

Testing models of accreting stars in massive binaries on ζ Ophiuchi

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ABSTRACT

Binarity dominates the evolution of massive stars, and the nearest O-type star to Earth, ζ Ophiuchi, has long been proposed to be a product of binary evolution. Despite this, most stellar models have tried unsuccessfully to reproduce its observable properties relying on single-star rotating models. ■ **[Here we do better]** ■

Keywords: stars: individual: ζ Ophiuchi – stars: massive – stars: binaries

1. INTRODUCTION

The overwhelming majority of massive stars is born in multiple systems (e.g., Mason et al. 2009; Almeida et al. 2017), and a large fraction will exchange mass or merge with a companion in their lifetime (e.g., Sana et al. 2012). The most common type of interaction is a post-main-sequence stable mass transfer (case B) through Roche Lobe overflow (RLOF, Kippenhahn & Weigert 1967). Many studies (e.g., Götzberg et al. 2017, 2018; Laplace et al. 2020, 2021; Blagorodnova et al. 2021) ■ **[more refs. from other groups]** ■ have focused on the dramatic impact of these interactions on the initially more massive donor star. Often the closest binary companion is treated as a point mass.

However, binary interactions have a crucial impact on the initially less massive star too: during mass transfer, these are expected to accrete mass, spin up to critical rotation (e.g., Packet 1981; Cantiello et al. 2007), and possibly be polluted by CNO-processed material from the inner core of the donor star (e.g., Blaauw 1993). The growth of the convective core due to the increased mass leads to “rejuvenation” of the accretor (e.g., Neo et al. 1977; Schneider et al. 2016).

Understanding the evolution of accretors in massive binaries has wider and crucial implications for stellar populations, electromagnetic transient observations, and gravitational-wave progenitors. Accretors (and mergers) can appear as blue stragglers and thus impact cluster populations and their age estimates and main sequence morphology (e.g., Pols & Marinus 1994; Wang et al. 2020). Moreover, the majority of massive binaries will be disrupted by the first supernova ejecting the companion (“binary SN scenario”, Blaauw 1961; De Donder et al. 1997; Eldridge et al. 2011; Renzo et al.

2019; Evans et al. 2020). Therefore, populations of field massive stars contain presently single O-type stars that accreted mass earlier on. The majority of these will be too slow to stand out in astrometric surveys (e.g., Eldridge et al. 2011; Renzo et al. 2019). Assuming a constant star formation history, Renzo et al. (2019) estimated that $10.1^{+4.6}_{-8.6}\%$ of O-type stars might be accretors released after a SN – where the errors span a range of parameter variations.

From the transients perspective, massive accretors stars are also important: Zapartas et al. (2019) showed that $14^{+4}_{-11}\%$ of hydrogen-rich (type II) SNe might come from these progenitors after being ejected from a binary. The fact that they accreted mass before exploding can influence their helium (He) core mass and thus the explosion properties and the inferred progenitors (Zapartas et al. 2021).

Finally, the majority of isolated binary evolutionary scenarios for gravitational-wave progenitors go through a common-envelope phase initiated by the originally less massive accretor after the formation of the first compact object (e.g., Belczynski et al. 2016; Tauris et al. 2017; Broekgaarden et al. 2021). Therefore, it is possible that accretion of mass before the formation of the first compact object could modify the internal structure of the star that will initiate the common-envelope phase (e.g. Law-Smith et al. 2020; Klencki et al. 2021).

Despite their importance, accretor stars in binaries have so far received much less attention than the donor stars, with the pioneering studies of Ulrich & Burger (1976); Hellings (1983, 1984), and Braun & Langer (1995) as notable exceptions. Large grids of accretor models are lacking, most of the studies focus on lower mass B-type donors (e.g., van Rensbergen et al. 2006, 2011, but see also Wang et al. 2020) and only few sparse

massive models exist (e.g., [Cantiello et al. 2007](#)). This is because of the complexity of modeling these, which requires following in detail the *coupled* evolution of two rotating stars exchanging mass. Moreover, the admittedly large number of free parameters involved in the modeling of each individual star and their interactions makes robust predictions challenging to obtain. Here, we argue that the nearest O-type star to Earth, ζ Ophiuchi¹ (ζ Oph) provides a unique opportunity to constrain these models.

ζ Oph has a distance from Earth of 107 ± 4 pc ([Neuhäuser et al. 2020](#), and references therein), and a spectral type O9.5IVnn ([Sota et al. 2014](#)). It occasionally shows emission lines ([Walker et al. 1979](#); [Vink et al. 2009](#)), making it an Oe star. It was originally identified as a runaway because of its large proper motion by [Blaauw \(1952\)](#). Unfortunately, the *Gaia* data for this object are not of sufficient quality² to improve previous astrometric results, but estimates of the peculiar velocity range in $30 - 50$ km s⁻¹ (e.g., [Zehe et al. 2018](#); [Neuhäuser et al. 2020](#)). The large velocity with respect to the surrounding interstellar material is also confirmed by the presence of a prominent bow-shock (e.g., [Bodensteiner et al. 2018](#)).

Because of its young apparent age, extremely fast rotation ($v \sin(i) \gtrsim 400$ km s⁻¹, e.g., [Zehe et al. 2018](#)), and nitrogen (N) and He rich surface (e.g., [Herrero et al. 1992](#); [Blaauw 1993](#); [Villamariz & Herrero 2005](#); [Marcolino et al. 2009](#)), ζ Oph is a prime candidate for the binary SN scenario ([Blaauw 1993](#)). Many studies have suggested ζ Oph might have accreted mass from a companion before acquiring its large velocity, both from spectroscopic and kinematic considerations (e.g., [Blaauw 1993](#); [Hoogerwerf et al. 2000, 2001](#); [Tetzlaff et al. 2010](#); [Neuhäuser et al. 2020](#)) and using stellar modeling arguments (e.g., [van Rensbergen et al. 1996](#)). Recently, [Neuhäuser et al. \(2020\)](#) suggested that 1.78 ± 0.21 Myr ago a supernova in Upper-Centaurus-Lupus produced the pulsar PSR B1706-16, ejected ζ Oph, and also injected the short-lived radioactive isotope ⁶⁰Fe on Earth. This argues strongly for a successful supernova explosion of the companion with a large ~ 250 km s⁻¹ natal kick, which in most cases would be sufficient to disrupt the binary (e.g., [Tauris 2015](#); [Renzo et al. 2019](#); [Evans et al. 2020](#)).

Although the nature of ζ Oph as a binary product is well established, because of its observed large surface rotation rate, previous attempts to model it rely purely

on rotational mixing to explain the surface composition (e.g., [Maeder & Meynet 2000](#)). Even the binary models of [van Rensbergen et al. \(1996\)](#) assumed spin-up due to mass accretion to drive rotational mixing from the interior of the accreting star (see also [Cantiello et al. 2007](#)). However, [Villamariz & Herrero \(2005\)](#) (hereafter, [VH05](#)) were unable to find good fit for the stellar spectra using the rotating models from [Meynet & Maeder \(2000\)](#).

This may not be surprising: rotational mixing has lower efficiency for metal-rich and relatively low mass stars because of the increased importance of mean molecular weight gradients and longer thermal timescales compared to more massive stars (e.g., [Yoon et al. 2006](#); [Perna et al. 2014](#)). The parent association has a metallicity $Z = 0.01 \simeq Z_{\odot}$ (based on asteroseismology from [Murphy et al. 2021](#)), and mass estimates for ζ Oph range from $13 - 25 M_{\odot}$, at the lower end of the range where efficient mixing might bring He and CNO-processed material to the surface (chemically homogeneous evolution).

Given the challenges in explaining the surface composition of ζ Oph with rotational mixing from the stellar interior and the strong evidence for its past as a member of a binary system, this star offers a unique opportunity to constrain the evolution of accreting stars in massive binary systems.

Here, we present self-consistent binary evolution models for ζ Oph computing simultaneously the coupled evolution of *both* donor and accretor star and their orbit. ■ **[fix order description]** ■ After presenting our MESA setup in Sec. 2, we show our best model which reproduces the majority of the salient features of this star in Sec. 3. We discuss the sensitivity of our results to the admittedly many free parameters required for this kind of computations in Sec. ???. Finally, we conclude in Sec. 5.

2. MODELING MASSIVE BINARIES WITH MESA

Modeling the evolution of massive binaries ($M_1 \gtrsim 20 M_{\odot} \geq M_2$) is challenging because of the intricate role of several notoriously difficult stellar physics ingredients (differential rotation, mixing, high mass-loss rates, accretion, etc.). Here we follow self-consistently the coupled evolution of two massive stars in a binary system using MESA (version 15140). Our choice of input parameters and our numerical results are available at ■ **[link]** ■. We discuss here only the main relevant physical parameters, and Appendix A gives more details on our choice of input physics.

We adopt the Ledoux criterion to determine convective stability and a mixing length parameter of 1.5. We include semiconvection and thermohaline mixing follow-

¹ also known as HD 149 757.

