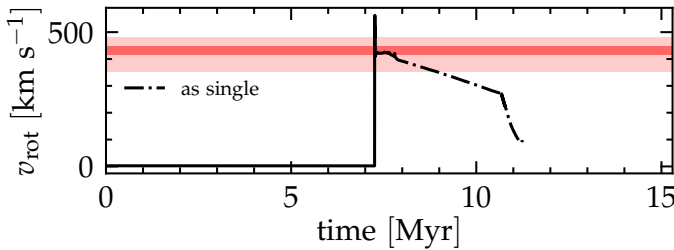


Figure 3. Surface averaged rotation rate for the accretor model. Shortly after ~ 7 Myr the mass transfer quickly spins up the accretor at critical rotation. By the time the donor detaches from the RLOF the accretor is still spinning at ~ 400 km s $^{-1}$. At this point (beginning of the dot-dashed line), we continue the evolution as a single star, and the accretor quickly spins down. Note however that we use a wind mass-loss rate from Vink et al. (2001), which is observed to be ~ 2 orders of magnitude too high.

3.1. Mixing and surface composition

4. ROBUSTNESS OF THE MODEL

In this section we investigate the sensitivity of our results to physical parameters.

■ [How to present results? Table? Showing what? surface mass fractions, rotation, L, Teff] ■

■ [Binary parameters:

- M_1
- M_2
- P
- J-accretion

] ■

■ [Single star parameters:

- thermohaline mixing
- Eddington-Sweet circulations
- metallicity

] ■

■ [others?] ■

5. DISCUSSION

■ [no SN pollution, but Hirai et al. (2018) shows this is a small effect.] ■

6. CONCLUSIONS

We have demonstrated that self-consistent one-dimensional calculations of coupled stellar models with masses $\gtrsim 20 M_\odot$ are possible with the MESA software instrument. As a first application, we focused on finding a model for ζ Oph, assuming its runaway nature is explained by the binary SN scenario.

We found that it is likely possible to explain its surface composition without assuming that the surface excess of He and N comes from within the star. Instead, this material comes from the receding core of the donor star. Therefore, the present day abundances constrain the accretion efficiency and mixing in the accretor.

ζ Oph should therefore *not* be used to test models of rotational mixing in single star evolution, nor its more extreme version of chemically homogeneous evolution.

Software: mesaPlot (Farmer 2018), mesaSDK (Townsend 2018), ipython/jupyter (Pérez & Granger 2007), matplotlib (Hunter 2007), NumPy (van der Walt et al. 2011), MESA (Paxton et al. 2011, 2013, 2015, 2018, 2019)

ACKNOWLEDGEMENTS

APPENDIX

A. MESA SETUP

■ [MLT-?] ■

■ [possibly move to methods] ■ We use

MESA version 15140 to compute our models. The MESA equation of state (EOS) is a blend of the OPAL Rogers & Nayfonov (2002), SCVH Saumon et al. (1995), PTEH Pols et al. (1995), HELM Timmes & Swesty (2000), and PC Potekhin & Chabrier (2010) EOSes. ■ [check if updated EOS?] ■

Radiative opacities are primarily from OPAL (Iglesias & Rogers 1993, 1996), with low-temperature data from Ferguson et al. (2005) and the high-temperature, Compton-scattering dominated regime by Buchler & Yueh (1976). Electron conduction opacities are from Cassisi et al. (2007).

Nuclear reaction rates are a combination of rates from NACRE (Angulo et al. 1999), JINA REACLIB (Cyburt et al. 2010), plus additional tabulated weak reaction rates Fuller et al. (1985); Oda et al. (1994); Langanke & Martínez-Pinedo (2000). Screening is included via the prescription of Chugunov et al. (2007). Thermal neu-

trino loss rates are from Itoh et al. (1996). We use a 22-isotope nuclear network (approx_21_plus_cr56).

We treat convection using the Ledoux criterion, and include thermohaline mixing and semiconvection, both with an efficiency factor of 1. We assume $\alpha_{\text{MLT}} = 1.5$ and use ■ [fix] ■ Brott et al. (2011) overshooting for the convective core burning. ■ [fix] ■ Moreover, we employ the MLT++ artificial enhancement of the convective flux (e.g., Paxton et al. 2015). Stellar winds are included using the algorithms from Vink et al. (2001) with an efficiency factor of 1.

