

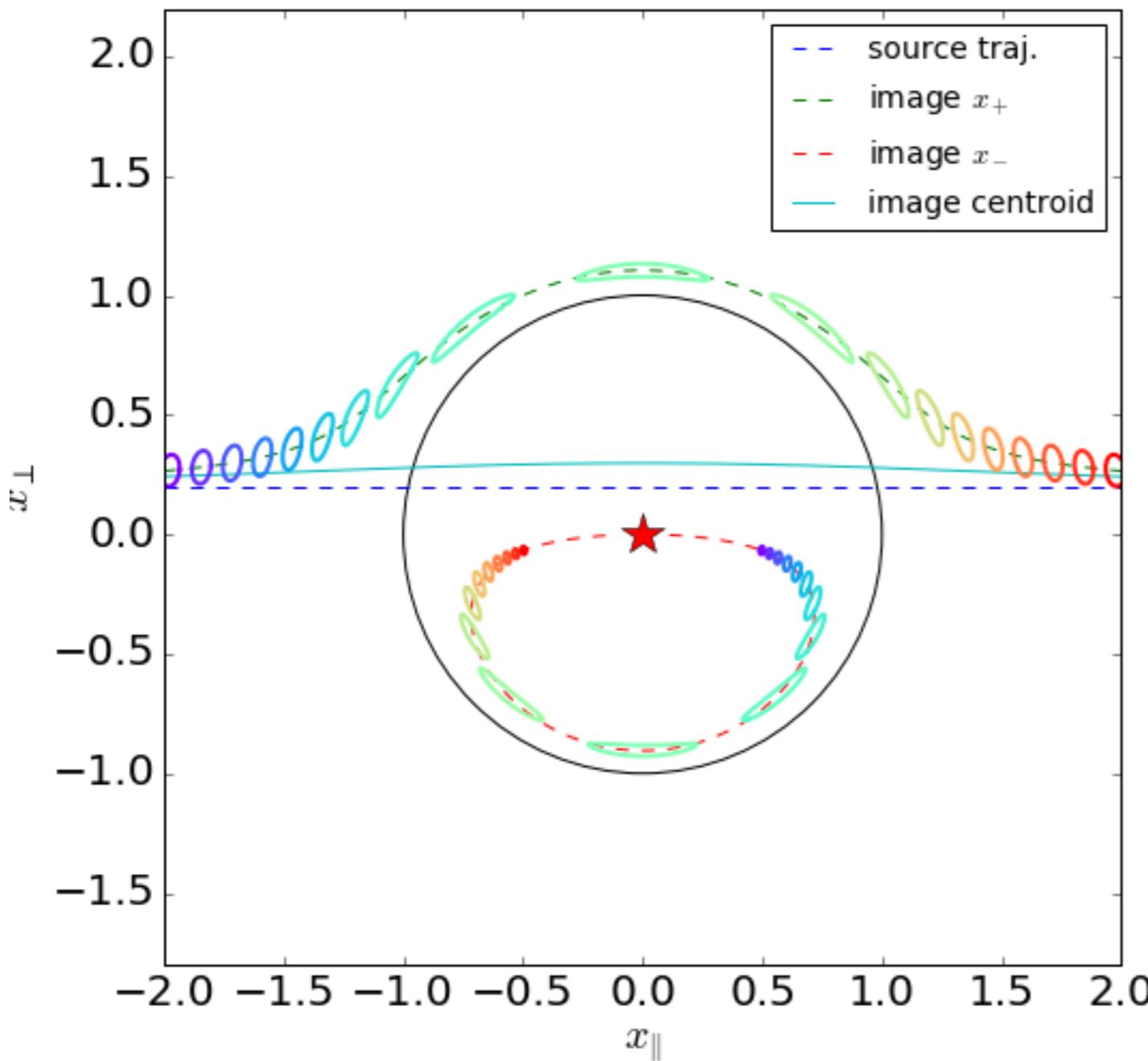
GRAVITATIONAL LENSING

15 - PLANET MICROLENSING (III)

Massimo Meneghetti
AA 2019-2020

ANOTHER WAY TO LOOK AT THE LIGHT CURVES: POINT MASS LENS

Lensing of an extended circular source



A point lens always produces two images, namely

$$x_{\pm} = \frac{1}{2} \left[y \pm \sqrt{y^2 + 4} \right]$$

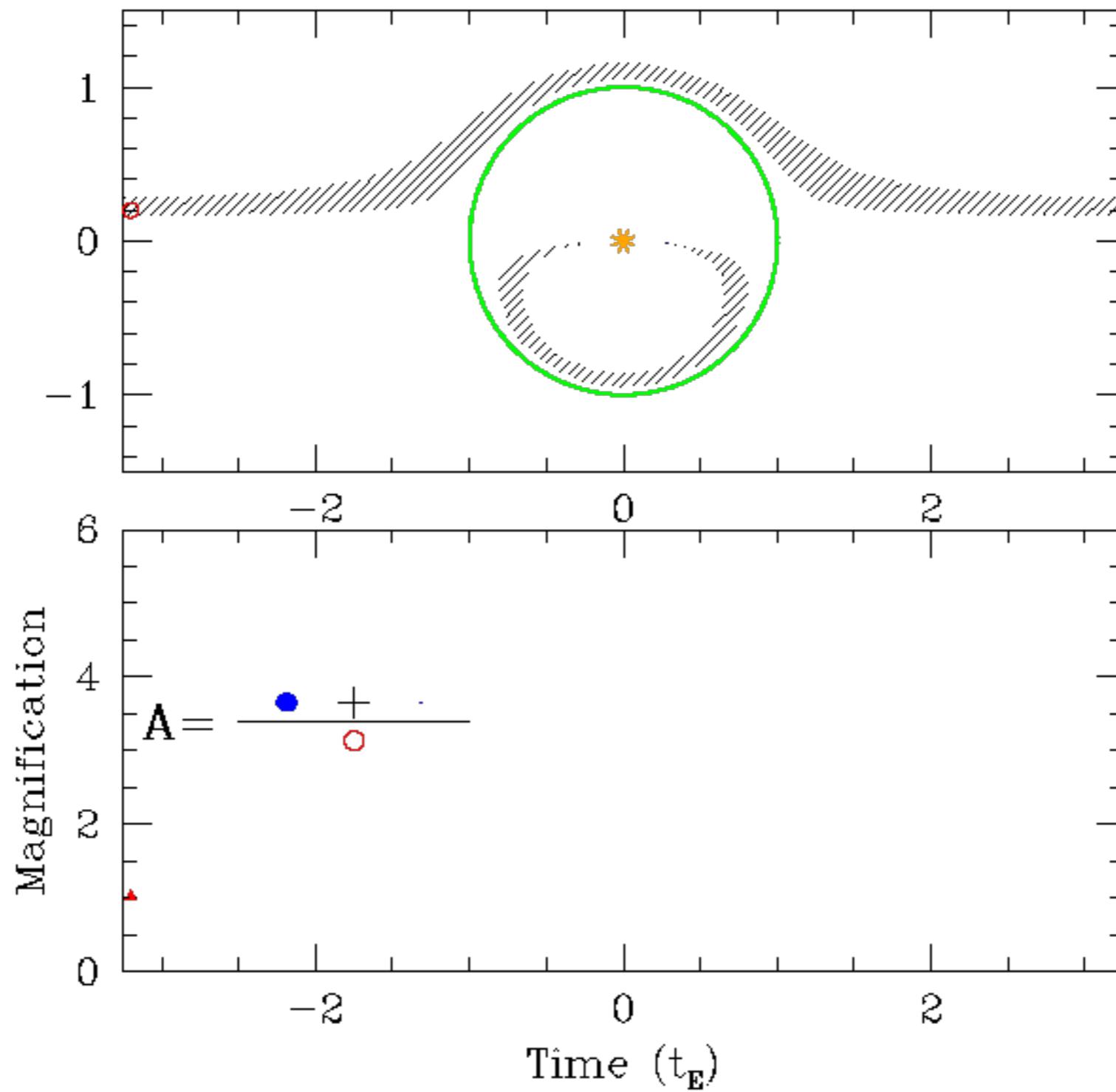
Imagine a source moving along the dashed line in the figure...

Remember: the two images are always aligned with the lens and the source!

As the source move, also the images move...

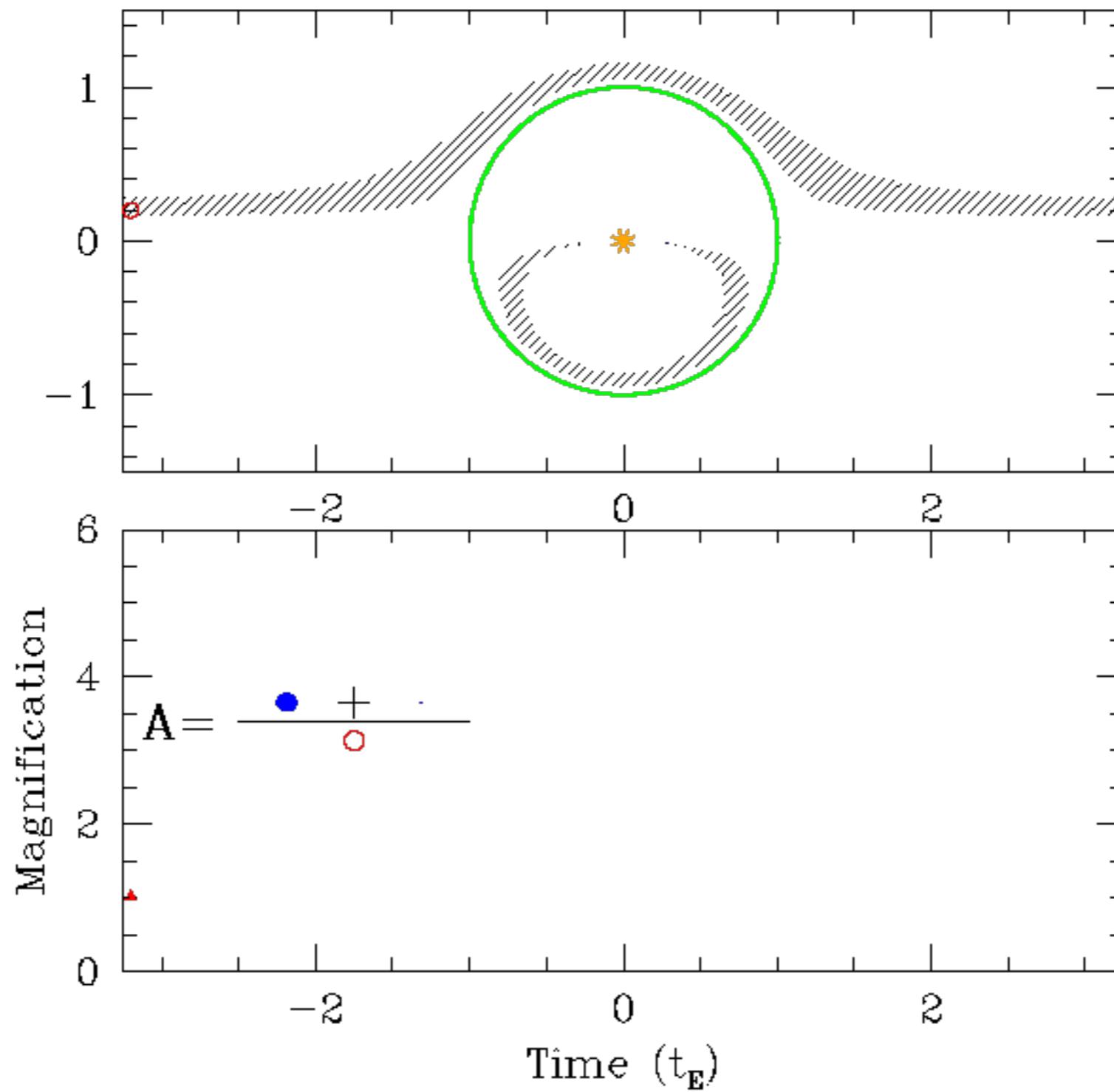
ANIMATION OF A MICROLENSING EVENT

The animation can be found here: <http://www.astronomy.ohio-state.edu/~gaudi/movies.html>



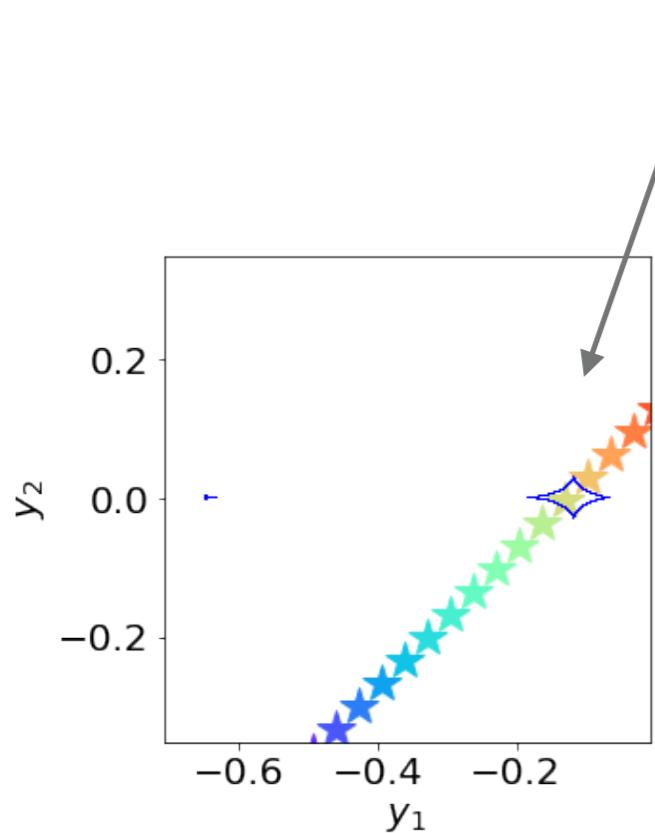
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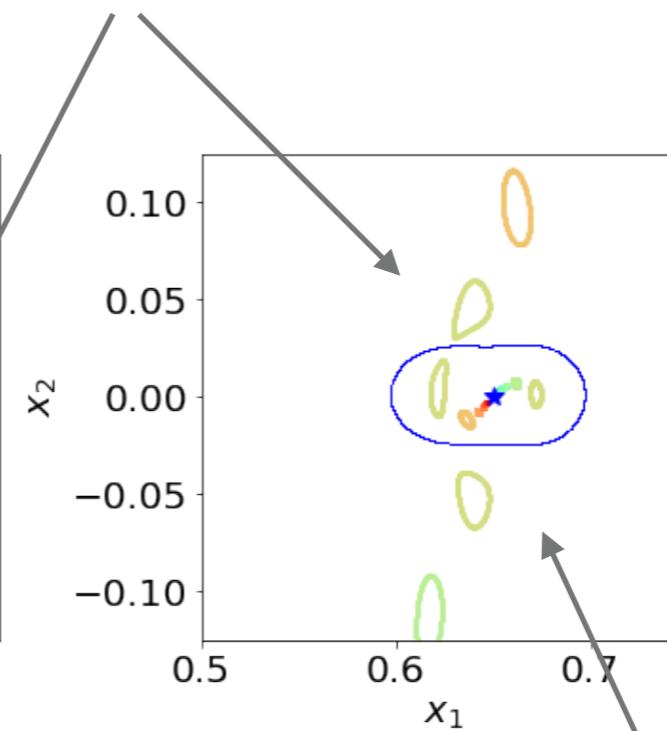
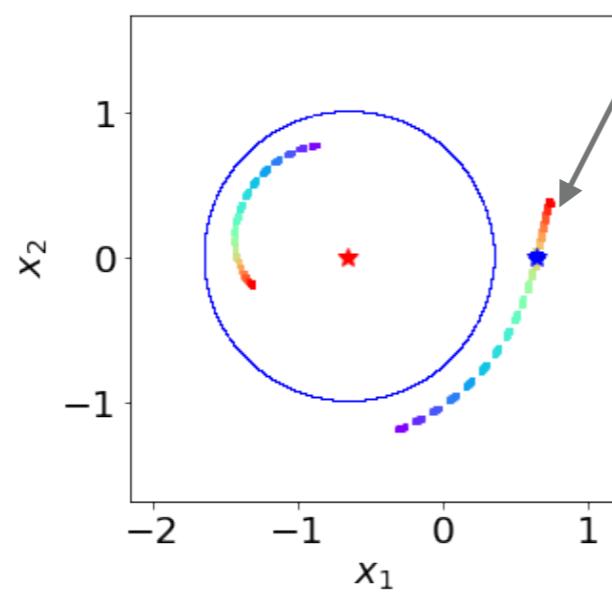