² The renormalized unit weighted error (RUWE) of this star in *Gaia* EDR3 is 4.48.

ing Langer et al. (1983) and Kippenhahn et al. (1980), respectively, each with efficiency 1.0. We use the exponential core overshooting from Herwig (2000) with free parameters $(f, f_0) = (4.25 \times 10^{-2}, 10^{-3})$ (Claret & Torres 2017) which broadly reproduce the width of the main sequence from Brott et al. (2011). We also use the local implicit enhancement of the convective flux in superadiabatic regions (MLT++) introduced in MESA 15140.

We treat rotation in the “shellular” approximation and initialize it assuming tidal synchronization at the beginning of the evolution. For our fiducial period choice ($P = 100$ days), this effectively means both the stars in our binary are initially slow rotators. Our models include in a diffusive approximation the effect of Eddington-Sweet circulations (Sweet 1950), which dominates the chemical mixing due to rotation. We also include the secular and dynamical shear instabilities, and the Goldreich-Schubert-Fricke instability as in Götberg et al. (2017, 2018); Laplace et al. (2020, 2021). We assume a Spruit-Tayler dynamo for the transport of angular momentum (Spruit 2002), and chose the same free parameters as Heger et al. (2000). This also includes the rotational enhancement of wind mass loss as in Langer (1998).

We assume a fiducial metallicity of $Z = 0.01$ informed by the present-day Z of the parent cluster (Murphy et al. 2021), and assume scaling of the relative element abundances with the solar abundances of Grevesse & Sauval (1998). We include wind mass loss with the Vink et al. (2000, 2001) hot wind, and de Jager et al. (1988) for effective temperature $T_{\text{eff}} < 10^{4.2}$ K, both with a scaling factor of 1. Nominally, this means our wind mass-loss rate post-mass transfer is overestimated by almost a factor of 100 compared to observations (weak wind problem, see Marcolino et al. 2009). However, Lucy (2012) and Lagae et al. (2021) proposed that the temperature structure of the winds of low-luminosity O-type stars might affect the spectral lines and cause an empirical underestimate of the mass-loss rate.

Both stars are evolved simultaneously on the same timesteps until after the donor detaches from its Roche lobe. We follow Kolb & Ritter (1990) to calculate the mass transfer rate from optically thick layers of the donor star during Roche lobe overflow (RLOF). Moreover, we assume that the specific angular momentum and entropy of the transferred layers match the surface, while the chemical composition is determined structure of the donor star. Mass transfer is conservative until the accretor reaches critical rotation, after which rotationally enhanced mass loss governs the accretion efficiency.

After losing their envelope, massive donors are not expected to expand to hundreds of R_{\odot} during He-shell

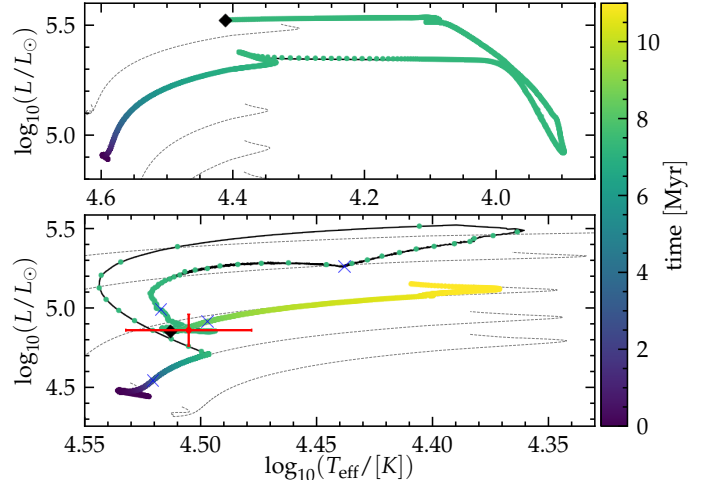


Figure 1. HRD for the donor star (top) and accretor star (bottom) of the progenitor binary of ζ Oph. Each point is separated by 50 years of evolution. The colors represent the stellar age, the red datapoint shows the position of ζ Oph according to VH05, thin blue crosses mark the position of the profiles shown in Fig. 3, and the black diamonds mark the position at the end of the binary run. We continue the accretor evolution as a single star from there until core H depletion, hence the bottom panel shows a longer time. We emphasize the different scales on the two panels. The thin gray dashed line show the main sequence evolution of non-rotating single stars of 15, 17, 25, and $30 M_{\odot}$ at $Z = 0.01$ for comparison.

burning at the metallicity we consider (e.g., Laplace et al. 2020). Thus, we stop evolving a binary system when the donor’s surface He mass fraction is larger than 0.35 – indicating that a significant amount of envelope has been lost or transferred, and the radius is smaller than both the Roche radius and the terminal-age main sequence radius (TAMS, defined as when the central mass fraction of H drops below 10^4). From here onwards, we continue the evolution of the accretor as a single star until its TAMS with the same setup.

■ [describe parameter variations in this sec.] ■

3. MASSIVE BINARY EVOLUTION NATURALLY EXPLAINS ζ OPHIUCHI’S PROPERTIES

We describe here the evolution of a binary system where the accretor star can broadly reproduce all the observed features of ζ Oph. We assume initial masses $M_1 = 25 M_{\odot}$, $M_2 = 17 M_{\odot}$ on a period of 100 days at $Z = 0.01$.

Fig. 1 shows the Hertzsprung-Russell diagrams (HRD) of both stars. After ~ 7.24 Myr, the donor star (top panel) evolves off the main sequence and ~ 8400 years later, when the donor’s effective temperature reaches

about $T_{\text{eff}} \simeq 10^4$ K, mass transfer starts. This results in a stable case B RLOF. We refer to [Götberg et al. \(2017\)](#); [Laplace et al. \(2021\)](#); [Blagorodnova et al. \(2021\)](#) and references therein for a detailed description of the evolution of massive donor stars in binaries. Although our models are more massive, the qualitative behavior of the donor star is similar.

At the onset of RLOF, the accretor star (bottom panel of Fig. 1) is still on the main sequence with $T_{\text{eff}} \simeq 10^{4.5}$ K. Because of accretion, it quickly becomes over-luminous ($L \simeq 10^{5.4} L_{\odot}$), and its radius increases dramatically from $\sim 7.5 R_{\odot}$ to $\sim 35 R_{\odot}$. Once the accretor reaches critical rotation (roughly at the lowest T_{eff} in the bottom panel of Fig. 1), the star begins contracting and its T_{eff} increases. At $T_{\text{eff}} \simeq 4.43$ K the material transferred from the companion star becomes progressively more He-rich, causing a “v-shaped” feature in the evolutionary track. This indicates that the partially processed outer layers of the donor’s core are uncovered by mass transfer. This late mass transfer puts material at high mean molecular weight μ on top of the primordial envelope of the accretor, modifying the morphology of the evolutionary track. Thermohaline mixing starts in the outer layers of the accreting star, and, together with rotational mixing, it progressively dilutes the surface He and N mass fractions and causes noisy features on the HR diagram (e.g., [Cantiello et al. 2007](#)). The (standard) algorithmic choices in modelling mixing and rotation might impact the morphology of the accretor’s evolutionary track during RLOF. The entire duration of RLOF is only about 10^4 years, and therefore unlikely to be observable to probe directly the accuracy of our treatment of mixing. We expand on the mixing processes inside the accretor in Sec. 3.1.

We evolve the binary system until the black diamonds in Fig. 1, which occurs well after the donor detaches from the Roche Lobe. At this point, the accretor is a H-rich fast-rotating star of $\sim 20.1 M_{\odot}$. Available mass estimates for the presently single ζ Oph are highly uncertain, but most include $20 M_{\odot}$ (e.g., [Hoogerwerf et al. 2001](#), [VH05](#), [Neuhäuser et al. 2020](#)). The accretor’s post-RLOF orbital velocity is $v_2 \simeq 40 \text{ km s}^{-1}$, which is expected to decrease a bit further due to wind-driven widening of the binary, but is in good agreement with the presently observed runaway velocity of ζ Oph.

Accounting for both wind mass loss and the amount of mass transferred, at the end of RLOF the donor becomes a He star of $\sim 9.4 M_{\odot}$, likely to contract further and appear as a Wolf-Rayet star. Its surface H mass fraction is $\lesssim 0.2$ and most of the H is likely to be removed by further wind mass loss (e.g., [Götberg et al. 2017](#)). ■ [Ylva: want to expand?] ■

From the black diamond onwards, we evolve the accretor as a single star with the same MESA setup until TAMS. The main-sequence track on which the accretor settles post-RLOF has a higher luminosity compared to the original track because of the accretion of mass, and it has also a slightly different slope due to the close-to-critical rotation and the accretion of partially nuclearly processed material (He- and N-rich) material.

The red errorbars in the bottom panel of Fig. 1 mark the approximate position of ζ Oph based on the analysis of [VH05](#). The color of the track in Fig. 1 indicate that our accreting star spends about ~ 2 Myr within the represented errorbars after the end of RLOF. Assuming the kinematic age of 1.78 ± 0.21 ([Neuhäuser et al. 2020](#)), and estimating a remaining lifetime of the donor of ~ 0.5 Myr, this gives the correct timescale for the binary SN scenario.