The inlists, processing scripts, and model output will be made available at [link](#).

B. RESOLUTION TESTS

B.1. Spatial resolution

ACKNOWLEDGMENTS

E. Zapartas

REFERENCES

- Angulo, C., Arnould, M., Rayet, M., et al. 1999, Nuclear Physics A, 656, 3, doi: [10.1016/S0375-9474\(99\)00030-5](#)
- Belczynski, K., Holz, D. E., Bulik, T., & O’Shaughnessy, R. 2016, Nature, 534, 512, doi: [10.1038/nature18322](#)
- Blaauw, A. 1952, BAN, 11, 414
- . 1961, BAN, 15, 265
- Blaauw, A. 1993, in Astronomical Society of the Pacific Conference Series, Vol. 35, Massive Stars: Their Lives in the Interstellar Medium, ed. J. P. Cassinelli & E. B. Churchwell, 207
- Blagorodnova, N., Klencki, J., Pejcha, O., et al. 2021, arXiv e-prints, arXiv:2102.05662, <https://arxiv.org/abs/2102.05662>
- Bodensteiner, J., Baade, D., Greiner, J., & Langer, N. 2018, A&A, 618, A110, doi: [10.1051/0004-6361/201832722](#)
- Braun, H., & Langer, N. 1995, A&A, 297, 483
- Brott, I., de Mink, S. E., Cantiello, M., et al. 2011, A&A, 530, A115, doi: [10.1051/0004-6361/201016113](#)
- Buchler, J. R., & Yueh, W. R. 1976, ApJ, 210, 440, doi: [10.1086/154847](#)
- Cantiello, M., Yoon, S., Langer, N., & Livio, M. 2007, A&A, 465, L29
- Cassisi, S., Potekhin, A. Y., Pietrinferni, A., Catelan, M., & Salaris, M. 2007, ApJ, 661, 1094, doi: [10.1086/516819](#)
- Chugunov, A. I., Dewitt, H. E., & Yakovlev, D. G. 2007, PhRvD, 76, 025028, doi: [10.1103/PhysRevD.76.025028](#)
- Claret, A., & Torres, G. 2017, ApJ, 849, 18, doi: [10.3847/1538-4357/aa8770](#)
- Cyburt, R. H., Amthor, A. M., Ferguson, R., et al. 2010, ApJS, 189, 240, doi: [10.1088/0067-0049/189/1/240](#)
- de Jager, C., Nieuwenhuijzen, H., & van der Hucht, K. A. 1988, A&AS, 72, 259
- Farmer, R. 2018, rjfarmer/mesaplot, doi: [10.5281/zenodo.1441329](#)
- Ferguson, J. W., Alexander, D. R., Allard, F., et al. 2005, ApJ, 623, 585, doi: [10.1086/428642](#)
- Fuller, G. M., Fowler, W. A., & Newman, M. J. 1985, ApJ, 293, 1, doi: [10.1086/163208](#)
- Gotberg, Y., de Mink, S. E., & Groh, J. H. 2017, <https://arxiv.org/abs/1701.07439>
- Götberg, Y., de Mink, S. E., Groh, J. H., et al. 2018, A&A, 615, A78, doi: [10.1051/0004-6361/201732274](#)
- Heger, A., Langer, N., & Woosley, S. E. 2000, ApJ, 528, 368
- Hellings, P. 1983, Ap&SS, 96, 37, doi: [10.1007/BF00661941](#)
- . 1984, Ap&SS, 104, 83, doi: [10.1007/BF00653994](#)



Figure 4. Left: HRD comparison for our fiducial binary model varying the number of mesh points. We only show the evolution until our definition of RLOF detachment. Right: number of mesh points as a function of timestep number. In both panels, the blue/cyan tracks show the donor stars, the red/pink tracks show the accretor. Thicker dashed lines correspond to the models at higher resolution (i.e., lower Δ which indicates the value of `mesh_delta_coeff`).