PLANETARY PERTURBATIONS AS PERTURBATIONS OF SINGLE IMAGES

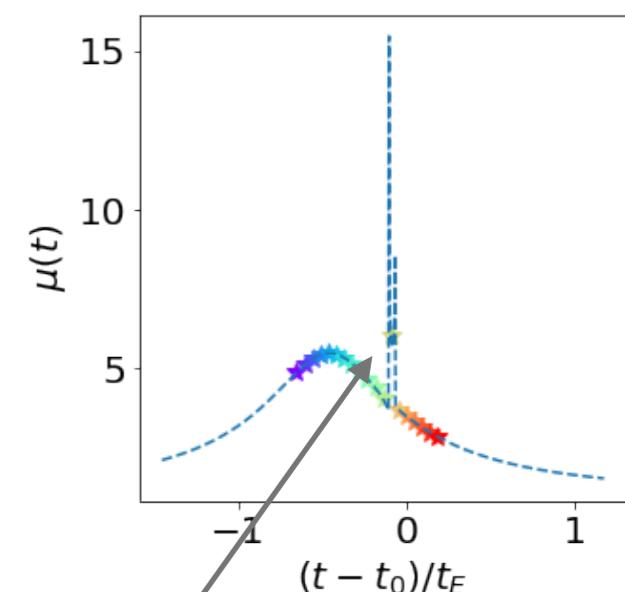
Planetary caustics



Planetary critical lines

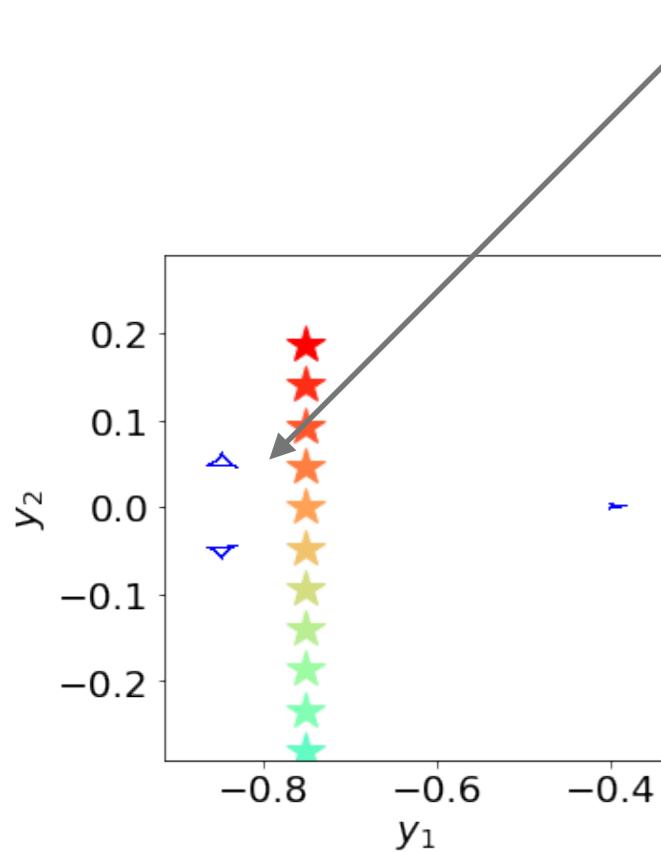


magnified outer image

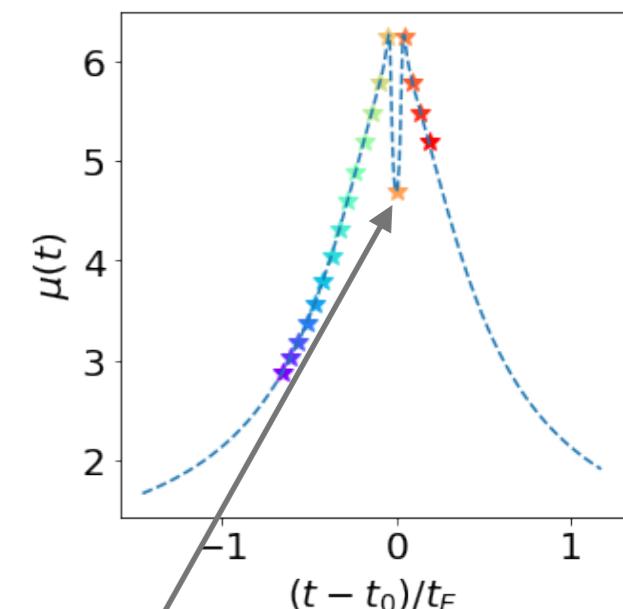
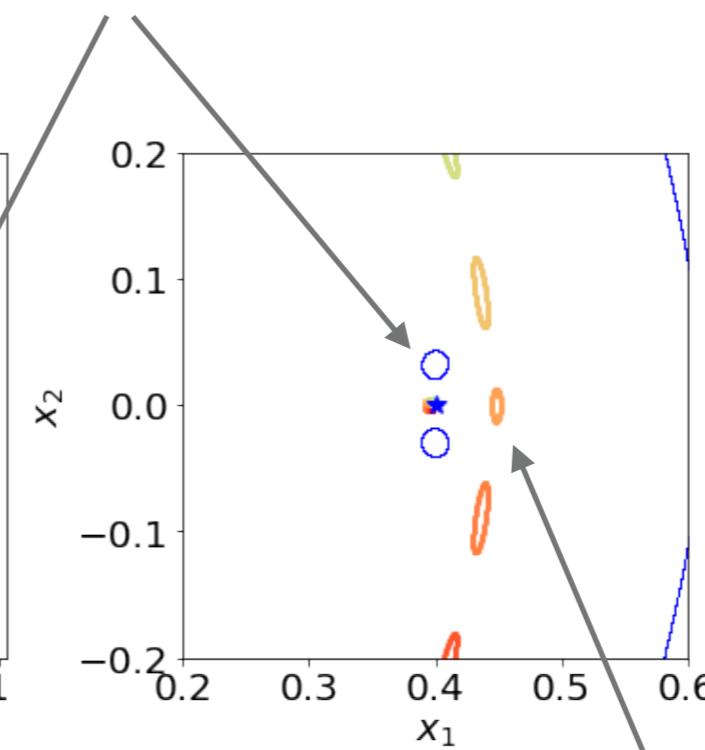
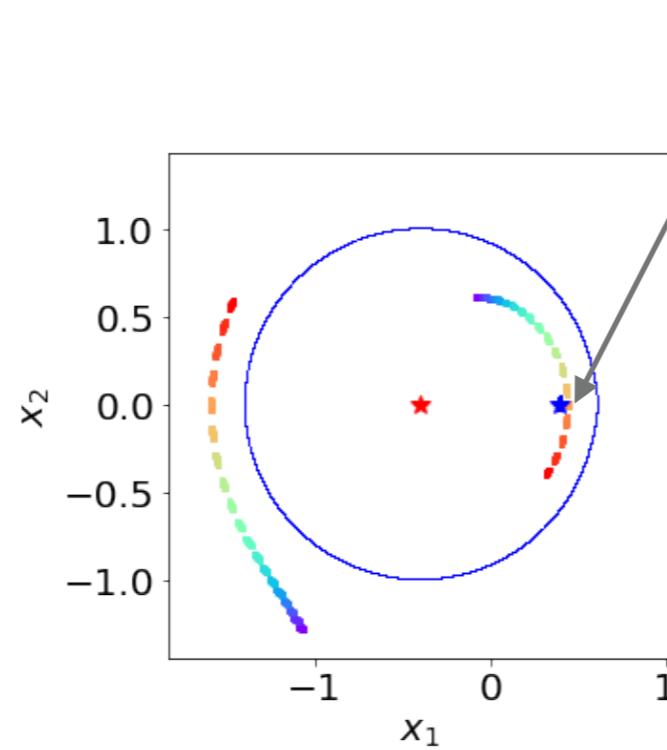


PLANETARY PERTURBATIONS AS PERTURBATIONS OF SINGLE IMAGES

Planetary caustics



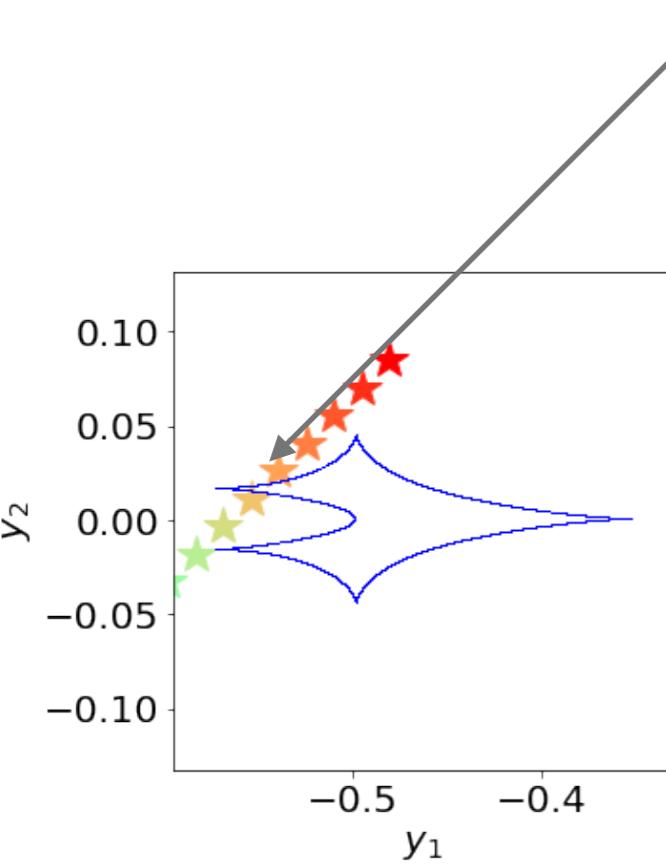
Planetary critical lines



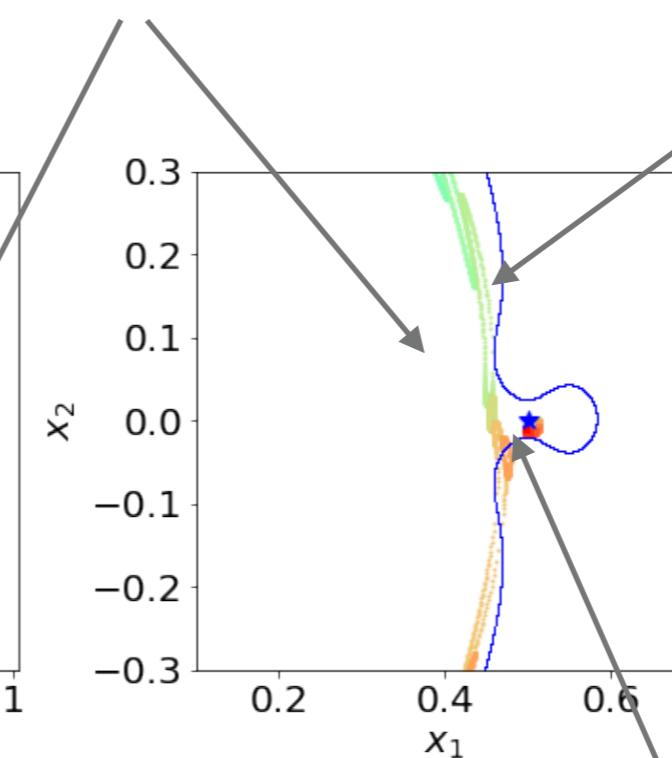
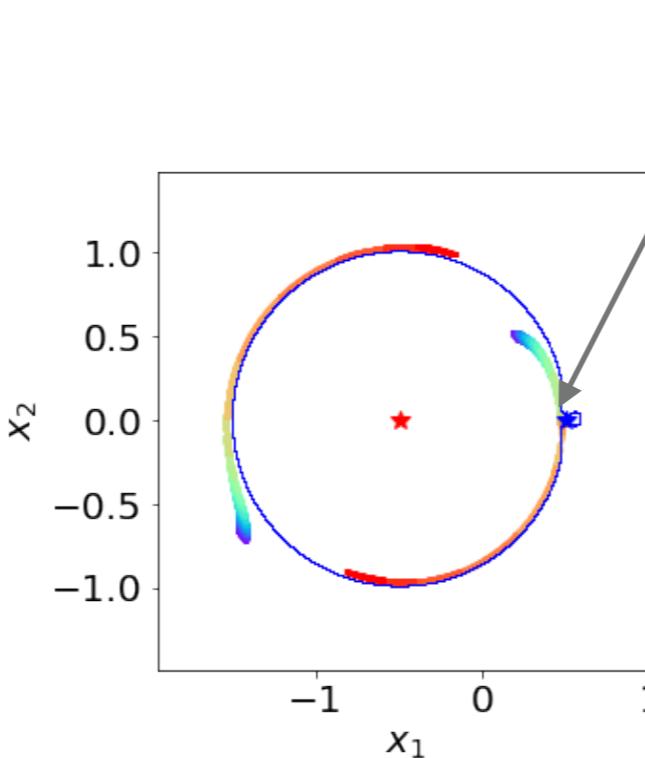
Demagnified inner image