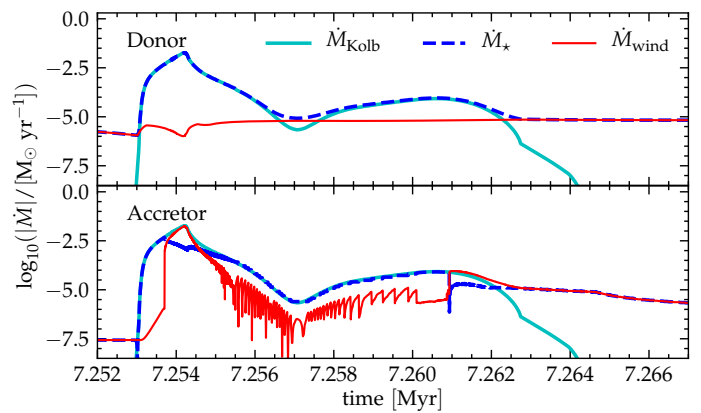


Figure 2. Mass transfer rates as a function of time during RLOF. The top (bottom) panel shows the donor (accretor) star. The cyan solid lines show the mass transfer rate between the two stars. The dashed blue lines show the actual change in the mass of the stars (due to the combination of wind, and accretion efficiency). The thin red lines show the wind mass loss rates. During RLOF the accretor reaches critical rotation, which leads to oscillations in the rotationally-enhanced wind mass loss.

Fig. 2 shows the rate of mass change for each star during RLOF. The top panel focuses on the donor star which loses mass to RLOF (cyan line) and wind mass loss (thin red line). The dashed blue lines show their combination resulting in the actual rate of mass change of the stars. The bottom panel shows instead the accreting star, which grows in mass because of the mass transfer. At peak the mass transfer rates reaches very high values above $10^{-2.5} M_{\odot} \text{ yr}^{-1}$, and taps into the optically thick matter of the donor.

At the end of RLOF, the donor star briefly expands again ($T_{\text{eff}} \simeq 10^{4.1}$ K, $L \simeq 10^{5.5} L_{\odot}$). This is due to the

partial recombination of the now He-rich outer layers, which causes a transient surface convection layer. This causes the second broad peak in the mass transfer rates centered at 7.261 Myrs. We find this to be the culprit of the numerical difficulties for massive mass-transferring binaries with older MESA releases: although only a very small amount of mass is involved, the onset of convection causes a large radius variation which impacts the mass transfer rate.

The wind mass loss (in red) controls the accretion efficiency and thus the difference between the actual rate of change in mass of the accretor (thick dashed blue) and the rate at which mass is being transferred. At peak, where the red and the cyan lines overlap, mass transfer becomes very non-conservative, but for most of the evolution the (rotationally enhanced) wind removes only a fraction of the accreted mass. The interplay between the stellar radius and rotation causes the oscillations visible in the bottom panel, whose amplitude is generally lower than the RLOF mass transfer rate.

3.1. *Mixing and composition*

MESA treats mixing in the diffusion approximation (Paxton et al. 2011). To illustrate the dominant processes throughout the accretor’s evolution, we show in Fig. 3 the diffusion coefficients for various mixing processes as a function of mass coordinate at selected times. Each panel corresponds to one of the thin blue crosses in the bottom panel of Fig. 1, and the gray shaded areas highlight mass accreted during RLOF. The last panel roughly represents the predicted internal structure of ζ Oph as observed today.

In Fig. 3, the thin red lines correspond to convection, with the initial convective core of $\sim 6 M_{\odot}$ clearly visible in the first panel. In all models, a tiny sub-surface convective region is also visible in the outermost layers (see e.g., Cantiello et al. 2021). The thin blue lines show the exponentially decreasing overshooting above the convective core. Purple and pink represent semiconvection and thermohaline mixing, respectively. Before mass transfer (left-most panel), only a small amount of sub-surface thermohaline mixing occurs, with a mass extent comparable or smaller to the sub-surface convective zone, and no semiconvection occurs. The thick cyan line corresponds to the total diffusion coefficient, obtained as the sum of the diffusion coefficients for each process modeled: where the cyan line is not overlapping with the others, rotational mixing (and more specifically Eddington-Sweet meridional circulation) is the dominant process.

During RLOF (second and third panel), the spin-up due to accretion causes an increase in the rotational mixing (see also Sec. 3.2), and the accretion of nuclearily

processed material progressively widens the thermohaline mixing region at the surface. Late during the mass transfer (third panel), thermohaline mixing dominates the outermost layers – except within the sub-surface convective zone. Nevertheless, throughout most of the envelope, rotation does the lion’s share of the mixing. Thermohaline mixing and Eddington-Sweet circulations together mix inwards and dilute the CNO-enriched material coming from the donor’s surface.

At the same time, the increase in the accretor mass drives rejuvenation (e.g., Schneider et al. 2016). This can be seen as a growth of the convective core from $\sim 6 M_{\odot}$ to almost $\sim 8 M_{\odot}$, plus the corresponding growth of the overshooting region. This mixes inward H-rich material resulting in an elongation of the accretor’s lifetime, and at the same time mixes outward CNO-equilibrium matter, connecting the N-rich core with the outer envelope polluted from the top.

Tab. 1 summarizes the surface properties of the accretor star at the time shown in the last panel of Fig. 3, that is shortly after the RLOF phase, while the model is still roughly at the observed position of ζ Oph.

Both the mass and radius agree reasonably well with the estimates from VH05 and previous studies, that is $20 M_{\odot}$ and $8.3 \pm 1.5 R_{\odot}$, respectively. The surface rotational velocity in excess of 350 km s^{-1} is also in the correct ballpark albeit possibly on the low end. We report the surface H mass fraction³, lower than primordial because of the accretion of nuclearily processed material, and the surface mass fraction of the most prominent species ^4He , ^{12}C , ^{14}N , ^{16}O . Assuming our surface H mass fraction $X(^1\text{H})$, the corresponding mass fractions of ^4He , ^{12}C , ^{14}N , ^{16}O obtained by VH05 are $0.33^{+0.14}_{-0.05}$, 0.0006 ± 0.0004 , 0.002 ± 0.001 , and 0.005 ± 0.004 . Our values are sensitive to the interplay between several poorly understood processes treated in one dimension: mass accretion efficiency, rotationally enhanced wind mass loss, thermohaline, and inward rotational mixing. Therefore, although not perfect, we consider the match with the mass fractions reported by VH05 surprisingly satisfactory.

3.1.1. *Comparison to single fast-rotating stars*

We now compare the mixing processes happening in a single rotating massive stars and in our accretor model. Fig. 4 shows the mass fraction of ^{14}N as a function of mass coordinate along the evolution of three $20 M_{\odot}$ stars initialized with $\omega/\omega_{\text{crit}} = 0.2, 0.3, 0.4, 0.5$

³ This is needed to convert mass fractions reported here into $\epsilon(X) = 12 + \log_{10}(N_X/N_H)$, where N_X and N_H are the number fractions of species X and H, respectively.



Figure 3. Mixing diffusion coefficients in the accretor star. From left to right, each panel shows times during the main sequence (2.71 Myr), right before the “v-shaped” feature during RLOF (7.25 Myr), close to the end of RLOF (7.26 Myr), and after mass transfer (8.38 Myr) – see the corresponding thin blue crosses in Fig. 1. The total diffusion coefficient (thick cyan line) is obtained as the sum of non-rotational mixing processes (i.e., here overshooting, thin blue line), convection (shown in red), thermohaline mixing (pink) and semiconvection (in purple). The gray area corresponds to mass accreted during RLOF.

$M [M_{\odot}]$	$R [R_{\odot}]$	$\log_{10}(\omega/[s^{-1}])$	$v_{\text{rot}} [\text{km s}^{-1}]$	$X(^1\text{H})$	$X(^4\text{He})$	$X(^{12}\text{C})$	$X(^{14}\text{N})$	$X(^{16}\text{O})$
20.1	9.6	-4.263	366.1	0.678010	0.312093	0.001344	0.001340	0.004148

Table 1. Properties of the accretors shortly after the end of RLOF (last thin blue cross in Fig. 1 and last panel of Fig. 3).

where ω is the surface angular frequency and $\omega_{\text{crit}} = \sqrt{(1 - L/L_{\text{Edd}})GM/R^3}$ and L_{Edd} is the Eddington luminosity computed using the stellar opacity from the outermost mesh point down to optical depth $\tau = 2/3$, L is the luminosity, R the radius of the star, and G the gravitational constant. These rotating single stars have an otherwise identical setup as our binary model. The last panel of Fig. 4 shows our accretor model. The dotted red line marks the primordial mass fraction of ^{14}N for the adopted $Z = 0.01$, the thin dashed lines mark the surface value at TAMS.