Herrero, A., Kudritzki, R. P., Vilchez, J. M., et al. 1992, A&A, 261, 209
 Herwig, F. 2000, A&A, 360, 952
 Hirai, R., Podsiadlowski, P., & Yamada, S. 2018, <https://arxiv.org/abs/1803.10808>
 Hoogerwerf, R., de Bruijne, J. H. J., & de Zeeuw, P. T. 2000, ApJL, 544, L133, doi: [10.1086/317315](https://doi.org/10.1086/317315)
 —. 2001, A&A, 365, 49, doi: [10.1051/0004-6361:20000014](https://doi.org/10.1051/0004-6361:20000014)
 Hunter, J. D. 2007, Computing In Science & Engineering, 9, 90
 Iglesias, C. A., & Rogers, F. J. 1993, ApJ, 412, 752, doi: [10.1086/172958](https://doi.org/10.1086/172958)
 —. 1996, ApJ, 464, 943, doi: [10.1086/177381](https://doi.org/10.1086/177381)
 Itoh, N., Hayashi, H., Nishikawa, A., & Kohyama, Y. 1996, ApJS, 102, 411, doi: [10.1086/192264](https://doi.org/10.1086/192264)
 Kippenhahn, R., Ruschenplatt, G., & Thomas, H.-C. 1980, A&A, 91, 175
 Kippenhahn, R., & Weigert, A. 1967, ZA, 65, 251
 Kolb, U., & Ritter, H. 1990, A&A, 236, 385
 Langanke, K., & Martínez-Pinedo, G. 2000, Nuclear Physics A, 673, 481, doi: [10.1016/S0375-9474\(00\)00131-7](https://doi.org/10.1016/S0375-9474(00)00131-7)
 Langer, N. 1998, A&A, 329, 551
 Langer, N., Fricke, K. J., & Sugimoto, D. 1983, A&A, 126, 207

Laplace, E., Götberg, Y., de Mink, S. E., Justham, S., & Farmer, R. 2020, A&A, 637, A6, doi: [10.1051/0004-6361/201937300](https://doi.org/10.1051/0004-6361/201937300)
 Laplace, E., Justham, S., Renzo, M., et al. 2021, arXiv e-prints, arXiv:2102.05036, <https://arxiv.org/abs/2102.05036>
 Law-Smith, J. A. P., Everson, R. W., Ramirez-Ruiz, E., et al. 2020, arXiv e-prints, arXiv:2011.06630, <https://arxiv.org/abs/2011.06630>
 Maeder, A., & Meynet, G. 2000, ARA&A, 38, 143, doi: [10.1146/annurev.astro.38.1.143](https://doi.org/10.1146/annurev.astro.38.1.143)
 Marcolino, W. L. F., Bouret, J. C., Martins, F., et al. 2009, A&A, 498, 837, doi: [10.1051/0004-6361/200811289](https://doi.org/10.1051/0004-6361/200811289)
 Meynet, G., & Maeder, A. 2000, A&A, 361, 101
 Murphy, S. J., Joyce, M., Bedding, T. R., White, T. R., & Kama, M. 2021, MNRAS, 502, 1633, doi: [10.1093/mnras/stab144](https://doi.org/10.1093/mnras/stab144)
 Neuhauser, R., Gießler, F., & Hambaryan, V. V. 2020, MNRAS, 498, 899, doi: [10.1093/mnras/stz2629](https://doi.org/10.1093/mnras/stz2629)
 Oda, T., Hino, M., Muto, K., Takahara, M., & Sato, K. 1994, Atomic Data and Nuclear Data Tables, 56, 231, doi: [10.1006/adnd.1994.1007](https://doi.org/10.1006/adnd.1994.1007)
 Packet, W. 1981, A&A, 102, 17
 Paxton, B., Bildsten, L., Dotter, A., et al. 2011, ApJS, 192, 3, doi: [10.1088/0067-0049/192/1/3](https://doi.org/10.1088/0067-0049/192/1/3)