PLANETARY PERTURBATIONS AS PERTURBATIONS OF SINGLE IMAGES

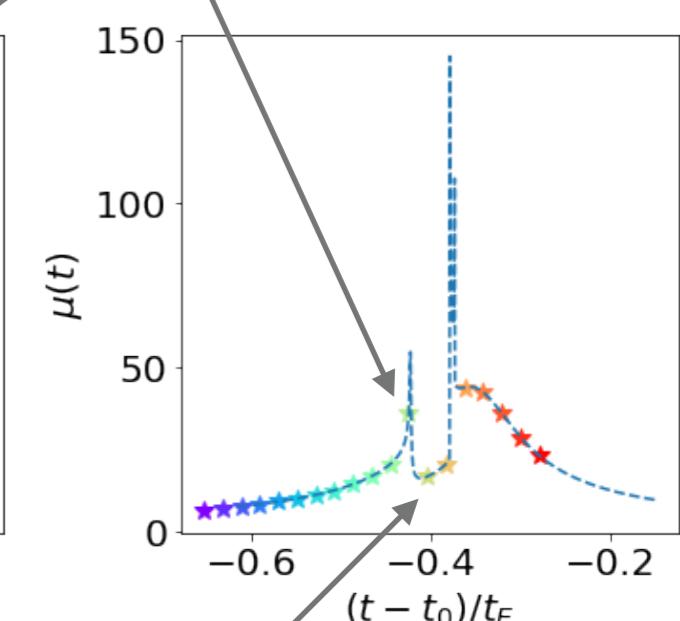
Planetary caustics



Planetary critical lines



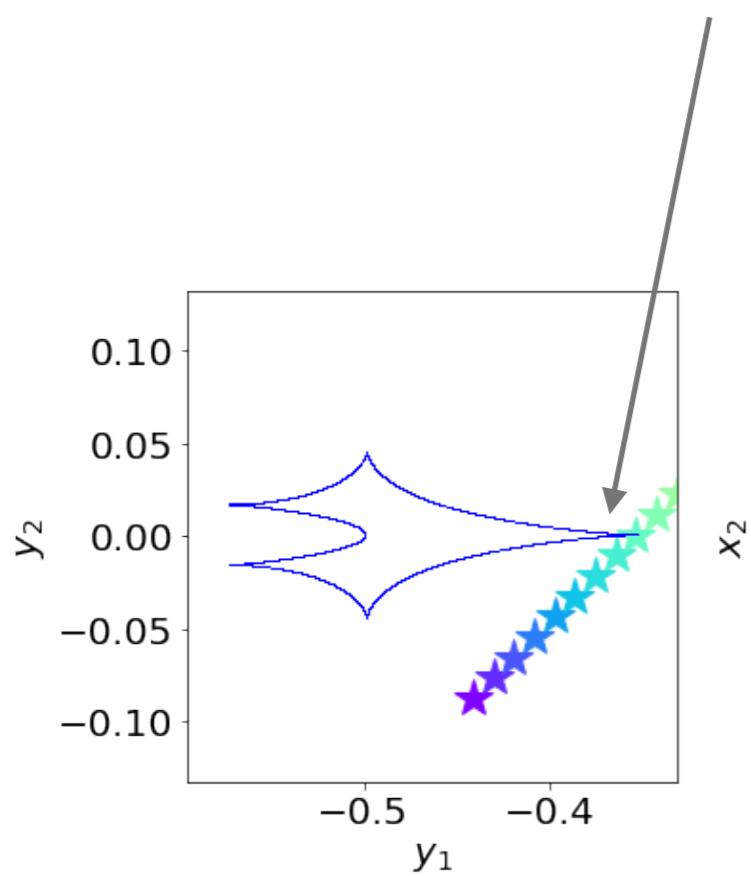
Magnified inner image



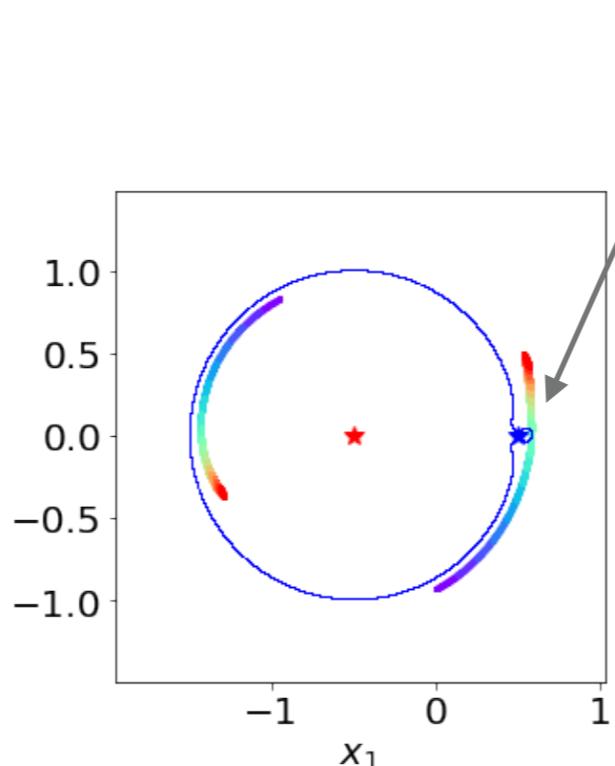
Demagnified inner image

PLANETARY PERTURBATIONS AS PERTURBATIONS OF SINGLE IMAGES

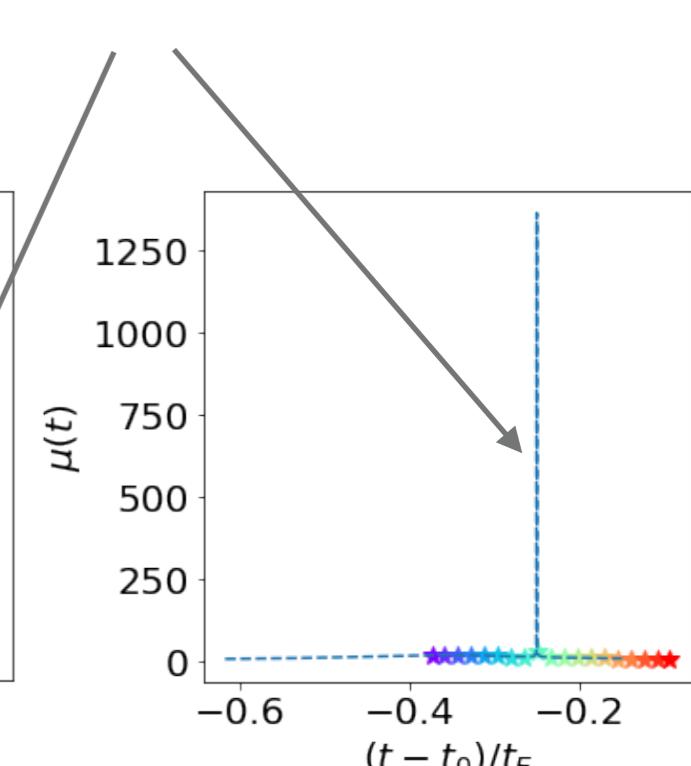
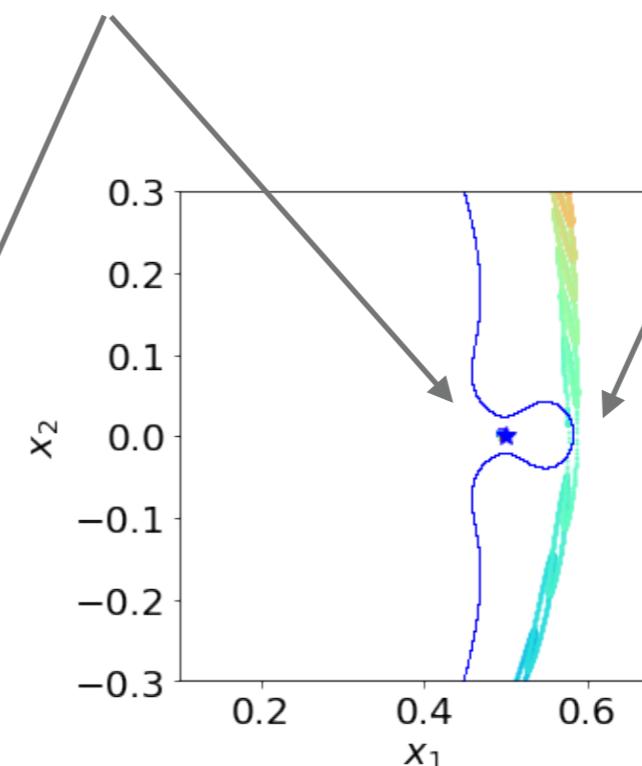
central caustic



Planetary critical lines



Magnified outer image



INTERPRETING THE LIGHT CURVES

If we notice a planetary caustic perturbation, it means that the planet is located at the position of one of the images:

$$|x_{\pm}| = d$$

Consequently the position of the caustic which is being crossed can be derived from the lens equation (which is satisfied by the images)

$$x_{\pm} = \frac{1}{2} \left[y \pm \sqrt{y^2 + 4} \right]$$

INTERPRETING THE LIGHT CURVES

If we notice a planetary caustic perturbation, it means that the planet is located at the position of one of the images:

$$|x_{\pm}| = d$$

$$x_{\pm} = \frac{1}{2} \left[y \pm \sqrt{y^2 + 4} \right]$$

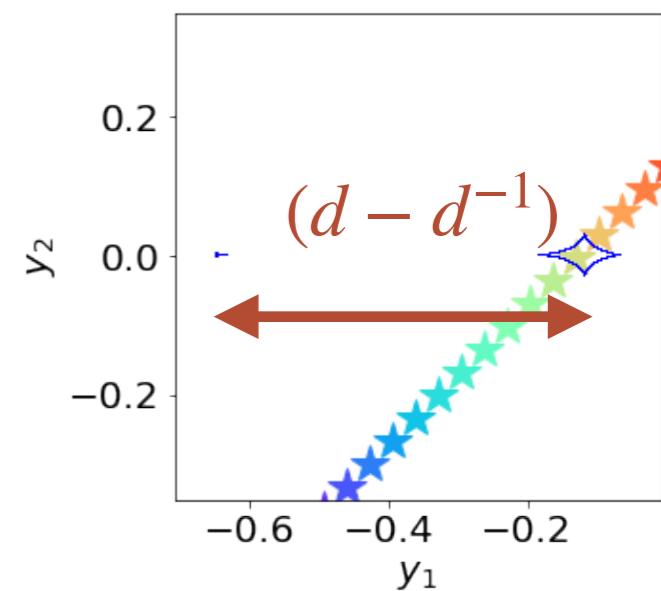
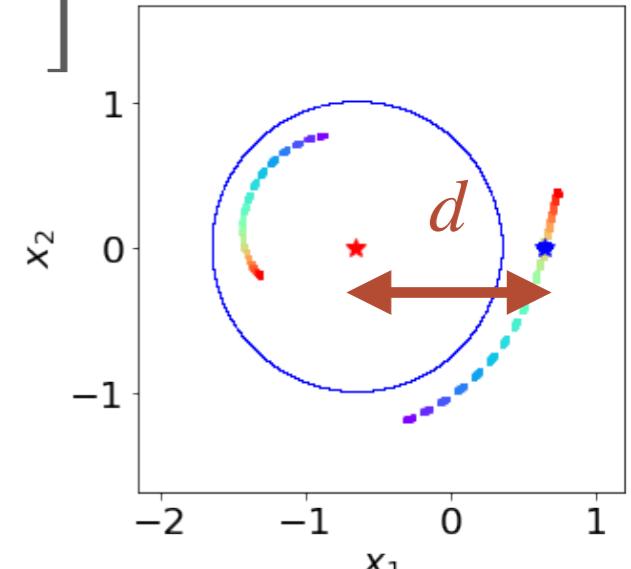
Case 1: perturbation of the outer image ($x_+ > 0$):

$$d = \frac{1}{2}y + \frac{1}{2}\sqrt{y^2 + 4}$$

$$\frac{1}{2}\sqrt{y^2 + 4} = \left(d - \frac{1}{2}y \right)$$

$$y^2 + 4 = 4 \left(d^2 + \frac{y^2}{4} - yd \right) \Rightarrow yd = d^2 - 1$$

$$y = (d - d^{-1})$$



INTERPRETING THE LIGHT CURVES

If we notice a planetary caustic perturbation, it means that the planet is located at the position of one of the images:

$$|x_{\pm}| = d$$

$$x_{\pm} = \frac{1}{2} \left[y \pm \sqrt{y^2 + 4} \right]$$

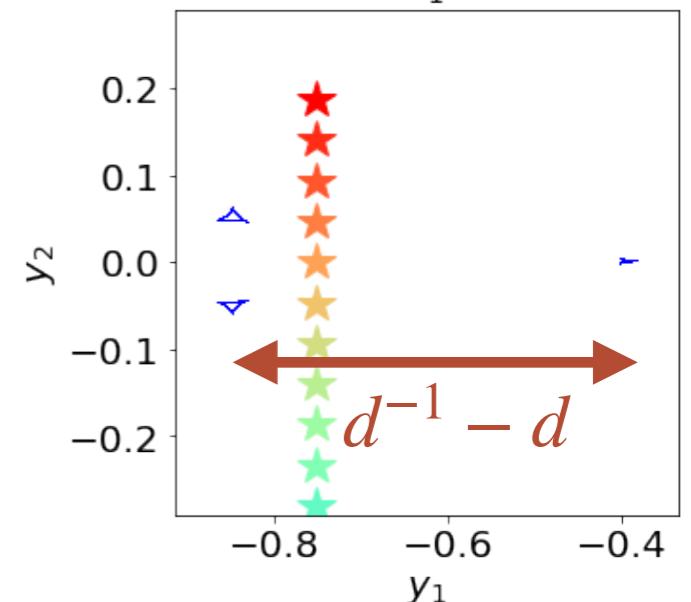
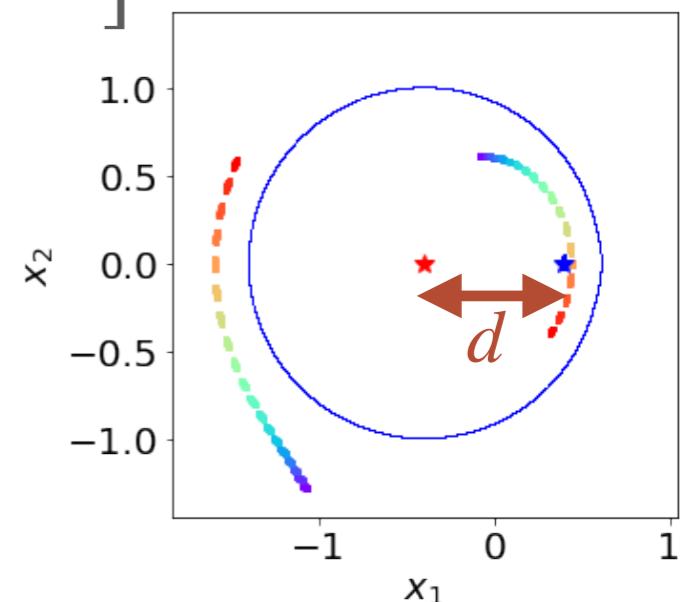
Case 2: perturbation of the inner image ($x_- < 0$):

$$d = - \left(\frac{1}{2}y - \frac{1}{2}\sqrt{y^2 + 4} \right)$$

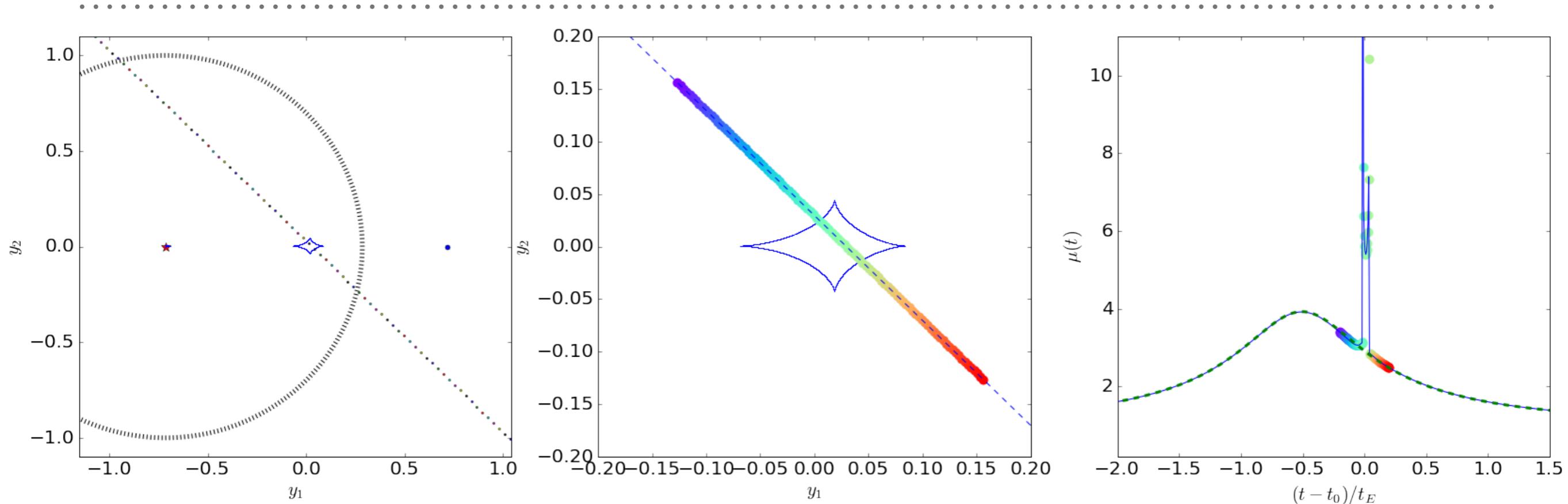
$$\frac{1}{2}\sqrt{y^2 + 4} = \left(\frac{1}{2}y + d \right)$$