The colored tracks show selected profiles throughout the main sequence, with lighter colors corresponding to more evolved stars. The accretor model (rightmost panel) starts as a $17 M_{\odot}$ and is rejuvenated by binary interactions, thus it reaches TAMS at 11.24 Myr. For comparison, the initially $20 M_{\odot}$ rotating models have a main-sequence lifetime of 9.2-9.6 Myr (longer for higher initial rotation rates), hence their TAMS profile does not have as light a color in Fig. 4.

The first four panels of Fig. 4 show the typical rotational mixing profiles: ^{14}N rapidly rises in the core because of the CNO burning, and it is then mixed outwards. At any time the ^{14}N profile is monotonically decreasing in mass coordinate, and the higher the initial rotation, the higher the surface ^{14}N mass fraction reached at TAMS.

Conversely, the ^{14}N mass fraction profile of the accretor is *not* monotonic throughout the evolution. It is shaped not only by outward rotational mixing, but also by the accretion of matter from the outer layers of the donor’s star core mixed inward by rotation and thermohaline mixing.

Initially, the tidally synced accretor star rotates too slowly for significant outward rotational mixing out of the core, and until the onset of RLOF (roughly at 7.25 Myr) no appreciable variation of the surface $X(^{14}\text{N})$ occurs. During late RLOF after the “v-shaped” feature in Fig. 1, N-rich material from the donor’s core piles onto the accretor’s surface – inside the gray area in the

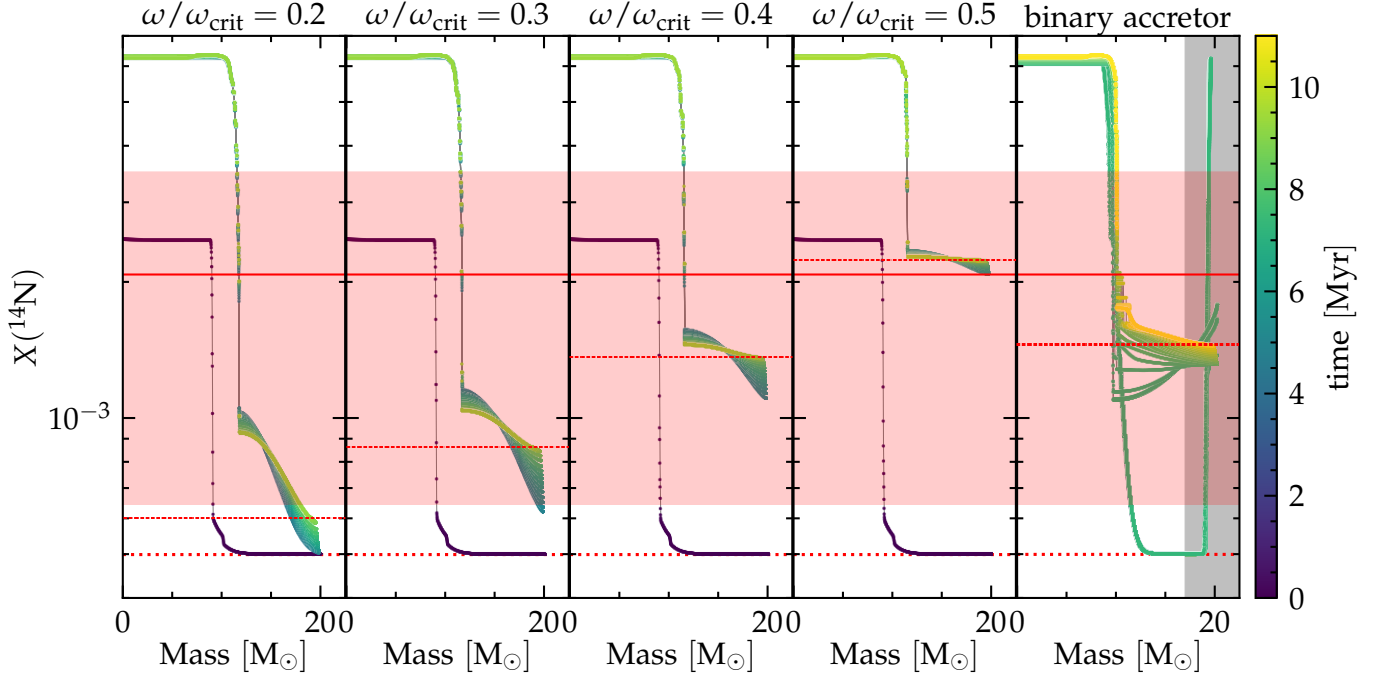


Figure 4. ^{14}N mass fraction as a function of mass coordinate for $20 M_{\odot}$ single star models with increasing $\omega/\omega_{\text{crit}}$ at birth (first four panels), and for the accretor of our fiducial binary. The dotted thick red line marks the primordial value, the thin dashed red line marks the surface value at TAMS. In the last panel, the gray area highlights mass accreted during RLOF. The colors of each profile go from dark to light at TAMS, and selected profiles along the main sequence are shown. The solid red line and the shaded red region correspond to the mass fraction of ^{14}N estimated by VH05 assuming the surface mass fraction of H from Tab. 1. The abundance of ^{14}N alone is not strongly constraining.

rightmost panel of Fig. 4. The close-to-critical rotation of the accretor and the inversion in the mean molecular weight μ then drive inward mixing (see also Fig. 3) of this N-rich material and dilute it in the envelope.

Simultaneously, the mere growth in mass causes the steepening of the core-temperature gradient and increase in the convective core mass (rejuvenation, e.g., Schneider et al. 2016), driving some outward convective mixing of N-rich material. Because convection turnover timescales are much shorter than evolutionary timescales, the growth of the convective core produces “steps” at the outer edge of the core (slightly outside mass coordinate $10 M_{\odot}$). In the post-RLOF evolution, outward rotational mixing from the rejuvenated core and inward rotational mixing and thermohaline mixing from the surface connect the excess ^{14}N .

In Fig. 4, the solid red line and red shaded area across all panels show the ^{14}N from VH05 (assuming the surface mass fraction from our model listed in Tab. 1): the mass fraction of ^{14}N alone is not sufficient to distinguish with these models, and already a moderate $\omega/\omega_{\text{crit}} \geq 0.3$ is sufficient for models to reach the lower-limit of the error bar.

3.2. Angular momentum transport and surface rotation

One of the main distinguishing features of ζ Oph is its extremely high surface rotation rate. Spectroscopic measurements of the projected rotational velocity exceed $v \sin(i) \gtrsim 400 \text{ km s}^{-1}$, which implies close to critical rotation. Zehe et al. (2018) recently estimated $v \sin(i) = 432 \pm 16 \text{ km s}^{-1}$ and $i \sim 56$ degrees.

Fig. 5 shows the surface average rotation rate of our accretor model as a function of time (ignoring the projection angle i). The dark red band corresponds to the $v \sin(i)$ from Zehe et al. (2018), and the lighter band shows a range of 5 times their error bar.

The initial binary is wide enough that the initial tidal synchronization implies a very low rotation. At 7.25 Myr, RLOF rapidly spins up the accretor to critical rotation, up to $v_{\text{crit}} \simeq 520 \text{ km s}^{-1}$. The star remains fast rotating throughout the mass transfer phase, which ends at the black diamond in Fig. 5. In the remaining evolution, the star spins down progressively through wind mass loss, and within ~ 2 Myr its averaged surface rotational velocity drops below 350 km s^{-1} . Close to the end of the main sequence, the internal transport of angular momentum causes a change in the spin-down slope.

Fig. 5 shows that, without accounting for the inclination angle, our model can retain a significant surface ro-

tation for a time comparable to the kinematic age of the star, which is shorter than the remaining main-sequence lifetime. We emphasize that throughout its evolution this model is computed using the Vink et al. (2000, 2001) wind mass-loss rate with full efficiency. Marcolino et al. (2009) found the predicted mass loss rate to exceed the observed one by ~ 2 orders of magnitude. While this could impact the evolution of the binary even before RLOF, it certainly increases the spin-down rate of our model compared to the observations. We attempted running models with artificially decreased wind mass loss rate (e.g., Renzo et al. 2017), but these resulted in super-critical $\omega/\omega_{\text{crit}} > 1$ accretor stars with untrustworthy numerical results. Nevertheless, we expect that an accreting star modeled with lower wind-mass loss rate post-RLOF would retain an even higher surface rotation for longer.

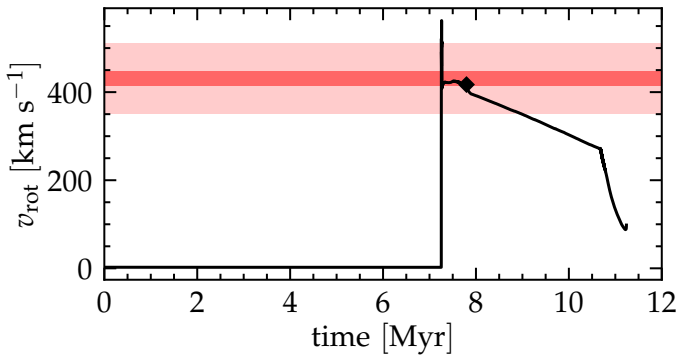


Figure 5. Surface averaged rotation rate for the accretor model. At ~ 7.25 Myr the mass transfer quickly spins up the accretor at critical rotation. By the time the donor detaches from the RLOF the accretor is still spinning at ~ 400 km s $^{-1}$. At this point (beginning of the dot-dashed line), we continue the evolution as a single star, and the accretor quickly spins down. Note however that we use a wind mass-loss rate from Vink et al. (2001), which is observed to be ~ 2 orders of magnitude too high (Marcolino et al. 2009).