- Paxton, B., Cantiello, M., Arras, P., et al. 2013, *ApJS*, 208, 4, doi: [10.1088/0067-0049/208/1/4](https://doi.org/10.1088/0067-0049/208/1/4)
- Paxton, B., Marchant, P., Schwab, J., et al. 2015, *ApJS*, 220, 15, doi: [10.1088/0067-0049/220/1/15](https://doi.org/10.1088/0067-0049/220/1/15)
- Paxton, B., Schwab, J., Bauer, E. B., et al. 2018, *ApJS*, 234, 34, doi: [10.3847/1538-4365/aaa5a8](https://doi.org/10.3847/1538-4365/aaa5a8)
- Paxton, B., Smolec, R., Gautschy, A., et al. 2019. <https://arxiv.org/abs/1903.01426>
- Pérez, F., & Granger, B. E. 2007, *Computing in Science & Engineering*, 9, 21
- Perna, R., Duffell, P., Cantiello, M., & MacFadyen, A. I. 2014, *ApJ*, 781, 119, doi: [10.1088/0004-637X/781/2/119](https://doi.org/10.1088/0004-637X/781/2/119)
- Pols, O. R., Tout, C. A., Eggleton, P. P., & Han, Z. 1995, *MNRAS*, 274, 964, doi: [10.1093/mnras/274.3.964](https://doi.org/10.1093/mnras/274.3.964)
- Potekhin, A. Y., & Chabrier, G. 2010, *Contributions to Plasma Physics*, 50, 82, doi: [10.1002/ctpp.201010017](https://doi.org/10.1002/ctpp.201010017)
- Renzo, M., Zapartas, E., de Mink, S. E., et al. 2019, *A&A*, 624, A66, doi: [10.1051/0004-6361/201833297](https://doi.org/10.1051/0004-6361/201833297)
- Rogers, F. J., & Nayfonov, A. 2002, *ApJ*, 576, 1064, doi: [10.1086/341894](https://doi.org/10.1086/341894)
- Saumon, D., Chabrier, G., & van Horn, H. M. 1995, *ApJS*, 99, 713, doi: [10.1086/192204](https://doi.org/10.1086/192204)
- Sota, A., Maíz Apellániz, J., Morrell, N. I., et al. 2014, *ApJS*, 211, 10, doi: [10.1088/0067-0049/211/1/10](https://doi.org/10.1088/0067-0049/211/1/10)
- Spruit, H. C. 2002, *A&A*, 381, 923, doi: [10.1051/0004-6361:20011465](https://doi.org/10.1051/0004-6361:20011465)
- Sweet, P. A. 1950, *MNRAS*, 110, 548, doi: [10.1093/mnras/110.6.548](https://doi.org/10.1093/mnras/110.6.548)
- Tauris, T. M., Kramer, M., Freire, P. C. C., et al. 2017, *ApJ*, 846, 170, doi: [10.3847/1538-4357/aa7e89](https://doi.org/10.3847/1538-4357/aa7e89)
- Tetzlaff, N., Neuhäuser, R., Hohle, M. M., & Maciejewski, G. 2010, *MNRAS*, 402, 2369, doi: [10.1111/j.1365-2966.2009.16093.x](https://doi.org/10.1111/j.1365-2966.2009.16093.x)
- Timmes, F. X., & Swesty, F. D. 2000, *ApJS*, 126, 501, doi: [10.1086/313304](https://doi.org/10.1086/313304)
- Townsend, R. 2018, *MESA SDK for Linux*: 20180822, doi: [10.5281/zenodo.2603170](https://doi.org/10.5281/zenodo.2603170)
- van der Walt, S., Colbert, S. C., & Varoquaux, G. 2011, *Computing in Science Engineering*, 13, 22, doi: [10.1109/MCSE.2011.37](https://doi.org/10.1109/MCSE.2011.37)
- van Rensbergen, W., Vanbeveren, D., & De Loore, C. 1996, *A&A*, 305, 825
- Villamariz, M. R., & Herrero, A. 2005, *A&A*, 442, 263, doi: [10.1051/0004-6361:20052848](https://doi.org/10.1051/0004-6361:20052848)
- Vink, J. S., de Koter, A., & Lamers, H. J. G. L. M. 2000, *A&A*, 362, 295
- . 2001, *A&A*, 369, 574, doi: [10.1051/0004-6361:20010127](https://doi.org/10.1051/0004-6361:20010127)
- Walker, G. A. H., Yang, S., & Fahlman, G. G. 1979, *ApJ*, 233, 199, doi: [10.1086/157381](https://doi.org/10.1086/157381)
- Yoon, S.-C., Langer, N., & Norman, C. 2006, *A&A*, 460, 199, doi: [10.1051/0004-6361:20065912](https://doi.org/10.1051/0004-6361:20065912)
- Zehe, T., Mugrauer, M., Neuhäuser, R., et al. 2018, *Astronomische Nachrichten*, 339, 46, doi: [10.1002/asna.201713383](https://doi.org/10.1002/asna.201713383)