$$y^2 + 4 = 4 \left(\frac{y^2}{4} + yd + d^2 \right) \Rightarrow yd = 1 - d^2$$

$$y = (d^{-1} - d)$$

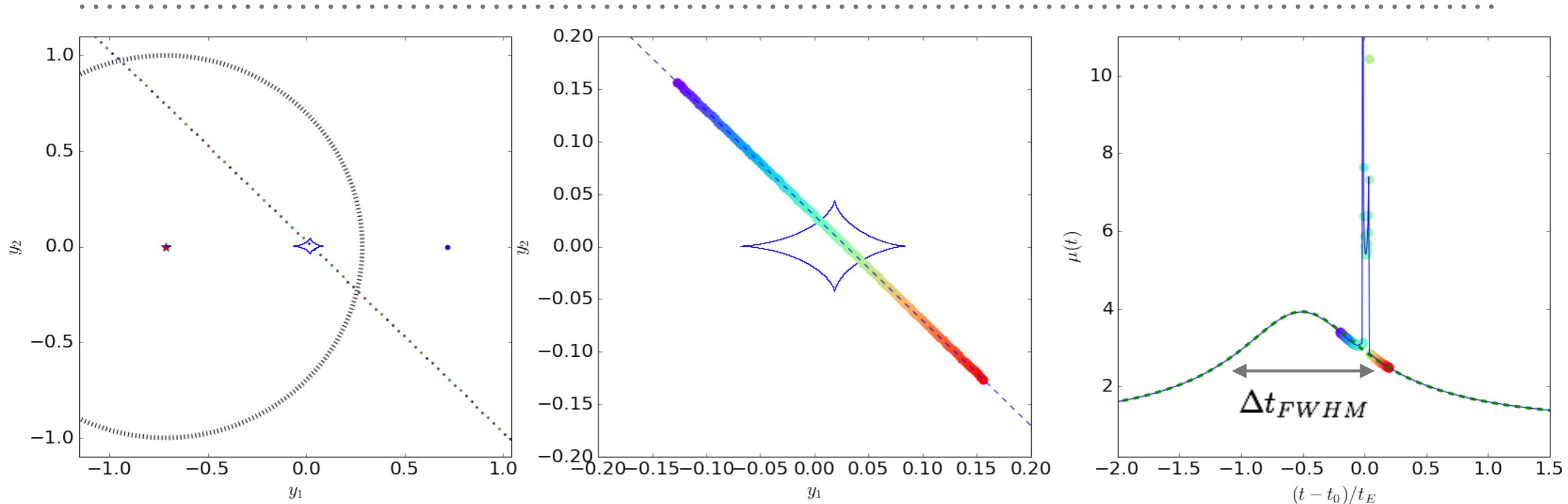


PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



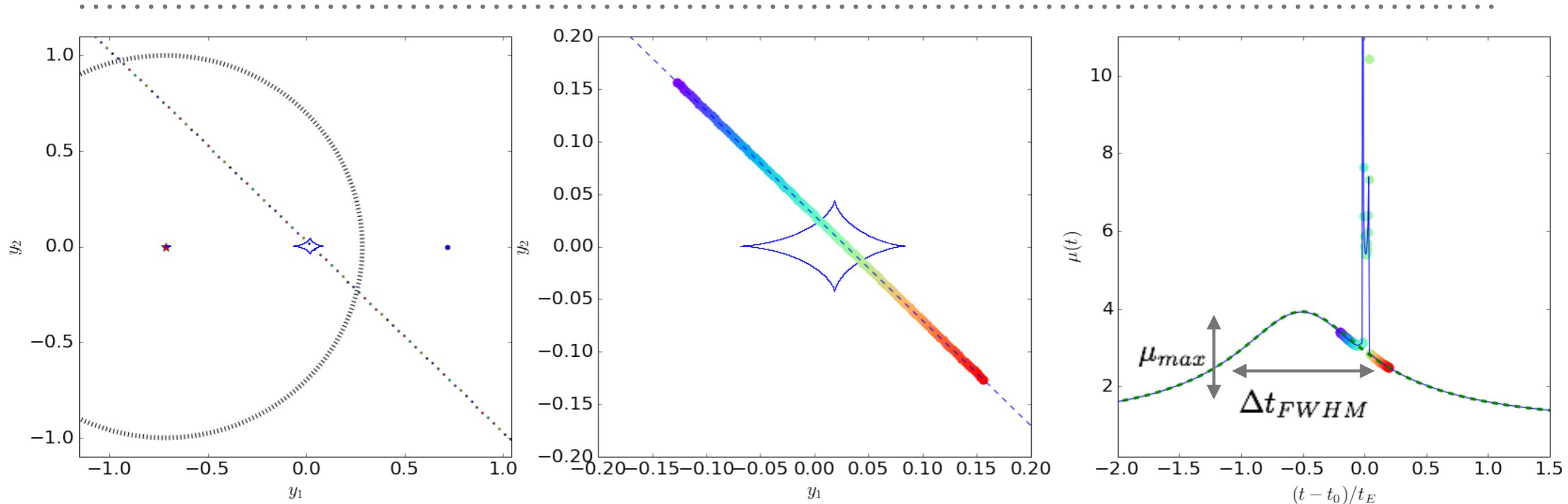
- primary event:
- planetary perturbation:

PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



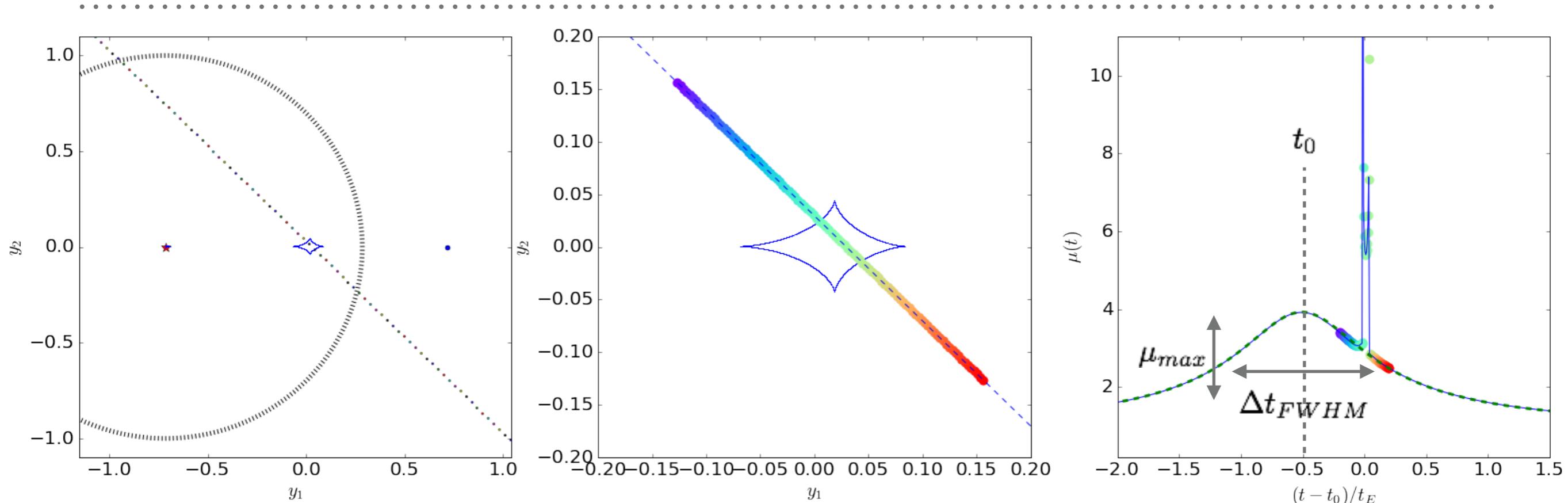
- primary event: Δt_{FWHM}
- planetary perturbation:

PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



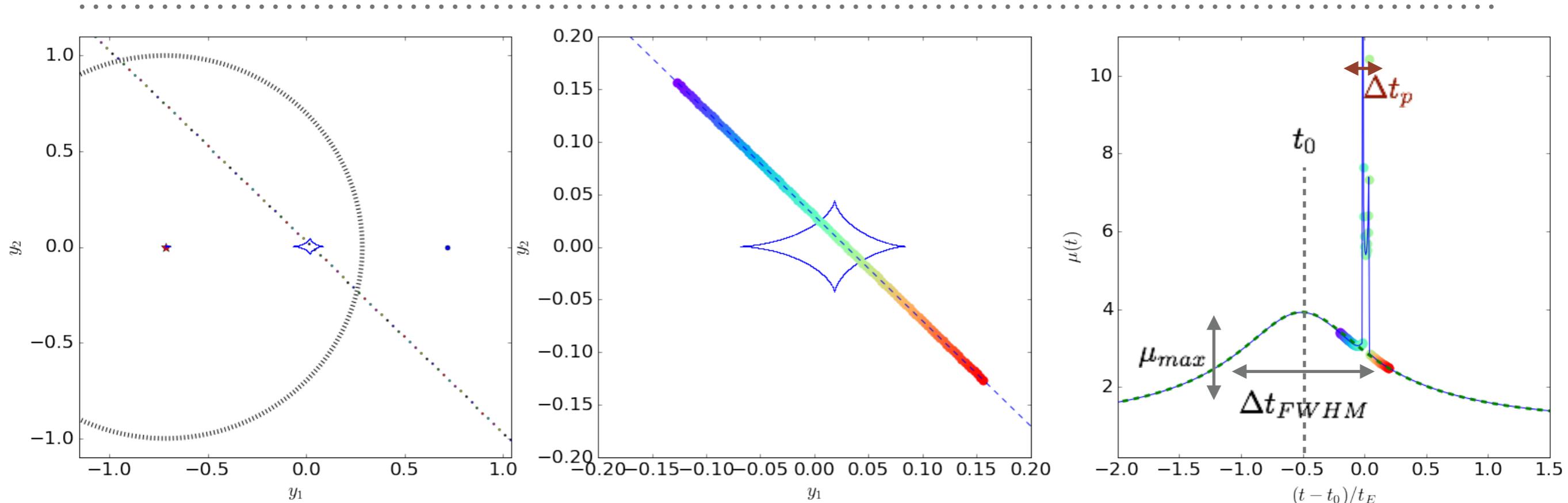
- primary event: Δt_{FWHM} μ_{max}
- planetary perturbation:

PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



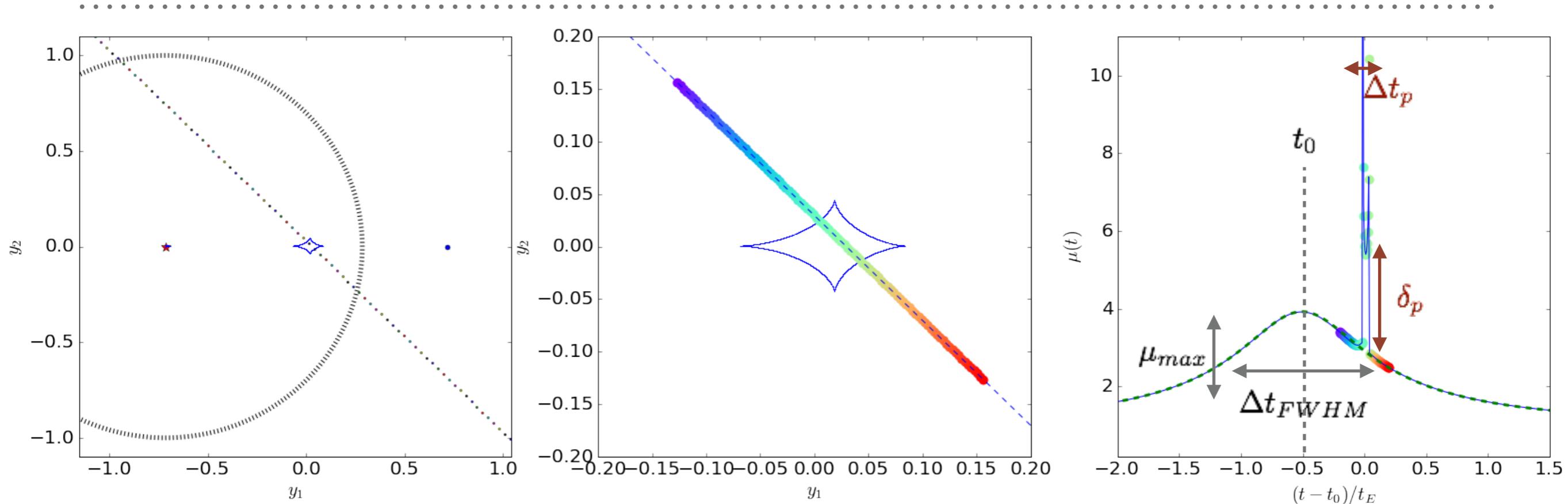
- primary event: Δt_{FWHM} μ_{max} t_0
- planetary perturbation:

PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



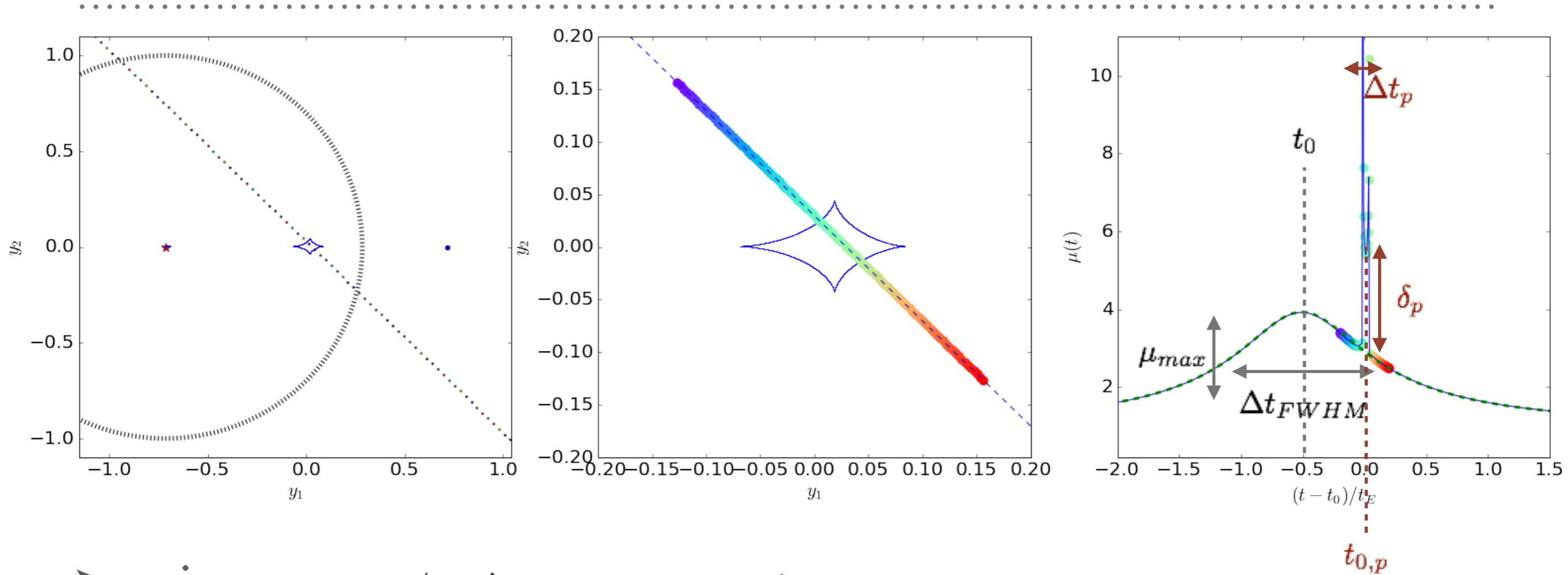
- primary event: Δt_{FWHM} μ_{max} t_0
- planetary perturbation: Δt_p

PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



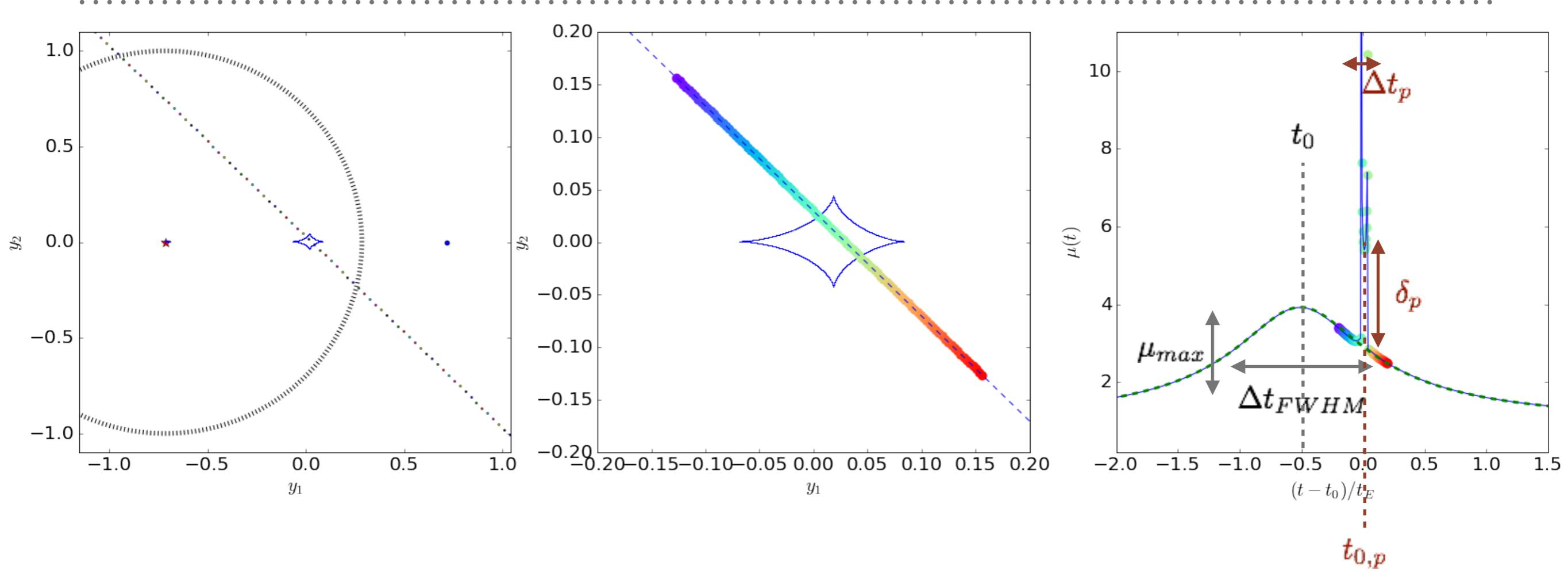
- primary event: Δt_{FWHM} μ_{max} t_0
- planetary perturbation: Δt_p δ_p

PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



- primary event: Δt_{FWHM} μ_{max} t_0
- planetary perturbation: Δt_p δ_p $t_{0,p}$