3.2.1. Comparison to single fast-rotating stars

To illustrate the angular momentum transport in our accretor stars, it is helpful to compare with the single rotating $20 M_{\odot}$ models. The internal rotational profile of a single star rigidly rotating at birth is different than the profile obtained spinning up the secondary star at a later evolutionary stage and from its surface. This even within the framework of a specific model for the angular momentum transport in stars (Spruit 2002).

Fig. 6 shows the internal equatorial rotational velocity $v_{\text{rot}} = \omega \times r$. As in Fig. 4, the first four panels show single rotating stars with increasing initial $\omega/\omega_{\text{crit}}$, the last panel shows our accretor model, and the colors go

from dark (close to zero age main sequence, ZAMS) to light (TAMS), with the accretor reaching lighter colors because of its rejuvenation. The gray area in the last panel represents mass accreted during RLOF.

The thin dashed red lines in each panel mark the TAMS surface rotation rates: all our single star models reach a TAMS surface $v_{\text{rot}} \simeq 50$ km s $^{-1}$. Initially faster rotating models spin down more in their outer layers, have slightly longer main sequence lifetimes (because of rotational mixing increasing the available fuel), and develop stronger differential rotation which drives more inwards transport of angular momentum. The single star profiles show the progressive development of a core-envelope interface, and the core rotation rate is sensitive to the initial value of $\omega/\omega_{\text{crit}}$.

Conversely, the last panel shows that the entire interior of the accretor has a negligible equatorial rotational velocity until RLOF. Because of binary interactions, rotation does not start as rigid, but instead angular momentum is injected from the top. In our model, inward transport of angular momentum creates the monotonically increasing v_{rot} profile seen in the green lines of the last panel. When angular momentum is transported across the chemical gradient at the edge of the convective core, a discontinuity stronger than in the single stars arises.

By the end of the main-sequence evolution of the accretor, the surface still spins with $v_{\text{rot}} \simeq 100$ km s $^{-1}$ (twice as fast as the single star models). Perhaps more importantly, the outer-edge of the core has a similar rotational velocity as the surface, and much larger than the rotational velocity of the single star models. This might have important implications for the rotation rate of the compact objects formed by the initially less massive star in a binary, and the models of compact objects spins for gravitational-wave progenitors (e.g., Zaldarriaga et al. 2018; Qin et al. 2018; Callister et al. 2020).

4. ROBUSTNESS OF THE MODELS AND DISCUSSION

4.1. Uncertainties in the single-star physics

■ [write about Z variation, no eddington sweet, higher thermohaline mixing,] ■

4.2. Uncertainties in the treatment of mass transfer

We regulate the accretion efficiency through the rotational enhancement of mass loss (e.g. Langer 1998). However, whether critical rotation can effectively stop the accretion of matter is still unclear. Popham & Narayan (1991) and Paczynski (1991) argued that accretion of mass (but no angular momentum) might be possible even at critical rotation.



Figure 6. Internal rotational profile for $20 M_{\odot}$ single star models with increasing $\omega/\omega_{\text{crit}}$ at birth (first four panels), and for the accretor of our fiducial binary. As in Fig. 4, the colors go from dark (close to ZAMS) to light at TAMS, and the thin dashed red line mark the TAMS surface rotation rate. In the last panel, the gray area indicates mass accreted during RLOF. The yellow lines (TAMS) in the last panel show that the core of the accretor is rotating almost as fast as its surface, and both are faster than the surface of single star models.

During RLOF, the total amount of mass lost by the donor is $\Delta M_{\text{donor}} \simeq 10.6 M_{\odot}$, of which only $\Delta M_{\text{accretor}} \simeq 3.4 M_{\odot}$ are successfully accreted. This corresponds to an overall mass transfer efficiency $\beta_{\text{RLOF}} \equiv \Delta M_{\text{accretor}}/\Delta M_{\text{donor}} \simeq 0.3$, although the accretion efficiency is *not* constant throughout the mass transfer (e.g., van Rensbergen et al. 2006). In our models it depends on the radial and rotational evolution of the accreting star. During RLOF, the accretor is out of gravothermal equilibrium with significant impact on its radius and ultimately on the amount of mass transferred and its angular momentum. In reality, geometric distortion of the outer layers because of the centrifugal forces would also occur, which is not modeled in a 1D code as MESA.

While the mass transfer efficiency β_{RLOF} and importantly its time-evolution need further studies, we emphasize that most studies, especially using rapid population synthesis tools, typically assume a constant β_{RLOF} and neglect to model the out-of-equilibrium phase of the accretor and how this can impact the binary and orbital evolution.

Another free parameter in the treatment of mass transfer is the specific angular momentum of the accreted material. In our models, for the sake of numerical stability, we assume the incoming material and the

stellar surface to have the same specific angular momentum. This approximation corresponds to a scenario where angular momentum transport in the circumstellar disk during RLOF quickly homogenizes the rotation rate.

We also attempted calculations using the algorithm from de Mink et al. (2013) based on the fit from Ulrich & Burger (1976) to the numerical results of Lubow & Shu (1975). This algorithm distinguishes between direct impact of the L1 stream and circumstellar disk formation and determines the specific angular momentum of the incoming material. However, these models proved numerically more unstable and providing less trustworthy results. Generally speaking, allowing for a faster accretion of angular momentum results in less radial expansion of the accretor (cf. Fig. 1) and a lower overall mass transfer efficiency β_{RLOF} because of the faster achievement of critical rotation.

Finally, while the composition of the transferred material is determined by the structure of the donor and the mass transfer rate calculated following Kolb & Ritter (1990), we still need to specify its specific entropy when it reaches the accretor surface. We follow the common practice of assuming the specific entropy of the incoming material to be same as the accreting surface. The scenario justifying this hypothesis is that during

RLOF the matter is sufficiently optically thin so radiative processes can rapidly equalize the entropy between the RLOF stream and the accreting surface. However, the very large mass-transfer rates we find (cf. Fig. 2) might result in optically thick flows for which this approximation might not be appropriate.

4.3. Variations in the initial binary parameters

■ [discuss variations in M1, M2, P] ■

Since neither the initial donor mass M_1 nor the initial period can be directly constrained, it is possible that different values would result in easier-to-explode donors with a similar accretor on a and faster (or slower) orbit.

The observed position of ζ Oph on the HRD, and especially its relatively high T_{eff} would be hard to reproduce assuming initially less massive accretors (which would remain too cool even after accreting mass), or more equal initial mass ratio (which would produce a too evolved accretor at the onset of mass transfer).

4.4. The explosion of the former companion

Throughout this study, we have assumed the “binary SN scenario”: after the mass transfer phase, the explosion of the donor breaks the binary and ejects the accretor at roughly its pre-explosion orbital velocity (e.g., Renzo et al. 2019). This fate occurs to the majority of massive binary systems, and ζ Oph might be the best example of it (e.g., Blaauw 1952, 1961; Hoogerwerf et al. 2000). Neuhäuser et al. (2020) suggested not only the companion successfully exploded producing the pulsar PSR B1706-16, but that the explosion produced radioactive ^{60}Fe which polluted Earth.

From kinematic and orbital considerations they estimated the pulsar received a natal kick of $\sim 253 \pm 54 \text{ km s}^{-1}$, which would be sufficiently large to unbind the binary. The ejecta mass would depend on the post-RLOF wind mass loss of our donor star, which we do not model. At the end of our binary model (black diamond in Fig. 1), our stripped donor is $\sim 9.4 M_{\odot}$, with a surface H fraction of $X \lesssim 0.2$ for a layer of $\Delta M \simeq 2.5 M_{\odot}$. Its wind mass-loss rate is $\sim 10^{-5} M_{\odot} \text{ yr}^{-1}$ (cf. Fig. 2), likely to increase as it contracts into a Wolf-Rayet star and increases its luminosity and effective temperature. We expect its explosion to appear as H-less type Ib SN. Although our stripped donor is rather massive, recent studies suggest a higher “explodability” of donor stars in binary systems (e.g., Schneider et al. 2021; Laplace et al. 2021; ?).

We have neglected the impact of the explosion on the structure of the accretor star. At the time of the explosion, the accretor subtends a solid angle $\sim R^2/a^2 \simeq 0.05$ degrees with R the accretor radius and a the binary

separation. We neglect the post-RLOF wind-driven orbital widening for this estimate. The blast wave will hit the accretor causing mass loss – directly via ablation and by injecting energy in the envelope, inflating it and enhancing its wind (Wheeler et al. 1975; Tauris & Takens 1998; Podsiadlowski 2003; Hirai et al. 2018). Because of the SN shock, the just ejected new runaway star might appear bloated and redder (long before it overtakes the slowing SN remnant). The impact of this brief out of thermal equilibrium phase on the stellar spin should be investigated further. Using 2D hydrodynamic simulations of the star-SN ejecta interactions in close binaries ($a \lesssim 60 R_{\odot}$, cf. $a \gtrsim 343 R_{\odot}$ in our fiducial binary model), Hirai et al. (2018) found that the companion star recovers its pre-explosion luminosity and effective temperature within a few years to decades, and the amount of mass removed by the SN shock is $\lesssim 10^{-2} M_{\odot}$. The SN ejecta might also pollute the surface of the runaway depositing processed nuclear material (e.g. Przybilla et al. 2008). However, enhanced mass loss, rapid rotation and mixing might rapidly dilute the yields.

5. CONCLUSIONS

We have demonstrated that self-consistent 1D calculations of coupled stellar models with masses $\gtrsim 20 M_{\odot}$ are possible with the MESA software instrument. As a first application, we focused on finding a model for ζ Oph, assuming its runaway nature is explained by the binary SN scenario.

We found that it is possible to qualitatively explain the observed nitrogen and helium rich surface composition without assuming that the surface excess of He and N comes entirely from within the star. Instead, this material is transferred from the receding core of the donor star and mixed inwards but rotation, and to a smaller degree, thermohaline mixing.

Thus, the present day surface mass fraction of ζ Oph put a coupled constrain the mass transfer efficiency and mixing in the accretor. Standard stellar physics assumptions common in the numerical modeling of these processes reproduce reasonably well the main observational features of ζ Oph. Therefore, such star should *not* be used to calibrate models of rotational mixing in single star evolution, nor its more extreme version of chemically homogeneous evolution.

Software: mesaPlot (Farmer 2018), mesaSDK (Townsend 2018), ipython/jupyter (Pérez & Granger 2007), matplotlib (Hunter 2007), NumPy (van der Walt et al. 2011), MESA (Paxton et al. 2011, 2013, 2015, 2018, 2019)

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APPENDIX

A. MESA SETUP

■ [MLT-?] ■

■ [possibly move to methods] ■ We use

MESA version 15140 to compute our models. The MESA equation of state (EOS) is a blend of the OPAL Rogers & Nayfonov (2002), SCVH Saumon et al. (1995), PTEH Pols et al. (1995), HELM Timmes & Swesty (2000), and PC Potekhin & Chabrier (2010) EOSes.

OPAL (Iglesias & Rogers 1993, 1996) provides the main radiative opacities, with low-temperature data from Ferguson et al. (2005) and the high-temperature from Buchler & Yueh (1976). Electron conduction opacities are from Cassisi et al. (2007).

Nuclear reaction rates are a combination of rates from NACRE (Angulo et al. 1999), JINA REACLIB (Cyburt et al. 2010), plus additional tabulated weak reaction rates Fuller et al. (1985); Oda et al. (1994); Langanke & Martínez-Pinedo (2000). Screening is included via the prescription of Chugunov et al. (2007). Thermal neutrino loss rates are from Itoh et al. (1996). We use a 22-isotope nuclear network (approx_21_plus_cr56).

The inlists, processing scripts, and model output will be made available at [link](#).

B. RESOLUTION TESTS

We extensively check the numerical convergence of our stellar evolution calculations with increasing number of

mesh points. Fig. 7 shows that all the features described extensively here do not vary when increasing the spatial resolution by decreasing `mesh_delta_coeff`. The right panel shows the number of mesh points for the accretor (top) and donor (bottom), which are $\sim 20\%$ higher in the high resolution runs. The left panel shows the HRD evolution until the detachment of the binary for the two accretor models (pink/red) and the two donor models (blue/cyan).

Similarly, we tested the numerical convergence with decreasing timestep size. This can be done decreasing the parameter `mesh_time_coeff`. However, we were unable to successfully compute models at higher temporal resolution. Partial results show a good agreement with our fiducial model until they crash (typically during RLOF), and lower temporal resolution models showed a similar qualitative agreement but increased noisiness during the late RLOF phase. For our fiducial model the adaptive timestep size never exceeds $10^{3.8}$ years with typical pre-RLOF timesteps of the order of $10^{3.2}$ years and sub-decade during RLOF. The main factor limiting the timestep sizes is the change of surface angular momentum in both stars during the mass transfer.

REFERENCES

- Almeida, L. A., Sana, H., Taylor, W., et al. 2017, A&A, 598, A84, doi: [10.1051/0004-6361/201629844](#)
- Angulo, C., Arnould, M., Rayet, M., et al. 1999, Nuclear Physics A, 656, 3, doi: [10.1016/S0375-9474\(99\)00030-5](#)
- Belczynski, K., Holz, D. E., Bulik, T., & O’Shaughnessy, R. 2016, Nature, 534, 512, doi: [10.1038/nature18322](#)
- Blaauw, A. 1952, BAN, 11, 414
- . 1961, BAN, 15, 265
- Blaauw, A. 1993, in Astronomical Society of the Pacific Conference Series, Vol. 35, Massive Stars: Their Lives in the Interstellar Medium, ed. J. P. Cassinelli & E. B. Churchwell, 207
- Blagorodnova, N., Klencki, J., Pejcha, O., et al. 2021, arXiv e-prints, arXiv:2102.05662.
<https://arxiv.org/abs/2102.05662>
- Bodensteiner, J., Baade, D., Greiner, J., & Langer, N. 2018, A&A, 618, A110, doi: [10.1051/0004-6361/201832722](#)
- Braun, H., & Langer, N. 1995, A&A, 297, 483
- Broekgaarden, F. S., Berger, E., Neijssel, C. J., et al. 2021, arXiv e-prints, arXiv:2103.02608.
<https://arxiv.org/abs/2103.02608>
- Brott, I., de Mink, S. E., Cantiello, M., et al. 2011, A&A, 530, A115, doi: [10.1051/0004-6361/201016113](#)
- Buchler, J. R., & Yueh, W. R. 1976, ApJ, 210, 440, doi: [10.1086/154847](#)

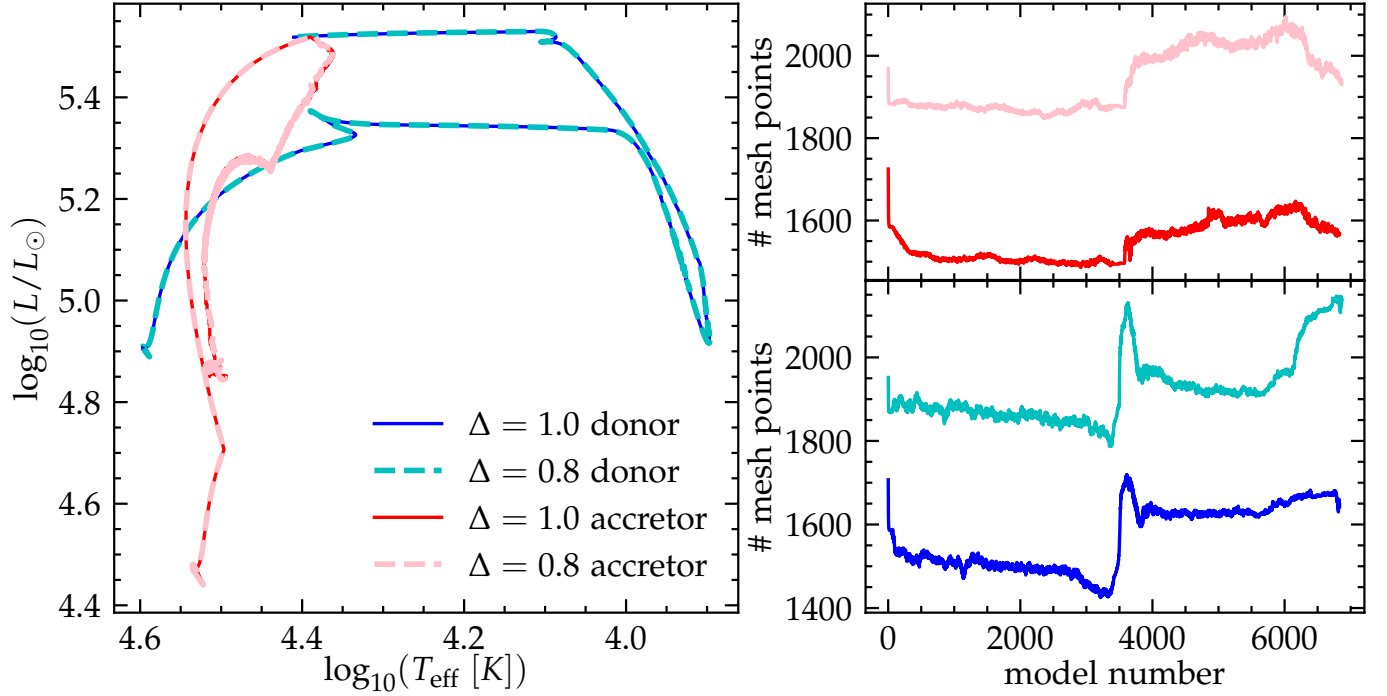


Figure 7. Left: HRD comparison for our fiducial binary model varying the number of mesh points. We only show the evolution until our definition of RLOF detachment. Right: number of mesh points as a function of timestep number. In both panels, the blue/cyan tracks show the donor stars, the red/pink tracks show the accretor. Thicker dashed lines correspond to the models at higher resolution (i.e., lower Δ which indicates the value of `mesh_delta_coeff`).