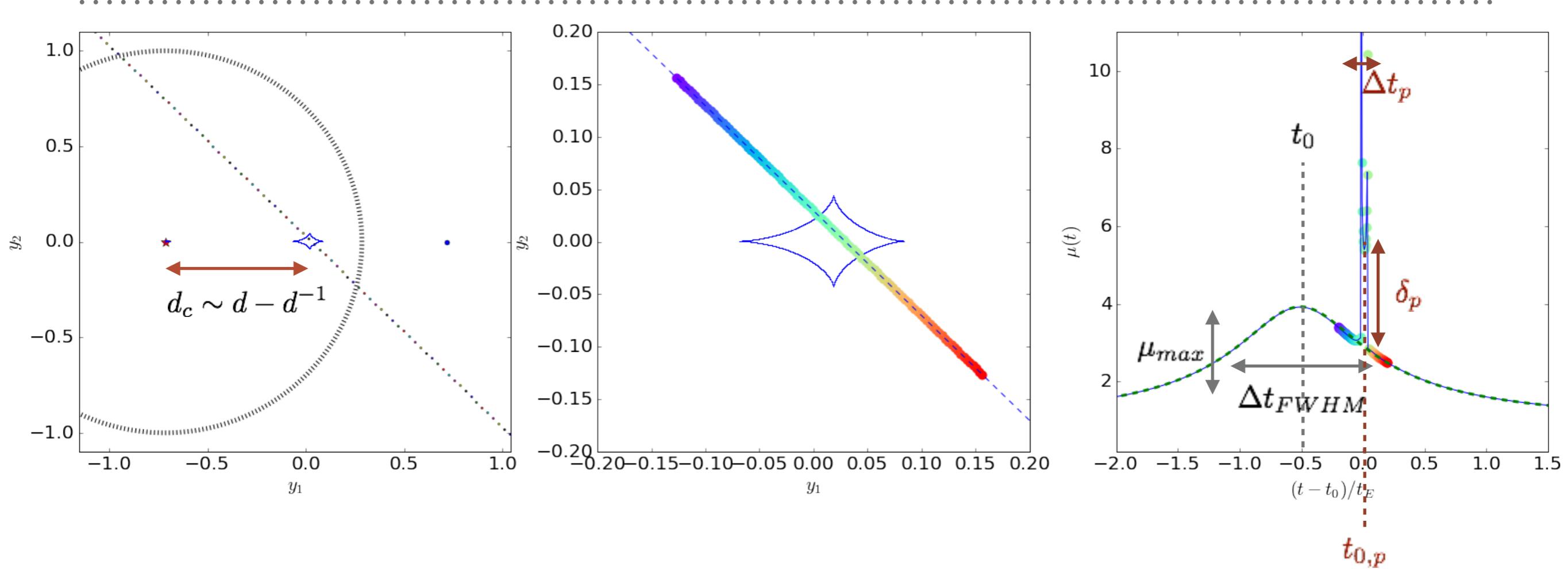
PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



$$\Delta t_{FWHM}, \mu_{max}, t_0 \Rightarrow \mu(y) = \frac{y^2 + 2}{y\sqrt{y^2 + 4}} \quad y(t) = \sqrt{y_0^2 + \left(\frac{t - t_0}{t_E}\right)^2}$$

$$\Rightarrow \quad y_0 \quad t_E$$

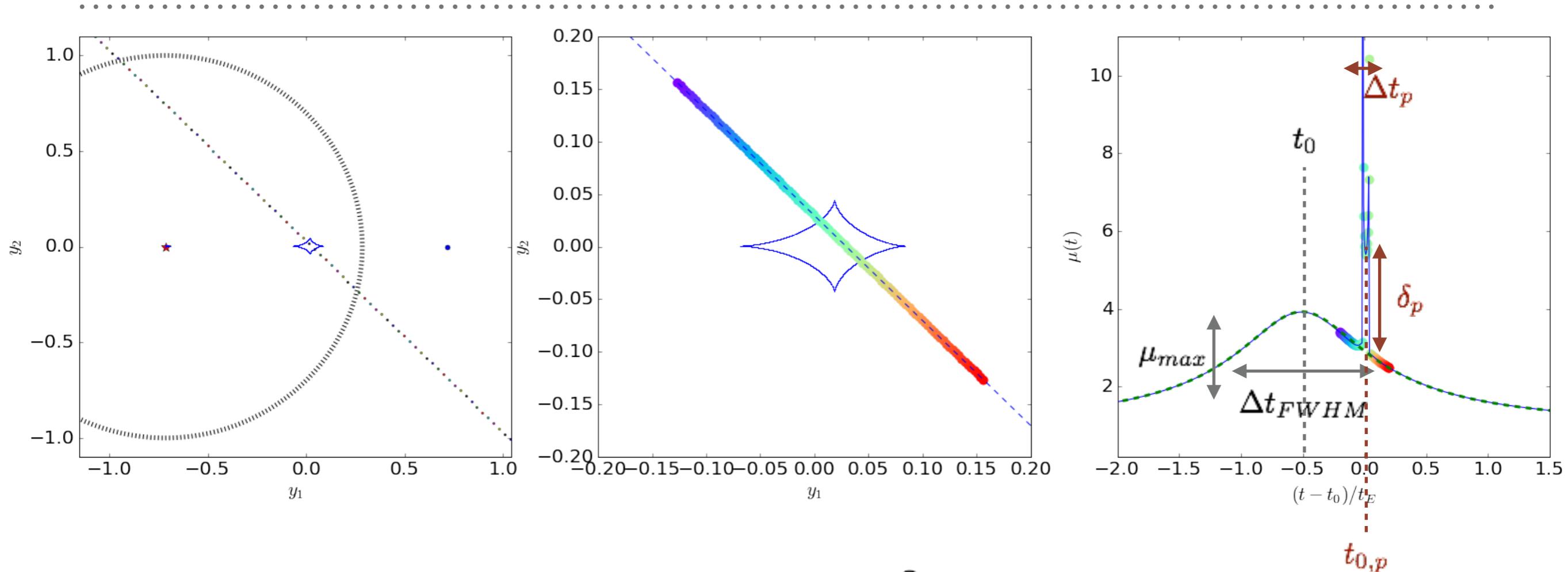
PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



$$t_{0,p} \Rightarrow y_p = \sqrt{y_0^2 + \left(\frac{t_{0,p} - t_0}{t_E} \right)^2}$$

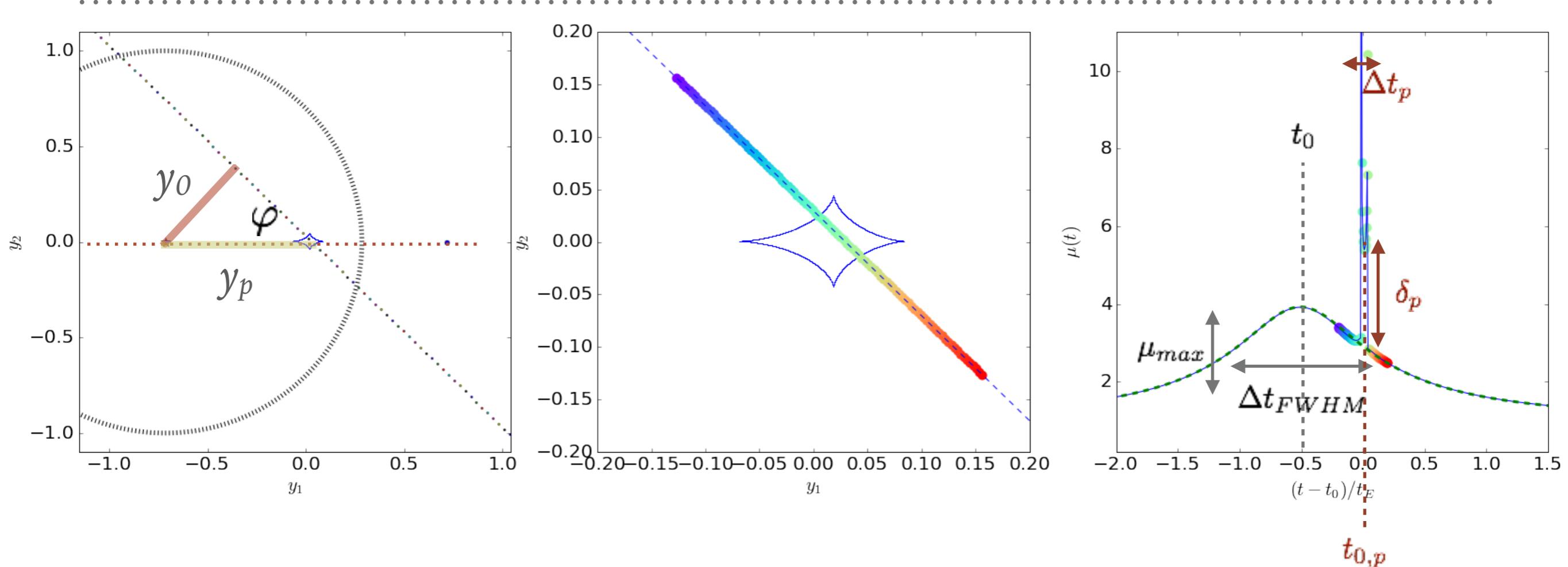
$$\Rightarrow d \sim \frac{1}{2} \left(y_p + \sqrt{y_p^2 + 4} \right)$$

PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



$$\Delta t_p \sim t_{E,p} \Rightarrow t_E \Rightarrow q = \left(\frac{t_{E,p}}{t_E} \right)^2$$

PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES

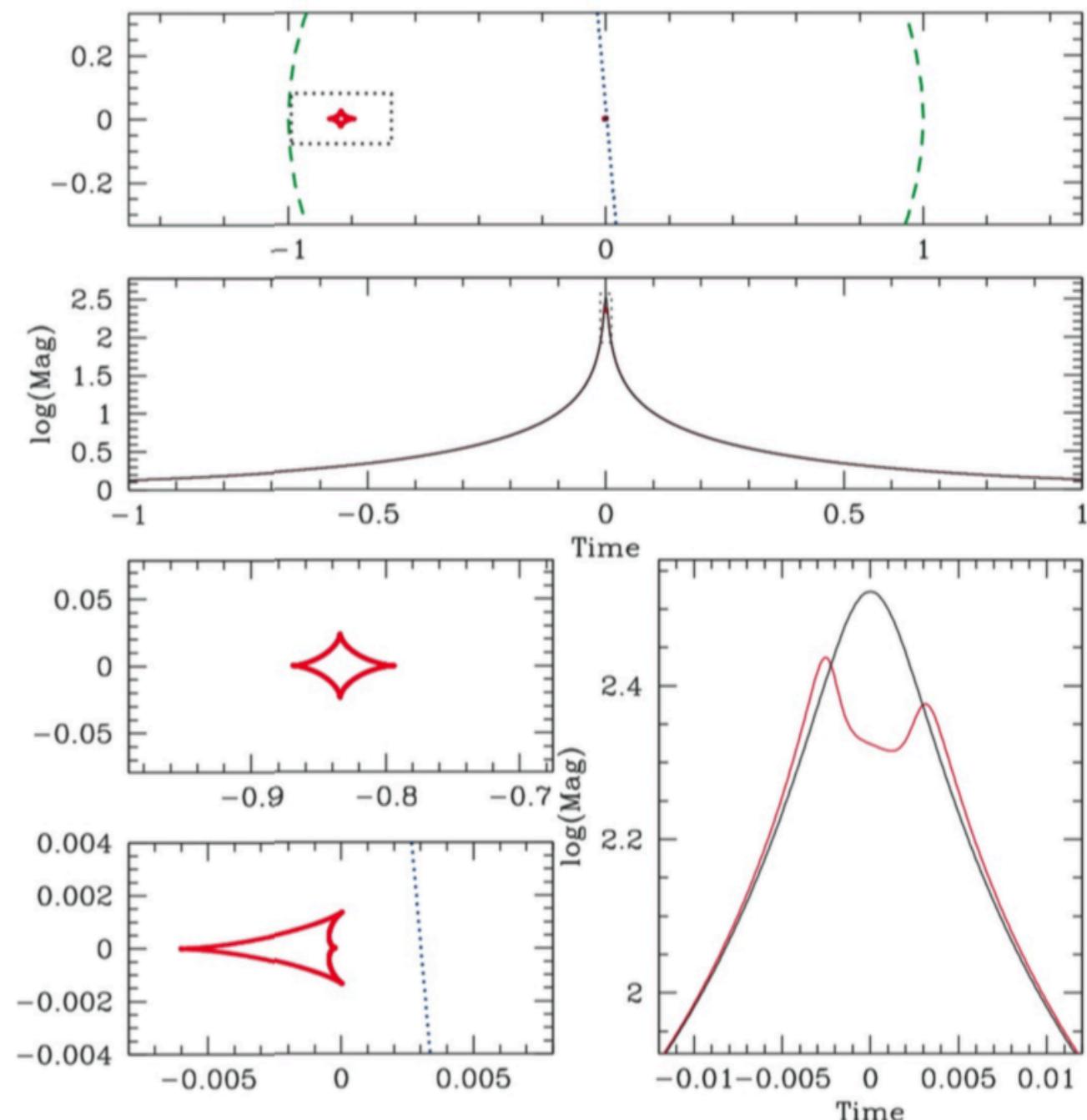
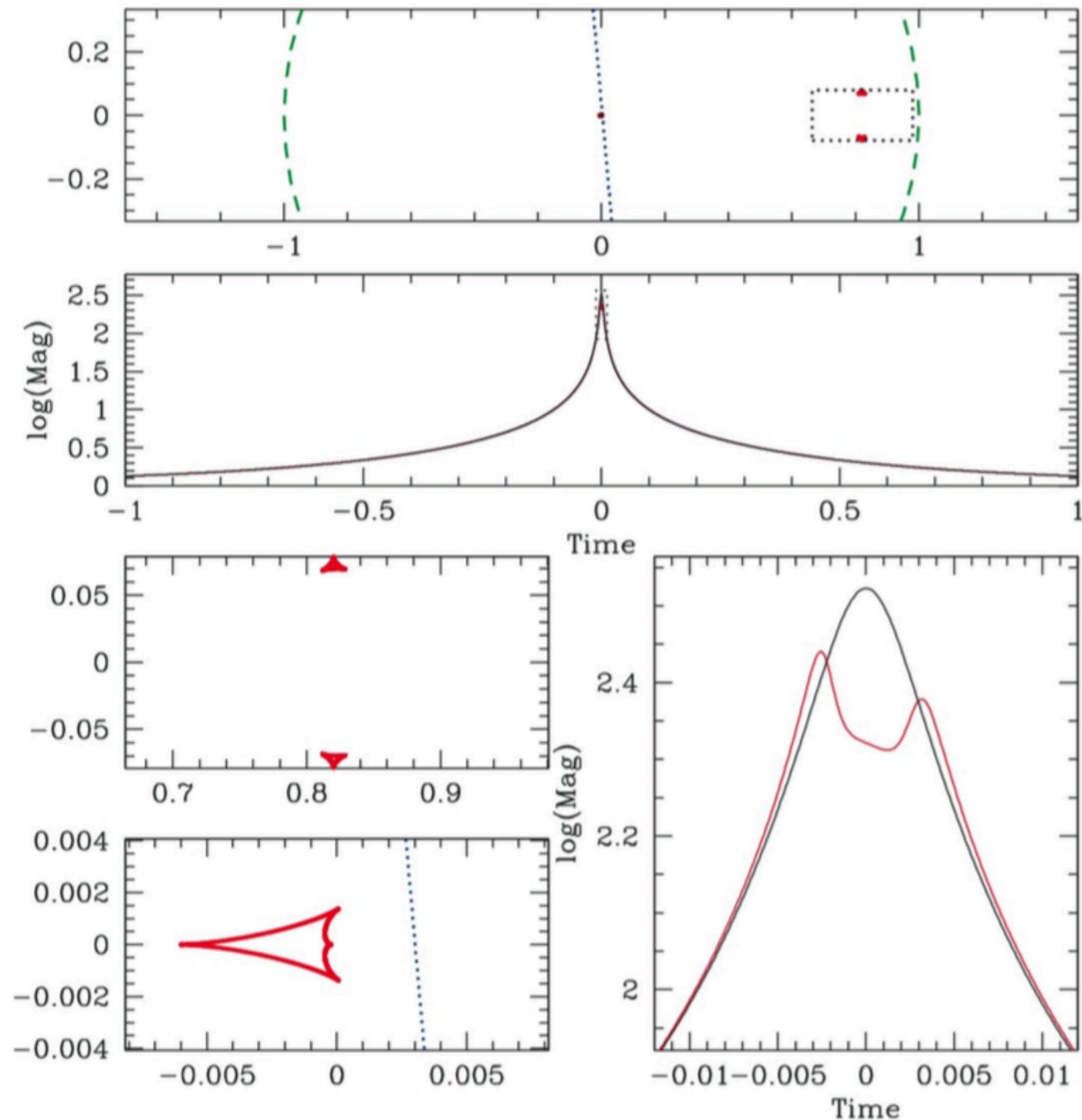