Callister, T. A., Farr, W. M., & Renzo, M. 2020, arXiv e-prints, arXiv:2011.09570.
<https://arxiv.org/abs/2011.09570>
Cantiello, M., Lecoanet, D., Jermyn, A. S., & Grassitelli, L. 2021, arXiv e-prints, arXiv:2102.05670.
<https://arxiv.org/abs/2102.05670>
Cantiello, M., Yoon, S., Langer, N., & Livio, M. 2007, *A&A*, 465, L29
Cassisi, S., Potekhin, A. Y., Pietrinferni, A., Catelan, M., & Salaris, M. 2007, *ApJ*, 661, 1094, doi: [10.1086/516819](https://doi.org/10.1086/516819)
Chugunov, A. I., Dewitt, H. E., & Yakovlev, D. G. 2007, *PhRvD*, 76, 025028, doi: [10.1103/PhysRevD.76.025028](https://doi.org/10.1103/PhysRevD.76.025028)
Claret, A., & Torres, G. 2017, *ApJ*, 849, 18, doi: [10.3847/1538-4357/aa8770](https://doi.org/10.3847/1538-4357/aa8770)
Cyburt, R. H., Amthor, A. M., Ferguson, R., et al. 2010, *ApJS*, 189, 240, doi: [10.1088/0067-0049/189/1/240](https://doi.org/10.1088/0067-0049/189/1/240)
De Donder, E., Vanbeveren, D., & van Bever, J. 1997, *A&A*, 318, 812
de Jager, C., Nieuwenhuijzen, H., & van der Hucht, K. A. 1988, *A&AS*, 72, 259
de Mink, S. E., Langer, N., Izzard, R. G., Sana, H., & de Koter, A. 2013, *ApJ*, 764, 166, doi: [10.1088/0004-637X/764/2/166](https://doi.org/10.1088/0004-637X/764/2/166)
Eldridge, J. J., Langer, N., & Tout, C. A. 2011, *MNRAS*, 414, 3501, doi: [10.1111/j.1365-2966.2011.18650.x](https://doi.org/10.1111/j.1365-2966.2011.18650.x)

Evans, F. A., Renzo, M., & Rossi, E. M. 2020, arXiv e-prints, arXiv:2006.00849.
<https://arxiv.org/abs/2006.00849>
Farmer, R. 2018, rjfarmer/mesaplot, doi: [10.5281/zenodo.1441329](https://doi.org/10.5281/zenodo.1441329)
Ferguson, J. W., Alexander, D. R., Allard, F., et al. 2005, *ApJ*, 623, 585, doi: [10.1086/428642](https://doi.org/10.1086/428642)
Fuller, G. M., Fowler, W. A., & Newman, M. J. 1985, *ApJ*, 293, 1, doi: [10.1086/163208](https://doi.org/10.1086/163208)
Götberg, Y., de Mink, S. E., & Groh, J. H. 2017, <https://arxiv.org/abs/1701.07439>
Götberg, Y., de Mink, S. E., Groh, J. H., et al. 2018, *A&A*, 615, A78, doi: [10.1051/0004-6361/201732274](https://doi.org/10.1051/0004-6361/201732274)
Grevesse, N., & Sauval, A. J. 1998, *SSRv*, 85, 161, doi: [10.1023/A:1005161325181](https://doi.org/10.1023/A:1005161325181)
Heger, A., Langer, N., & Woosley, S. E. 2000, *ApJ*, 528, 368
Hellings, P. 1983, *Ap&SS*, 96, 37, doi: [10.1007/BF00661941](https://doi.org/10.1007/BF00661941)
—. 1984, *Ap&SS*, 104, 83, doi: [10.1007/BF00653994](https://doi.org/10.1007/BF00653994)
Herrero, A., Kudritzki, R. P., Vilchez, J. M., et al. 1992, *A&A*, 261, 209
Herwig, F. 2000, *A&A*, 360, 952
Hirai, R., Podsiadlowski, P., & Yamada, S. 2018, <https://arxiv.org/abs/1803.10808>
Hoogerwerf, R., de Bruijne, J. H. J., & de Zeeuw, P. T. 2000, *ApJL*, 544, L133, doi: [10.1086/317315](https://doi.org/10.1086/317315)