$$y_0, y_p \Rightarrow \varphi = \sin^{-1} \frac{y_0}{y_p}$$

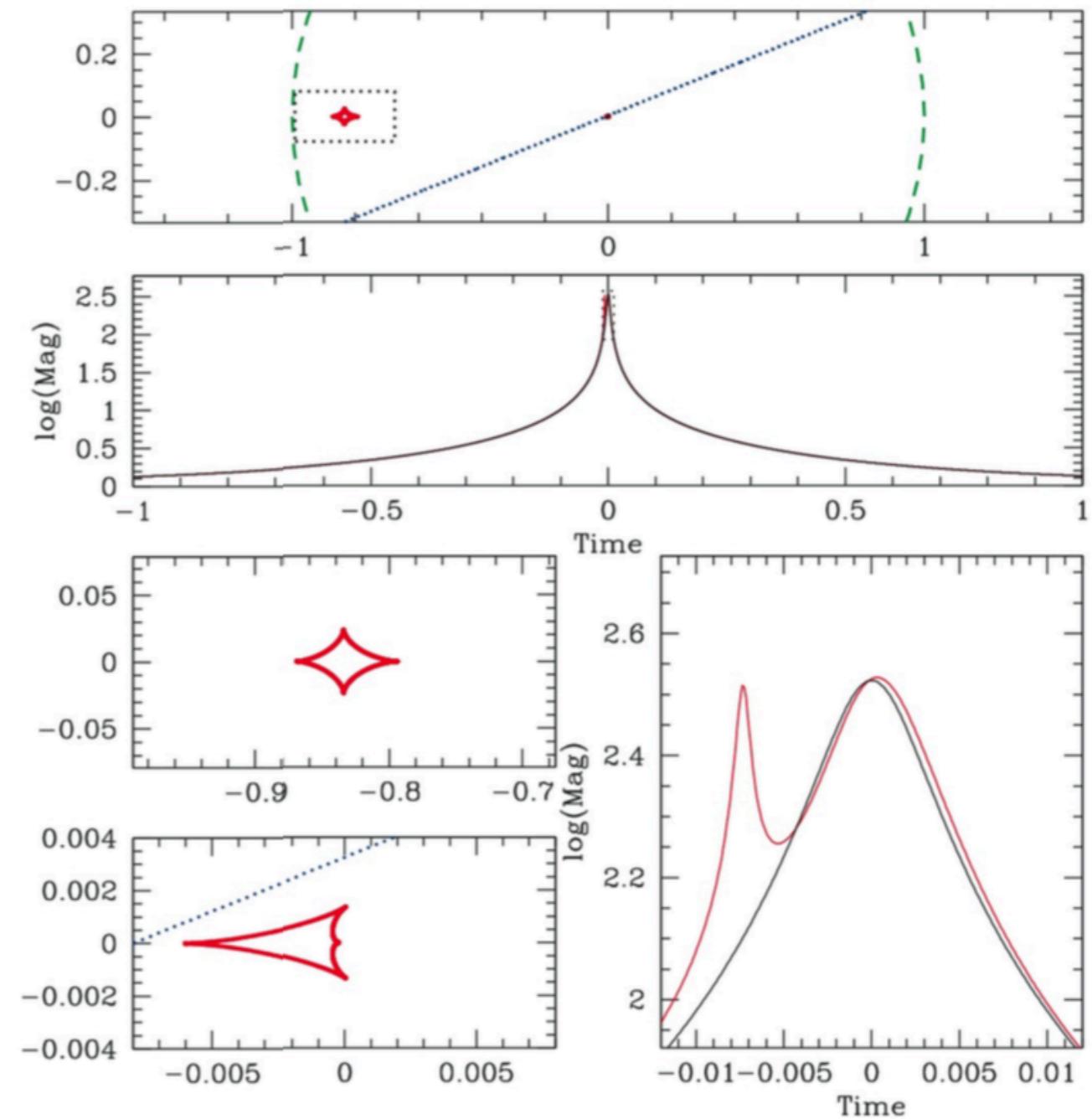
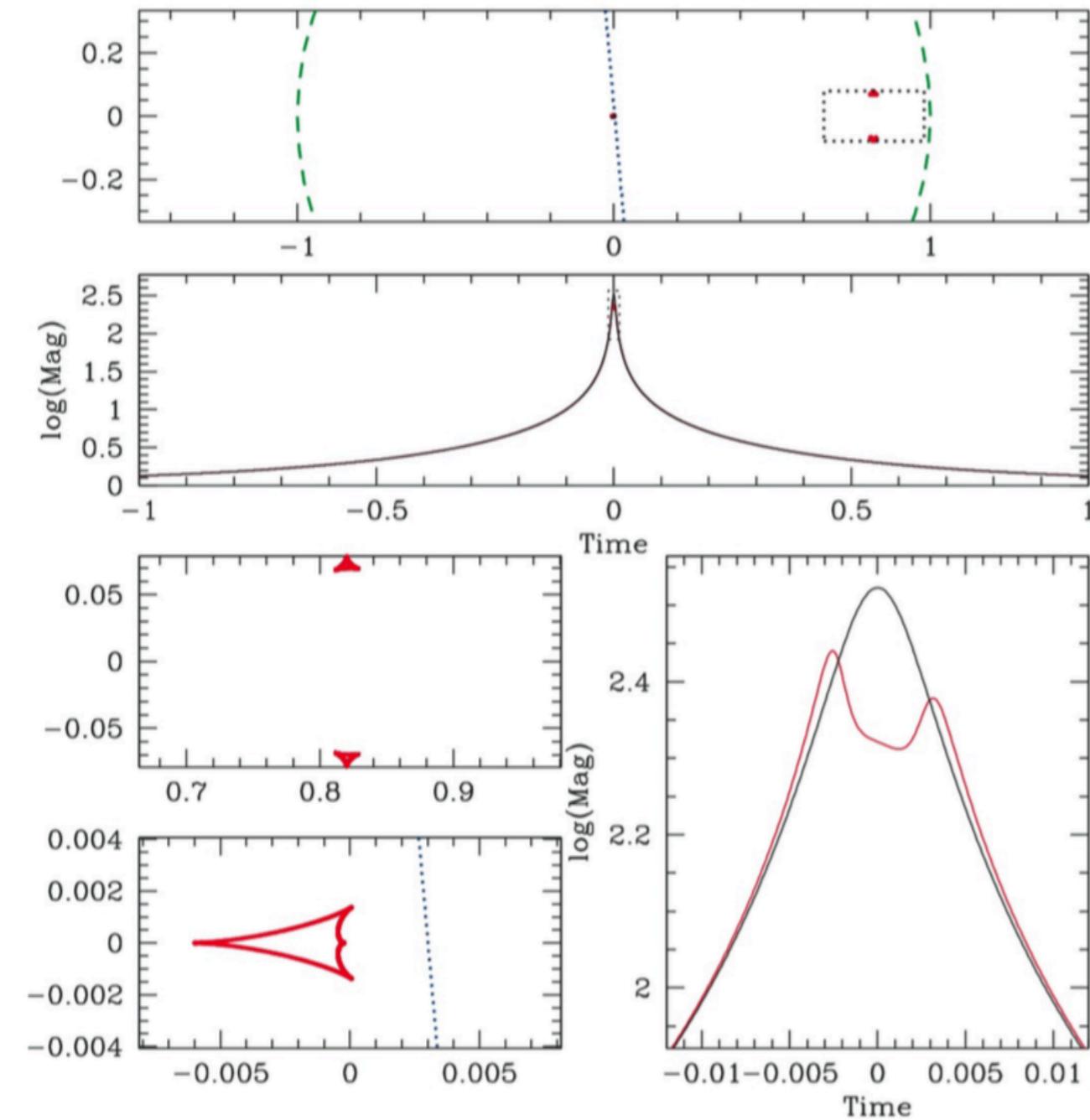
TO SUMMARIZE

- different caustic topologies give rise to different kind of perturbations on the light curves
- planets can be detected in only a few qualitatively different ways:
 - at relatively low magnification of the primary, if the source crosses the planetary caustics from close or wide planets
 - near the peak of the light curve, if the source has a small impact parameter, in both cases of wide and close planets
 - at modest to high-magnification, through the perturbations from the resonant caustic.
 - in the case of free-floating planets, as single, short time-scale events.
- Light curves can be used to extract parameters of the primary and of the planet
- As seen for single point masses, degeneracies can be broken (finite source effects, microlensing parallax)
- Some cases are more difficult than others...

CLOSE-WIDE DEGENERACY

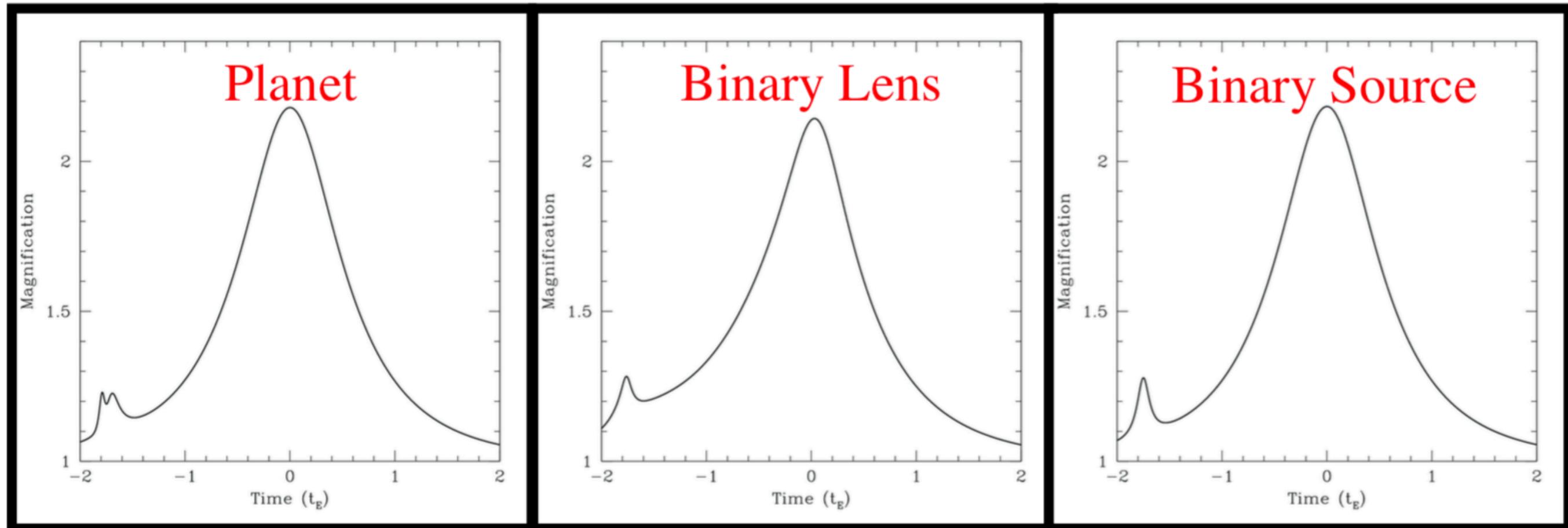


DOUBLE HORN OR BUMP



UNCERTAINTIES: SOME FEATURES CAN BE EXPLAINED IN DIFFERENT WAYS

Short duration deviations in the wings:



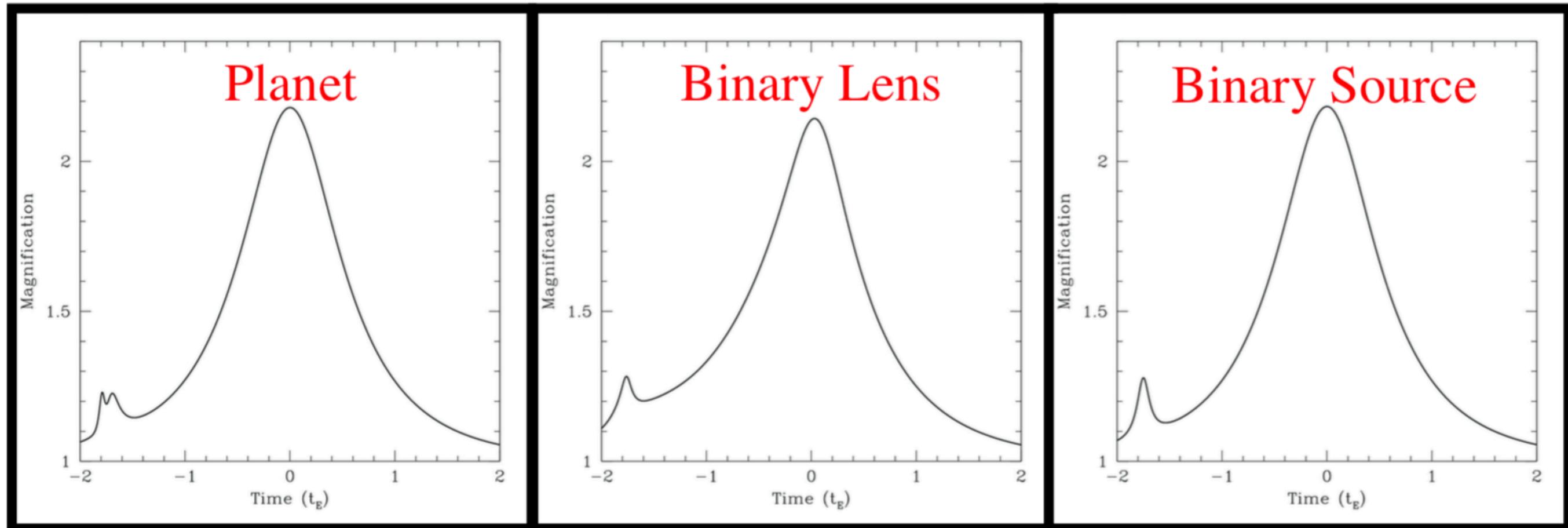
Can be caused by:

- Planets
- close binary lenses
- extreme flux ratio binary sources (rare)

Rule: negative deviations are exclusively planets

UNCERTAINTIES: SOME FEATURES CAN BE EXPLAINED IN DIFFERENT WAYS

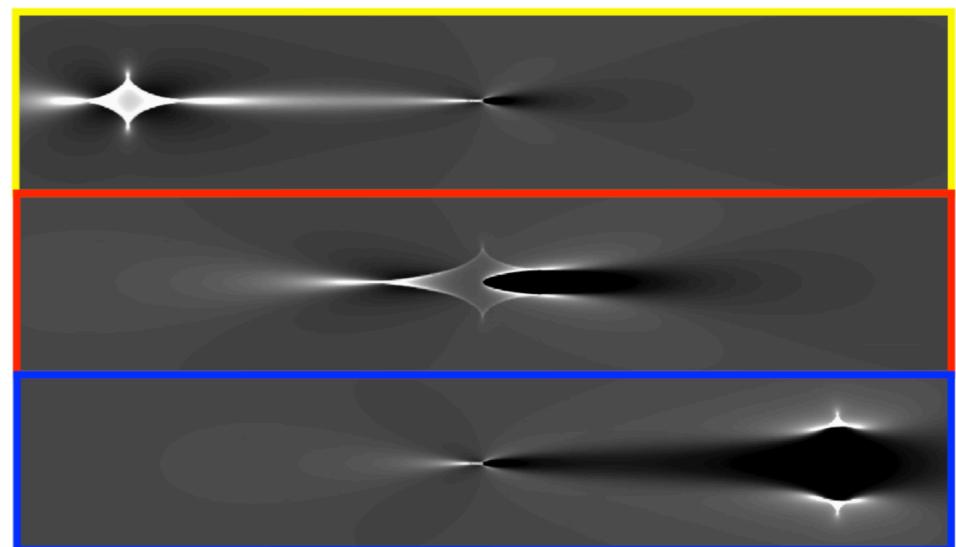
Short duration deviations in the wings:



Can be caused by:

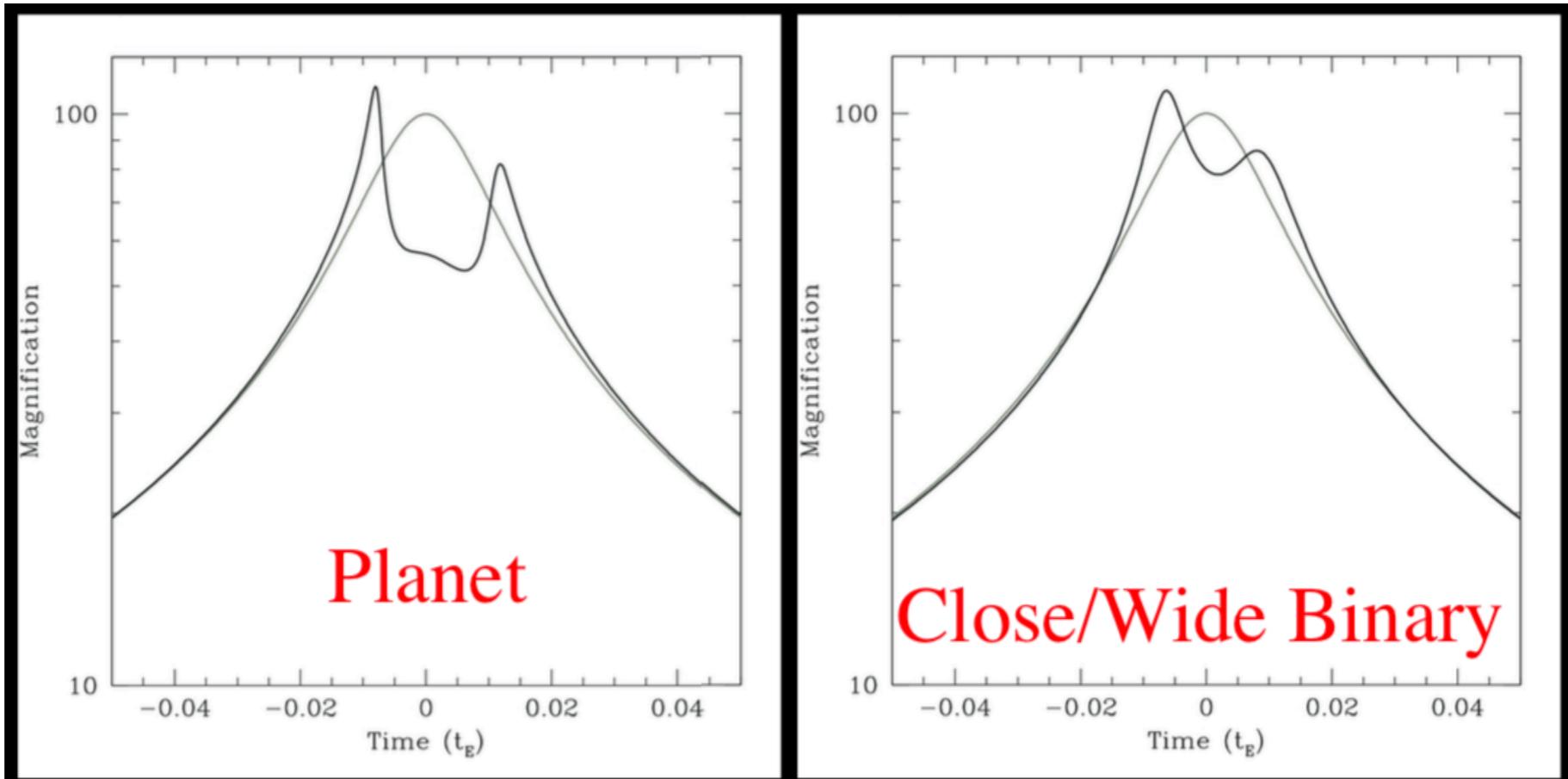
- Planets
- close binary lenses
- extreme flux ratio binary sources (rare)

Rule: negative deviations are exclusively planets



UNCERTAINTIES: SOME FEATURES CAN BE EXPLAINED IN DIFFERENT WAYS

Short duration deviations at the peak:

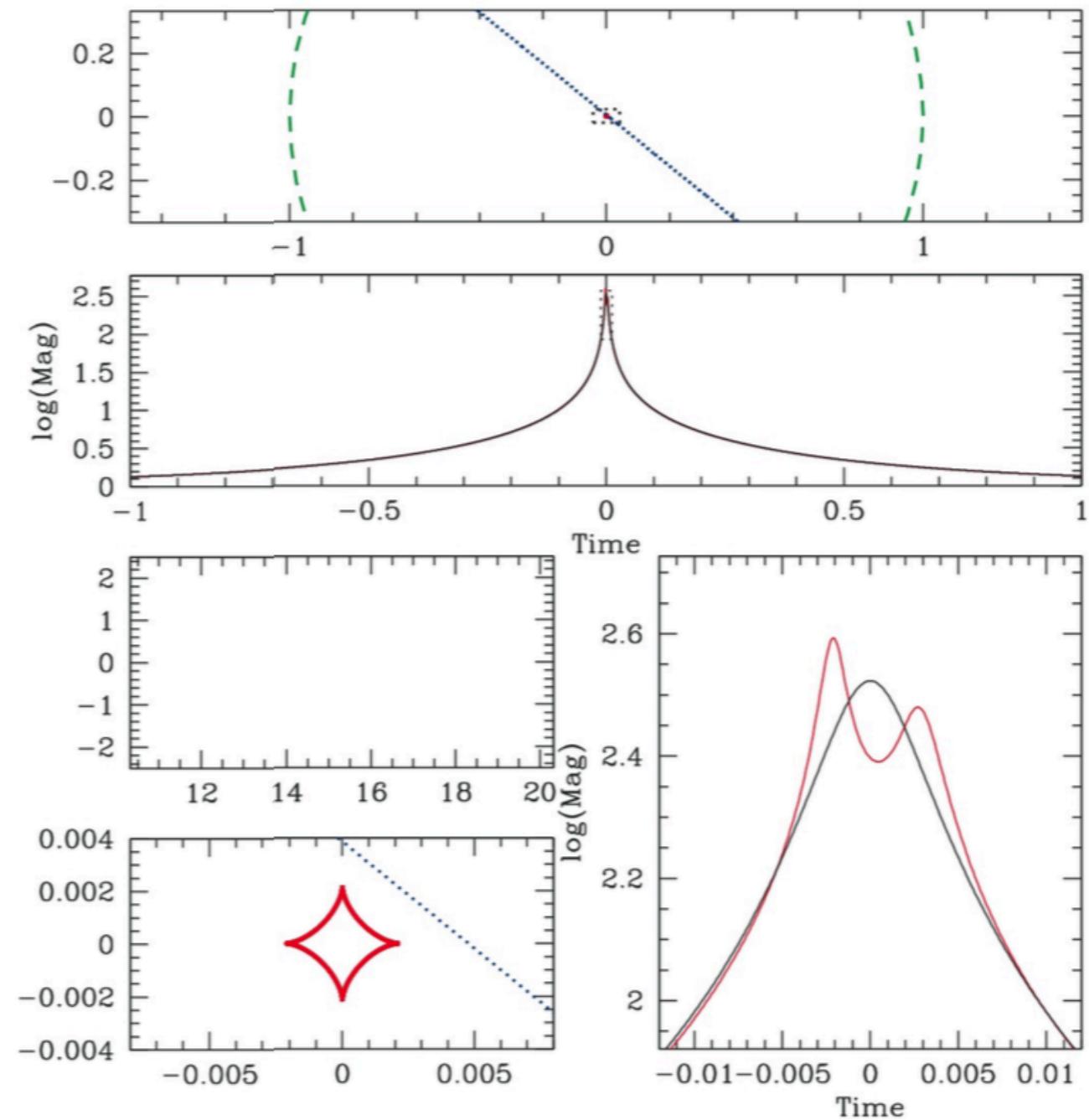
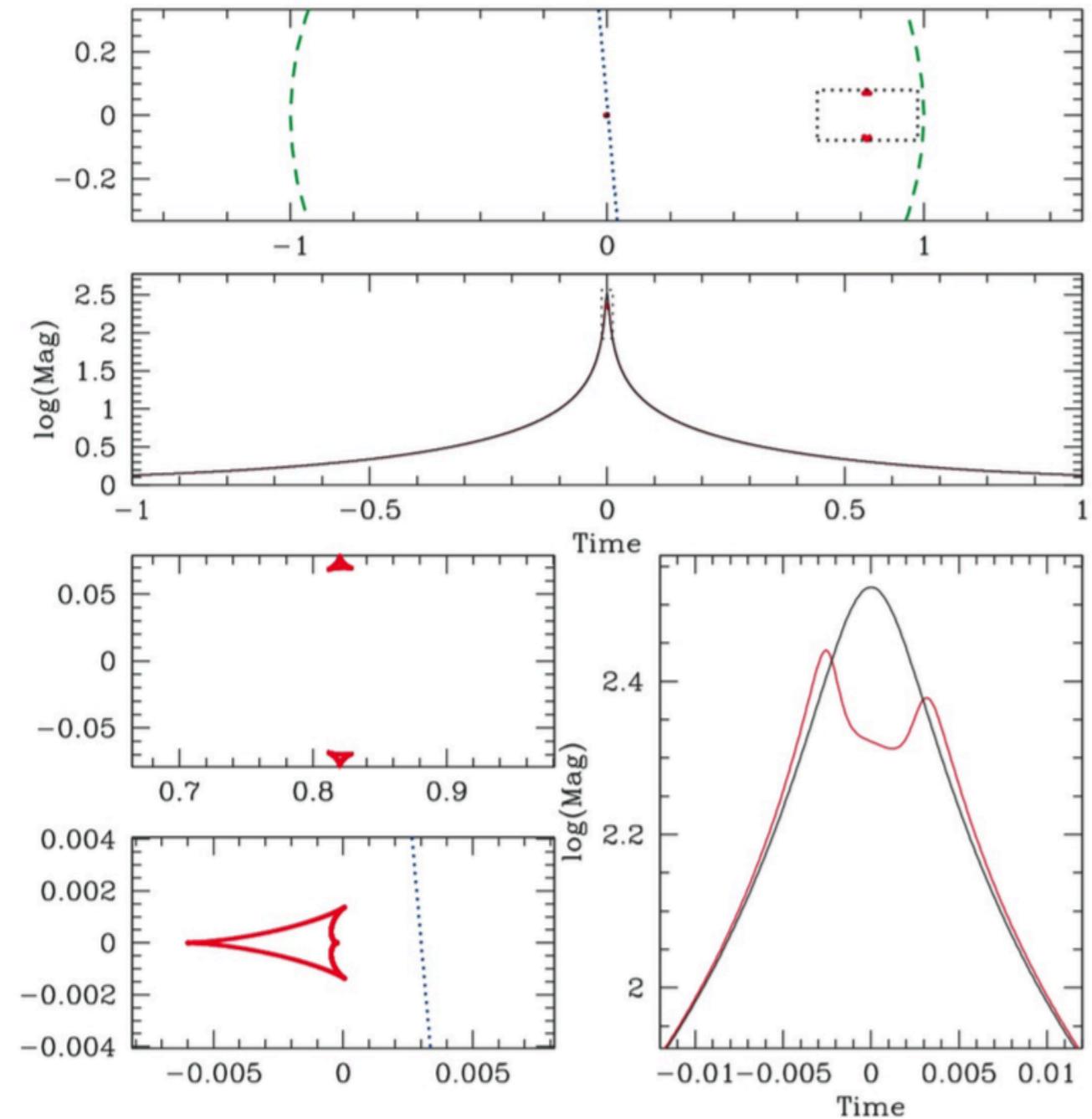


Can be caused by:

- Planets
- very close or very wide binary lenses

Rule: look for the central bump in the middle of the horns

CLOSE BINARIES VS PLANETS

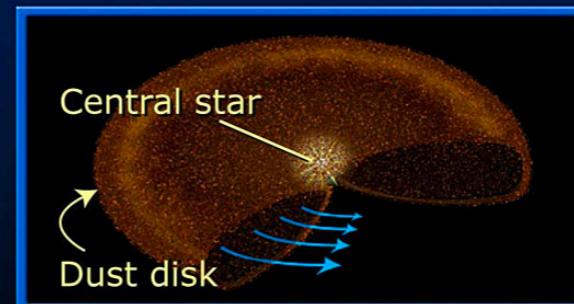


WHY SEARCHING PLANETS?

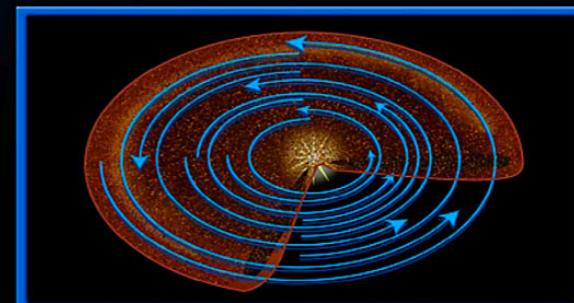
- Planet formation and evolution is still not fully understood
- Different models predict different distributions of planet masses and distances from the host stars
- Sizes of planets may depend on the mass of the host star, on the position in the galaxy (e.g. on the local metallicity), etc
- Models are thus tested by counting planets of different masses and orbital parameters

TWO PLANET FORMATION SCENARIOS

Accretion model



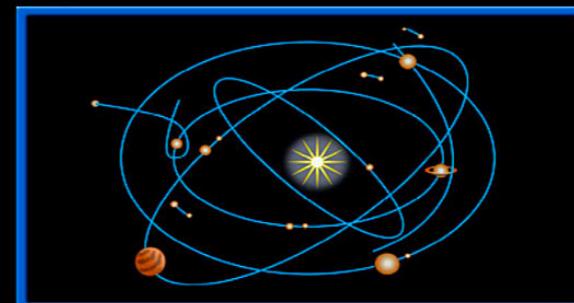
Orbiting dust grains accrete into "planetesimals" through nongravitational forces.



Planetesimals grow, moving in near-coplanar orbits, to form "planetary embryos."



Gas-giant planets accrete gas envelopes before disk gas disappears.



Gas-giant planets scatter or accrete remaining planetesimals and embryos.

Gas-collapse model



A protoplanetary disk of gas and dust forms around a young star.



Gravitational disk instabilities form a clump of gas that becomes a self-gravitating planet.



Dust grains coagulate and sediment to the center of the protoplanet, forming a core.



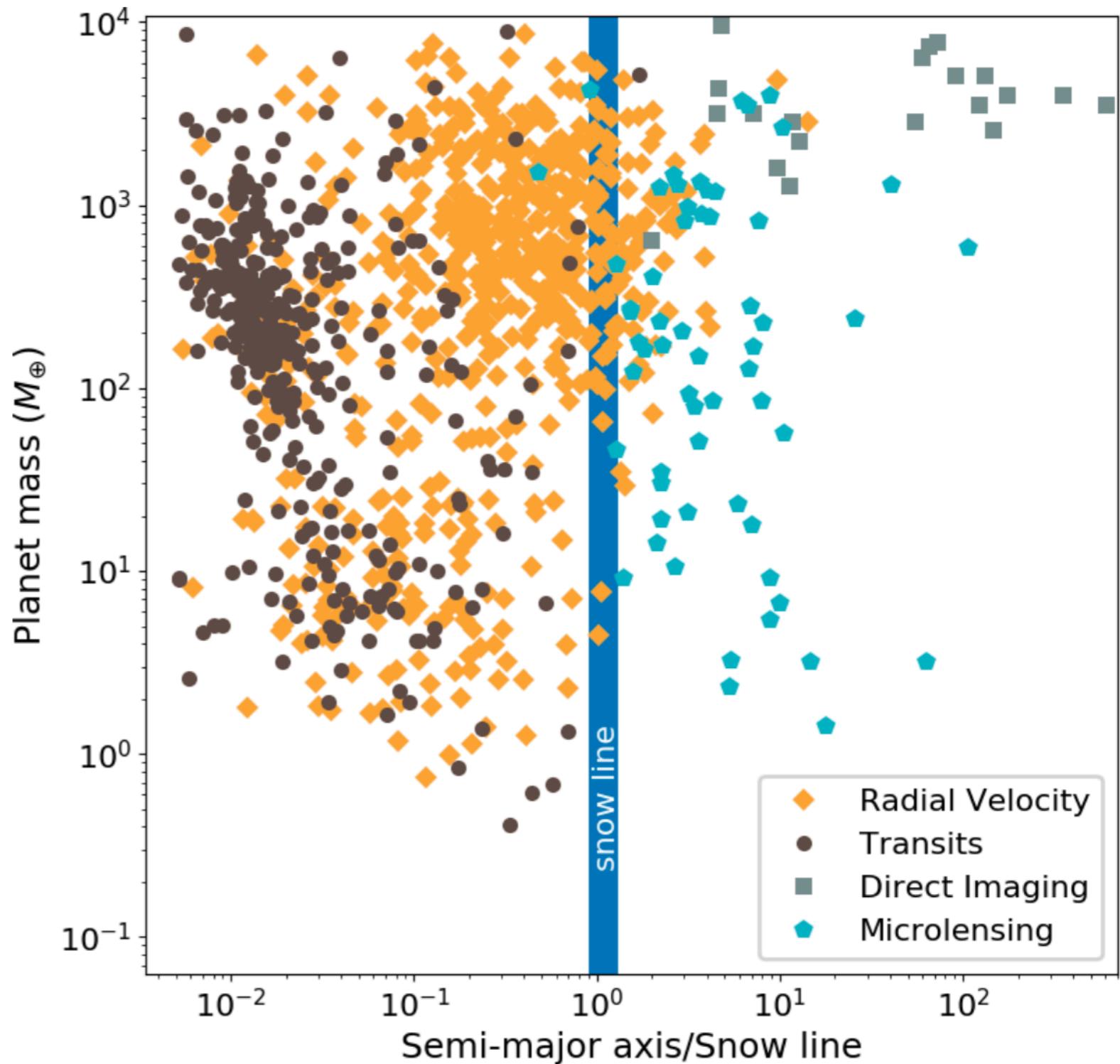
The planet sweeps out a wide gap as it continues to feed on gas in the disk.