- . 2001, *A&A*, 365, 49, doi: [10.1051/0004-6361:20000014](https://doi.org/10.1051/0004-6361:20000014)
- Hunter, J. D. 2007, *Computing In Science & Engineering*, 9, 90
- Iglesias, C. A., & Rogers, F. J. 1993, *ApJ*, 412, 752, doi: [10.1086/172958](https://doi.org/10.1086/172958)
- . 1996, *ApJ*, 464, 943, doi: [10.1086/177381](https://doi.org/10.1086/177381)
- Itoh, N., Hayashi, H., Nishikawa, A., & Kohyama, Y. 1996, *ApJS*, 102, 411, doi: [10.1086/192264](https://doi.org/10.1086/192264)
- Kippenhahn, R., Ruschenplatt, G., & Thomas, H.-C. 1980, *A&A*, 91, 175
- Kippenhahn, R., & Weigert, A. 1967, *ZA*, 65, 251
- Klencki, J., Nelemans, G., Istrate, A. G., & Chruslinska, M. 2021, *A&A*, 645, A54, doi: [10.1051/0004-6361/202038707](https://doi.org/10.1051/0004-6361/202038707)
- Kolb, U., & Ritter, H. 1990, *A&A*, 236, 385
- Lagae, C., Driessen, F. A., Hennicker, L., Kee, N. D., & Sundqvist, J. O. 2021, *arXiv e-prints*, arXiv:2103.15904. <https://arxiv.org/abs/2103.15904>
- Langanke, K., & Martínez-Pinedo, G. 2000, *Nuclear Physics A*, 673, 481, doi: [10.1016/S0375-9474\(00\)00131-7](https://doi.org/10.1016/S0375-9474(00)00131-7)
- Langer, N. 1998, *A&A*, 329, 551
- Langer, N., Fricke, K. J., & Sugimoto, D. 1983, *A&A*, 126, 207
- Laplace, E., Götberg, Y., de Mink, S. E., Justham, S., & Farmer, R. 2020, *A&A*, 637, A6, doi: [10.1051/0004-6361/201937300](https://doi.org/10.1051/0004-6361/201937300)
- Laplace, E., Justham, S., Renzo, M., et al. 2021, *arXiv e-prints*, arXiv:2102.05036. <https://arxiv.org/abs/2102.05036>
- Law-Smith, J. A. P., Everson, R. W., Ramirez-Ruiz, E., et al. 2020, *arXiv e-prints*, arXiv:2011.06630. <https://arxiv.org/abs/2011.06630>
- Lubow, S. H., & Shu, F. H. 1975, *ApJ*, 198, 383, doi: [10.1086/153614](https://doi.org/10.1086/153614)
- Lucy, L. B. 2012, *A&A*, 544, A120, doi: [10.1051/0004-6361/201118753](https://doi.org/10.1051/0004-6361/201118753)
- Maeder, A., & Meynet, G. 2000, *ARA&A*, 38, 143, doi: [10.1146/annurev.astro.38.1.143](https://doi.org/10.1146/annurev.astro.38.1.143)
- Marcolino, W. L. F., Bouret, J. C., Martins, F., et al. 2009, *A&A*, 498, 837, doi: [10.1051/0004-6361/200811289](https://doi.org/10.1051/0004-6361/200811289)
- Mason, B. D., Hartkopf, W. I., Gies, D. R., Henry, T. J., & Helsel, J. W. 2009, *AJ*, 137, 3358, doi: [10.1088/0004-6256/137/2/3358](https://doi.org/10.1088/0004-6256/137/2/3358)
- Meynet, G., & Maeder, A. 2000, *A&A*, 361, 101
- Murphy, S. J., Joyce, M., Bedding, T. R., White, T. R., & Kama, M. 2021, *MNRAS*, 502, 1633, doi: [10.1093/mnras/stab144](https://doi.org/10.1093/mnras/stab144)
- Neo, S., Miyaji, S., Nomoto, K., & Sugimoto, D. 1977, *PASJ*, 29, 249
- Neuhäuser, R., Gießler, F., & Hambaryan, V. V. 2020, *MNRAS*, 498, 899, doi: [10.1093/mnras/stz2629](https://doi.org/10.1093/mnras/stz2629)
- Oda, T., Hino, M., Muto, K., Takahara, M., & Sato, K. 1994, *Atomic Data and Nuclear Data Tables*, 56, 231, doi: [10.1006/adnd.1994.1007](https://doi.org/10.1006/adnd.1994.1007)
- Packet, W. 1981, *A&A*, 102, 17
- Paczynski, B. 1991, *ApJ*, 370, 597, doi: [10.1086/169846](https://doi.org/10.1086/169846)
- Paxton, B., Bildsten, L., Dotter, A., et al. 2011, *ApJS*, 192, 3, doi: [10.1088/0067-0049/192/1/3](https://doi.org/10.1088/0067-0049/192/1/3)
- Paxton, B., Cantiello, M., Arras, P., et al. 2013, *ApJS*, 208, 4, doi: [10.1088/0067-0049/208/1/4](https://doi.org/10.1088/0067-0049/208/1/4)
- Paxton, B., Marchant, P., Schwab, J., et al. 2015, *ApJS*, 220, 15, doi: [10.1088/0067-0049/220/1/15](https://doi.org/10.1088/0067-0049/220/1/15)
- Paxton, B., Schwab, J., Bauer, E. B., et al. 2018, *ApJS*, 234, 34, doi: [10.3847/1538-4365/aaa5a8](https://doi.org/10.3847/1538-4365/aaa5a8)
- Paxton, B., Smolec, R., Gaudy, A., et al. 2019. <https://arxiv.org/abs/1903.01426>
- Pérez, F., & Granger, B. E. 2007, *Computing in Science & Engineering*, 9, 21
- Perna, R., Duffell, P., Cantiello, M., & MacFadyen, A. I. 2014, *ApJ*, 781, 119, doi: [10.1088/0004-637X/781/2/119](https://doi.org/10.1088/0004-637X/781/2/119)
- Podsiadlowski, P. 2003, *arXiv e-prints*, astro. <https://arxiv.org/abs/astro-ph/0303660>
- Pols, O. R., & Marinus, M. 1994, *A&A*, 288, 475
- Pols, O. R., Tout, C. A., Eggleton, P. P., & Han, Z. 1995, *MNRAS*, 274, 964, doi: [10.1093/mnras/274.3.964](https://doi.org/10.1093/mnras/274.3.964)
- Popham, R., & Narayan, R. 1991, *ApJ*, 370, 604, doi: [10.1086/169847](https://doi.org/10.1086/169847)
- Potekhin, A. Y., & Chabrier, G. 2010, *Contributions to Plasma Physics*, 50, 82, doi: [10.1002/ctpp.201010017](https://doi.org/10.1002/ctpp.201010017)
- Przybilla, N., Nieva, M. F., Heber, U., & Butler, K. 2008, *The Astrophysical Journal*, 684, L103, doi: [10.1086/592245](https://doi.org/10.1086/592245)
- Qin, Y., Fragos, T., Meynet, G., et al. 2018, *A&A*, 616, A28, doi: [10.1051/0004-6361/201832839](https://doi.org/10.1051/0004-6361/201832839)
- Renzo, M., Ott, C. D., Shore, S. N., & de Mink, S. E. 2017, *A&A*, 603, A118, doi: [10.1051/0004-6361/201730698](https://doi.org/10.1051/0004-6361/201730698)
- Renzo, M., Zapartas, E., de Mink, S. E., et al. 2019, *A&A*, 624, A66, doi: [10.1051/0004-6361/201833297](https://doi.org/10.1051/0004-6361/201833297)
- Rogers, F. J., & Nayfonov, A. 2002, *ApJ*, 576, 1064, doi: [10.1086/341894](https://doi.org/10.1086/341894)
- Sana, H., de Mink, S. E., de Koter, A., et al. 2012, *Science*, 337, 444, doi: [10.1126/science.1223344](https://doi.org/10.1126/science.1223344)
- Saumon, D., Chabrier, G., & van Horn, H. M. 1995, *ApJS*, 99, 713, doi: [10.1086/192204](https://doi.org/10.1086/192204)
- Schneider, F. R. N., Podsiadlowski, P., Langer, N., Castro, N., & Fossati, L. 2016, *MNRAS*, 457, 2355, doi: [10.1093/mnras/stw148](https://doi.org/10.1093/mnras/stw148)
- Schneider, F. R. N., Podsiadlowski, P., & Müller, B. 2021, *A&A*, 645, A5, doi: [10.1051/0004-6361/202039219](https://doi.org/10.1051/0004-6361/202039219)
- Sota, A., Maíz Apellániz, J., Morrell, N. I., et al. 2014, *ApJS*, 211, 10, doi: [10.1088/0067-0049/211/1/10](https://doi.org/10.1088/0067-0049/211/1/10)

- Spruit, H. C. 2002, *A&A*, 381, 923, doi: [10.1051/0004-6361:20011465](https://doi.org/10.1051/0004-6361:20011465)
- Sweet, P. A. 1950, *MNRAS*, 110, 548, doi: [10.1093/mnras/110.6.548](https://doi.org/10.1093/mnras/110.6.548)
- Tauris, T. M. 2015, *MNRAS*, 448, L6, doi: [10.1093/mnrasl/slu189](https://doi.org/10.1093/mnrasl/slu189)
- Tauris, T. M., & Takens, R. J. 1998, *A&A*, 330, 1047
- Tauris, T. M., Kramer, M., Freire, P. C. C., et al. 2017, *ApJ*, 846, 170, doi: [10.3847/1538-4357/aa7e89](https://doi.org/10.3847/1538-4357/aa7e89)
- Tetzlaff, N., Neuhäuser, R., Hohle, M. M., & Maciejewski, G. 2010, *MNRAS*, 402, 2369, doi: [10.1111/j.1365-2966.2009.16093.x](https://doi.org/10.1111/j.1365-2966.2009.16093.x)
- Timmes, F. X., & Swesty, F. D. 2000, *ApJS*, 126, 501, doi: [10.1086/313304](https://doi.org/10.1086/313304)
- Townsend, R. 2018, MESA SDK for Linux: 20180822, doi: [10.5281/zenodo.2603170](https://doi.org/10.5281/zenodo.2603170)
- Ulrich, R. K., & Burger, H. L. 1976, *ApJ*, 206, 509, doi: [10.1086/154406](https://doi.org/10.1086/154406)
- van der Walt, S., Colbert, S. C., & Varoquaux, G. 2011, *Computing in Science Engineering*, 13, 22, doi: [10.1109/MCSE.2011.37](https://doi.org/10.1109/MCSE.2011.37)
- van Rensbergen, W., de Greve, J. P., Mennekens, N., Jansen, K., & de Loore, C. 2011, *A&A*, 528, A16, doi: [10.1051/0004-6361/201015596](https://doi.org/10.1051/0004-6361/201015596)
- van Rensbergen, W., De Loore, C., & Jansen, K. 2006, *A&A*, 446, 1071, doi: [10.1051/0004-6361:20053543](https://doi.org/10.1051/0004-6361:20053543)
- van Rensbergen, W., Vanbeveren, D., & De Loore, C. 1996, *A&A*, 305, 825
- Villamariz, M. R., & Herrero, A. 2005, *A&A*, 442, 263, doi: [10.1051/0004-6361:20052848](https://doi.org/10.1051/0004-6361:20052848)
- Vink, J. S., Davies, B., Harries, T. J., Oudmaijer, R. D., & Walborn, N. R. 2009, *A&A*, 505, 743, doi: [10.1051/0004-6361/200912610](https://doi.org/10.1051/0004-6361/200912610)
- Vink, J. S., de Koter, A., & Lamers, H. J. G. L. M. 2000, *A&A*, 362, 295
- . 2001, *A&A*, 369, 574, doi: [10.1051/0004-6361:20010127](https://doi.org/10.1051/0004-6361:20010127)
- Walker, G. A. H., Yang, S., & Fahlman, G. G. 1979, *ApJ*, 233, 199, doi: [10.1086/157381](https://doi.org/10.1086/157381)
- Wang, C., Langer, N., Schootemeijer, A., et al. 2020, *ApJL*, 888, L12, doi: [10.3847/2041-8213/ab6171](https://doi.org/10.3847/2041-8213/ab6171)
- Wheeler, J. C., Lecar, M., & McKee, C. F. 1975, *ApJ*, 200, 145, doi: [10.1086/153771](https://doi.org/10.1086/153771)
- Yoon, S.-C., Langer, N., & Norman, C. 2006, *A&A*, 460, 199, doi: [10.1051/0004-6361:20065912](https://doi.org/10.1051/0004-6361:20065912)
- Zaldarriaga, M., Kushnir, D., & Kollmeier, J. A. 2018, *MNRAS*, 473, 4174, doi: [10.1093/mnras/stx2577](https://doi.org/10.1093/mnras/stx2577)
- Zapartas, E., de Mink, S. E., Justham, S., et al. 2021, *A&A*, 645, A6, doi: [10.1051/0004-6361/202037744](https://doi.org/10.1051/0004-6361/202037744)
- . 2019. <https://arxiv.org/abs/1907.06687>
- Zehe, T., Mugrauer, M., Neuhäuser, R., et al. 2018, *Astronomische Nachrichten*, 339, 46, doi: [10.1002/asna.201713383](https://doi.org/10.1002/asna.201713383)