METHODS TO SEARCH PLANETS OTHER THAN MICROLENSING

- **Radial velocity shift:** relies on the fact that a star does not remain completely stationary when it is orbited by a planet. The star moves, ever so slightly, in a small circle or ellipse, responding to the gravitational tug of its smaller companion. This produces periodic shifts of lines in the stellar spectra. This method was very successful in *discovering giant planets near their hosts*.
- **Transit surveys:** identify exoplanets with near edge-on orbits that pass in front of their host stars. **Hundreds of planets within ~ 1 AU from their hosts** were found by e.g. the NASA's Kepler space mission.
- **Direct imaging:** Massive planets at large distances from their hosts can be visually identified in planetary systems that are not too far away.
- **Astrometry:** involves very precise measurements of a star's position in the sky. If the star is orbited by a planet, periodic shifts of its position occur (for the same reasons that cause the radial velocity shifts).
- **Pulsar timing:** pulsars are rapidly rotating neutron stars that emit periodic pulses of electromagnetic radiation. These pulses become irregular in case the pulsar is orbited by a planet.

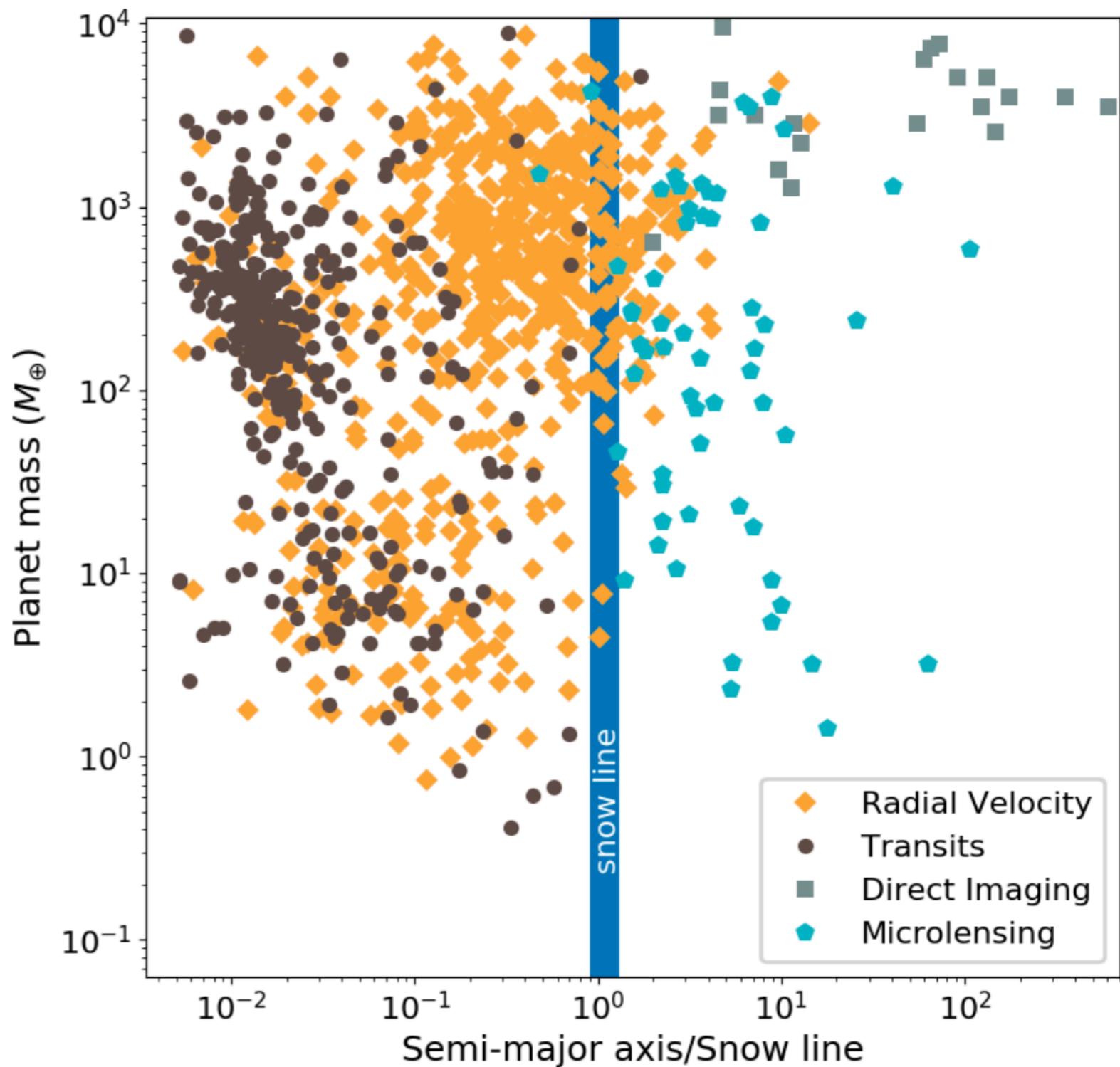
THE CURRENT PICTURE

- ~4400 confirmed exoplanets
- Transits and radial velocity shifts are by far the most successful techniques
- Astrometry: very precise measurements are necessary. Only one detection (not confirmed). Possibly GAIA will revolutionise the picture
- Vast majority of detections are massive planets close to their hosts (<1-2 AU)
- To explore the outer parts of planetary systems, only direct imaging works but it is limited to very massive planets



USING MICROLENSING FOR PLANET SEARCHES

- ~90 planets discovered via microlensing so far
- ~1% of all microlensing events contain planetary anomalies
- $d_{\min} = 0.66$ AU
- bulk of planets at $d \sim 3$ AU
- wide range of masses
- complementary technique to others that are most sensitive to planets near their host stars



USING MICROLENSING FOR PLANET SEARCHES

- planets are most easily identified when they are at a distance \sim
- example: 1 mas at $\sim 5\text{kpc} = 5\text{A}$
- peak sensitivity beyond the snow line
- the snow line marks a very important region for planet formation!
- Boundary distance from the star beyond which the ambient temperature drops below $\sim 160\text{K}$ and water turns to ice

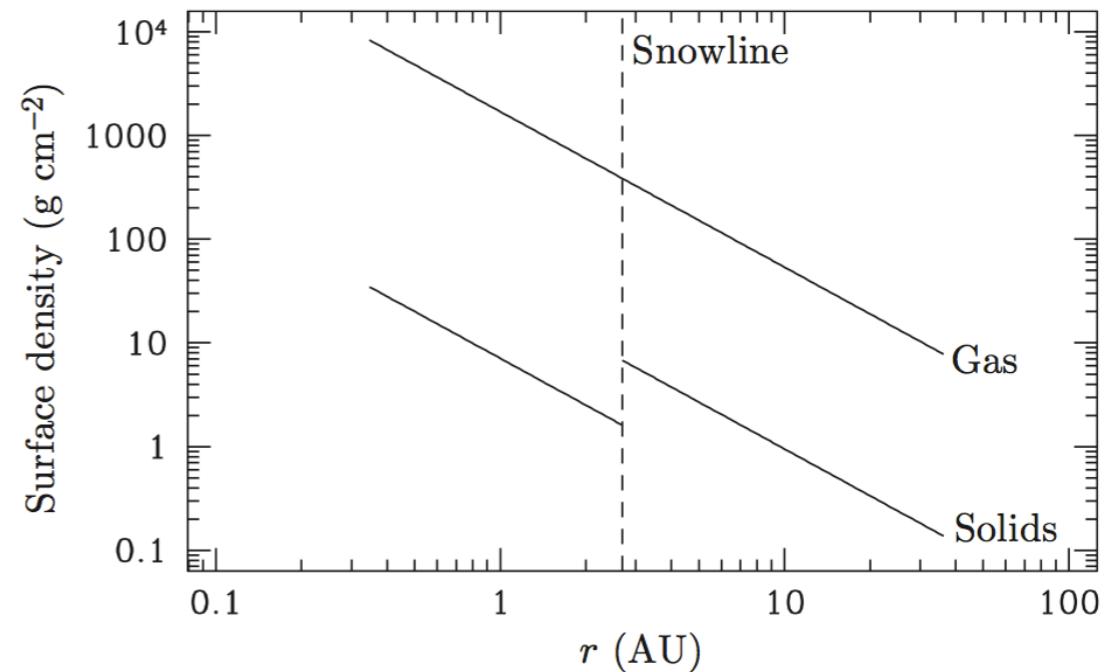
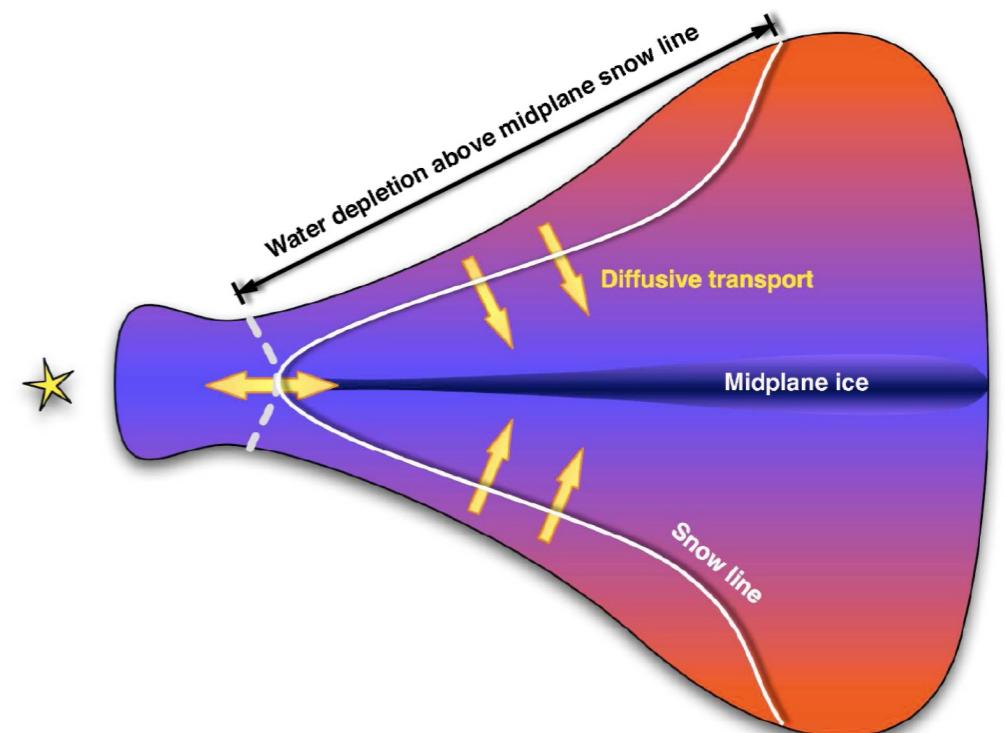
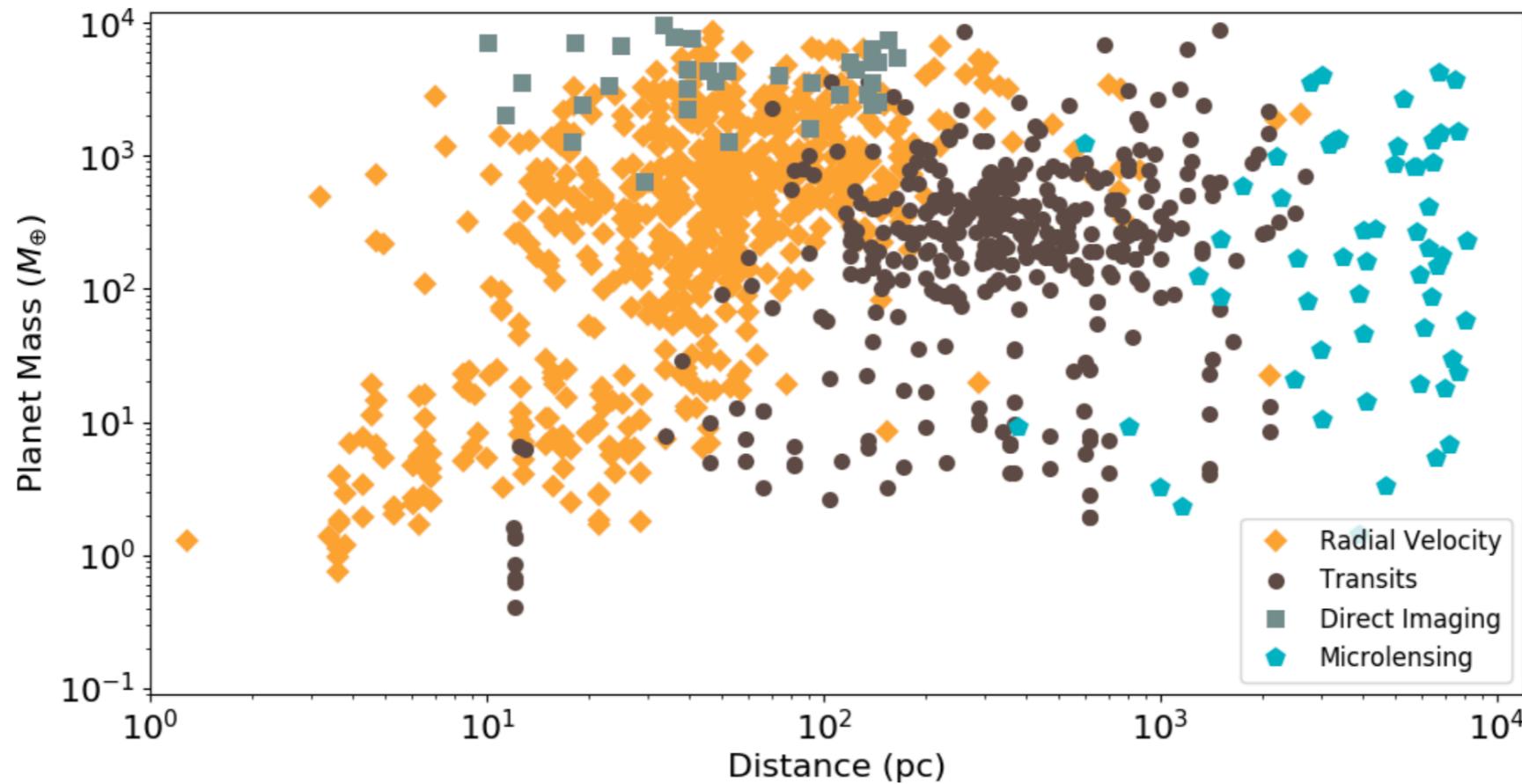


Fig. 1.1. The surface density in gas (upper line) and solids (lower broken line) as a function of radius in Hayashi's minimum mass Solar Nebula. The dashed vertical line denotes the location of the snowline.



IN ADDITION...



- sensitivity to low-mass planets
- sensitivity to long period and free-floating planets
- sensitivity to a wide range of host stars over a wide range of galacto-centric distances
- sensitivity to multiple planets and orbital parameters...

STRATEGIES TO FIND PLANETS WITH MICROLENSING

By-product of microlensing searches!

1. Find microlensing event: OGLE, MOA, now 10-30 min cadence; Korean Microlensing Telescope Network (KMTNet), 3 telescopes in Australia, South-Africa, and Chile, 1.6 m each monitoring 16 sq. degrees on the sky with a cadence of \sim 10 mins
2. Planets found as anomalies in the standard light curves: automatic modelling
3. trigger follow-up from other telescopes (e.g. Spitzer)

THE FUTURE: WFIRST

*2.4m telescope with a FOV 100x bigger
than Hubble*

To be launched (may be) in 2025



AND IN ADDITION...

- Astrometric microlensing (GAIA)
- VLBI observations to separate the images in a microlensing event

